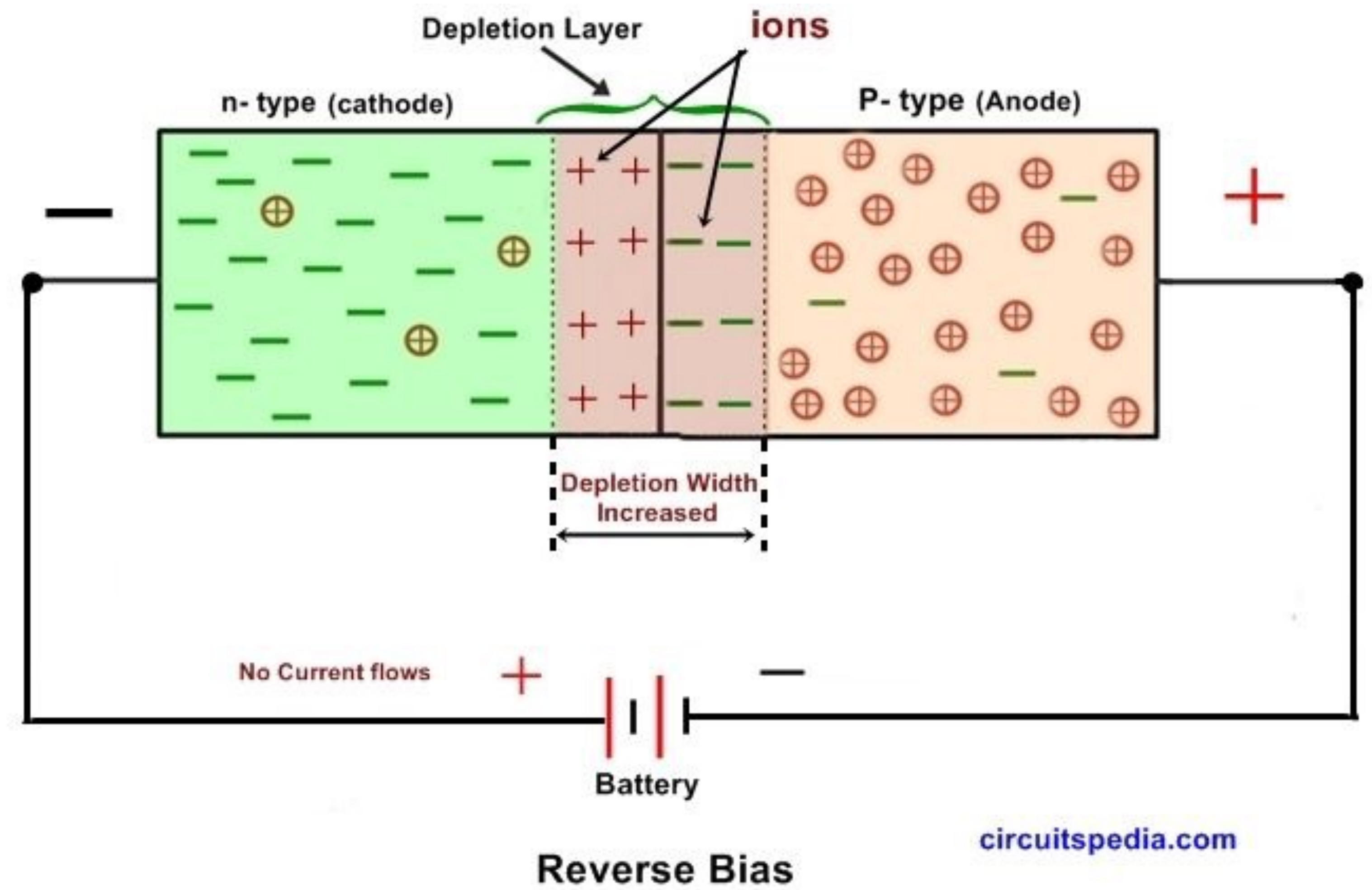
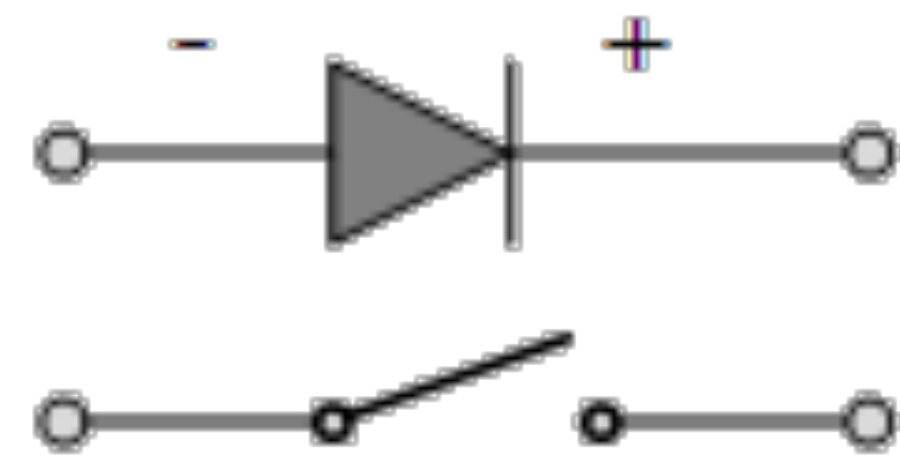
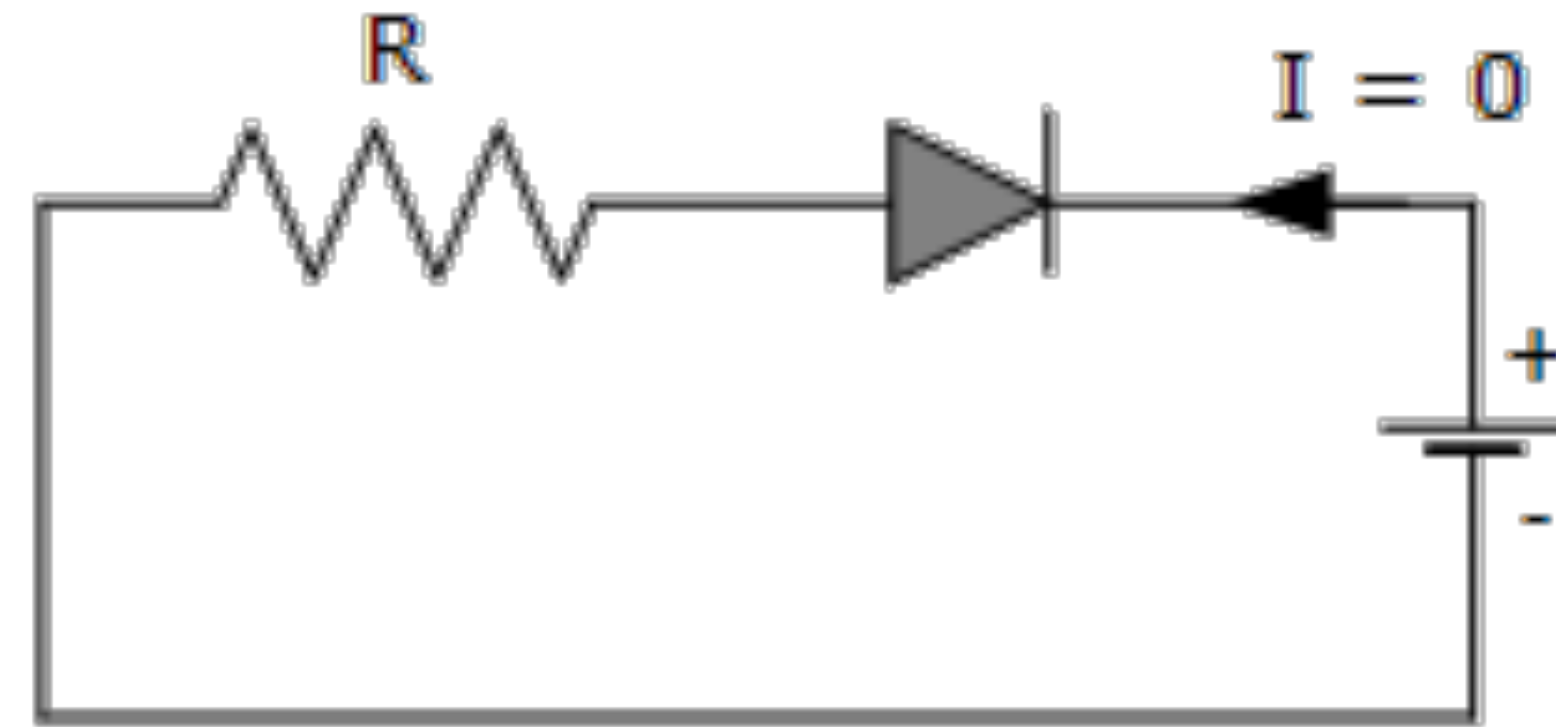
