08/04/2023 Evening



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# Memory Based Answers & Solutions for

Time : 3 hrs. M.M. : 300

# JEE (Main)-2023 (Online) Phase-2

(Physics, Chemistry and Mathematics)

#### IMPORTANT INSTRUCTIONS:

- (1) The test is of **3 hours** duration.
- (2) The Test Booklet consists of 90 questions. The maximum marks are 300.
- (3) There are **three** parts in the question paper consisting of **Physics, Chemistry** and **Mathematics** having 30 questions in each part of equal weightage. Each part (subject) has two sections.
  - (i) **Section-A:** This section contains 20 multiple choice questions which have only one correct answer. Each question carries **4 marks** for correct answer and **-1 mark** for wrong answer.
  - (ii) Section-B: This section contains 10 questions. In Section-B, attempt any five questions out of 10. The answer to each of the questions is a numerical value. Each question carries 4 marks for correct answer and -1 mark for wrong answer. For Section-B, the answer should be rounded off to the nearest integer.



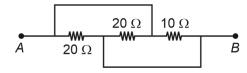
# **PHYSICS**

#### **SECTION - A**

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

#### Choose the correct answer:

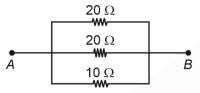
The effective resistance in the following circuit across terminal A and B is equal to



- (1)  $5\Omega$
- (2)  $10 \Omega$
- (3)  $20 \Omega$
- (4)  $40 \Omega$

#### Answer (1)

Sol. Equivalent circuit



$$\frac{1}{R} = \frac{1}{10} + \frac{1}{20} + \frac{1}{20}$$

$$\Rightarrow R = 5 \Omega$$

If the emf generated in the moving rod in uniform 2. magnetic field B is 0.08 V, then find the speed (v) of the rod.

$$\begin{array}{c|c} x & x \\ x & x \\ 10 \text{ cm} \\ x & x \end{array}$$

- (1) 1 m/s
- (2) 2 m/s
- (3) 3 m/s
- (4) 4 m/s

# Answer (2)

**Sol.**  $\varepsilon = Blv$ 

$$v = \frac{\varepsilon}{BI} = \frac{0.08 \times 100}{0.4 \times 10} = 2 \text{ m/s}$$

3. Which of the following expressions give the value of acceleration due to gravity (g') at the altitude h above the surface of earth. (R: radius of earth, g: acceleration due to gravity at surface of earth)

(1) 
$$g' = g \frac{h^2}{R^2}$$

(1) 
$$g' = g \frac{h^2}{R^2}$$
 (2)  $g' = \frac{gR^2}{(R+h)^2}$ 

$$(3) \quad g' = g \left( 1 - \frac{h}{R} \right)$$

(3) 
$$g' = g\left(1 - \frac{h}{R}\right)$$
 (4)  $g' = g\left(1 - \frac{h^2}{R^2}\right)$ 

# Answer (2)

**Sol.** 
$$g' = \frac{GM_e}{(R+h)^2}$$

$$g' = \frac{gR^2}{(R+h)^2}$$

- Find the distance from a point charge of magnitude 4.  $5 \times 10^{-9}$  C, where the electric potential is 50 V
  - (1) 90 cm
- (2) 70 cm
- (3) 60 cm
- (4) 50 cm

#### Answer (1)

**Sol.** 
$$V = \frac{kQ}{r}$$

$$50 = \frac{9 \times 10^9 \times 5 \times 10^{-9}}{r}$$

$$r = 0.9 \text{ m}$$

5. Match column I with column II and choose the correct option.

7	Column I		Column II
l.	Torque	a.	M <sup>0</sup> LT <sup>-2</sup>
II.	Stress	b.	ML <sup>-1</sup> T <sup>-1</sup>
III.	Coefficient of viscosity	C.	ML <sup>-1</sup> T <sup>-2</sup>
IV.	Gravitational potential gradient	d.	ML <sup>2</sup> T <sup>-2</sup>

