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Team Note.

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1 Typedef

```
typedef long long LL;
typedef vector<LL> VLL; // vector
typedef vector< VLL > Matrix; // vector
typedef double D;
typedef queue<LL> Q; //queue
typedef deque<LL> DQ; // deque
typedef priority queue<LL, vector<LL>, greater<LL> > min heap;
typedef priority queue<LL> max heap: //(Heap : functional, vector)
2 Numerical Algorithm
2.1 GCD / LCM / MODULAR
LL gcd(LL a, LL b) { while(b) { int t = a%b; a=b; b=t;} return a; }}
LL lcm(LL a, LL b) { return a / qcd(a,b)*b; }
LL mod(LL num, LL div){ return ((num%div) + div) % div; }
LL combination(LL n, LL k)\{n=k:1,(k<0||k>n):0,k<1:1\}, c(n,k)=c(n-1,k-1)+c(n-1,k)
2.2 Matrix
2.2.1 Matrix Multiplication with Operator Overloading
//Matrix a(n by m), Matrix b(m by l), result Matrix c(n by l)
typedef vector< VLL > matrix;
const LL mod = 31991:
matrix operator* (const matrix &a, const matrix &b) {
    int n = a.size(), m = a[0].size(), l = b[0].size();
    matrix c(n, vector<long long>(l));
    for (int i = 0; i<n; i++) {
        for (int j = 0; j<l; j++) {
            for (int k = 0; k < m; k++) {
                c[i][j] += a[i][k] * b[k][j];
            c[i][i] %= mod; //If not need = erase;
    return c;
```

```
2.2.1 Fastpow of Matrix (M^n in log n)
//a=source matrix, t=몋승, ans=result matrix(Unit matrix, I)
while (t > 0) {
    if (t % 2 == 1) {
        ans = ans * a;
    a = a * a:
    t /= 2;
}
2.3 Fast Exponential ( is calculated in (\lg n))
const LL MOD = 1000000;
LL fast power(LL base, LL power) {
    LL result = 1:
    while(power > 0) {
        if(power & 1) {
            result = (result*base) % MOD;
        base = (base * base) % MOD;
        power >>=1;
    return result;
}
2.4 C++ Next Permutation (Get all permutation of vector<int>)
int main () {
  int myints[] = \{1,2,3\};
  sort (myints, myints+3);
  do {
    std::cout << myints[0] << ' ' << myints[1] << ' ' << myints[2];</pre>
  } while ( std::next permutation(myints, myints+3) );
  return 0;
}
```

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2.5 Count Prime Number in range

```
// credit : https://github.com/stjepang/snippets/blob/master/count primes.cpp
// Primes up to 10^12 can be counted in ~1 second.
const int MAXN = 1000005; // MAXN is the maximum value of sqrt(N) + 2
bool prime[MAXN];
int prec[MAXN];
vector<int> P:
void init() {
    prime[2] = true;
    for (int i = 3; i < MAXN; i += 2) prime[i] = true;
    for (int i = 3; i*i < MAXN; i += 2){
        if (prime[i]){
            for (int i = i*i: i < MAXN: i += i+i) prime[i] = false:
    for(int i=1; i<MAXN; i++){</pre>
    if (prime[i]) P.push back(i);
        prec[i] = prec[i-1] + prime[i];
}
LL rec(LL N, int K) {
    if (N <= 1 | K < 0) return 0;
    if (N \leftarrow P[K]) return N-1;
    if (N < MAXN && 1|l * P[K]*P[K] > N) return N-1 - prec[N] + prec[P]
[K]];
    const int LIM = 250:
    static int memo[LIM*LIM][LIM];
    bool ok = N < LIM*LIM;</pre>
    if (ok && memo[N][K]) return memo[N][K];
    LL ret = N/P[K] - rec(N/P[K], K-1) + rec(N, K-1);
    if (ok) memo[N][K] = ret;
    return ret;
LL count primes(LL N) { //less than or equal to
    if (N < MAXN) return prec[N];</pre>
    int K = prec[(int)sart(N) + 1];
    return N-1 - rec(N, K) + prec[P[K]];
```

3 Graph Theory

3.1 DFS / BFS with Graph Class (Adjacency List)

```
// credit: https://www.geeksforgeeks.org/breadth-first-search-or-bfs-for-a-graph/
using namespace std:
// Have to include <list>, <vector>, <algorithm>
// This class represents a directed graph using
// adjacency list representation
class Graph
    int V:
             // No. of vertices
    // Pointer to an array containing adjacency
    // lists
    list<int> *adi:
    void DFSUtil(int v, bool visited[]);
public:
    Graph(int V); // Constructor
    // function to add an edge to graph
    void addEdge(int v, int w);
    // prints BFS traversal from a given source s
    void BFS(int s):
    void DFS(int v);
};
Graph::Graph(int V)
    this->V = V:
    adj = new list<int>[V];
}
void Graph::addEdge(int v, int w)
    adj[v].push back(w); // Add w to v's list.
void Graph::DFSUtil(int v, bool visited[])
    // Mark the current node as visited and
    // print it
```

