

①

a) $V_Z = V_{Z0} + I_Z r_Z$

$$\Rightarrow 5.75 = V_{Z0} + 5 \times 0.05$$

$$\Rightarrow V_{Z0} = 5.5 \text{ V}$$

⑥

$$V_S = \min = 9 \text{ V}$$

$$I_Z = I_{ZK} = 0.3 \text{ mA}$$

$$V_Z = V_{Z0} + I_Z r_Z \approx 5.6 \text{ V}$$

⑦

$$I_S = \frac{V_{in} - V_Z}{R_S} = \frac{9 - 5.5}{0.5} = 7 \text{ mA}$$

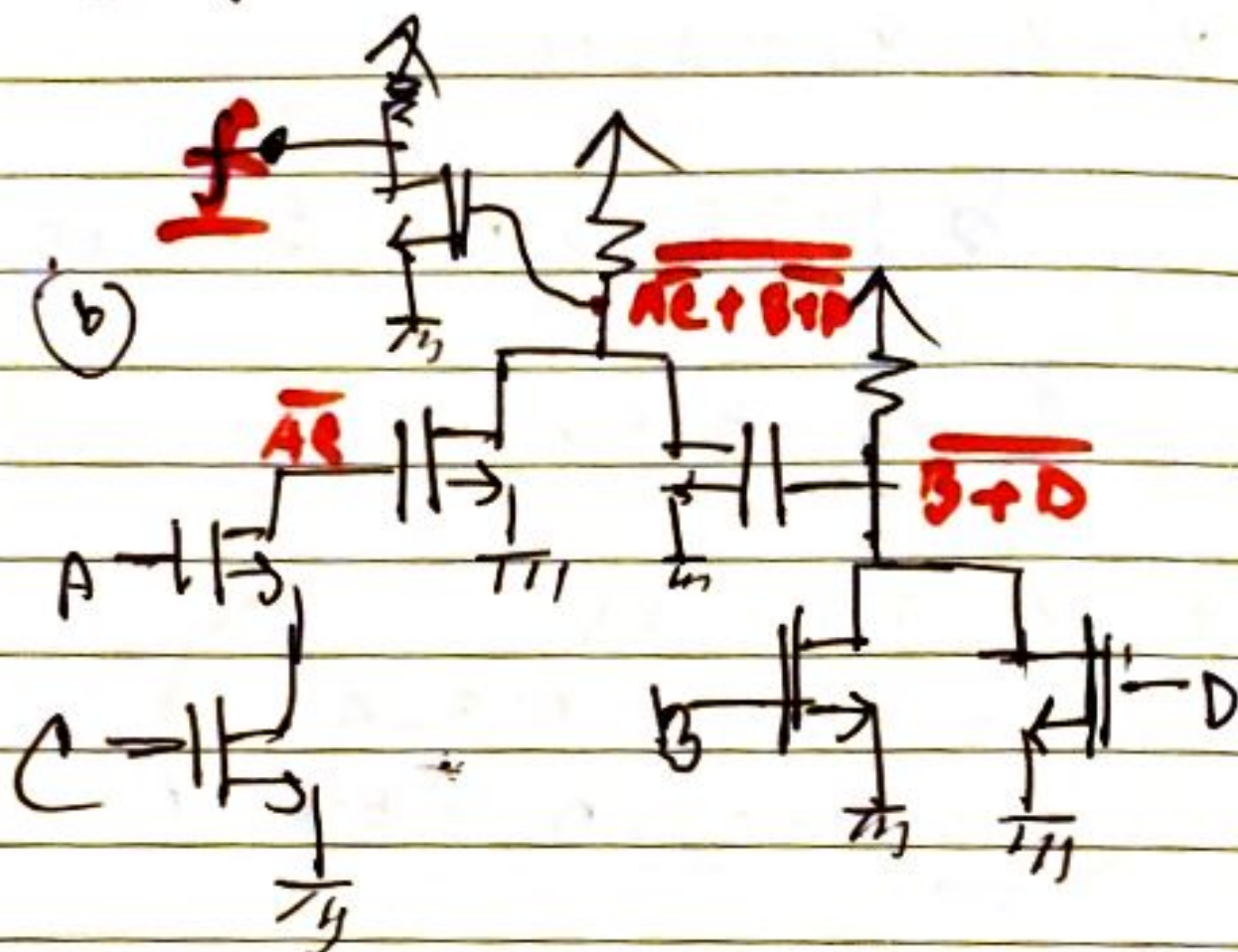
$$I_S = I_Z + I_L$$

$$\Rightarrow I_L = 6.7 \text{ mA}$$

⑧

$$R_L = \frac{V_Z}{I_L} = \frac{5.5}{6.7} \approx 0.8 \text{ k}\Omega$$

② a) $f = AB(C + \overline{D}E)$



$$I_B = \frac{I_C}{\beta} \Rightarrow \alpha I_E$$

③ ACTIVE

$$\text{KVL} \rightarrow 0 - (-15) = 20 I_B + V_{BE} + 2 I_E$$

$$\Rightarrow 15 = 20 \times \frac{\alpha}{\beta} I_E + 0.7 + 2 I_E$$

$$\Rightarrow I_E = 1.98 \text{ mA}$$

$$I_C = \alpha I_E = 1.96 \text{ mA}$$