- (1)  $I \rightarrow a$ ,  $II \rightarrow c$ ,  $III \rightarrow b$ ,  $IV \rightarrow d$
- (2)  $I \rightarrow d$ ,  $II \rightarrow b$ ,  $III \rightarrow c$ ,  $IV \rightarrow a$
- (3)  $I \rightarrow d$ ,  $II \rightarrow c$ ,  $III \rightarrow b$ ,  $IV \rightarrow a$
- (4)  $I \rightarrow a$ ,  $II \rightarrow c$ ,  $III \rightarrow d$ ,  $IV \rightarrow b$

# Answer (3)

**Sol.** Torque =  $r \times F = ML^2T^{-2}$ 

Stress = 
$$\frac{F}{A} = ML^{-1}T^{-2}$$

Coefficient of viscosity =  $ML^{-1}T^{-1}$ 

Gravitational potential gradient = M<sup>0</sup>LT<sup>-2</sup>

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- 6. Which of the following is the highest energy electromagnetic wave?
  - (1) X-rays
- (2) Infra Red
- (3) Microwaves
- (4) Radiowave

# Answer (1)

- **Sol.** Since out of the given options, X-rays have the highest frequency.
- ⇒ Option (1) is correct
- A carnot engine working between 27°C and 127° performs 2 kJ of work. The amount of heat energy rejected is equal to
  - (1) 4 kJ
- (2) 6 kJ
- (3) 8 kJ
- (4) 12 kJ

# Answer (2)

**Sol.** 2 kJ = 
$$x \left( 1 - \frac{300}{400} \right)$$

$$2 \text{ kJ} = \frac{x}{4}$$

- $\Rightarrow x = 8 \text{ kJ}$
- ⇒ Heat lost = 6 kJ
- 8. **Statement-I:** Electromagnet are made of soft iron.

**Statement-II:** Soft iron has lower permeability and high retentivity.

Choose the correct option related to statements.

- (1) Statement-I is true and statement-II is true
- (2) Statement-I is true and statement-II is false
- (3) Statement-I is false and statement-II is true
- (4) Statement-I is false and statement-II is false

#### Answer (2)

**Sol.** Soft iron has low retentivity and high permeability.

- 9. If a satellite is orbiting the earth at a height *h* (from the centre of earth) has angular momentum '*L*'. Then, the same satellite at a height 10 times '*h*' will have angular momentum equal to
  - (1)  $\sqrt{10} L$
- (2)  $\sqrt{5} L$

- (3) 3L
- (4)  $\sqrt{20} L$

# Answer (1)

**Sol.** : 
$$\frac{mv^2}{r} = \frac{GMm}{r^2}$$

$$\Rightarrow m^2 v^2 r^2 = GMmr$$

$$L^2 \propto r$$

$$\therefore \quad \frac{L_1}{L_2} = \sqrt{\frac{h}{10h}}$$

$$\Rightarrow L_2 = \sqrt{10}L$$

10. Consider 2 statements:

**Statement 1:** We can get displacement from acceleration-time graph.

**Statement 2:** We can get acceleration from velocity-time graph.

Then

- (1) Both statements are true
- (2) Both statements are false
- (3) Statement 1 is true and statement 2 is false
- (4) Statement 1 is false and statement 2 is true

#### Answer (4)

**Sol.** To get displacement from acceleration-time graph, we will need 1 initial value (for velocity).

Also, 
$$a = \frac{dv}{dt}$$

- $\Rightarrow$  Slope will give a.
- 11. A projectile launched on a horizontal surface follows a trajectory given by  $y = x \frac{x^2}{20}$  where y-axis is in vertical upward direction. Maximum height attained by projectile is (All units are in SI)
  - (1) 10 m
- (2) 5 m
- (3) 20 m
- (4) 40 m

# Answer (2)

**Sol.** 
$$y = x - \frac{x^2}{20}$$

at maximum height  $\frac{dy}{dx} = 0$ 

$$\Rightarrow x = 10 \text{ m}$$

at 
$$x = 10 \text{ m}$$
,  $y = 10 - 5 = 5 \text{ m}$ 

- 12. An antenna of length / emits radiation of wavelength  $\lambda$ . The power emitted by the antenna is proportional to:
  - $(1) \left(\frac{I}{\lambda}\right)^2$
- (2)  $\frac{1}{\lambda}$

(3)  $\frac{\lambda}{I}$ 

(4)  $\frac{1}{12}$ 

# Answer (1)

**Sol.** Since 
$$P \propto \left(\frac{I}{\lambda}\right)^2$$

 $\Rightarrow$  Option (1) is correct.

