

CSE 260

Assignment 02

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sec: 1 (NRT)

Ans to the q no 1

a

$$x'yz' + x'yz + xyz + x'yz'$$

$$= x'yz' + x'yz' + x'yz + xyz$$

$$= x'yz' + x'yz + xyz \quad [x + x = x]$$

$$= x'y(z' + z) + xyz \quad [x + x' = 1]$$

$$= x'y + xyz$$

$$= y(x' + xz)$$

$$= y(x' + x)(x' + z)$$

$$= y(x' + z)$$

$$= x'y + yz$$

$$[x + yz = (x + y)(x + z)]$$

b

$$(x' + y') (x + y)$$

$$= xx' + x'y + xy' + yy'$$

$$= 0 + x'y + xy' + 0 \quad [x, x' = 0]$$

$$= x'y + xy'$$

$$= x \oplus y$$

$$[AB' + A'B = A \oplus B]$$

c

$$(a' + b)' (a + b)'$$

$$= (a'' \cdot b') (a' \cdot b'') \quad [(x+y)' = x' \cdot y']$$

$$= (a \cdot b') (a' \cdot b)$$

$$[(x')' = x]$$

$$= (a \cdot a') (b \cdot b')$$

$$[x \cdot x' = 0]$$

$$= 0$$

Ans to the or no 2

$$(a) x'y' + xy'$$

$$= (x'y') + (xy') \quad [\text{Dual of the function}]$$

$$= (x+y) \cdot (x'+y) \quad [\text{complement literals}]$$

$$= xx' + xy + x'y + yy$$

$$= 0 + y(x+x') + y \quad [x \cdot x = x, x \cdot x' = 0]$$

$$= y + y \quad [x+x' = 1]$$

$$= y \quad (\text{Ans})$$

$$(b) (x' + y + z')(x' + y')(x + z')$$

$$= (x' \cdot y \cdot z') + (x' \cdot y') + (x \cdot z') \quad [\text{Dual}]$$

$$= (x \cdot y' \cdot z) + (x \cdot y) + (x' \cdot z) \quad [\text{complement literals}]$$