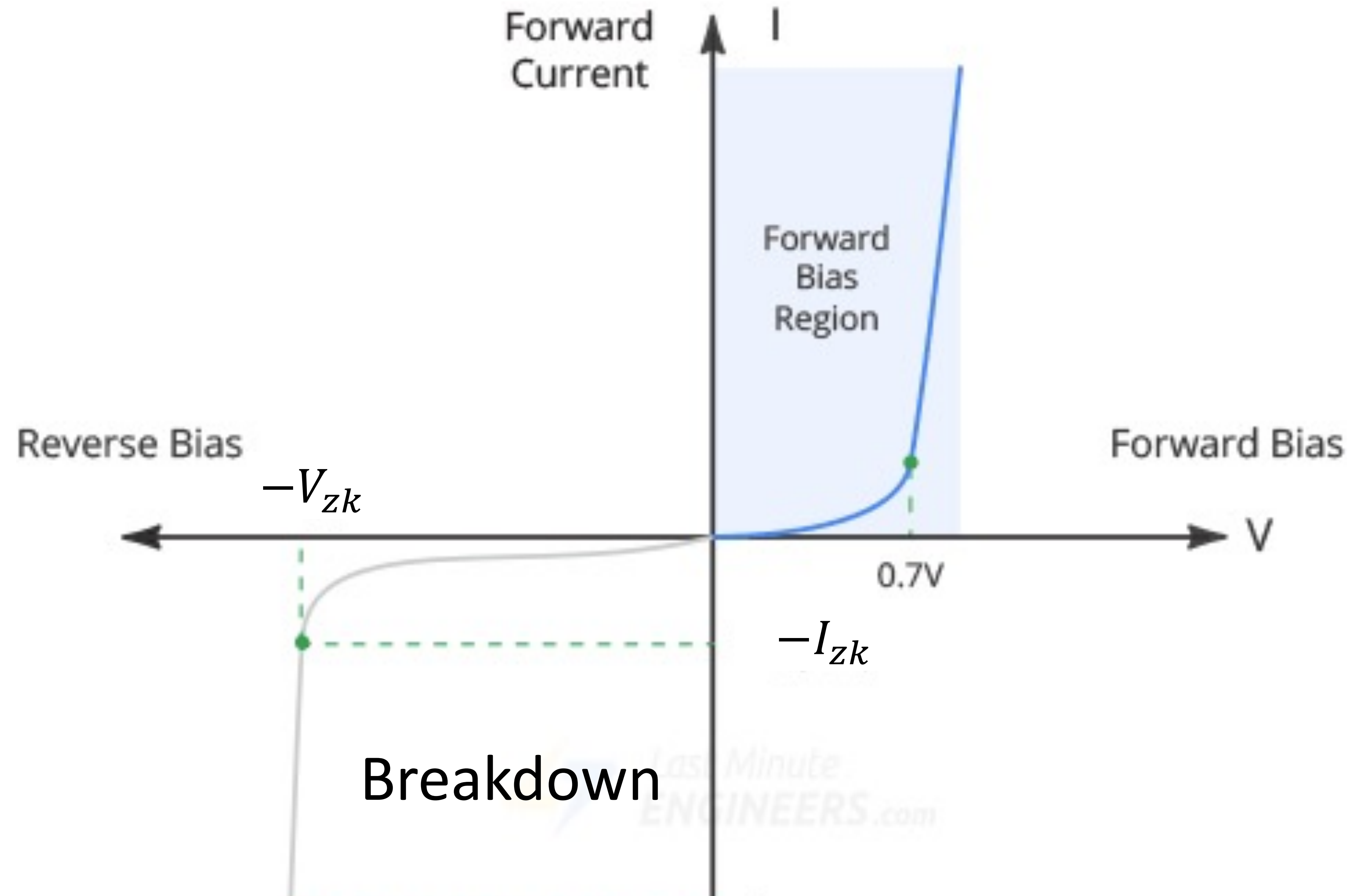
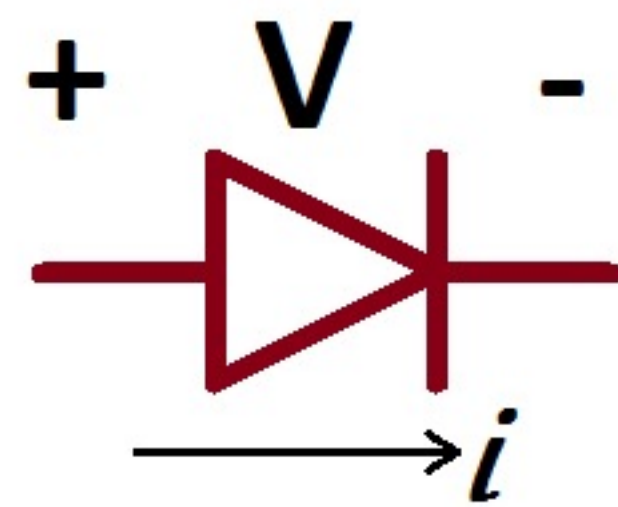