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```
visited[v] = true;
    cout << v << " ":
    // Recur for all the vertices adjacent
    // to this vertex
    list<int>::iterator i:
    for (i = adj[v].begin(); i != adj[v].end(); ++i)
        if (!visited[*i])
            DFSUtil(*i, visited);
}
// DFS traversal of the vertices reachable from v.
// It uses recursive DFSUtil()
void Graph::DFS(int v)
    // Mark all the vertices as not visited
    bool *visited = new bool[V];
    for (int i = 0; i < V; i++)
        visited[i] = false;
    // Call the recursive helper function
    // to print DFS traversal
    DFSUtil(v, visited);
void Graph::BFS(int s)
    // Mark all the vertices as not visited
    bool *visited = new bool[V];
    for(int i = 0; i < V; i++)
        visited[i] = false;
    // Create a queue for BFS
    list<int> queue;
    // Mark the current node as visited and enqueue it
    visited[s] = true;
    queue.push back(s);
    // 'i' will be used to get all adjacent
    // vertices of a vertex
    list<int>::iterator i;
```

```
while(!queue.empty())
        // Dequeue a vertex from gueue and print it
        s = queue.front();
        cout << s << " ";
        queue.pop front():
        // Get all adjacent vertices of the dequeued
        // vertex s. If a adjacent has not been visited,
        // then mark it visited and enqueue it
        for (i = adj[s].begin(); i != adj[s].end(); ++i)
            if (!visited[*i])
                visited[*i] = true;
                queue.push back(*i);
}
3.2 Find Existence of Cycle in DAG by DFS
// This function is a variation of DFSUvtil() in https://www.geeks.forgeeks.org/archives/18212
// Have to of declaration of Function in public: and private:
bool Graph::isCyclicUtil(int v, bool visited[], bool *recStack){
    if(visited[v] == false)
        // Mark the current node as visited and part of recursion stack
        visited[v] = true;
        recStack[v] = true;
        // Recur for all the vertices adjacent to this vertex
        list<int>::iterator i:
        for(i = adj[v].begin(); i != adj[v].end(); ++i)
            if (!visited[*i] && isCyclicUtil(*i, visited, recStack) )
                return true:
            else if (recStack[*i])
                return true;
```

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```
recStack[v] = false: // remove the vertex from recursion stack
    return false:
// Returns true if the graph contains a cycle, else false.
// This function is a variation of DFS() in https://www.geeksforgeeks.org/archives/18212
bool Graph::isCvclic()
    // Mark all the vertices as not visited and not part of recursion
    // stack
    bool *visited = new bool[V];
    bool *recStack = new bool[V];
    for(int i = 0; i < V; i++)</pre>
        visited[i] = false;
        recStack[i] = false;
    // Call the recursive helper function to detect cycle in different
    // DFS trees
    for(int i = 0; i < V; i++)
        if (isCyclicUtil(i, visited, recStack))
            return true;
    return false;
3.3 Strong Connected Components (Tarian)
                                                         V+E) with
graph class
// A recursive function to print DFS starting from v
// Have to include <stack> <list>
// Have to add public:printSCCs,getTranspose private:fillOrder,DFSUtil
void Graph::DFSUtil(int v, bool visited[])
    // Mark the current node as visited and print it
    visited[v] = true;
    cout << v << " ";
    // Recur for all the vertices adjacent to this vertex
    list<int>::iterator i;
```

```
for (i = adj[v].begin(); i != adj[v].end(); ++i)
        if (!visited[*i])
            DFSUtil(*i, visited);
}
Graph Graph::getTranspose()
    Graph q(V);
    for (int v = 0; v < V; v++)
        // Recur for all the vertices adjacent to this vertex
        list<int>::iterator i:
        for(i = adj[v].begin(); i != adj[v].end(); ++i)
            g.adj[*i].push back(v);
    return g;
}
void Graph::addEdge(int v, int w)
    adi[v].push back(w); // Add w to v's list.
void Graph::fillOrder(int v, bool visited[], stack<int> &Stack)
    // Mark the current node as visited and print it
    visited[v] = true;
    // Recur for all the vertices adjacent to this vertex
    list<int>::iterator i:
    for(i = adj[v].begin(); i != adj[v].end(); ++i)
        if(!visited[*i])
            fillOrder(*i, visited, Stack);
    // All vertices reachable from v are processed by now, push v
    Stack.push(v);
}
// The main function that finds and prints all strongly connected
// components
void Graph::printSCCs()
```