$$= x(y + y'z) + x'z$$

$$= x(y + y')(y + z) + x'z \quad [x + yz = (x + y)(x + z)]$$

$$= x(y + z) + x'z \quad [x + x' = 1]$$

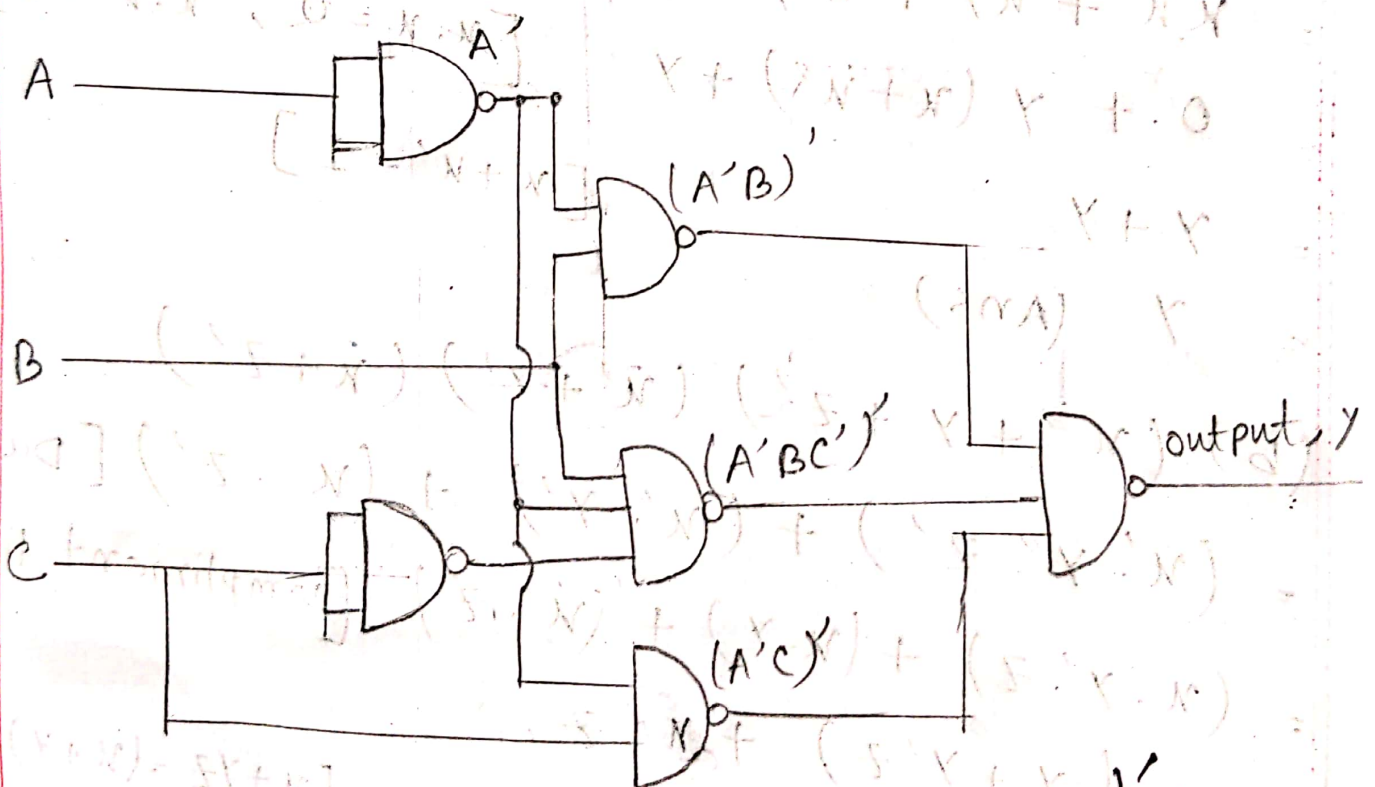
$$= xy + xz + x'z$$

$$= xy + z(x + x')$$

$$= xy + z \quad (\text{Ans})$$

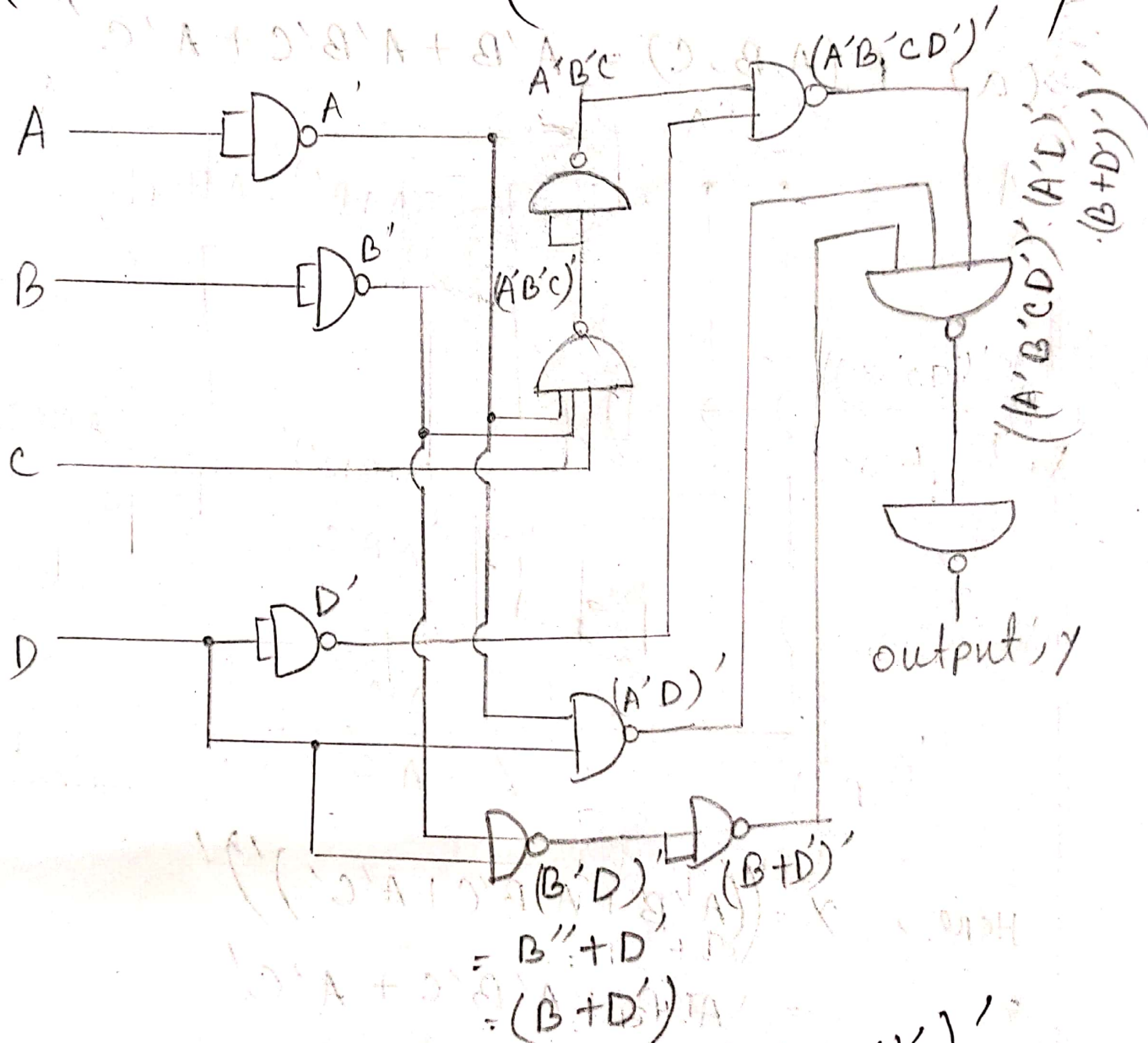
Ans to the or no (3)

