

Working Item	Specification	Simulation result			Hand calculation		
Vdd	1.5-V						
Current (μA)	(μA)#1	2306.0					
Transimpedance gain ($\text{K}\Omega$)	> 0.95K Ω	0.9507807			0.9517468		
core amp size (W/LN, W/LP)		NMOS:W=99u L=0.27u M=4 PMOS:W=26u L=0.28u M=4					
core amp gm (gmN, gmP)		NMOS:38.2993m PMOS:9.8606m					
core amp ro (roN, roP)(ohm)		NMOS:902 PMOS:2.94k					
Bandwidth (-3dB) (MHz)	>150MHz#2	724			665.91		
Closed-loop poles/zeros(HZ)			real	Img		real	Img
		Pole1	-355.242M	494.767M	Pole1	-369.999M	550.862M
		Pole2	-355.242M	-494.767M	Pole2	-369.999M	-550.862M
		zero	39.4854G	0	zero	42.643G	0
Closed-loop input impedance(ohm)		48.7320			47.7753		
Closed-loop output impedance(ohm)		20.1021			19.7049		
FoM (MHz/ μA)	#2/#1	0.31396					

a.

M1 W=99u L=0.27u m=4

M2 W=26u L=0.28u m=4

b.

**** small-signal transfer characteristics

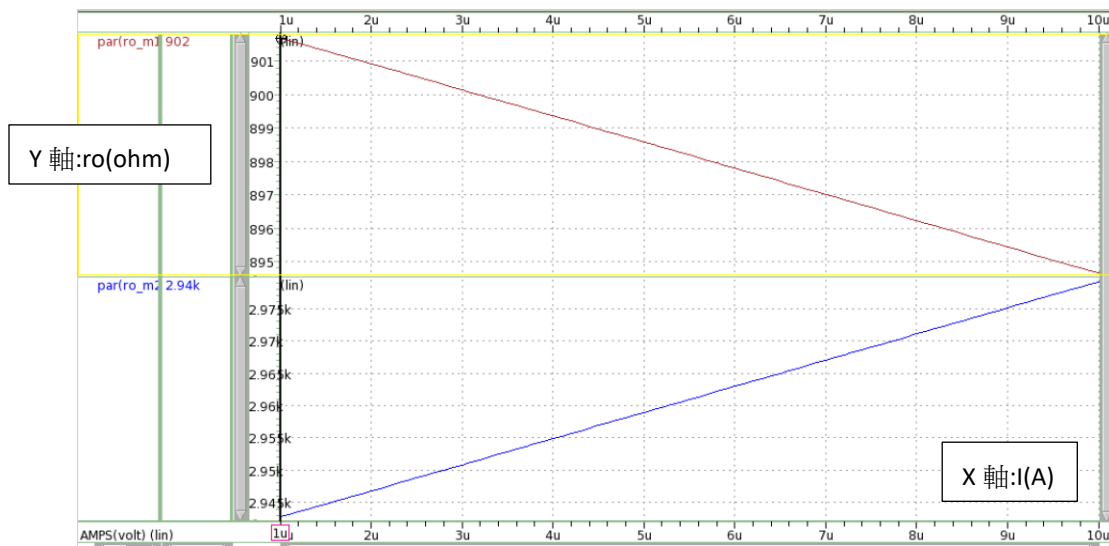
$v(\text{out})/i_{\text{in}}$ = -950.7807
 input resistance at i_{in} = 48.7320
 output resistance at $v(\text{out})$ = 20.1021

c.

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subckt
element 0:m1n 0:m2p
model 0:n_18.1 0:p_18.1
region Saturati Saturati
id 2.3060m -2.3106m
ibs -3.862e-19 2.468e-19
ibd -15.9270f 4.4217f
vgs 559.8611m -940.1389m
vds 564.4597m -935.5403m
vbs 0. 0.
vth 493.2101m -516.2981m
vdsat 115.2230m -402.0517m
vod 66.6510m -423.8409m
beta 502.8922m 28.9122m
gam_eff 507.4463m 557.0843m
gm 38.9223m 9.8606m
gds 1.1090m 339.8186u
gmb 6.4751m 3.1587m
cdtot 535.9406f 114.1288f
cgtot 866.0077f 234.3900f
cstot 1.1591p 312.4927f
cbtot 1.0054p 231.3879f
cgs 639.1496f 185.2894f
cgd 144.6956f 37.3719f

