

A VLSI Array Processor for 16-Point FFT

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Abstract—This paper describes an implementation of a two-dimensional array processor for fast Fourier transform (FFT) using a 2- μ m CMOS technology. The array processor, which is dedicated to 16-point FFT, implements a 4×4 mesh array of 16 processing elements (PE's) working in parallel. Design considerations both in chip level and in PE level have been examined. A layout design methodology based on bit-slice units (BSU's) results in a very simple design and easy debugging, as well as a regular interconnection scheme through abutment. It contains about 48 000 transistors on an area of 53.52 mm², excluding the 83-pad area, and operation is on a 15-MHz clock. The array processor performs 24.6 million complex multiplications per second, and computes a 16-point FFT in 3 μ s.

I. INTRODUCTION

RECENT advances in very large scale integration (VLSI) technology make the implementation of array processors technologically realizable and economically feasible. So, a new approach adopting algorithm-based VLSI array processors is becoming increasingly competitive for real-time digital signal processing (DSP) and image processing applications [1].

The fast Fourier transform (FFT) is probably one of the most important algorithms in DSP applications. There are two approaches for computing this transform: software implemented on a programmable DSP [2], [3], [23], [24], and dedicated FFT processor development [4]–[6]. Real-time DSP favors the use of the latter, which offers parallel processing capability.

In this paper, a dedicated array processor implementation is described. As known, the FFT algorithm requires global data exchanges for butterfly computation, thus the direct implementation of the FFT flow graph onto silicon is considered to be inefficient because of its inherent communication cost in terms of area and time. To achieve area-efficient implementation of the FFT with a high degree of regularity and parallelism, we utilize two-dimensional mesh array of processing elements (PE's).

This paper is organized as follows. Section II describes design considerations. Then an algorithm to compute

FFT using half-butterfly arithmetic (HBA) will be presented in Section III. Section IV will describe the circuit and layout design. Finally, fabrication and some measurement results will be discussed in Section V.

II. DESIGN CONSIDERATIONS

This section discusses design considerations for our FFT array processor including chip architecture, the arithmetic function of a PE, and time complexity.

A. Chip Architecture

A number of approaches for FFT implementation are known including an FFT network [7], a perfect-shuffle network [8], a 2-D mesh array [9]–[12], pipelined architectures utilizing delay commutator [13] or systolic elevator [14], and a 1-D systolic DFT array [15]. Table I compares these architectures in terms of area, time, and regularity. From Table I, it is easily found that the FFT network and the perfect-shuffle network are not suitable for VLSI realization since irregular interconnections between PE's dominate the chip area. The pipelined architectures utilizing delay commutator or systolic elevator require additional hardware overhead of $O(N \log N)$ for the data shuffling of N -point FFT.

Our design goal in the architectural level is to determine a parallel architecture satisfying the following criteria: 1) highly parallel processing capability; 2) architectural regularity; 3) local data communications; and 4) no hardware overhead for data shuffling operation. Since the minimization of chip area with architectural regularity is considered much more important than any other factors in VLSI design, we choose the 2-D mesh array shown in Fig. 1(a) as the chip architecture.

B. Arithmetic Function of PE

In the implementation of a 2-D mesh array for FFT, careful examinations into the trade-offs between the number of PE's, the arithmetic function of PE, and control complexity should be made.

When N -point FFT is computed using a 2-D mesh array having M (where $2M \leq N$) PE's whose arithmetic functions are the usual radix-2 butterfly [22], each PE requires $P = N/M$ data storages, and each datum should be identified using $O(\log_2 N)$ bits of address in order to control data shuffling operations through $\log_2 N$ butterfly stages. In this case, all PE's participate in butterfly computations. Note that a 2-D mesh array of $N/2$

Manuscript received May 21, 1990; revised April 22, 1991.

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IEEE Log Number 9101784.