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return 0:

```
stack<int> Stack;
    // Mark all the vertices as not visited (For first DFS)
    bool *visited = new bool[V];
    for(int i = 0; i < V; i++)
         visited[i] = false;
    // Fill vertices in stack according to their finishing times
    for(int i = 0; i < V; i++)
         if(visited[i] == false)
             fillOrder(i, visited, Stack);
    // Create a reversed graph
    Graph gr = getTranspose();
    // Mark all the vertices as not visited (For second DFS)
    for(int i = 0; i < V; i++)
         visited[i] = false;
    // Now process all vertices in order defined by Stack
    while (Stack.empty() == false)
         // Pop a vertex from stack
         int v = Stack.top();
         Stack.pop();
         // Print Strongly connected component of the popped vertex
         if (visited[v] == false)
             gr.DFSUtil(v, visited);
             cout << endl:</pre>
// Driver program to test above functions
int main()
  // Create a graph given in the above diagram
  Graph g(5);
  g.addEdge(1, 0);
  g.addEdge(0, 2);
  g.addEdge(2, 1);
  g.addEdge(0, 3);
  g.addEdge(3, 4);
  cout << "Following are strongly connected components in '</pre>
        "given graph \n";
  g.printSCCs(); //
```

```
3.4 Flovd
               n
int map [ ][ ] = \{0,\};
for (int k = 0; k < N; k++)
    for (int i = 0; i < N; i++)
        for (int i = 0; i < N; i++)
            if (map[i][k] \&\& map[k][i]) map[i][i] = 1;
3.5 Fast Diikstra (NOT IN GRAPH CLASS)
//정점 index는 0에서 n-1까지!
//vector< vector<edge> >& graph는 idx -> to로 향하는 모든 edge
//distance will overflow an int. If you have time, change it LL
//INT MAX는 <climits>헤더에
struct edge { int to, length; };
int dijkstra(const vector< vector<edge> > &graph, int source, int target) {
    vector<int> min distance( graph.size(), INT MAX );
    min distance | source | = 0;
    set< pair<int,int> > active vertices;
    active vertices.insert( {0,source} );
    while (!active vertices.empty()) {
       int where = active vertices.begin()->second;
       if (where == target) return min distance[where];
       active vertices.erase( active vertices.begin() );
       for (auto ed : graph[where])
           if (min distance[ed.to] > min distance[where] + ed.length) {
               active vertices.erase( { min distance[ed.to], ed.to } );
               min distance[ed.to] = min distance[where] + ed.length;
               active vertices.insert( { min distance[ed.to], ed.to } );
    return INT MAX;
}
```

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4 Tree

```
4.1 LCA in tree (Adjacency Matrix)
const int MAXN = 100; //Can be changed
const int MAXLN = 9; //Can be changed
vector<int> tree[MAXN];
int depth[MAXN];
int par[MAXLN][MAXN];
void dfs(int nod, int parent) {
        for (int next : tree[nod]) {
            if (next == parent) continue;
            depth[next] = depth[nod] + 1;
            par[0][next] = nod;
            dfs(next, nod);
        }
void prepare lca() {
    const int root = 0;
    dfs(root, -1);
    par[0][root] = root;
    for (int i = 1; i < MAXLN; ++i)
        for (int i = 0; i < n; ++i)
            par[i][i] = par[i - 1][par[i - 1][i]];
// find lowest common ancestor in tree between u & v
// assumption : must call 'prepare lca' once before call this
// O(logV)
int lca(int u, int v) {
    if (depth[u] < depth[v]) swap(u, v);</pre>
    if (depth[u] > depth[v]) {
        for (int i = MAXLN - 1; i >= 0; --i)
            if (depth[u] - (1 << i) >= depth[v])
                u = par[i][u];
    if (u == v) return u;
    for (int i = MAXLN - 1; i \ge 0; --i) {
        if (par[i][u] != par[i][v]) {
            u = par[i][u];
            v = par[i][v];
        }
    return par[0][u];
```

```
4.2 Union & Find
// LL is long long
// VLL is vector<LL>
LL find(VLL& C, LL x) { return (C[x] == x) ? x : C[x] = find(C,C[X]); }
void merge(VLL& C, LL x, LL y) { C[find(C, x)] = find(C, y); } //union
4.3 Kruskal (Making MST)
#include <iostream>
#include <cstdio>
#include <vector>
#include <utility>
#include <algorithm>
using namespace std;
typedef long long lld;
typedef long double Ld;
typedef pair<lld, lld> pll:
#define sci(n) scanf("%lld", &(n))
typedef pair<lld, pll> edge;
void link(vector<int> &, int, int);
int find(vector<int> &, int);
int main(void)
    lld n, e;
    sci(n), sci(e);
    vector<edge> edges;
    for (int i = 0; i < e; ++i)
        lld v, w, c;
        sci(v), sci(w), sci(c);
        edges.push back(edge(c, pll(v, w)));
    vector < int > uf(n + 1);
```

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```
uf[i] = i;
    for (int i = 0; i < n + 1; ++i)
    sort(edges.begin(), edges.end());
    lld cost = 0:
    for (int i = 0; i < e; ++i)
        lld v = edges[i].second.first, w = edges[i].second.second;
        if (find(uf, v) != find(uf, w))
            link(uf, v, w);
            cost += edges[i].first;
       }
    cout << cost << endl;</pre>
    return 0;
}
void link(vector<int> &uf, int x, int y)
    uf[find(uf, x)] = find(uf, y);
int find(vector<int> &uf, int x)
    if (uf[x] == x)
                     return x;
    return uf[x] = find(uf, uf[x]);
   Flow, Matching
5.1 Ford-Fulkerson
#include <iostream>
#include <vector>
```

```
#include <iostream>
#include <vector>
#include <queue>
#include <algorithm>
#include <cstring>
#define MAX_V 100
#define INF 2100000000
```