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Ro: M1:902(ohm) M2:2.94K(ohm)

$$V_{in} = I_{in} (R_F // R_S)$$

$$V_{out} = -(g_{m1} + g_{m2})(r_{o1} // r_{o2} // R_F)(R_F // R_S)V_{in}$$

$$\text{Gain} = \frac{A}{1 + KA}$$

$$K = -\frac{1}{R_F} = -\frac{1}{1000}$$

$$\begin{aligned}
 A &= -(g_{m1} + g_{m2}) \times (r_{o1} // r_{o2} // R_F) \times (R_F // R_S) \\
 &= (38.9223\text{m} + 9.8606\text{m}) \times (902 // 2.94\text{K} // 1000) \times (1000 // 100\text{K}) = -19724.0388
 \end{aligned}$$

$$\text{Gain} = \frac{-19724.0388}{1 + \frac{1}{1000} \times 19724.0388} = -951.746857(\text{ohm})$$

$$Z_{in} = \frac{(R_F // R_S)}{1 + KA} = \frac{(1000 // 100K)}{1 + \frac{1}{1000} \times 19724.0388} = 47.7753(\text{ohm})$$

$$Z_{out} = \frac{(r_{o1} // r_{o2} // R_F)}{1 + KA} = \frac{(902 // 2.94K // 1000)}{1 + \frac{1}{1000} \times 19724.0388} = 19.7049(\text{ohm})$$

模擬與手算誤差:

$$\text{Gain} = \frac{950.7807 - 951.7468}{950.7807} \times 100\% = -0.1016\%$$

$$Z_{in} = \frac{47.7753 - 48.7320}{47.7753} \times 100\% = -2.002\%$$

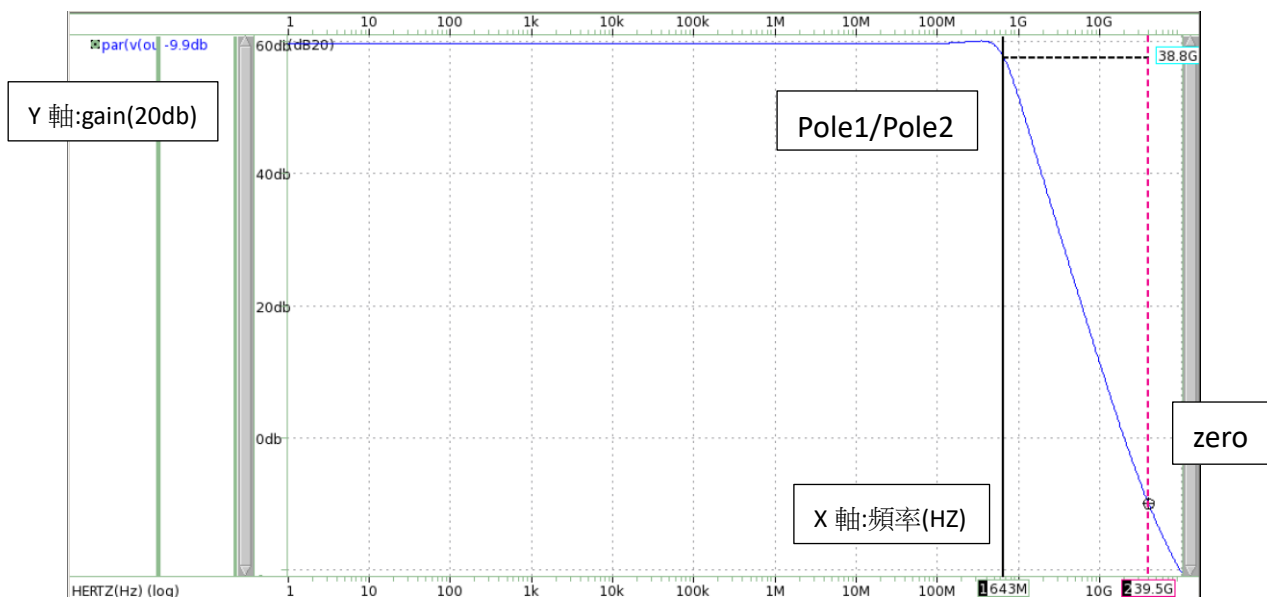
$$Z_{out} = \frac{19.7049 - 20.1021}{19.7049} \times 100\% = -2.0157\%$$