TABLE I
COMPARISON OF VARIOUS PARALLEL ARCHITECTURES FOR FFT COMPUTATION

| | FFT network [7] | Perfect shuffle network [8] | 2-D mesh array [9]–[12] | Parallel arch. using DC's [13] | Parallel arch. using SE's [14] | 1-D systolic DFT array [15] |
|--|-----------------|-----------------------------|-------------------------|--------------------------------|--------------------------------|-----------------------------|
| Number of PE's | $(N/2)\log N$ | $N/2$ | N | $\log N$ | $N \log N$ | $2N - 1$ |
| Butterfly steps | pipelined | $\log N$ | $\log N$ | pipelined | pipelined | pipelined |
| Interconnection area | $O(N)$ | $O(N^2/\log^2 N)$ | No area | No area | No area | No area |
| Data shuffling time | $O(\log N)$ | $O(\log N)$ | $O(\sqrt{N})$ | $O(N)$ | $O(N)$ | $O(N)$ |
| Interconnection regularity | irregular | irregular | very regular | regular | regular | very regular |
| Additional hardware for data shuffling | No | No | No | $O(N \log N)$ DC's | $O(N \log N)$ SE's | No |
| Dominant factor | Time | Pipelined | Butterfly steps | pipelined | pipelined | pipelined |
| | Area | interconnection | interconnection | PE's + DC's | PE's + SE's | PE's |

PE's: Processing Elements, DC's: Delay Commutators, SE's: Systolic Elevators

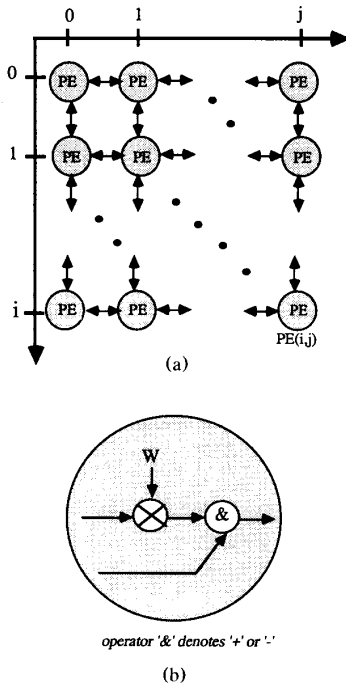


Fig. 1. (a) Two-dimensional mesh array for FFT computation. (b) Arithmetic function of a PE.

PE's for N -point FFT computation is considered to be a special case with $P = 2$.

On the other hand, a 2-D mesh array composed of N PE's whose arithmetic function is also the usual radix-2 butterfly [19] can perform data shuffling operation without $O(\log_2 N)$ bits of address. It, however, reveals some inefficiencies as follows: a) it requires data reshuffling operations after butterfly computation; and b) only half of the PE's in the array participate in butterfly computation.

In order to resolve these problems inherent in 2-D mesh array implementation for FFT, we make a compromise by adopting half-butterfly arithmetic (HBA) [16] as

the arithmetic function of PE (see Fig. 1(b)), rather than the usual radix-2 butterfly. The HBA takes its name from the definition given in (1), which represents half of the conventional radix-2 butterfly:

$$\text{HBA} = f(q-1, k) \& f(q-1, k + D(q)) \cdot W^{P^q} \quad (1)$$

where

$$q = 1, 2, 3, \dots, \log_2 N$$

$$W^{P^q} = \exp(-j2\pi p^q t / N).$$

In (1), the operator "&" denotes either "+" (addition) or "-" (subtraction) and $D(q)$ represents the shuffling distance of the q th butterfly stage. An algorithm for computing FFT using HBA will be described in Section III.

The adoption of HBA as the arithmetic function of PE results in a simple control which does not require $O(\log_2 N)$ bits of address, as well as 100% PE utilization (i.e., no idle PE's during butterfly computation) and no data reshuffling. These facts reveal the merits of using the HBA concept.

C. Time Complexity

The time required to compute N -point FFT can be evaluated in terms of total time for data shuffling and butterfly arithmetic through $\log_2 N$ butterfly stages. A summation of the time contributions of all shuffling distances will give the total shuffling time of $2(\sqrt{N} - 1)T_s$, if a unit shuffling distance takes time T_s . Also, the total time for butterfly arithmetic will be given by $T_{hb} \log_2 N$, where T_{hb} represents the times for HBA. Both T_{hb} and T_s can be considered to be a unit clock if the HBA is implemented with parallel arithmetic.

