

1. State which of the following are not the probability distributions of a random variable. Give reasons for your answer.

(i)

| | | | |
|------|-----|-----|-----|
| X | 0 | 1 | 2 |
| P(X) | 0.4 | 0.4 | 0.2 |

(ii)

| | | | | | |
|------|-----|-----|-----|------|-----|
| X | 0 | 1 | 2 | 3 | 4 |
| P(X) | 0.1 | 0.5 | 0.2 | -0.1 | 0.3 |

(iii)

| | | | |
|------|-----|-----|-----|
| Y | -1 | 0 | 1 |
| P(Y) | 0.6 | 0.1 | 0.2 |

(iv)

| | | | | | |
|------|-----|-----|-----|-----|------|
| Z | 3 | 2 | 1 | 0 | -1 |
| P(Z) | 0.3 | 0.2 | 0.4 | 0.1 | 0.05 |

2. Find the probability distribution of

- (i) number of heads in two tosses of a coin
- (ii) number of tails in the simultaneous tosses of three coins
- (iii) number of heads in four tosses of a coin

3. A coin is biased so that the head is 3 times as likely to occur as tail. If the coin is tossed twice, find the probability distribution of number of tails.

4. A random variable X has the following probability distribution.

| | | | | | | | | |
|------|---|---|----|----|----|----------------|-----------------|---------------------|
| X | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| P(X) | 0 | k | 2k | 2k | 3k | k ² | 2k ² | 7k ² + k |

Determine i) k ii) $P(X < 3)$ iii) $P(X > 6)$ iv) $P(0 < x < 3)$

5. The random variable X has probability distribution P(X) of the following form, where k is some number:

$$P(X) = \begin{cases} k, & \text{if } x = 0 \\ 2k, & \text{if } x = 1 \\ 3k, & \text{if } x = 2 \\ 0, & \text{otherwise} \end{cases}$$

(a) Determine the value of k.

(b) Find $P(X < 2)$, $P(X \geq 2)$, $P(X \geq 2)$.

6. Let X be a discrete random variable with a probability function

| | | | |
|-----------------|-----|-----|-----|
| Values of X : x | 1 | 4 | 9 |
| f(x) | 0.1 | 0.4 | 0.5 |

Find the mean of X, X^2 , \sqrt{X} and $2\sqrt{X}$.