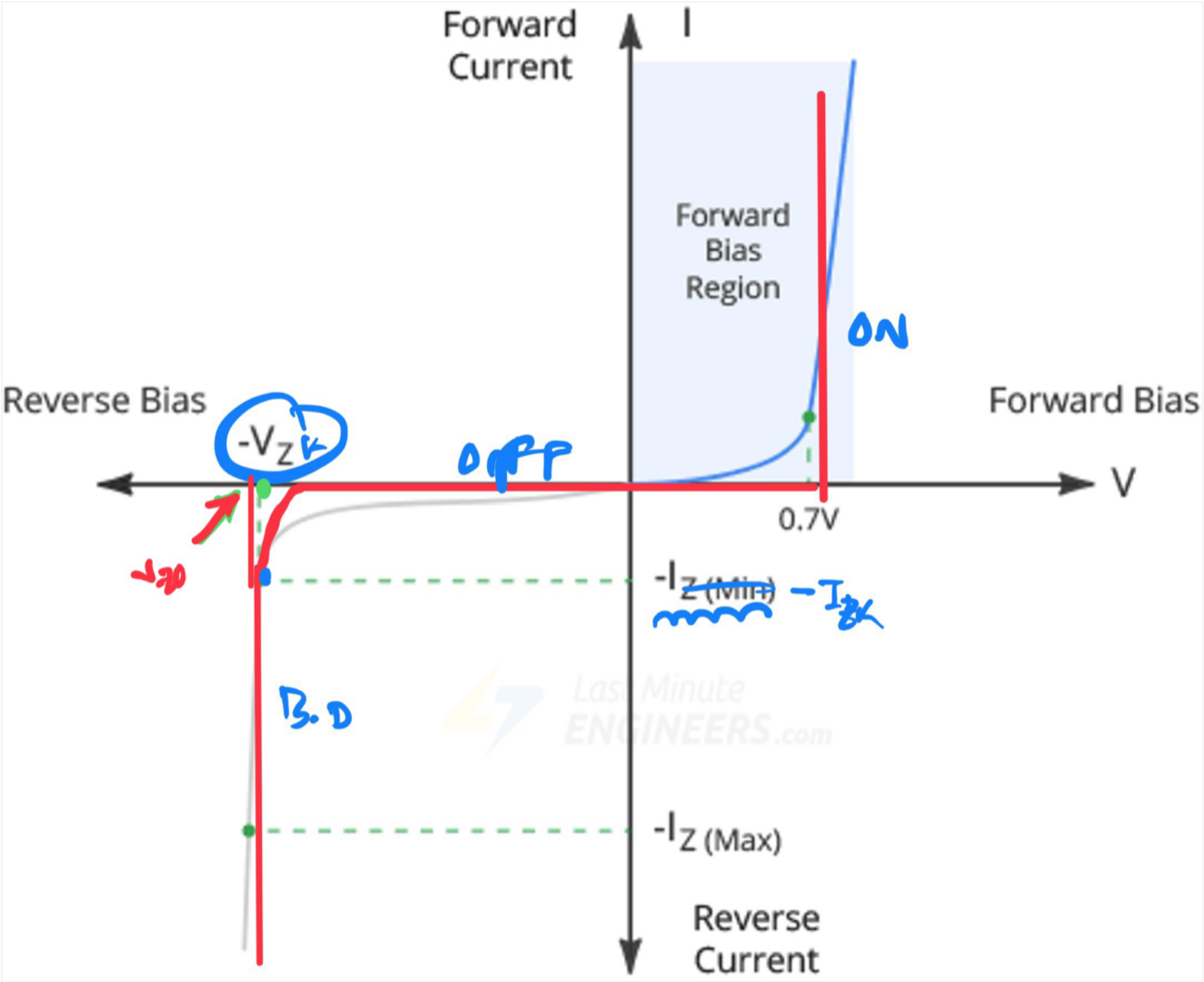
Diode in Reverse Bias

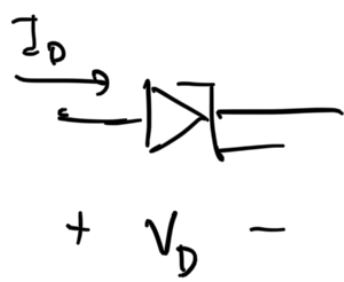


$$I = I_s \left(\exp \frac{V_d}{nV_T} - 1 \right) \approx -I_s$$

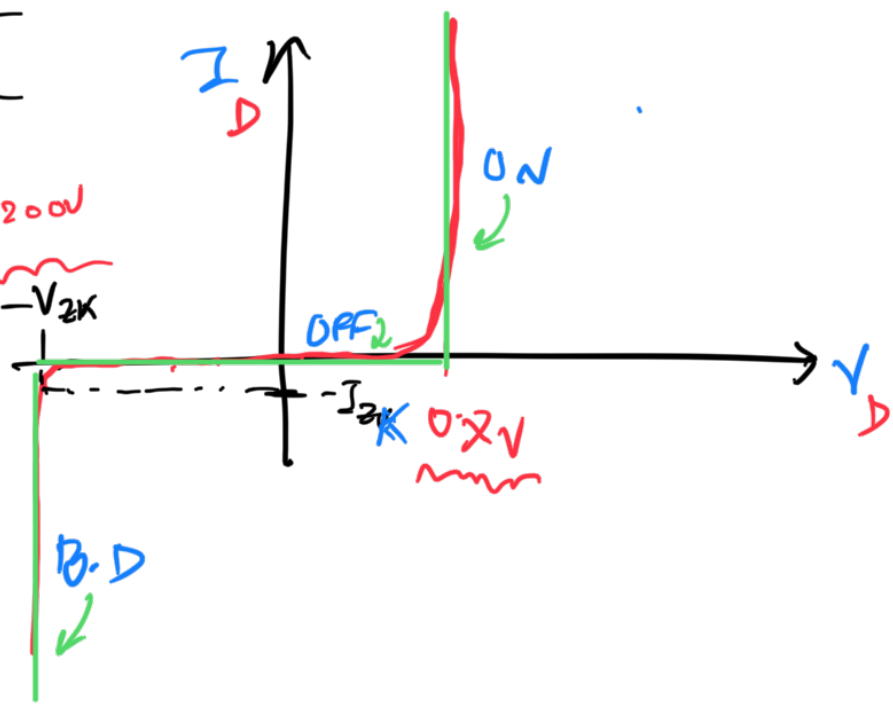


Zener Diode





Zener diode



Operation mode

ON

OFF

B.D.

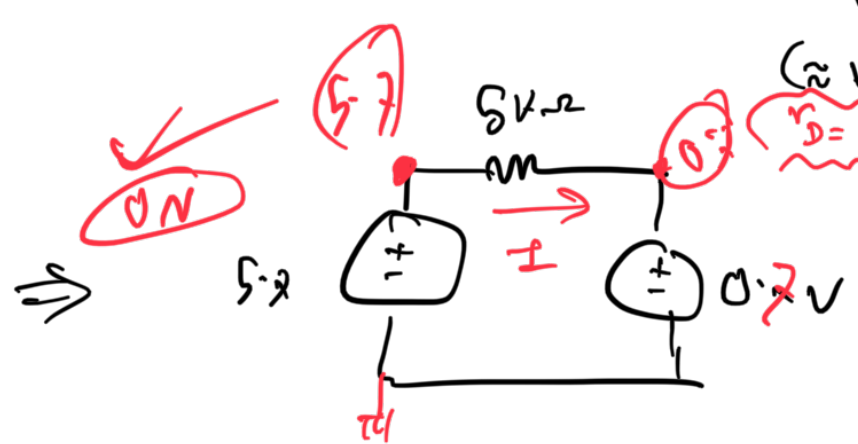
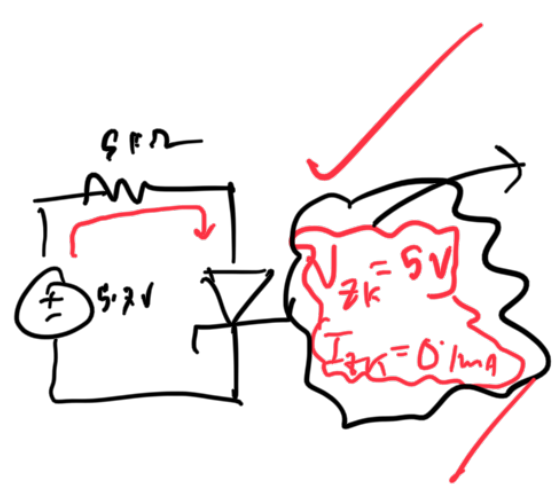
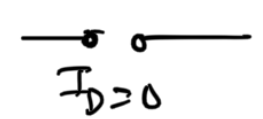
condition