Asymptotically, however, $2(\sqrt{N} - 1)T_s + T_{hb} \log_2 N$ can be reduced to $O(\sqrt{N})$, since T_s and T_{hb} are independent of N . This fact suggests that a bit-parallel communication scheme between PE's is preferable.

III. ALGORITHM FOR FFT COMPUTATION ON THE ARCHITECTURE

This section describes an algorithm for FFT computation using HBA. A procedure for computing a 16-point

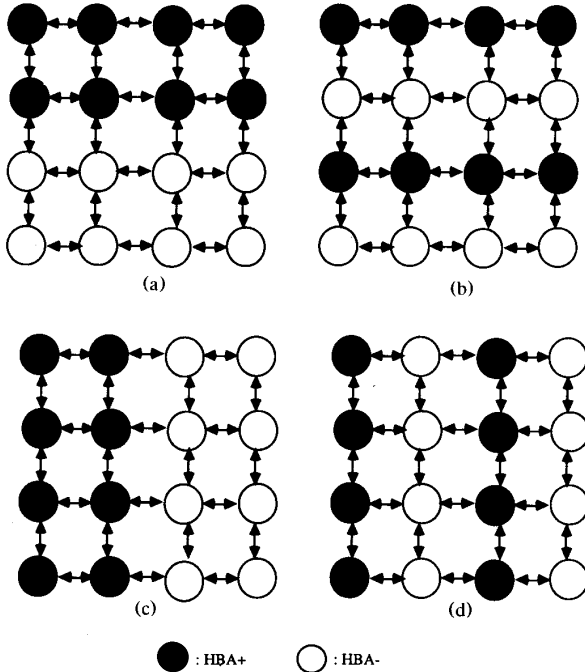


Fig. 2. Sixteen-point FFT computation using HBA: (a) first butterfly stage ($q = 1$), (b) second butterfly stage ($q = 2$), (c) third butterfly stage ($q = 3$), and (d) fourth butterfly stage ($q = 4$).

FFT is described as follows:

```

BEGIN
  FOR  $q = 1$  TO 4 DO IN PARALLEL for all PE's
    BEGIN
      data shuffling (ALGORITHM I)
      HBA computation (ALGORITHM II)
    END
  END.

```

Initially, 16 input data are loaded into the array in row-major order. Then, data shuffling and HBA computation are repeated through four (i.e., $\log_2 16$) butterfly stages according to the Algorithms I and II, respectively (see the Appendix). After the fourth butterfly stage has been completed, the array pipes out the results and accepts new input data in parallel and pipelined fashion through each of the four boundary PE's.

Fig. 2 visualizes these procedures. In the first butterfly stage (Fig. 2(a)), PE's in the first row send and receive data to and from the PE's in the third row; at the same time, the PE's in the second row send and receive data to and from the PE's in the fourth row. It takes two units of time to carry out this data shuffling operation because shuffling distance is 2. Then, the PE's in the first and second rows denoted as black circles compute HBA+, and the PE's in the third and fourth rows denoted as white circles compute HBA-. Similar operations are repeated in the second (Fig. 2(b)), third (Fig. 2(c)), and fourth (Fig. 2(d)) butterfly stages.

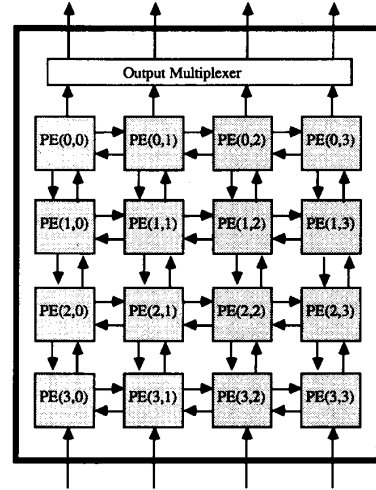


Fig. 3. Chip architecture.