$$I_B = I_E - I_C = 0.02 \text{ mA}$$

$$\text{KVL} \Rightarrow 15 - (-15) = 5 I_B + V_{CE} + 2 I_E$$

$$\Rightarrow V_{CE} = 6.34 \text{ V}$$

Verification

$$V_{CE} > 0.2 \text{ V}$$

④ ~~Ass~~ Saturation

$$\text{let } I_D = x$$

$$V_G = 5V$$

$$\frac{10 - V_D}{5} = x \Rightarrow V_D = 10 - 5x$$

$$\frac{V_S - 0}{3} = x \Rightarrow V_S = 3x$$

$$\therefore V_{DS} = V_D - V_S = 10 - 8x$$

$$V_{GS} = 5 - 3x$$

$$x = \frac{1}{2} \times 2x (5 - 3x - 1)^2$$

$$\Rightarrow x = 4^2 - 24x + 2x^2$$

$$\Rightarrow 2x^2 - 25x + 16 = 0$$

$$\Rightarrow x = 1, 1.778$$

smaller

$$\therefore I_D = 1 \text{ mA}$$

$$V_{DS} = 2V$$

$$V_{GS} = 2V$$

$$\therefore V_{ov} = 1V$$

Verification

$$V_{DS} > V_{ov} \checkmark$$

$$V_{GS} > V_2 \checkmark$$

~~$\begin{pmatrix} 1 \\ a \end{pmatrix} \frac{1}{2}$~~

a) $V_{20} = 5.5V$ [see set 1]

