## Homework 6: Structural Models

Credit Risk (MF772) Fall 2021 Instructor: Roza Galeeva

Due date: 8 am, Thursday October 21 Please, note that late assignments will not be accepted.

## 1. Black Cox model: constant default threshold

- The asset value of the company  $V_0 = 12.5$  million USD,
- The volatility of the asset value  $\sigma_V = 20\%$ .
- The principal of the debt D=10 million USD and has maturity T=2 years.
- The risk free rate is r = 4%.
- The safety covenant ( default threshold) ,  $K_1 \leq De^{-rT}$  is constant.
- Let  $\rho = \frac{K_1}{De^{-rT}}$ ,  $0 < \rho \le 1$ . Consider  $\rho = 0.05, 0.1, 0.15, ...1$ .

Work on the following questions:

- a) For each  $\rho$  calculate:
  - The default probability and plot it as a function of  $\rho$ .
  - The credit spread s of the debt value (use definition from Merton model)
- (b) Plot credit spread as a function of default probability
- (c) Set up the asset prices scenarios by Monte Carlo. Consider  $\rho = 0.9$  and  $\rho = 0.0001$  Verify the analytical values for default probability by Monte Carlo simulations.