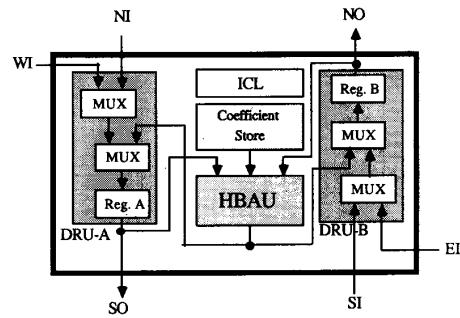


Fig. 4. Internal block diagram of PE.

IV. CIRCUIT AND LAYOUT DESIGN

A. Circuit Design

The chip architecture is a mesh array of 16 PE's as shown in Fig. 3. A PE consists of five blocks: two data routing units (DRU's), an HBA unit (HBAU), a coefficient store, and an internal control logic (ICL), as shown in Fig. 4.

The DRU's perform data communications with four nearest-neighbor PE's to perform data shuffling. It is composed of two multiplexers (MUX's) and a pipeline register. The MUX in the DRU controls data shuffling directions (i.e., vertical data shuffling or horizontal data shuffling). The pipeline register can be reconfigured depending on control inputs to serve three purposes. In data shuffling mode, it behaves as a parallel-in, parallel-out (PIPO) register to provide bit-parallel data communication with neighboring PE's. During the HBA computation, the pipeline register is reconfigured into a parallel-in, serial-out (PISO) register to carry out arithmetic shift right. Also, in self-testing mode, it is reconfigured into a linear feedback shift register (LFSR) to generate pseudo-random test patterns.

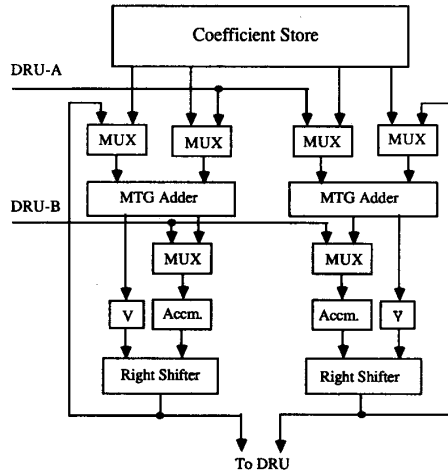


Fig. 5. Internal structure of the HBAU.

Fig. 5 shows the internal block diagram of the HBAU, which implements the HBA of (1) using the distributed arithmetic concept [17]. Using W -bit, fixed-point, fractional two's complement arithmetic, (1) is expressed by the distributed arithmetic as follows:

$$\begin{aligned} \text{Re}\{\text{HBA}\&\} &= A_r \& 2^{-(W-1)} K_i + \sum_{n=0}^{W-1} Q_{rn} 2^{-n} \\ \text{Im}\{\text{HBA}\&\} &= A_i \& 2^{-(W-1)} K_r + \sum_{n=0}^{W-1} Q_{in} 2^{-n} \end{aligned} \quad (2)$$

where

$$\begin{aligned} A_r &= \text{Re}\{f(q-1, k)\}, & A_i &= \text{Im}\{f(q-1, k)\} \\ B_r &= \text{Re}\{f(q-1, k + D(q))\}, \\ B_i &= \text{Im}\{f(q-1, k + D(q))\}. \end{aligned}$$

In (2), $f(q-1, k)$ and $f(q-1, k + D(q))$ represent the intermediate results obtained from the $(q-1)$ th butterfly stage, and subscript n represents the n th bit of B_r and B_i . Also, the Q_{rn} and Q_{in} are coefficients whose values are determined by an EXCLUSIVE-OR (XOR) and EXCLUSIVE-NOR (XNOR) combination of B_{rn} and B_{in} . All the values for Q_{rn} and Q_{in} in (2), which vary depending on not only the position of PE but also the butterfly stage q , are precomputed and stored within each PE.