$$I_D > 0$$

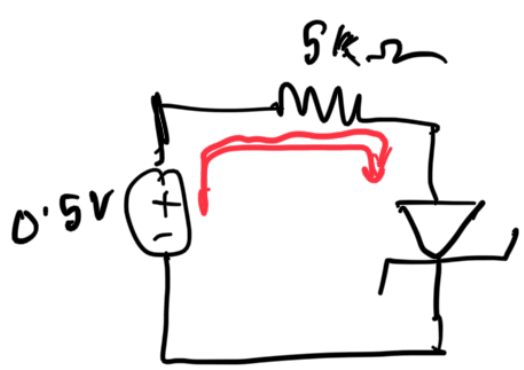
$$-V_{ZK} < V_D \leq 0.2V$$

$$I_D \leq -I_{ZK}$$

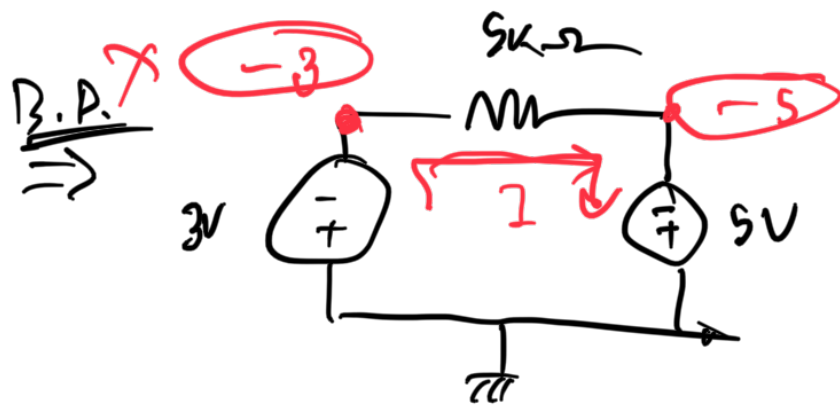
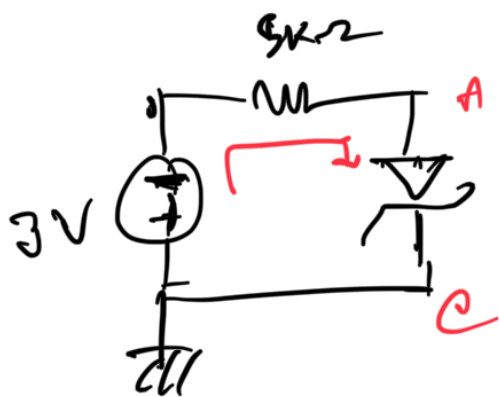
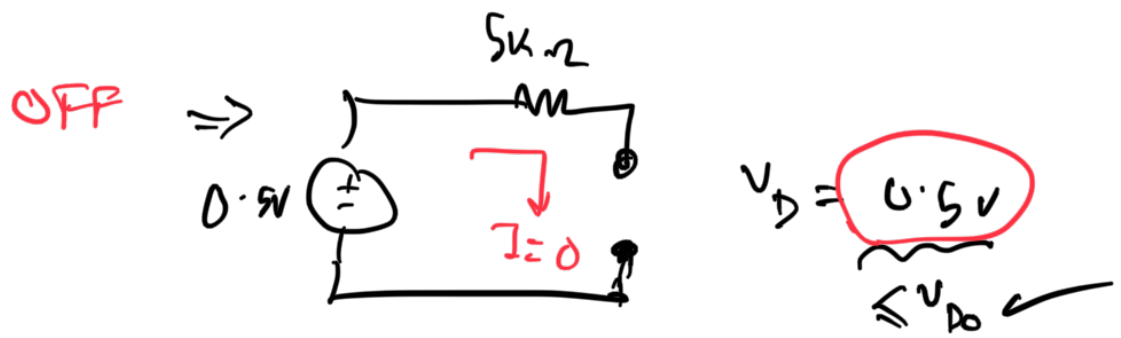
eqn / mode



$$I = \frac{5V - 0.2V}{5k\Omega} = 2mA$$



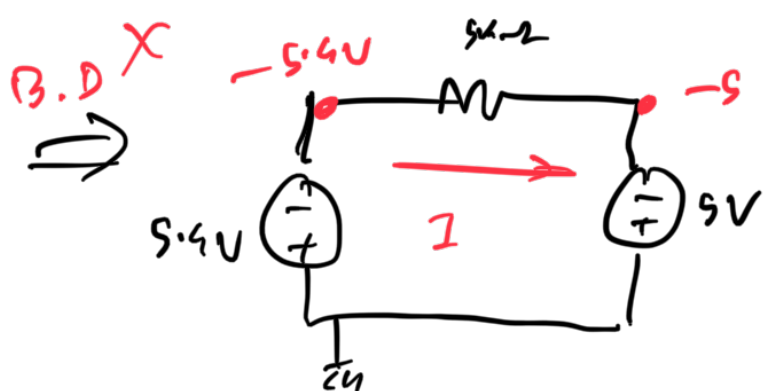
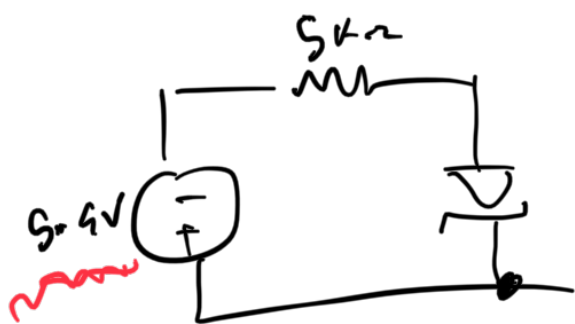
$$I = \frac{0.5V - 0.2V}{5k\Omega} = -0.06mA$$



$$I = \frac{-3 - (-5)}{5}$$

$$= 0.4 \text{ mA}$$

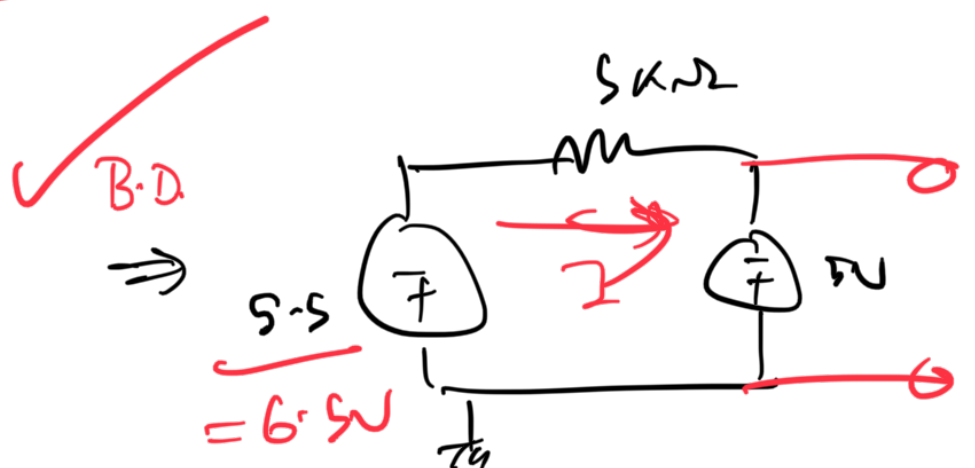
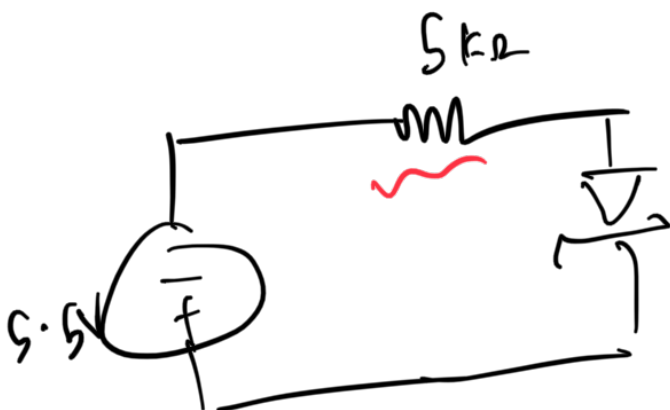
OFF