結果都與模擬非常接近

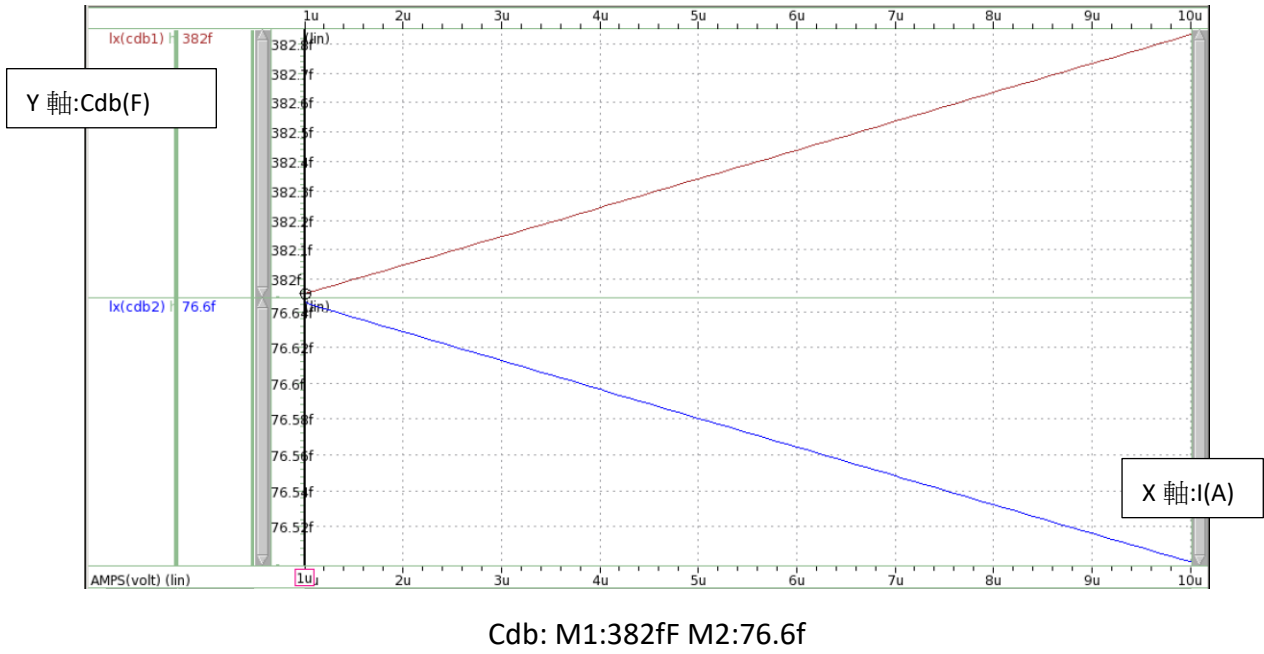
d.

poles (rad/sec)		poles (hertz)	
real	imag	real	imag
-2.23205g	3.10871g	-355.242x	494.767x
-2.23205g	-3.10871g	-355.242x	-494.767x
zeros (rad/sec)		zeros (hertz)	
real	imag	real	imag
248.094g	0.	39.4854g	0.

$$\text{pole1/pole2} = |355.242M + 494.767Mj| = 643.734M(\text{HZ})$$



e.



$$C_{GS}' = C_{GS1} + C_{GS2} + C_L = 639.1496f + 185.2894f + 1p = 1.8244 \times 10^{-12}$$

$$C_{GD}' = C_{GD1} + C_{GD2} = 144.6956f + 37.3719f + 1p = 1.182 \times 10^{-12}$$

$$C_{DB}' = C_{DB1} + C_{DB2} + C_L = 382f + 76.6f + 1p = 1.4586 \times 10^{-12}$$

$$\begin{aligned} a &= (R_F // R_S)(r_{o1} // r_{o2} // R_F)(C_{GS}'C_{GD}' + C_{DB}'C_{GD}' + C_{GS}'C_{DB}') \\ &= (1000 // 100k)(902 // 2.94k // 1000)(1.8244p \times 1.182p + 1.4586p \times 1.182p \\ &\quad + 1.8244p \times 1.4586p) = 2.6449 \times 10^{-18} \end{aligned}$$