From (2) it is known that the HBA implementation based on the distributed arithmetic requires W addition steps, and the results obtained from the distributed arithmetic are combined with A_r and A_i to complete the HBA.

As shown in Fig. 5, the HBAU is implemented with two identical parts: one is responsible for the real part of HBA& and the other is for the imaginary part of HBA&. As a result, the HBAU is simply realized with only two adders. Among various adder structures, we choose a modified transmission gate adder (MTGA) [3] in order to minimize chip area. A 1-b MTGA requires only 16 tran-

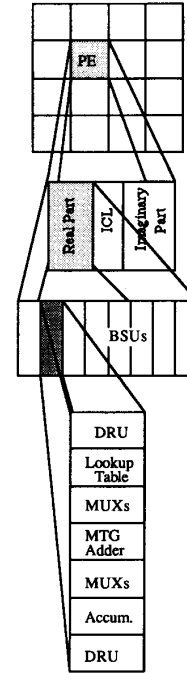


Fig. 6. Layout design hierarchy.

sistors which have no connections to power or ground. Since it allows all drain and source regions within the adder to be shared between two devices, a dense layout of $90 \times 98 \mu\text{m}^2$ is achieved for a 1-b MTGA. Circuit simulation for an 8-b MTGA shows an 18-ns delay.

According to Parseval's theorem, the FFT output signal is larger than the input signal power. Thus, in implementing the FFT with fixed-point arithmetic, a scaling policy is usually necessary to prevent overflow. For this purpose, we adopt a step-by-step scaling method which scales down data by a factor of 2 at every butterfly stage. This scaling is simply performed by 1-b shift right.

In general, finite register length within an arithmetic unit causes some roundoff errors, and reveals trade-offs between chip area and arithmetic error. In our array processor, a 1-b increase in register length results in an increase in the chip area of about 8%, but reduces total mean-squared error by 12 dB. In this prototype design, we use fixed-point 8-b as the operation data word, which yields a total mean-squared error of about -83 dB.

B. Layout Design

The layout design is accomplished in a hierarchical approach based on bit-slice units (BSU's). The hierarchy adopted is depicted in Fig. 6, and is described as follows:

- design basic cells in full custom,
- build a BSU by vertically stacking the basic cells,
- construct a PE by repeating the BSU's,
- complete the chip layout by abutting the PE's in 4×4 mesh array.

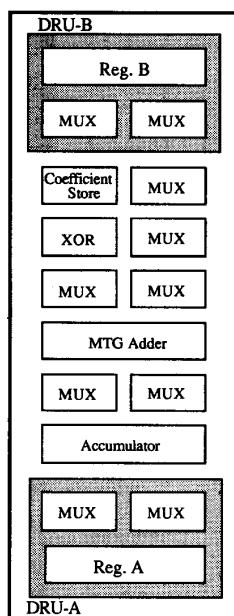


Fig. 7. Floor plan of a BSU.

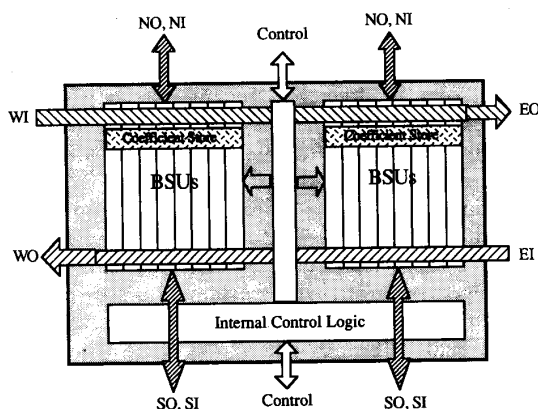


Fig. 8. Floor plan of a PE.

The physical layouts of the basic cells are tailored to satisfy the boundary connection requirements. To verify these basic cells, switch-level logic simulation is carried out using the netlist data extracted from layout.

Once all the basic cells have been physically designed and verified, a BSU is assembled from them. The BSU is constructed with seven basic cells stacked vertically, as shown in Fig. 7. The height and width of a BSU are 1468 and 90 μm , respectively.