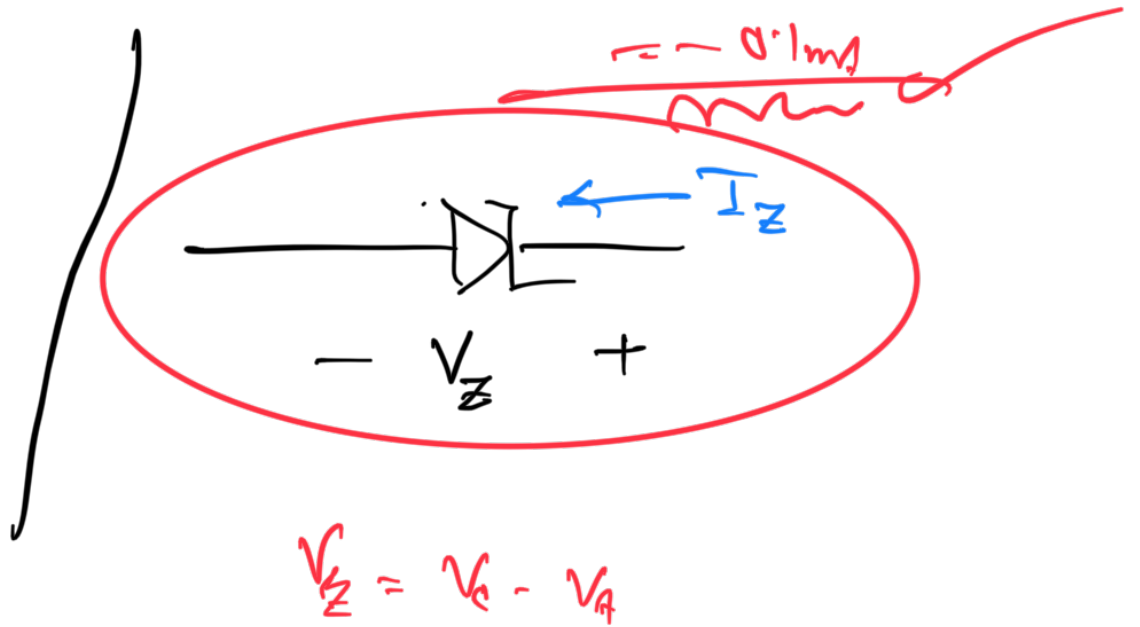
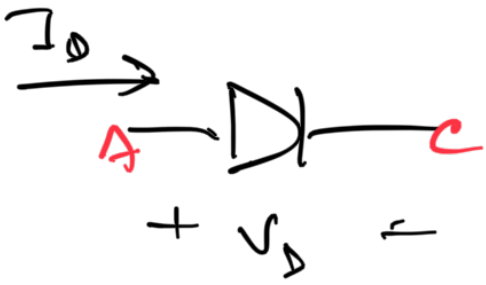
$$I = \frac{-5.4 - (-5)}{5k} = -0.08 \text{ mA}$$

$$-0.08 \Rightarrow -0.1$$

OFF!



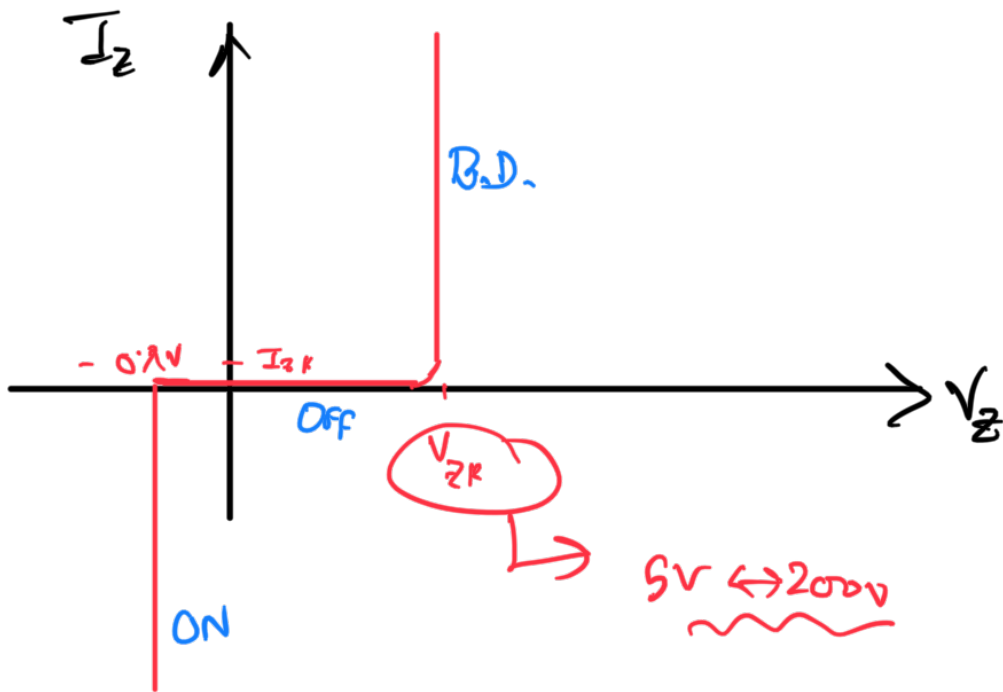
$$I = \frac{-5.5 - (-5)}{5k\Omega}$$



$$V_Z = V_C - V_A$$

$$I_Z = -I_D$$

$$V_Z = -V_D$$



Operation mode

ON

OFF

B.D

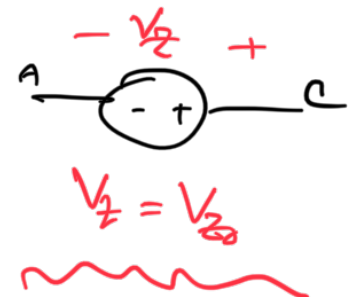
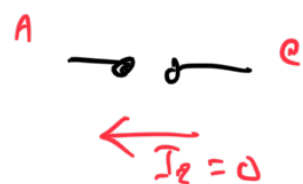
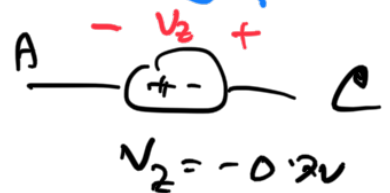
condition