```
typedef int network[MAX V][MAX V];
//capacity[u][v]: capacity of u -> v
//flow[u][v]: flow of u -> v
network capacity, flow;
int V, e;
int networkFlow(int, int);
int main(void)
    return 0:
}
int networkFlow(int source, int sink)
    memset(flow, 0, sizeof(flow));
    int totalFlow = 0;
    while (1)
           //search out augmenting path by using BFS
           std::vector<int> parent(MAX V, -1);
           std::queue<int> q:
           parent[source] = source;
           a.push(source);
           while (!q.empty() && parent[sink] == -1)
                   int h = q.front(); q.pop();
                   for (int t = 0; t < V; ++t)
                           //search out edge such that residual capacity > 0
                          if (capacity[h][t] - flow[h][t] > 0 && parent[t] = -1)
                                   parent[t] = h;
                                   a.push(t);
           //Termination condition
           if (parent[sink] == -1)
                   break:
           //determine how much send flow through augmenting path
           int amount = INF:
           for (int p = sink; p != source; p = parent[p])
```

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```
amount = std::min(capacity[parent[p]][p] - flow[parent[p]][p], amount);
           //send flow through augmenting path
           for (int p = sink; p != source; p = parent[p])
                   flow[parent[p]][p] += amount;
                   flow[p][parent[p]] -= amount;
           }
           totalFlow += amount;
    return totalFlow;
5.2 Dinic Algorithm( Get Max Flow in
                                                 VE)
struct Node
    vector<int> adi;
Node graf[MAX N];
struct Edge
    int u, v, cap;
    int flow:
};
vector<Edge> E;
int v, e;
int s, t;
int dist[MAX N];
int upTo[MAX_N];
int idd = 0;
//Dinicov algoritam za nalazenje maksimalnog protoka izmedju dva cvora
u grafu
//Slozenost: 0(V^2 * E)
inline bool BFS()
```

```
for (int i=1; i <= v; i++) dist[i] = -1;
    queue<int> bfs queue;
    bfs queue.push(s);
    dist[s] = 0;
    while (!bfs queue.empty())
        int xt = bfs queue.front();
        bfs queue.pop();
        for (int i=0;i<graf[xt].adj.size();i++)</pre>
            int currID = graf[xt].adj[i];
             int xt1 = E[currID].v;
            if (dist[xt1] == -1 && E[currID].flow < E[currID].cap)</pre>
                 bfs queue.push(xt1);
                 dist[xt1] = dist[xt] + 1;
    return (dist[t] != -1);
}
inline int DFS(int xt, int minCap)
    if (minCap == 0) return 0;
    if (xt == t) return minCap;
    while (upTo[xt] < graf[xt].adj.size())</pre>
        int currID = graf[xt].adj[upTo[xt]];
        int xt1 = E[currID].v;
        if (dist[xt1] != dist[xt] + 1)
            upTo[xt]++;
             continue;
        int aug = DFS(xt1, min(minCap, E[currID].cap - E[currID].flow)
);
        if (aug > 0)
             E[currID].flow += aug;
```

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```
if (currID&1) currID--; else currID++;
            E[currID].flow -= aug;
            return aug;
        upTo[xt]++;
    return 0;
inline int Dinic()
    int flow = 0;
    while (true)
        if (!BFS()) break;
        for (int i=1;i<=v;i++) upTo[i] = 0;</pre>
        while (true)
            int currFlow = DFS(s, INF);
            if (currFlow == 0) break;
            flow += currFlow;
        }
    return flow;
inline void addEdge(int u, int v, int cap)
    Edge E1, E2;
    E1.u = u, E1.v = v, E1.cap = cap, E1.flow = 0;
    E2.u = v, E2.v = u, E2.cap = 0, E2.flow = 0;
    graf[u].adj.push back(idd++);
    E.push_back(E1);
    graf[v].adj.push_back(idd++);
    E.push back(E2);
}
int main()
```

```
v = 4, e = 5;
    s = 1, t = 4:
    addEdge(1, 2, 40);
    addEdge(1, 4, 20);
    addEdge(2, 4, 20);
    addEdge(2, 3, 30);
    addEdge(3, 4, 10);
    printf("%d\n",Dinic());
    return 0;
}
    String
6.1 KMP
typedef vector<int> seg t;
void calculate_pi(vector<int>& pi, const seq_t& str) {
    pi[0] = -1;
    for (int i = 1, j = -1; i < str.size(); i++) {
        while (i \ge 0 \&\& str[i] != str[i + 1]) i = pi[i];
        if (str[i] == str[i + 1])
            pi[i] = ++j;
        else
            pi[i] = -1;
    }
}
// returns all positions matched
// 0(|text|+|pattern|)
vector<int> kmp(const seq t& text, const seq t& pattern) {
    vector<int> pi(pattern.size()), ans;
    if (pattern.size() == 0) return ans;
    calculate pi(pi, pattern);
    for (int i = 0, j = -1; i < text.size(); i++) {
        while (j \ge 0 \&\& text[i] != pattern[j + 1]) j = pi[j];
        if (text[i] == pattern[j + 1]) {
```

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```
j++;
    if (j + 1 == pattern.size()) {
        ans.push_back(i - j);
        j = pi[j];
    }
    }
} return ans;
}
```

6.1.1 How the KMP Algorithm is working (with Failure Func.)

KMP Algorithm은 패턴 P와 문자열 S가 있을 때, 문자열 S에 패턴 P가 부분 문자열로 있는지, 혹은 몇 개 있는지 선형시간 O(|S|+|P|)에 확인하는 방법이다.

