Torben Engelmeyer

Managing Intermittent Demand



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Torben Engelmeyer Wuppertal, Germany

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List of Symbols

α	Probability of satisfying the demand in a period directly from stock
β	Share of demand, which could be delivered directly from stock with no delay
δ	Expected number of periods between two consequtive positive demands
η	Inventory turnover
$\gamma(h)$	Autocovariance function at lag h
μ_y	Expectation of demand series
μ_{2ltd}	Second moment of the demand during lead time
$\mu_{\scriptscriptstyle Y}^+$	Expectation of positive demands
ω_i	CAPM risk measure
π_y^+	Probability of a positive demand in period t
π_{ltd}	Probability of a positive demand during lead time
$\rho(h)$	Autocorrelation function at lag h
σ_y	Standard deviation of demand
σ_Y^+	Standard deviation of positive demands

σ_{ltd}	Standard deviation of demand during lead time
$arepsilon_t$	Error terms
ξ	Probability vector of current Markov state
a_x	Selection vector
B_i	Bernoulli distributed random variable
C_i	Clustering criteria
c_{ij}	j-th criteria of the i -th SKU
CV^2	Squared coefficient of variation
D	Gap between s and S
f_{ltd}	Probabiliy density function of the demand during lead time
G	Maximal plausible demand in a period
h	Holding costs per unit per period
I_t	Inventory level in period t
J	Number of criteria in MCIC
K	Fixed order costs
L	Lead time
M	Transition matrix of an INAR(p)-process
P_x	Set of all paths, where the sum of the weights of the visited vertices equals \boldsymbol{x}
p_{ltd}	Probability mass function of the demand during lead time

List of Symbols XV

Q	Order quantity
q_t	Scaled forecasting error
r	Reorder interval
S	Order-up-to level
s	Reorder point
T	Time series length
U	Number of SKUs in MCIC
u_f	Return of a risk free asset
u_i	Return of asset i
u_m	Return of the market portfolio
w_{ij}	Weight of the j -th criteria of the i -th SKU
X_t	Random variable modeling the probability of a positive demand in period \boldsymbol{t}
y_f	First positive demand
Y_t	Random variable modeling the demand in period t
y_t	Observed demand in period t
Y_t^+	Random variable modeling the positive demand in period t