$$I_Z < 0$$

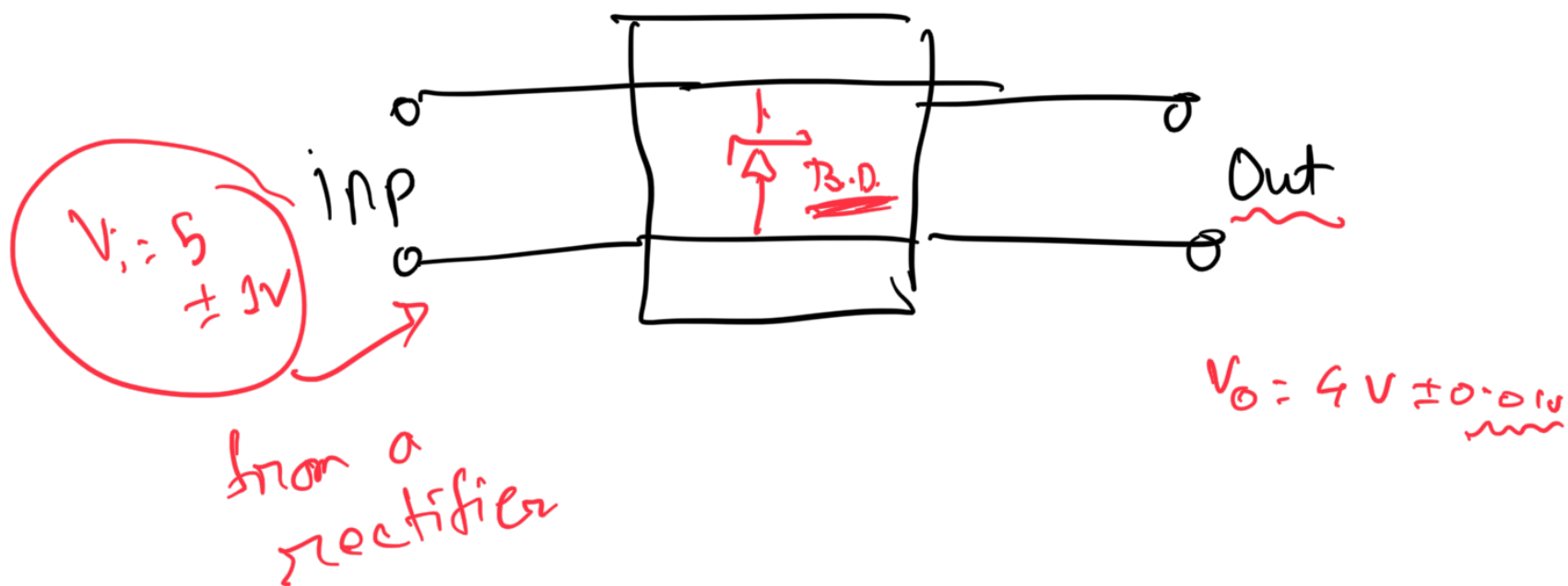
$$-0.2 \leq V_Z \leq V_{ZK}$$

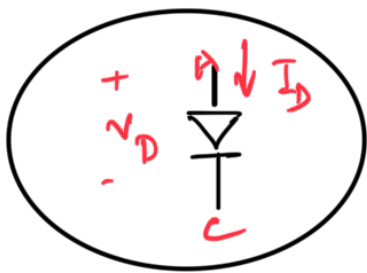
$$I_Z \geq I_{ZK}$$

eqn / mode



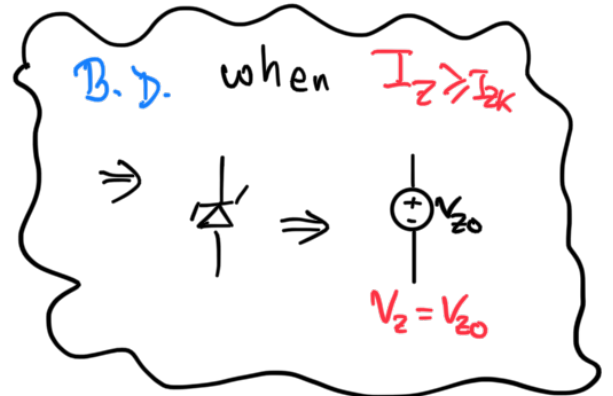
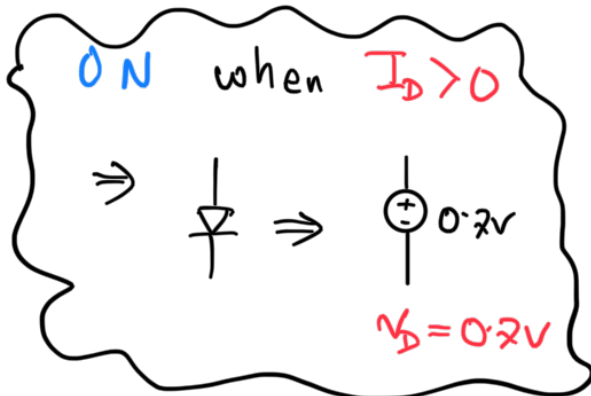
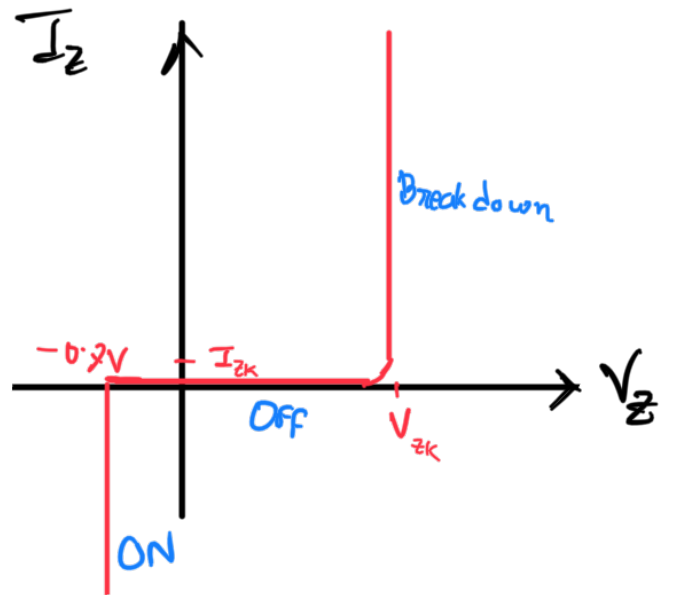
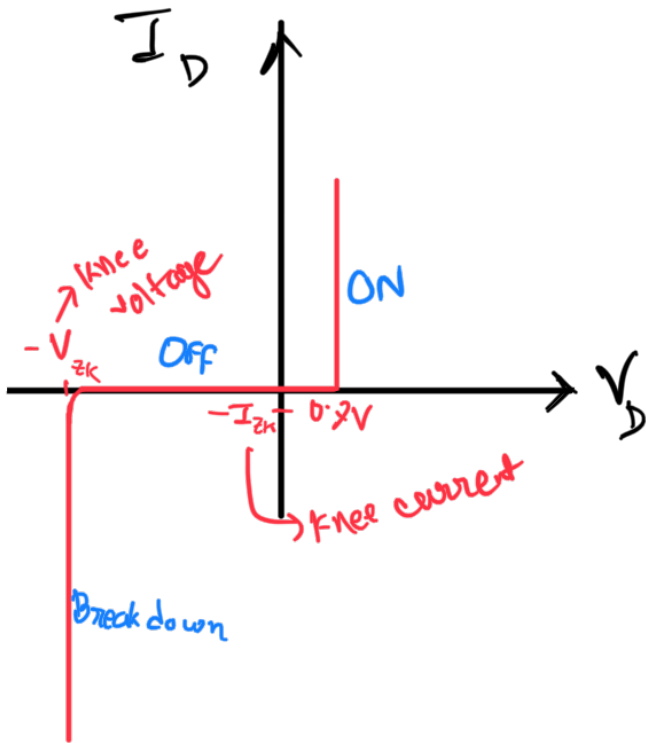
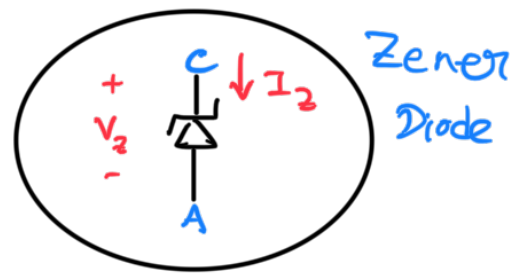
Regulator