기본적인 아이디어는 $\underline{\textbf{J}}$ 패 함수 f(i)에서 온다. 아래는 패턴 PP가 "abracadabra" 일 때 실패 함수 값을 표로 나타낸 것이다.

i	1	2	3	4	5	6	7	8	9	10	11
Р	а	b	r	а	С	а	d	а	b	r	а
f	0	0	0	1	0	1	0	1	2	3	4

P[i,j]를 패턴 P의 i번째 문자부터 j번째 문자까지로 구성된 부분문자열이라 하자. 실패 함수 f(i)는 i보다 작은 값이며, P[i-f(i)+1,i]와 P[1,f(i)]가 같도록 되는 최대값으로 정의된다.

패턴 P의 실패함수는 아래처럼 O(|P|)에 계산할 수 있다.

```
int k = 0;
F[1] = 0;
for (int i=2;i<=|P|;i++){
    while (k && P[k+1] != P[i]) k = F[k];
    if (P[k+1] == P[i]) k++;
    F[i] = k;
}</pre>
```

위 방법의 시간복잡도가 O(|P|)라는 것을 쉽게 보이기 위해서는 4번째 줄의 while문에 집중할 필요가 있다. while문을 한 번 돌 수록 변수 k는 적어도 1 감소하게된다. 변수 k는 0에서부터 시작해서 최대 |P|만큼 증가하므로 감소 또한 최대 |P|번 일어날 수 있다. 따라서 전체 시간복잡도가

```
0(¦P¦)가 된다.
실패 함수를 계산하는 것과 문자열 S에 패턴 P가 존재하는지 확인하는 것은
완전히 똑같다.
```

실패 함수를 구할 때와 마찬가지의 이유로 시간복잡도가 O(|S|)이다.

6.2 Aho-Corasick Algorithm (and its usage)

```
//https://gist.github.com/koosaga/96e5de4ccb99616f9bc3a760ec964cbe
const int MAXN = 100005, MAXC = 26;
struct aho corasick{
    int trie[MAXN][MAXC], piv; // trie
    int fail[MAXN]; // failure link
    int term[MAXN]; // output check
    void init(vector<string> &v){
        memset(trie, 0, sizeof(trie));
        memset(fail, 0, sizeof(fail));
        memset(term, 0, sizeof(term));
        piv = 0;
        for(auto &i : v){
            int p = 0;
            for(auto &i : i){
                if(!trie[p][j]) trie[p][j] = ++piv;
                p = trie[p][j];
            term[p] = 1;
        queue<int> que;
        for(int i=0; i<MAXC; i++){</pre>
            if(trie[0][i]) que.push(trie[0][i]);
```

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```
while(!que.empty()){
           int x = que.front();
           que.pop();
           for(int i=0; i<MAXC; i++){</pre>
               if(trie[x][i]){
                  int p = fail[x];
                  while(p && !trie[p][i]) p = fail[p];
                   p = trie[p][i];
                   fail[trie[x][i]] = p;
                  if(term[p]) term[trie[x][i]] = 1;
                   que.push(trie[x][i]);
           }
       }
    bool query(string &s){
       int p = 0;
       for(auto &i : s){
           while(p && !trie[p][i]) p = fail[p];
           p = trie[p][i];
           if(term[p]) return 1;
       return 0;
}aho corasick;
6.3 Usage of std::string
//문자열내부에 있는 특정문자 모두 치환
string ReplaceAll(string &str, const string& from, const string& to){
   size t start pos = 0; //string처음부터 검사
    while((start pos = str.find(from, start pos)) != string::npos)
   //from을 찾을 수 없을 때까지
       str.replace(start pos, from.length(), to);
       start pos += to.length();
    // 중복검사를 피하고 from.length() > to.length()인 경우를 위해서
    return str;
```