$$(a) F(A, B, C) = A'B + A'BC' + A'C$$



$$\begin{aligned} \text{Here, } Y &= ((A'B)' \cdot (A'BC')' \cdot (A'C)')' \\ &= (A'B)'' + (A'BC')'' + (A'C)'' \\ &= A'B + A'BC' + A'C \end{aligned}$$

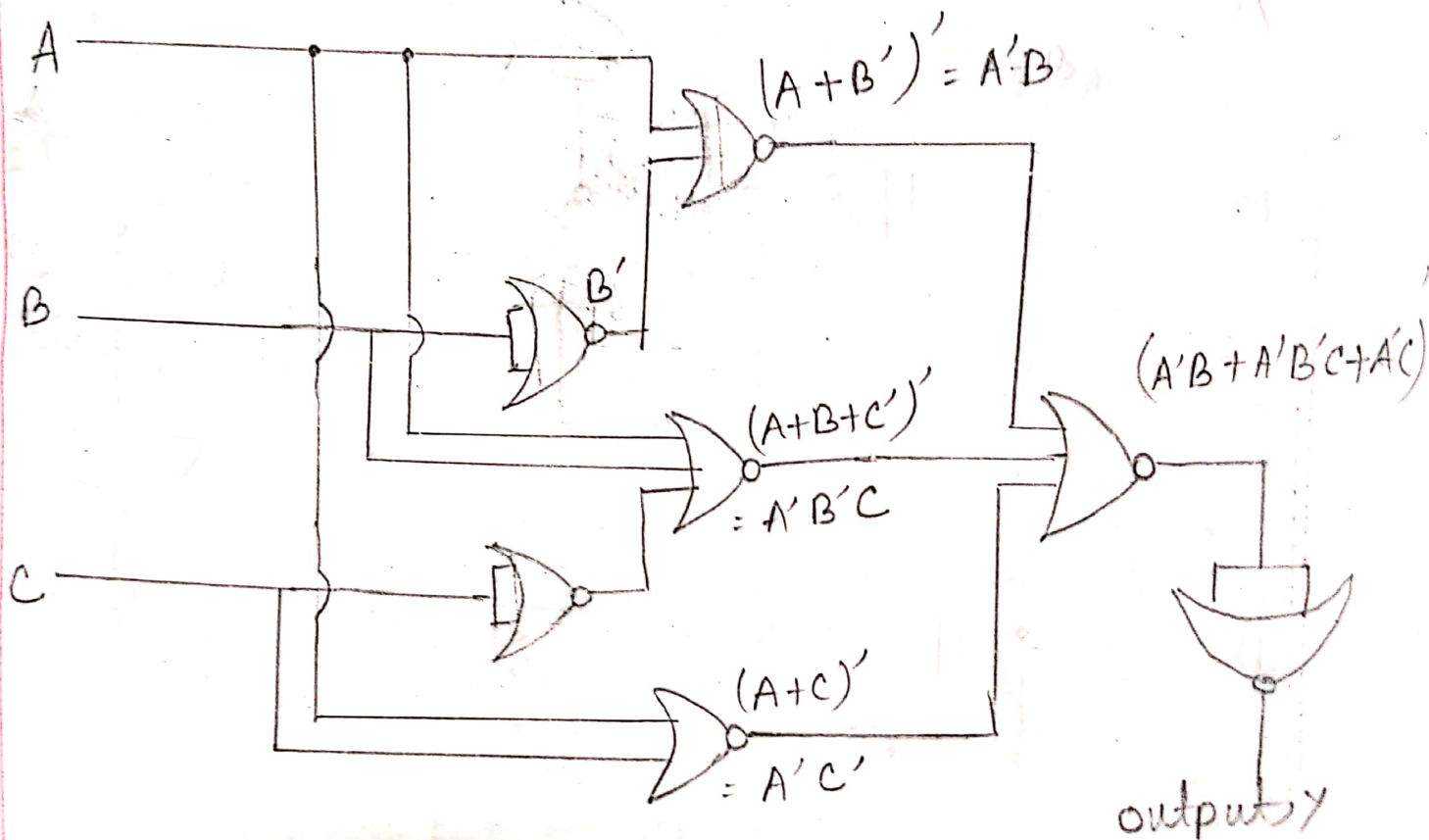
$$(b) F(A, B, C, D) = (A'B'CD' + A'D + (B+D'))'$$



$$\begin{aligned} \text{Here, } y &= ((A'B'CD')' \cdot (A'D)' \cdot (B+D')')' \\ &= (((A'B'CD')'' + (A'D)'' + (B+D')''))' \\ &= (A'B'CD' + A'D + (B+D'))' \end{aligned}$$