$$\begin{aligned} b &= (1 + (g_{m1} + g_{m2})(r_{o1} // r_{o2} // R_F))C_{GD}'(R_F // R_S) + (R_F // R_S)C_{GS}' + (r_{o1} // r_{o2} // R_F)(C_{DB}' + C_{GD}') \\ &= (1 + (38.9223m + 9.8606m)(902 // 2.94k // 1000))1.182p(1000 // 100k) \\ &\quad + (1000 // 100k)1.8244p + (902 // 2.94k // 1000)(1.4586p + 1.182p) = 2.73686 \times 10^{-8} \end{aligned}$$

$$\text{open pole1} = \frac{1}{2\pi \times b} = \frac{1}{2\pi \times 2.7368 \times 10^{-8}} = 5.815537 \times 10^7$$

$$\text{open pole2} = \frac{b}{2\pi \times a} = \frac{2.7368 \times 10^{-8}}{2\pi \times 2.6449 \times 10^{-18}} = 2.6468 \times 10^9$$

$$\begin{aligned} \text{closed loop pole} &= \frac{-(\text{pole1} + \text{pole2}) \pm \sqrt{(\text{pole1} + \text{pole2})^2 - 4(1 + KA)\text{pole1} \times \text{pole2}}}{2} \\ &= -369.999M \pm 550.862Mj \text{ (HZ)} \end{aligned}$$

$$\text{Bandwidth} = |-369.999M + 550.862Mj| = 665.91M \text{ (HZ)}$$

$$\text{zero} = \frac{(g_{m1} + g_{m2})}{2\pi(C_{GD1} + C_{GD2})} = \frac{(38.9223m + 9.8606m)}{2\pi(144.6956f + 37.3719f)} = 4.2643 \times 10^{10}$$

模擬與手算誤差:

$$Pole = \text{實部} = \frac{-369.999 - (-355.242)}{-369.999} \times 100\% = 3.9888\%$$

$$\text{虛部} = \frac{550.862 - 494.767}{550.862} \times 100\% = 10.1831\%$$

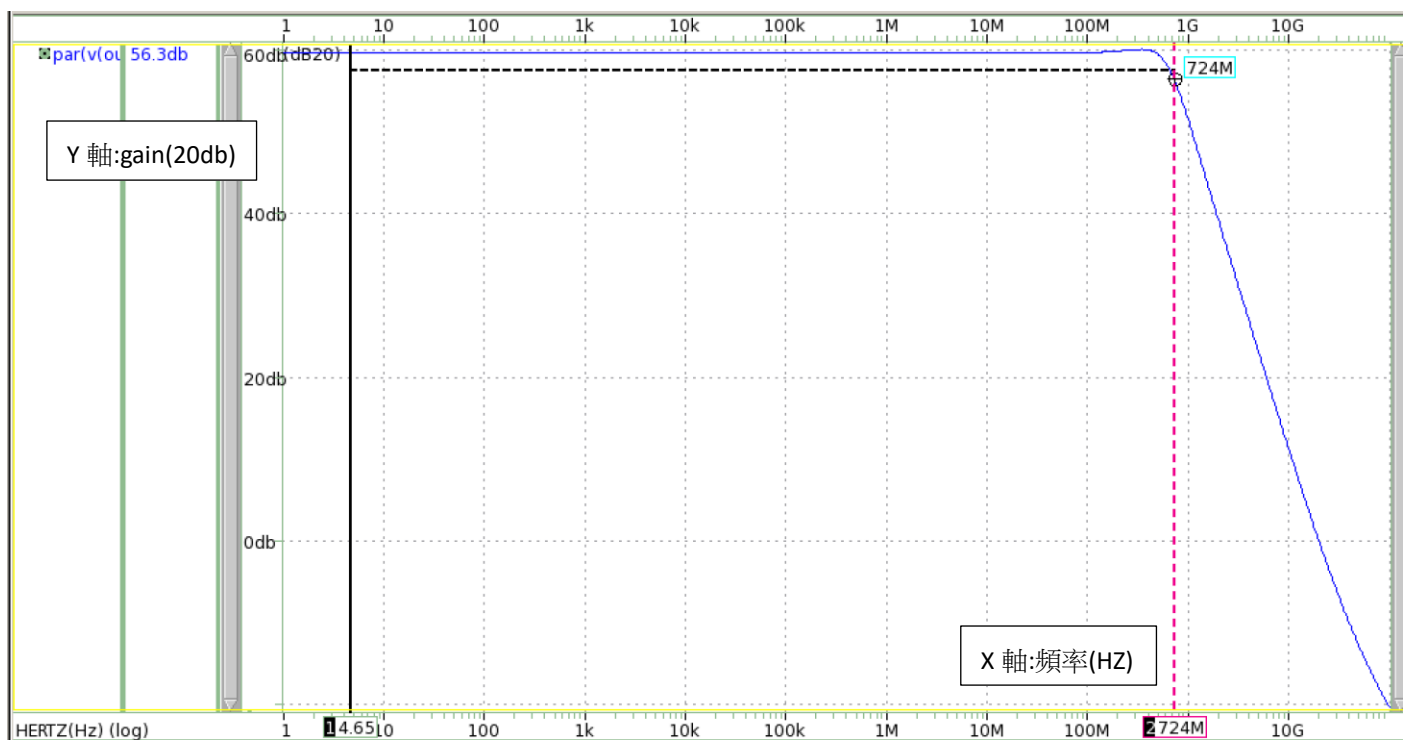
$$Zero = \frac{42.643 - 39.4854}{42.643} \times 100\% = 7.1702\%$$