(b) Set - 1

$$I_z = 0.3 \text{ mA}$$

$$V_2 = 5.5V$$

$$V_{in} = 9V$$

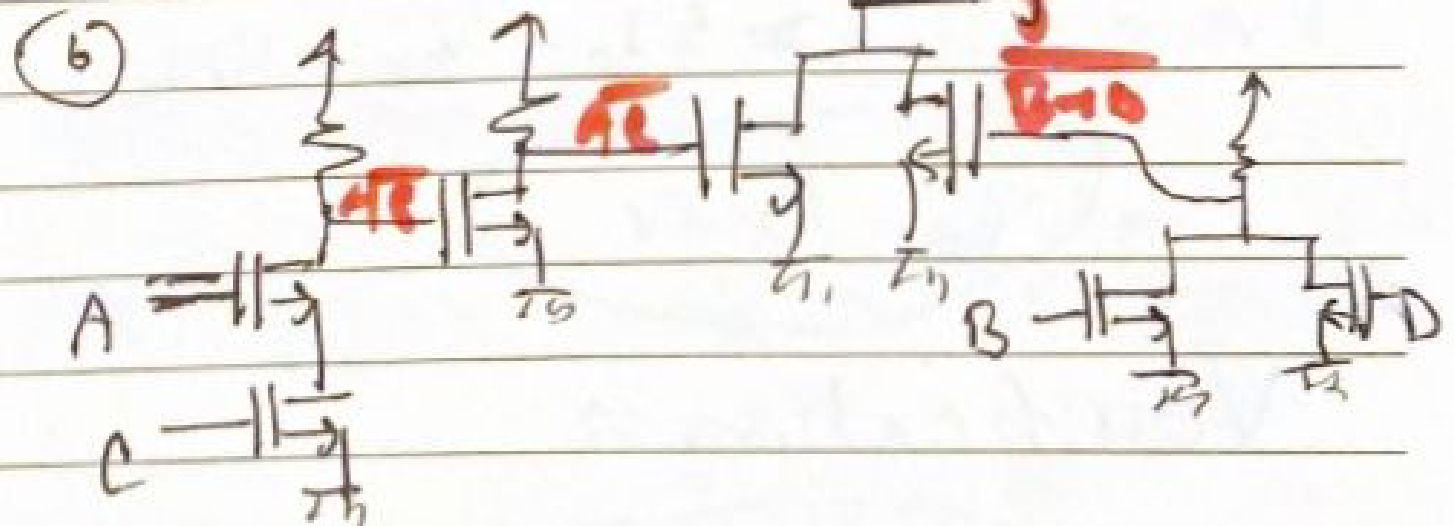
$$(a) I_L = \frac{V_Z}{R_L} = \frac{5.5}{10} = 0.55 \text{ mA}$$

$$I_s = I_L + I_z = 0.85 \text{ mA}$$

$$\textcircled{1} R_S = \frac{V_{in} - V_Z}{I_S} = \frac{9 - 5.5}{0.85} = \underline{\underline{4.375 \text{ k}\Omega}}$$

 $\frac{2}{10}$

(a) $(\bar{A}B + C)D$



$$I_B = \frac{I_C}{\beta} \Rightarrow \alpha I_E$$

③ ACTIVE

$$\text{KVL} \rightarrow 0 - (-15) = 20 I_B + V_{BE} + 2 I_E$$

$$\Rightarrow 15 = 20 \times \frac{\alpha}{\beta} I_E + 0.2 + 2 I_E$$

$$\Rightarrow I_E = 1.98 \text{ mA}$$

$$I_C = \alpha I_E = 1.96 \text{ mA}$$

$$I_B = I_E - I_C = 0.02 \text{ mA}$$

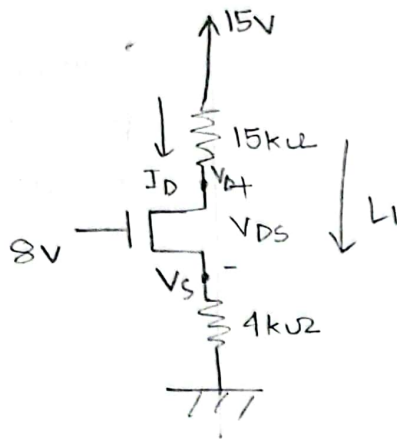
$$\text{KVL} \Rightarrow 15 - (-15) = 5 I_C + V_{CE} + 2 I_E$$

$$\Rightarrow V_{CE} = 6.34 \text{ V}$$

Verification

$$\underline{V_{CE} > 0.2 \text{ V}}$$

Answer to the Q^oN^o -4



Given

$$V_T = 1V$$

$$K_n' = 4mA/V^2$$

Assuming our circuit is in saturation region-

$$I_D = \frac{K_n'}{2} (V_{GS} - V_T)^2$$

$$= \frac{4}{2} (8 - V_S - 1)^2$$

$$= 2 (7 - V_S)^2$$

$$= 2 (49 - 14V_S + V_S^2)$$

$$I_D = 98 - 28V_S + 2V_S^2 \quad \text{--- i)}$$

$$I_D = \frac{V_S - 0}{4}$$

$$(98 - 28V_S + 2V_S^2) 4 = V_S$$

$$392 - 112V_S + 8V_S^2 - V_S = 0$$

$$8V_S^2 - 113V_S + 392 = 0$$

$$V_S = 8$$

$$\boxed{V_S = 6.125} \quad \text{[We will take smaller value]}$$

$$\therefore I_D = \frac{6.125}{4} = 1.53125 mA$$

Now to verify.