13. In a radioactive process, after 3 days,  $\frac{1}{8}$ th of the

initial amount of the element is undecayed. If in 5 days further, 8×10<sup>-3</sup> kg of the element decayed, find the original amount of element.

- (1) 128 grams
- (2) 64 grams
- (3) 256 grams
- (4) 32 grams

# Answer (2)

**Sol.** 
$$\frac{1}{8} = \frac{1}{2^3}$$

 $\Rightarrow$  3 half lives = 3 days

$$\Rightarrow \frac{b}{2} = 1 \text{ day}$$

Let m: initial mass

$$\Rightarrow \frac{m}{8} - \frac{m}{8 \times 32} = 8 \text{ grams}$$

$$\Rightarrow m = \frac{64 \times 32}{32 - 1} \simeq 65 gm$$

- 14. Find the change in energy stored in a capacitor of 600 pF capacitance charged at 50 V, once connected with another 600 pF uncharged capacitor.
  - (1) 0.56 μJ
- (2)  $0.4 \mu J$
- (3) 0.86 μJ
- (4) 0.32 μJ

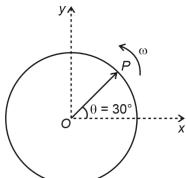
# Answer (1)

**Sol.** 
$$U_i = \frac{1}{2}Cv^2$$
,  $U_f = \frac{1}{2}C\left(\frac{v}{2}\right)^2$ 

$$\Delta U = \frac{3}{8}Cv^2$$

$$= \frac{3}{8} \times 600 \times 10^{-12} \times (50)^2$$

15. Phasor of a particle performing SHM is as shown in the diagram. The SHM has angular frequency  $\omega$ and at t = 0 the phasor lies along *OP*. At any time tfurther the projection of phasor along y-axis is given by



- (1)  $R\sin\left(\omega t + \frac{\pi}{6}\right)$  (2)  $R\cos\left(\omega t + \frac{\pi}{6}\right)$
- (3)  $R\sin\left(\omega t \frac{\pi}{6}\right)$  (4)  $R\cos\left(\omega t \frac{\pi}{6}\right)$

# Answer (1)

**Sol.**  $\theta$  at any time t

$$= \omega t = 30^{\circ}$$

$$\Rightarrow$$
  $y_{\text{projection}} = R \sin \theta$ 

$$=R\sin\left(\omega t+\frac{\pi}{6}\right)$$

- 16.
- 17.
- 18.
- 19.
- 20.

#### **SECTION - B**

Numerical Value Type Questions: This section contains 10 questions. In Section B, attempt any five questions out of 10. The answer to each question is a NUMERICAL VALUE. For each question, enter the correct numerical value (in decimal truncated/rounded-off to the second decimal place; e.g., 06.25, 07.00, -00.33, -00.30, 30.27, -27.30) using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.

21. A body of mass 5 kg has the linear momentum of 100 kg ms<sup>-1</sup> and acted upon by the force of 2 N in the direction of initial momentum for 2 seconds, then change in kinetic energy in Joule is

#### Answer (81.60)

**Sol.** 
$$F \times t = \Delta P$$

$$\Rightarrow$$
 2 x 2 =  $P_f$  - 100

$$P_f = 104 \text{ kg ms}^{-1}$$

$$\Delta K = \frac{P_f^2}{2m} - \frac{P_i^2}{2m} = \frac{1}{2 \times 5} \times (104^2 - 100^2)$$

$$=\frac{1}{10}\times4\times204=81.6 \text{ J}$$

22. In a YDSE experiment, fringe width is 2 mm when wavelength of light used is  $\lambda = 400$  nm. Find the fringe width (in mm) when wavelength is 600 nm.