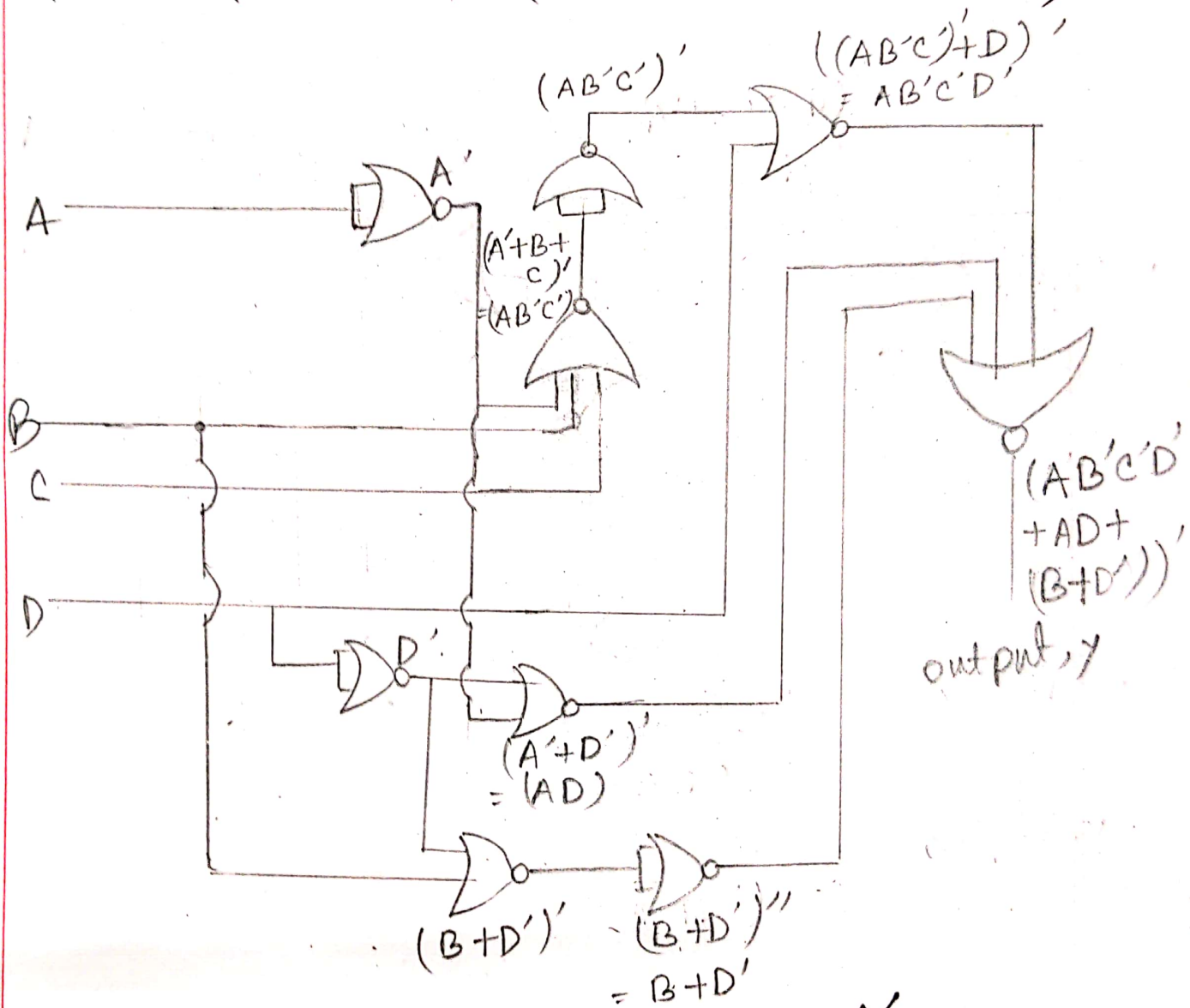
Ans to the q no 4

(a) $F(A, B, C) = A'B + A'B'C + A'C'$



Here, $y = ((A'B + A'B'C + A'C')')'$
 $= A'B + A'B'C + A'C'$

$$(b) \quad F(A, B, C, D) = (AB'C'D' + AD + (B+D'))'$$



$$\begin{aligned} \text{Here, } \gamma &= ((AB'C'D') + (AD) + (B+D'))' \\ &= (AB'C'D' + AD + (B+D'))' \end{aligned}$$