$$V_{DS} = V_D - V_S$$

$$I_D = \frac{15 - V_D}{15}$$

$$1.53125 = \frac{15 - V_D}{15}$$

$$\therefore V_D = -7.96875 \text{ V}$$

$$\begin{aligned}\therefore V_{DS} &= V_D - V_S \\ &= -7.96875 - 6.125 \\ &= -14.094 \text{ V}\end{aligned}$$

$$V_{DS} \geq V_{GS} - V_T$$

$$-14.094 \not\geq 1.875 - 1$$

$$-14.094 \not\geq 0.875$$

So our circuit is not in ~~act~~ saturation region.

Now let's assume the circuit is in triode region.

$$\begin{aligned}I_D &= K_n' [(V_{GS} - V_T)V_{DS} - \frac{1}{2}V_{DS}^2] \quad \left| \quad V_{GS} = 8 - V_S \right. \\ &= 4 [(8 - V_S)V_{DS} - \frac{1}{2}V_{DS}^2] \quad \text{--- (1)}\end{aligned}$$

Applying KVL along L_1 -

$$15 = I_D 15 + V_{DS} + I_D 4$$

$$15 = 19I_D + V_{DS}$$

$$\begin{aligned}V_{DS} &= 15 - 19I_D \\ \frac{15 - V_{DS}}{19} &= I_D\end{aligned}$$

$$\frac{15 + V_{DS}}{19} = I_D$$

$$V_{DS} = 15 - 19I_D$$

Substituting the value I_D in eqn 1)

$$\frac{15 - V_{DS}}{19} = 4 \left[(7 - V_{DS}) V_{DS} - \frac{1}{2} V_{DS}^2 \right]$$

Putting the value of I_D & V_{DS} in eqn i)

$$I_D = 4 \left[(7 - V_{DS})(15 - 19I_D) - \frac{1}{2} (15 - 19I_D)^2 \right]$$

Now-

$$I_D = \frac{V_{DS}}{4}$$

$$\therefore V_{DS} = 4I_D$$

$$I_D = 4 \left[(7 - 4I_D)(15 - 19I_D) - \frac{1}{2} (15 - 19I_D)^2 \right]$$

$$\begin{aligned} I_D &= 4 (15 - 19I_D) \left[7 - 4I_D - \frac{1}{2} (15 - 19I_D) \right] \\ &= 4(60 - 76I_D)(7 - 4I_D - 7.5 + 9.5I_D) \end{aligned}$$

$$I_D = (60 - 76I_D)(-0.5 + 9.5I_D)$$

$$I_D = -30 + 330I_D + 38I_D - 418I_D^2$$

$$-418I_D^2 + 367I_D - 30 = 0$$

$$I_D = 0.787 \text{ mA}$$

$$I_D = 0.091$$

$$\therefore V_{DS} = 0.364$$

For $I_D = 0.091$

$$V_{GS} > V_T$$

$$7.636 > 1$$

$$\therefore V_{DS} = 15 - 19 \cdot I_D$$

$$= 15 - 19 \cdot 0.091$$

$$= 13.271$$

$$V_{DS} < V_{GS} - V_T$$

$$13.271 < 6.636$$

Now for $I_D = 0.787$

$$V_{GS} > V_T$$

$$8 - 3.148 \geq 1$$

$$4.852 \geq 1$$

$$V_{DS} < V_{GS} - V_T$$

$$0.047 < 3.852$$

$$V_S = 4I_D \\ = 3.148 \text{ V}$$

$$V_{DS} = 15 - 19.0 \cdot 0.787 \\ \therefore V_{DS} = 0.047$$

So our MOSFET is in triode region.