手算結果與模擬有些誤差，推測是因為電路中會有電阻及寄生電容是手算沒辦法算到的。

f.

$$FoM = \frac{\text{bandwidth(MHZ)}}{\text{current}(\mu A)}$$

```
subckt
element 0:mln      0:m2p
model   0:n_18.1  0:p_18.1
region  Saturati  Saturati
id      2.3060m   -2.3106m
```



-3db 時，頻率為 724M(HZ)

$$FoM = \frac{724}{2306.0} = 0.31396$$

g.

$$\text{Gain} = \frac{A}{1 + KA}$$

$$A = -(g_{m1} + g_{m2}) \times (r_{o1} // r_{o2} // R_F) \times (R_F // R_S)$$

$$FoM = \frac{bandwidth(MHZ)}{current(\mu A)}$$

我一開始先想辦法讓 gain 大於 0.95K，gm1/gm2 越大 A 就越大，gain 就會越大，所以我將 M1 和 M2 的 W/L 的比值調到最大，發現都 gain 沒辦法到達 0.95K，就將 M1 和 M2 都並聯，並聯到達 m=4 時，gain 大約是 0.944K，接著我把 M1 的 L 調高一點點，Vgs-Vth 變大，gain 到達了 0.95K，這時候的 bandwidth 已經遠大於 150M(HZ)了。

接著要讓 FoM 越大越好，這時的電流很大，FoM 就很小，所以我將 M2 的 W 調小一半，電流減小了很多，但還是要讓 gain 維持在 0.95K 以上，這時的 bandwidth 還是遠大於 150M(HZ)。

我的 bandwidth 遠大於 150M(HZ)，跟同學的比較後，我認為是我的 gm 相對地比較小，而 gm 越小，pole 越大，所以我的 bandwidth 才很大。

.sp 檔

```
*hw6***
.proot
.lib 'cic018.1' TT
.unprot
.option
+ post=1
+ACCURATE=1
+ runlvl=6
.temp 25

.param
+ wn = 99u
+ ln = 0.27u
+ wp = 26u
+ lp = 0.28u
+ I = 1u

M1N out in gnd gnd N_18 w=wn l=ln m=4
M2P out in Vdd Vdd P_18 w=wp l=lp m=4

RF in out 1k
Rs in gnd 100k
Cin in gnd lp
Cout out gnd lp

Vdd Vdd gnd 1.5V
Iin gnd in dc=I ac=1m

.op
.probe DC
+ ro_m1 = par('1/LX8(M1N)')
+ ro_m2 = par('1/LX8(M2P)')
+ Cdb1 =LX29(M1N)
+ Cdb2 =LX29(M2P)
.tf V(out) Iin
.dc Iin 1u 10u 0.1u
.print par('V(out)/I(Iin)')
.pz V(out) Iin
.ac dec 100 1 100g

.probe par('V(out)/I(Iin)')

.end
```