```
//공백제거
str.erase(std::remove(str.begin(), str.end(), ' '), str.end());
//이렇게 하면 str안에 있는 문자열이 지워진다.
#include <iostream>
#include <string>
#include <algorithm>
using namespace std:
int main(){
string str="Hello World";
str.erase(remove(str.begin(), str.end(), ' '), str.end());
cout<<str<<endl; //HelloWorld</pre>
string output = ReplaceAll(str, "Hello", "Hell");
     cout<<output<<endl: //HellWorld</pre>
return 0;
}
    Special Data Structure
7.1 Segment Tree
#include <iostream>
#include <cstdio>
#include <vector>
using namespace std;
typedef long long LL;
vector<LL> seg;
vector<LL> arr;
vector<LL> lazy;
void init(int, int, int);
void propagate(int, int, int);
void update(int, int, int, LL, int, int);
```

LL sum(int, int, int, int, int);

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```
int main(void)
    int n, m, k;
    cin \gg n \gg m \gg k;
    arr.resize(n + 1);
    lazy.resize(n * 4, 0);
    seq.resize(n * 4):
    for (int i = 0; i < n; ++i)
        cin >> arr[i + 1];
    init(1, 1, n);
    for (int i = 0; i < m + k; ++i)
        int a, b, c;
        cin \gg a \gg b \gg c;
        if (a == 1)
            update(1, 1, n, c - arr[b], b, b);
            arr[b] = c;
        else
            cout \ll sum(1, 1, n, b, c) \ll endl;
    return 0;
void init(int nn, int l, int r)
   if (l == r)
        seg[nn] = arr[l];
        return;
    int mid = (l + r) / 2;
   init(nn * 2, l, mid);
   init(nn * 2 + 1, mid + 1, r);
    seg[nn] = seg[nn * 2] + seg[nn * 2 + 1];
//Lazy Propagation 쓰는 Segtree임
```

```
void propagate(int nn, int nl, int nr)
    if (lazy[nn] != 0)
        if (nl != nr)
            lazy[nn * 2] += lazy[nn];
            lazy[nn * 2 + 1] += lazy[nn];
        seg[nn] += lazy[nn] * (nr - nl + 1);
        lazy[nn] = 0;
void update(int nn, int nl, int nr, LL k, int l, int r)
    propagate(nn, nl, nr);
    if (nr < l || r < nl)
        return;
    if (l <= nl && nr <= r)</pre>
        lazy[nn] += k;
        propagate(nn, nl, nr);
        return;
    int mid = (nl + nr) / 2;
    update(nn * 2, nl, mid, k, l, r);
    update(nn * 2 + 1, mid + 1, nr, k, l, r);
    seg[nn] = seg[nn * 2] + seg[nn * 2 + 1];
}
LL sum(int nn, int nl, int nr, int l, int r)
    propagate(nn, nl, nr);
    if (nr < l || r < nl)</pre>
        return 0;
    if (l <= nl && nr <= r)
        return seg[nn];
    int mid = (nl + nr) / 2;
```

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```
return sum(nn * 2, nl, mid, l, r) + sum(nn * 2 + 1, mid + 1, nr, l, r);
}
```

7.2 Convex Hull Trick(For Dynamic Prgramming)

일부 dp문제에서 시간복잡도를 획기적으로 줄여주는 걸로 유명한 테크닉입니다. 이번에 koi 2014 전국본선 3번으로 나왔으니 인지도가 더 올라갈 거같네요.

개략적으로 설명하자면

$$dp[i] = \min_{i < i} (dp[j] + a[i]b[j])$$
 (단. $b[i-1] >= b[i]$)

문제를 풀다가 이런 형태의 점화식이 나올 때는 보통 n^2 말고는 희망이 없는데

$$f(i) = \min_{j < i} (a[i]b[j] + dp[j])$$

$$f(x = a[i]) = \min_{j < i} (b[j] * x + dp[j])$$

이걸 이런 식으로 해석하면 기울기와 절편이 j에 따라 결정되는 형태의 일 차함수들로 해석할수 있게 됩니다.

이러면 저러한 dp식을 구할때

(dp[0] = 0)

- 1. 0번 선분을 넣는다 (기울기 = b[0]. 절편 = dp[0])
- 2. 현재 들어간 선분 중 최솟값을 찾는다 (dp[1])
- 3. 1번 선분을 넣는다 (기울기 = b[1]. 절편 = dp[1])
- 4. 현재 들어간 선분 중 최솟값을 찾는다 (dp[2])

.

즉,

- * dp[i]를 구하고
- * 선분을 넣어주는

연산을 0(1)이나 $0(\lg n)$ 에 할 수 있는 자료구조가 있으면 시간복잡도 향상을 꾀할 수 있습니다.