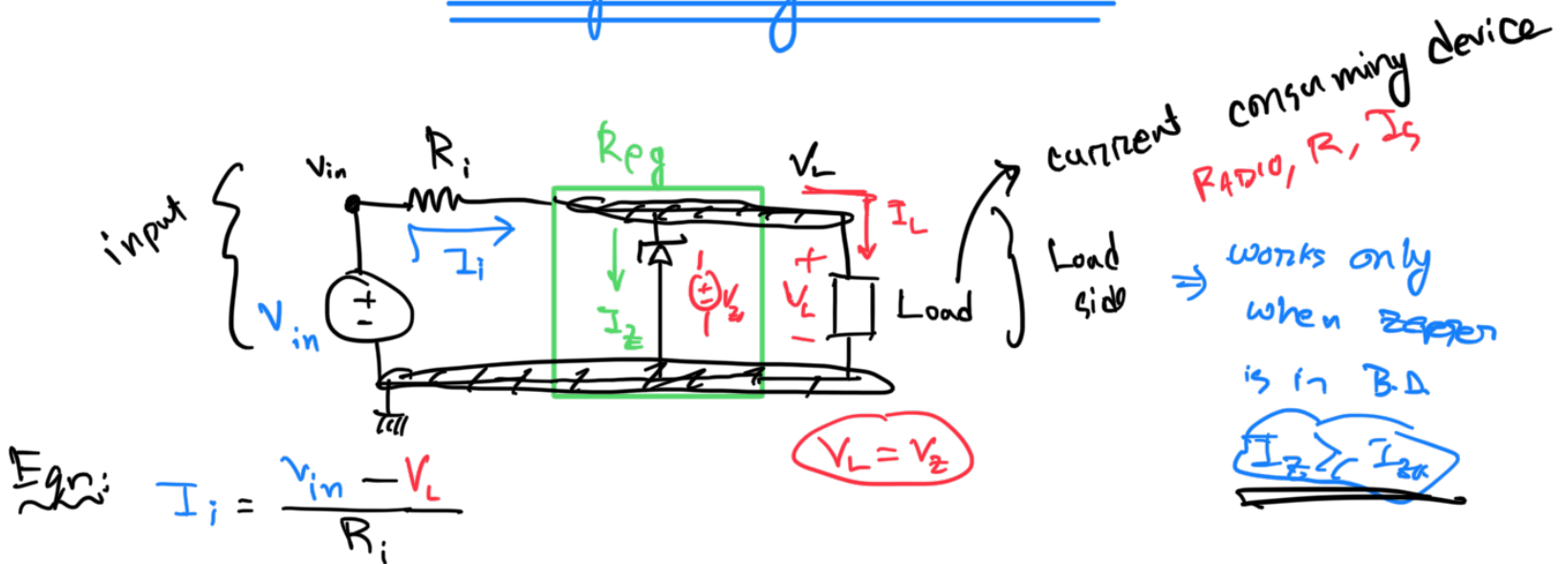


$$I_Z = -I_D$$

$$V_Z = -V_D$$



Application \Rightarrow Voltage Regulator



$$I_i = I_Z + I_L$$

$$\Rightarrow I_Z = I_i - I_L = \frac{V_{in} - V_L}{R_i} - I_L$$

$$V_{in} \uparrow \downarrow \Rightarrow I_Z \uparrow \downarrow$$

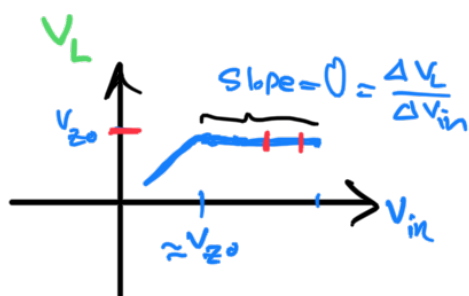
$$I_L \uparrow \downarrow \Rightarrow I_Z \downarrow \uparrow$$

For regulator to work, Zener MUST be in Break down

$$\Rightarrow I_Z > I_{ZK}$$

This means \Rightarrow ① V_{in} should be high
② I_L should be low

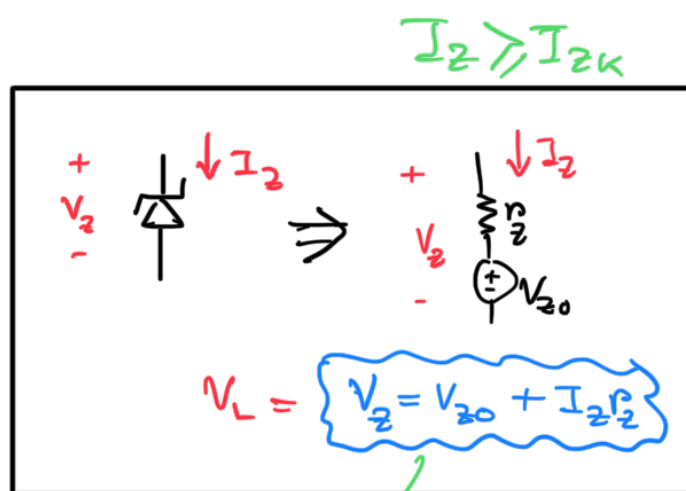
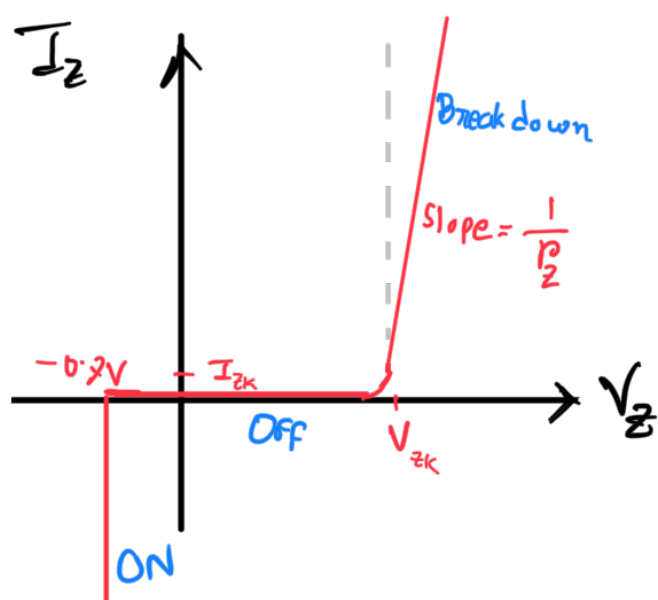
For regulator to work properly