Fig. 8 shows the floor plan of a PE, which is built up of two identical half-planes with a central control section. Each half-plane consists of eight BSU's. All interconnections between BSU's are achieved through abutment. Buffers are inserted between ICL and each half-plane to drive the control signals decoded by the ICL. The final

TABLE II
LAYOUT STATISTICS

| Block | Area (mm^2) | Transistors |
|----------------------------|------------------------|---------------------|
| BSU | 0.132 | 150 |
| ICL | 0.967 | 526 |
| PE | 3.345 | 2998 |
| 4 \times 4 Array | 53.52 | 48 000 |
| Die size including 83 pads | | 76.56 mm^2 |

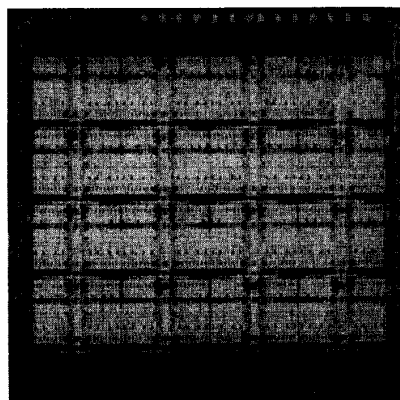


Fig. 9. Microphotograph of the fabricated array processor.

layout at the chip level is accomplished by a simple arrangement of the PE's in a 4 \times 4 mesh array.

The chip contains about 48 000 transistors in an area of 53.52 mm^2 , and die size including 83 pads is 76.56 mm^2 . The layout area of a BSU containing 150 transistors is 0.132 mm^2 , and a PE composed of 3000 transistors requires 3.345 mm^2 . Some layout statistics are summarized in Table II.

Since all PE's in the chip are synchronized by a global clock signal, a clock skew problem due to different path lengths from clock pad to each PE was eliminated by H-tree clock distribution scheme [18].

The layout design methodology adopted in this paper features: a) regular layout structure; b) fast design and easy debugging; c) minimum design errors; and d) flexible extension in both array size and data bit width.

V. FABRICATION AND MEASUREMENT RESULTS

The chip has been fabricated with a 2- μm p-well CMOS technology with two metal layers. The effective channel lengths of the PMOS and NMOS transistors are 1.6 and 1.44 μm , respectively. The microphotograph of the fabricated chip is shown in Fig. 9.

Fig. 10 shows the measured waveforms for load signal and data out for the DRU block. The measured delays from load signal to data out are 12, 8, and 6.2 ns at $V_{dd} = 4, 5$, and 6 V, respectively. This result says that each PE within the array can perform data communications with neighboring PE's at speeds up to 65 MHz.

From the measurement results, the HBA computation takes 0.65 μs , and the array processor computes a 16-point

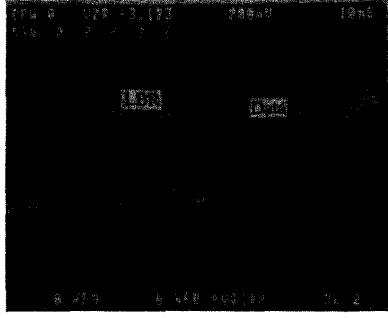


Fig. 10. Measured waveforms for the operation of DRU. Measured delay from load signal *LBR* to data out shows 8 ns at $V_{dd} = 5$ V.

FFT every 3 μ s, which is equivalently 24.6 million complex multiplications per second.

VI. DISCUSSION

According to the measurement results of the fabricated chip, the throughput rate (i.e., the number of samples processed per unit time) of our array processor is estimated to be 5.3 MHz, which is much higher than the 40 kHz of the processor computing the discrete Fourier transform (DFT) [21]. It has been reported that the programmable DSP processors execute 512-point complex FFT within 4.5 ms [23] and 1024-point FFT in 1.0–1.33 ms [3], [24], achieving throughput rates in the range of 0.1–1.0 MHz, which are much lower than that of our array processor. Also, it is comparable to 8.8 MHz of the FFT processor based on radix-4 butterfly [4] and 10 MHz of the FFT system built with 27 IC's [5].