```
이 때 convex hull trick은 저 작업들을 모조리 0(lan)만에 할 수 있습니
다.
뿐만 아니라 a[i] <a[i+1]일 경우에는 0(1)만에 해버릴 수도 있습니다. (사
실 스위핑이라서 정확히 O(1)은 아닙니다. 그냥 O(n/n)...
달리 할말이 없네요... 나머지는 코드포스 어셉먹인 소스코드로 대체하겠습
니다.
#include <cstdio>
typedef long long lint:
lint a[100005],b[100005],d[100005];
lint la[100005], lb[100005];
int sz.p.n:
double cross(int x, int y){return (double)(lb[v] - lb[x]) / (la[x] - l
a[y]);}
void insert(lint p, lint q){
    la[sz] = p;
   lb[sz] = q;
   // 일단 넣고
   while(sz>1 && cross(sz-1,sz-2) > cross(sz-1,sz)){
       // 자신 - (sz-1) 교점이 (sz-1) - (sz-2) 교점보다 앞에 있을때
      // sz-1 원소는 필요가 없다
       la[sz-1] = la[sz];
       lb[sz-1] = lb[sz];
       SZ--:
    SZ++;
}
lint query(lint x){
   while (p+1 < sz \&\& cross(p,p+1) <= x) p++;
   // 교점이 x 뒤에 있는 원소들은 모두 pop front
   return lb[p] + la[p] * x;
}
```

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```
int main(){
    scanf("%d",&n);
    for (int i=0; i<n; i++) {
        scanf("%I64d",&a[i]);
    for (int i=0; i<n; i++) {
        scanf("%I64d",&b[i]);
    insert(b[0],0);
    for (int i=1; i<n; i++) {
        d[i] = query(a[i]);
        insert(b[i],d[i]);
    printf("%I64d",d[n-1]);
}
7.3 Custom Heap with C++ STL, lambda
#include <queue>
auto comp = [](int a, int b) {
    //Coding Here
    //this is for Absolute Value MinHeap
    if (abs(a) == abs(b)) return a > b;
    else return abs(a) > abs(b);
};
priority queue< LL, vector<LL>, decltype(comp)> min heap(comp);
7.4 FFT(Fast Fourier Transform)-Multiplication of polynomial
//출처: http://blog.myungwoo.kr/54
#define USE MATH DEFINES
#include <math.h>
#include <complex>
#include <vector>
#include <algorithm>
using namespace std;
#define sz(v) ((int)(v).size())
```

```
#define all(v) (v).begin(),(v).end()
tvpedef complex<double> base;
void fft(vector <base> &a, bool invert)
    int n = sz(a);
    for (int i=1.i=0:i<n:i++){
        int bit = n \gg 1;
        for (; j>=bit; bit>>=1) j -= bit;
        i += bit:
        if (i < j) swap(a[i],a[i]);
    for (int len=2;len<=n;len<<=1){</pre>
        double ang = 2*M PI/len*(invert?-1:1);
        base wlen(cos(ang), sin(ang));
        for (int i=0;i<n;i+=len){</pre>
            base w(1);
            for (int j=0;j<len/2;j++){
                base u = a[i+j], v = a[i+j+len/2]*w;
                a[i+i] = u+v;
                a[i+j+len/2] = u-v;
                w *= wlen;
    if (invert){
        for (int i=0;i<n;i++) a[i] /= n;
}
void multiply(const vector<int> &a,const vector<int> &b,vector<int> &r
es)
{
    vector <base> fa(all(a)), fb(all(b));
    int n = 1:
    while (n < max(sz(a), sz(b))) n <<= 1;
    fa.resize(n); fb.resize(n);
    fft(fa,false); fft(fb,false);
    for (int i=0;i<n;i++) fa[i] *= fb[i];
    fft(fa,true);
```

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```
res.resize(n);
  for (int i=0;i<n;i++) res[i] = int(fa[i].real()+(fa[i].real()>0?0.
5:-0.5));
}
```

7.4.1 FFT Problem Example

문제) 크기가 N인 정수 배열 A와 크기가 M인 정수 배열 B가 있다. ($M \leq N \leq 500,000$). 크기가 M인 A의 (연속한) 부분 배열 C가 있을 때, 함수 f의 정의는 다음과 같다. $f(C) = \sum_{i=0M} B[i] \times C[i]$ 이 때, f(C)가 최대가 되는 C를 찾아 f(C) 값을 구하시오.

8 Geometry

8.1 Convex Hull 2D(그라함 스캔)

```
// A C++ program to find convex hull of a set of points. Refer
// https://www.geeksforgeeks.org/orientation-3-ordered-points/
// for explanation of orientation()
#include <iostream>
#include <stack>
#include <stdlib.h>
using namespace std;
struct Point
    int x, y;
};
// A globle point needed for sorting points with reference
// to the first point Used in compare function of qsort()
Point p0;
// A utility function to find next to top in a stack
Point nextToTop(stack<Point> &S)
    Point p = S.top();
    S.pop();
```