#### Answer (3)

# JEE (Main)-2023: Phase-2 (08-04-2023)-Evening



**Sol.** 
$$\beta = \frac{\lambda D}{d}$$

$$\Rightarrow \frac{\beta'}{\beta} = \frac{600}{400} = 1.5$$

$$\Rightarrow \beta' = 3 \text{ mm}$$

23. A block moving with speed 1 m/s comes to rest after moving for 20 cm over a rough surface. The coefficient of friction between the block and surface is\_\_\_\_

# Answer (00.25)

**Sol.** : 
$$v^2 - u^2 = 2aS$$

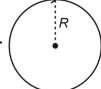
$$0^2 - 1^2 = 2(-\mu g) \frac{20}{100}$$

$$\mu=\frac{1}{4}=0.25$$

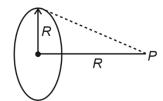
24. The ratio of magnetic field due to coil at centre and at a distance of R from the centre on the axis passing through the centre and perpendicular to the plane of ring is  $\sqrt{x}$ :1 (R is the radius of coil), find the value of x.

# Answer (8)





$$B_{\rm C} = \left(\frac{\mu_0 i}{2R}\right)$$

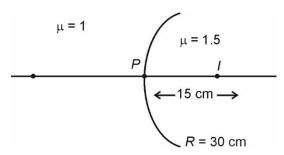


$$B_{P} = \frac{\mu_{0}}{4\pi} \times \frac{2 \times i \times \pi R^{2}}{(R^{2} + R^{2})^{3/2}}$$

$$=\frac{\mu_0}{2R}\frac{i}{2\sqrt{2}} = \left(\frac{\mu_0 i}{4\sqrt{2}R}\right)$$

$$\frac{B_C}{B_C} = \frac{4\sqrt{2}}{2} = \sqrt{8}:1$$

25. In the given diagram image forms at a distance of 15 cm inside the



medium of refractive index 1.5. Find the object distance (in cm) from point *P*.

# Answer (12.00)

**Sol.** 
$$\frac{1.5}{15} - \frac{1}{u} = \left(\frac{1.5 - 1}{30}\right) = \frac{0.5}{30} = \frac{1}{60}$$

$$\frac{1}{10} - \frac{1}{u} = \frac{1}{60} \Rightarrow \frac{1}{10} - \frac{1}{60} = \frac{1}{u}$$

$$\frac{1}{u} = \frac{5}{60} \Rightarrow u = \frac{60}{5} = 12 \text{ cm}$$

26. Ratio of wavelengths of photons corresponding to first and second line of Balmer series in an emission spectrum is given by  $\frac{x}{20}$  for a hydrogen like species. Value of x is equal to

#### Answer (27)

**Sol.** 
$$\frac{1}{\lambda_1} = -R\left(\frac{1}{9} - \frac{1}{4}\right)$$

$$\frac{1}{\lambda_2} = -R\left(\frac{1}{16} - \frac{1}{4}\right)$$

$$\Rightarrow \frac{\lambda_1}{\lambda_2} = \frac{36}{5} \times \frac{3}{16} = \frac{27}{20}$$

$$\Rightarrow x = 27$$

- 27.
- 28.
- 29.
- 30.



# **CHEMISTRY**

#### **SECTION - A**

**Multiple Choice Questions:** This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

#### Choose the correct answer:

- 1. Which of the following acts as a stabilizer in the decomposition of  $H_2O_2$ .
  - (1) Urea
- (2) Alkali
- (3) Glass
- (4) Dust

#### Answer (1)

**Sol.** Urea acts as a stabilizer in the decomposition of H<sub>2</sub>O<sub>2</sub>

2. IUPAC name of given compound is

- (1) 5-oxo-2-methyl hexanoic acid
- (2) 2-methyl-5-oxohexanoic acid
- (3) 5-oxo-2-methyl pentatonic acid
- (4) 5-carboxy-2-oxohexane