Although the array processor described in this paper implements only 16 PE's with a 2- μ m CMOS process, it will be possible to integrate more than 16 PE's into a single chip if a submicrometer technology is used. The area $A(N, \lambda)$ required for an array of N PE's can be parameterized as follow:

$$A(N, \lambda) = A_0 N \lambda^2 \times 10^6. \quad (3)$$

In (3), λ denotes half of the minimum feature size of a given technology, and A_0 represents the physical layout area of a PE. The value of A_0 will depend on the physical realization of PE. In our design using double-metal layer, A_0 is 3.345 (see Table II).

Fig. 11 shows this area estimation using the λ parameter, which is normalized by A_0 . Based on Fig. 11, it will be possible to implement an array processor for 32×32 2-D FFT in an area of about 1 cm^2 if a submicrometer CMOS technology is used.

VII. CONCLUSIONS

An array processor dedicated to compute 16-point FFT has been implemented using a 2- μ m CMOS process. To achieve an area-efficient computation of the FFT, some design considerations have been examined both in array level and in PE level. The novel features in designing the array processor are the half butterfly arithmetic concept

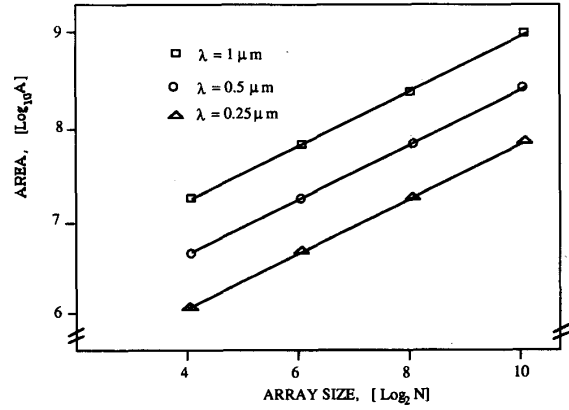


Fig. 11. Area estimation of the 2-D mesh array for FFT. Area is normalized by layout area of a PE A_0 .

realized with the distributed arithmetic, and the hierarchical design methodology based on bit-slice units.

The prototype implementation of this paper leads us to conclude that the 2-D mesh array architecture and algorithm presented in this paper will be one of the most attractive candidates for the real-time computation of the FFT in VLSI.

APPENDIX

Algorithm I: Data Shuffling Procedure Based on HBA

```

BEGIN
  FOR q = 1 TO 4 DO IN PARALLEL for all i and j
    (i = j = 0, 1, 2, 3)
    BEGIN
      IF (q ≤ 2) THEN
        D(q) = 22-q
        IF (i MOD 23-q < 22-q) THEN
          move data in PE(i, j) to PE(i + D(q), j)
        ELSE
          move data in PE(i, j) to PE(i - D(q), j)
        ELSE
          D(q) = 24-q
          IF (j MOD 25-q < 24-q) THEN
            move data in PE(i, j) to PE(i, j + D(q))
          ELSE
            move data in PE(i, j) to PE(i, j - D(q))
          END
        END
      END
    END
  END.

```

Algorithm II: Determination of the Arithmetic Type of the HBA&

```

BEGIN
  FOR q = 1 TO 4 DO IN PARALLEL for all i and j
    (i = j = 0, 1, 2, 3)
    BEGIN
      IF (q ≤ 2) THEN
        IF (i MOD 23-q < 22-q) THEN
          PE(i, j) compute the HBA +
        ELSE
          PE(i, j) compute the HBA -

```

```

ELSE
  IF (j MOD  $2^{5-q} < 2^{4-q}$ ) THEN
    PE(i,j) compute the HBA +
  ELSE
    PE(i,j) compute the HBA -
  END
END.

```

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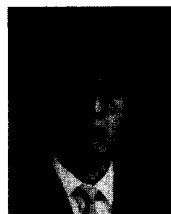
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