```
Point res = S.top();
    S.push(p):
    return res;
}
// A utility function to swap two points
int swap(Point &p1, Point &p2)
    Point temp = p1:
    p1 = p2;
    p2 = temp;
}
// A utility function to return square of distance
// between p1 and p2
int distSq(Point p1, Point p2)
    return (p1.x - p2.x)*(p1.x - p2.x) +
        (p1.y - p2.y)*(p1.y - p2.y);
}
// To find orientation of ordered triplet (p, q, r).
// The function returns following values
// 0 --> p, q and r are colinear
// 1 --> Clockwise
// 2 --> Counterclockwise
int orientation(Point p, Point q, Point r)
    int val = (q.y - p.y) * (r.x - q.x) -
        (a.x - p.x) * (r.v - a.v):
    if (val == 0) return 0; // colinear
    return (val > 0) ? 1 : 2; // clock or counterclock wise
}
// A function used by library function qsort() to sort an array of
// points with respect to the first point
int compare(const void *vp1, const void *vp2)
    Point *p1 = (Point *)vp1;
```

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```
Point *p2 = (Point *)vp2;
    // Find orientation
    int o = orientation(p0, *p1, *p2);
    if (0 == 0)
        return (distSq(p0, *p2) >= distSq(p0, *p1)) ? -1 : 1;
    return (o == 2) ? -1 : 1;
}
// Prints convex hull of a set of n points.
void convexHull(Point points[], int n)
    // Find the bottommost point
    int ymin = points[0].y, min = 0;
    for (int i = 1; i < n; i++)
        int y = points[i].y;
        // Pick the bottom-most or chose the left
        // most point in case of tie
        if ((y < ymin) || (ymin == y &&
            points[i].x < points[min].x))</pre>
            ymin = points[i].y, min = i;
    // Place the bottom-most point at first position
   swap(points[0], points[min]);
    // Sort n-1 points with respect to the first point.
    // A point p1 comes before p2 in sorted ouput if p2
    // has larger polar angle (in counterclockwise
    // direction) than p1
    p0 = points[0];
    gsort(&points[1], n - 1, sizeof(Point), compare);
    // If two or more points make same angle with p0,
    // Remove all but the one that is farthest from p0
    // Remember that, in above sorting, our criteria was
    // to keep the farthest point at the end when more than
```

```
// one points have same angle.
int m = 1; // Initialize size of modified array
for (int i = 1; i < n; i++)
    // Keep removing i while angle of i and i+1 is same
    // with respect to p0
    while (i < n − 1 && orientation(p0, points[i],
        points[i + 1]) == 0
        i++:
    points[m] = points[i];
    m++: // Update size of modified array
// If modified array of points has less than 3 points,
// convex hull is not possible
if (m < 3) return;
// Create an empty stack and push first three points
// to it.
stack<Point> S;
S.push(points[0]);
S.push(points[1]);
S.push(points[2]);
// Process remaining n-3 points
for (int i = 3; i < m; i++)
    // Keep removing top while the angle formed by
    // points next-to-top, top, and points[i] makes
    // a non-left turn
    while (orientation(nextToTop(S), S.top(), points[i]) != 2)
        S.pop();
    S.push(points[i]);
}
// Now stack has the output points, print contents of stack
while (!S.empty())
```

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```
Point p = S.top();
       //여기서 vector에 넣든, print를 하면 됨. 컨벡스헐 나오는곳
        S.pop();
}
8.2 Closest Pair(2D) by Line Sweeping
#include <iostream>
#include <cstdio>
#include <algorithm>
#include <cmath>
#include <vector>
#include <set>
using namespace std:
typedef long long LL;
typedef struct _dot {
    _dot() {};
    dot(int x, int y) {
       this-> x = x;
       this-> y = y;
    int _x;
    int _y;
    bool operator < (const dot &v) const {</pre>
        if (y == v. y) {
           return _x < v._x;</pre>
       }
        else {
           return _y < v._y;
    }
} dot;
auto cmp x = [](dot\& a, dot\& b) {
    return (a. x < b. x);
```

```
};
auto cmp y = [](dot\& a, dot\& b) {
    return (a. y < b. y);
};
LL distance(dot& a, dot& b) {
    LL x = a. x, xx = b. x, y = a. y, yy = b. y;
    return (((x - xx)*(x - xx)) + ((y - yy)*(y - yy)));
}
int main() {
    vector<dot> v:
    set<dot> s;
    int n; scanf("%d", &n);
    for (int i = 0; i < n; i++) {
        dot temp; int x, y;
        scanf("%d%d", &_x, &_y);
        v.push_back(dot(_x,_y));
    sort(v.begin(), v.end(), cmp x);
    s = \{ v[0], v[1] \};
    LL max dist = distance(v[0], v[1]);
    //일단 set을 사용하고, idx 2~n까지 전체탐색 하면서
    //처음 잰 거리보다 작은 dot들을 다 cutting 하는거임 그리고 일단
    //다 Bianry tree에 넣어
    LL start = 0;
    for (int idx = 2; idx \langle v.size(); idx++ \rangle {
        dot cur = v[idx];
        while(start<idx) {</pre>
            dot p = v[start];
            LL x = cur. x - p. x;
            if (x*x > max dist) {
                s.erase(p);
                start++;
            else {
                break;
```

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```
LL dist = max dist + 1;
        auto lo = dot(-10e5, cur._y-dist);
        auto hi = dot(10e5, cur. y +dist);
        auto lb = s.lower bound(lo);
        auto hb = s.upper bound(hi);
        for (auto iter = lb; iter != hb; iter++) {
            dot cmp_dot;
            cmp dot. x = (*iter). x;
            cmp dot. y = (*iter). y;
            LL d = distance(cur, cmp dot);
            if (d < max_dist) {</pre>
                max dist = d;
            }
        s.insert(cur);
    cout << max_dist;</pre>
    return 0;
9 Pre Coding
#define CRT SECURE NO WARNINGS
#include <iostream>
#include <cstdio>
#include <vector>
#include <utility>
#include <algorithm>
#include <string>
#include <queue>
#include <stack>
#include <tuple>
#include <set>
#include <map>
#include <functional>
```

```
#include <cmath>
#include <cstring>
using namespace std;

#define sci(n) scanf("%lld", &(n))
#define scd(n) scanf("%Ld", &(n))

typedef long long LL;
typedef long double LD;
typedef pair<LL,LL> pll;
int main(void)
{
    return 0;
}
```