Design Guideline: Make sure regulator works even in the worst case scenario

- ① $V_{in} = V_{in} (MIN)$
 - ② $I_L = I_L (MAX)$
 - ③ $I_Z = I_Z (MIN) = I_{ZK}$
- ~~$I_Z \leq I_Z (MAX)$~~

"REAL" Zener Diode



This implies V_Z changes with I_Z

Reminder: $V_{in} \uparrow \Rightarrow I_Z \uparrow$

$I_L \uparrow \Rightarrow I_Z \downarrow$



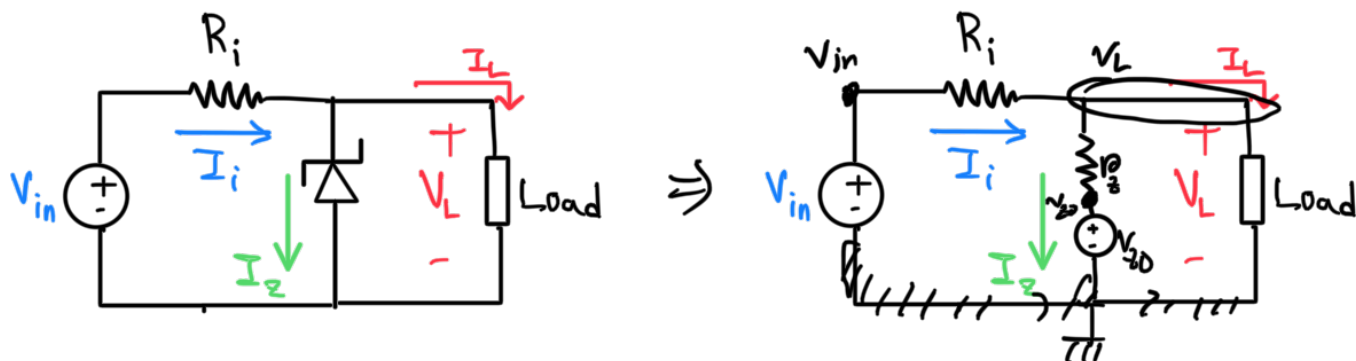
line regulation
 $\left[\frac{\Delta V_L}{\Delta V_{in}} \text{ (mV/V)} \right]$



load regulation
 $\left[\frac{\Delta V_L}{\Delta I_L} \text{ (mV/mA)} \right]$

What are the values of the slopes?

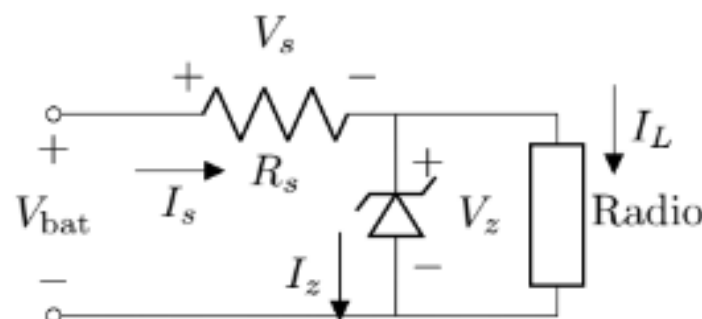
when the regulator is working



$$V_L = V_Z = \underbrace{\left(\frac{r_z}{R_i + r_z} \right) V_{in}}_{\text{line}} + \underbrace{\left(- \frac{r_z R_i}{R_i + r_z} \right) I_L}_{\text{load}} + \underbrace{\frac{R_i}{R_i + r_z} V_{Z0}}_{\text{const.}}$$

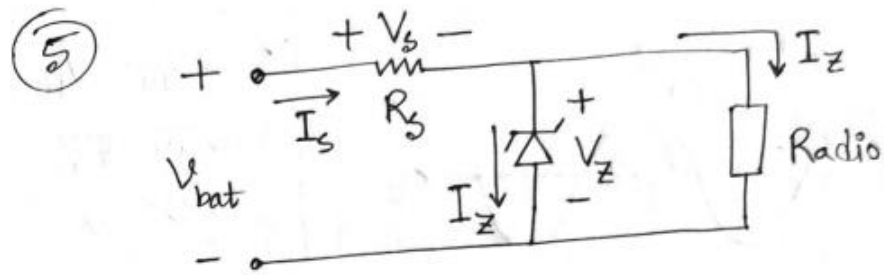
$$\therefore \text{Line regulation} = \frac{\Delta V_L}{\Delta V_{in}} = \frac{r_z}{R_i + r_z}$$

$$\therefore \text{Load regulation} = \frac{\Delta V_L}{\Delta I_L} = - \frac{r_z R_i}{R_i + r_z}$$



The circuit above is a voltage regulator used to power a car radio (which requires ≈ 9 V) from the car battery, V_{bat} whose voltage may vary between 11 and 13.6 V. The current in the radio, I_L , will vary between 0 (off) to 9 mA (full volume). The Zener diode in the circuit is specified with parameter $V_{z0} = 9$ V, $r_z = 0.05$ k Ω , and $I_{zk} = 1$ mA.

- Identify** the worst-case conditions and **calculate** the Zener current (I_z), Zener voltage (V_z), the input voltage (V_{bat}), and the load current (I_L) in this worst-case scenario. [1+1+1+1+1]
- Calculate** the current (I_s) and the voltage (V_s) the input resistor R_s in the worst-case scenario. [2]
- Design** the circuit, i.e., find the value of R_s , such that even in the worst-case scenario voltage regulation is maintained. Calculate the line regulation for this circuit. [2+1]



Given that, $V_{bat} = 11\text{ v} \sim 13.6\text{ v}$

$$I_L = 0 \sim 9\text{ mA}$$

$$V_{zo} = 9\text{ v}, \quad r_z = 0.05\text{ k}\Omega, \quad I_{zk} = 1\text{ mA}$$

① Worst case conditions:

$$\textcircled{1} V_{bat(\min)} = 11\text{ v}.$$

$$\textcircled{2} I_z(\min) = I_{zk} = 1\text{ mA}.$$

$$\text{So, } I_z = 1\text{ mA. (Ans)} \quad V_{bat} = 11\text{ v. (Ans)}$$

$$V_z = V_{zo} + I_z r_z$$

$$\hookrightarrow V_z = 9 + 1 \times 10^{-3} \times 0.05 \times 10^3$$

$$\hookrightarrow V_z = 9.05\text{ v. (Ans)}$$

$$I_L = I_{L(\max)} = 9\text{ mA}.$$

⑤ Applying KVL we get, $V_{bat} = V_s + V_z$
 $\hookrightarrow V_s = V_{bat} - V_z$
 $\hookrightarrow V_s = (11 - 9.05) \text{ V}$
 $\hookrightarrow V_s = 1.95 \text{ V. (Ans)}$

Applying KCL we get,

$$I_s = I_z + I_L$$

$$\hookrightarrow I_s = (1 + 9) \text{ mA}$$

$$\hookrightarrow I_s = 10 \text{ mA. (Ans)}$$

⑥ $R_s = \frac{V_s}{I_s} = \frac{1.95}{10 \times 10^{-3}} = 195 \Omega. (\text{Ans})$

Line Regulation,

$$\frac{\Delta V_L}{\Delta V_{bat}} = \frac{r}{r + R}$$

$$= \frac{0.05 \times 10^3}{0.05 \times 10^3 + 195} \text{ V/V}$$

$$= 0.20408 \text{ V/V}$$

$$= 204.08 \text{ mV/V. (Ans)}$$

here,

$$r = r_z = 0.05 \text{ k}\Omega$$

$$R = R_s = 195 \Omega$$