#### Answer (2)

Sol. 
$${}^{6}_{CH_{3}}$$
  ${}^{5}_{CH_{2}}$   ${}^{4}_{CH_{2}}$   ${}^{3}_{CH_{2}}$   ${}^{2}_{CH_{2}}$   ${}^{2}_{CH_{2}}$   ${}^{2}_{CH_{2}}$   ${}^{2}_{CH_{2}}$   ${}^{2}_{CH_{2}}$   ${}^{2}_{CH_{2}}$   ${}^{2}_{CH_{2}}$   ${}^{2}_{CH_{2}}$ 

- 3. Order of van der waals constant a for Ar,  $CH_4$ ,  $H_2O$ , and  $C_6H_6$ 
  - (1)  $H_2O > C_6H_6 > Ar > CH_4$
  - (2)  $Ar > H_2O > CH_4 > C_6H_6$
  - (3) Ar >  $C_6H_6$  >  $H_2O$  >  $CH_4$
  - (4)  $H_2O > C_6H_6 > CH_4 > Ar$

### Answer (4)

**Sol.** H<sub>2</sub>O has hydrogen bonding.

4. Find the correct order of acidity for the following

С

$$CI - CH_2 - COOH$$
,  $CH_3 - COOH$ ,  $CF_3 - COOH$ ,

CH<sub>2</sub> – COOH,

- (1) c > d > a > b
- (2) b > a > d > c
- (3) a > b > c > d
- (4) b>c>a>d

#### Answer (1)

Sol. Correct order of acidity is

c > d > a > b (based on –I effect of –F & –CI group) NO<sub>2</sub>

- (1)  $Br_2/Fe, \Delta \longrightarrow P$
- (2) Sn, HCI
- (3) NaNO<sub>2</sub> /HCI
- (4) H<sub>3</sub> PO<sub>2</sub>

Find out final product of this reaction

Br

Answer (1)

Sol.

$$\begin{array}{c|c}
 & NO_2 \\
\hline
 & Br_2/Fe, \\
\hline
 & CH_3
\end{array} \begin{array}{c}
 & NO_2 \\
\hline
 & Sn/HCI
\end{array} \begin{array}{c}
 & NH_2 \\
\hline
 & CH_3
\end{array}$$

$$\begin{array}{c}
 & Br \\
\hline
 & CH_3
\end{array}$$

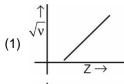
$$\begin{array}{c}
 & N_2 \\
\hline
 & N_2
\end{array}$$

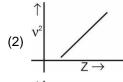
$$\begin{array}{c}
 & NaNO_2/HCI
\end{array}$$

$$\begin{array}{c}
 & Br \\
\hline
 & CH_3
\end{array}$$

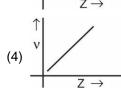
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6. Find the correct plot



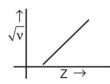






# Answer (1)

**Sol.** As per Moseley's law, cannot plot is  $\left(\sqrt{v} = a(\mathcal{Z} - b)\right]$ 



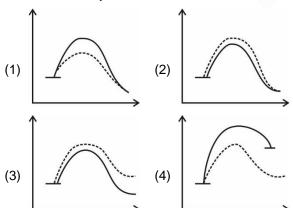
- 7. Total spin only magnetic moment of the ion  $[Mn(SCN)_6]^{x-}$  is 5.92 B.M. Find out the value of x.
  - (1) 5
  - (2) 3
  - (3) 2
  - (4) 4

### Answer (4)

- **Sol.** The value of magnetic moment showing the presence of five unpaired electrons hence the central atom Mn will be at +2.
- 8. Find out the correct option by using +ve catalyst.

\_\_\_\_ without catalyst

----- with catalyst



# Answer (1)

Sol. AH doesn't change

Eawill decrease

9. Match Column-I with Column-II

	Column-I		Column-II (Unpaired Electrons)
Α	[Ni(NH <sub>3</sub> ) <sub>6</sub> ] <sup>2+</sup>	Р	0
В	[Co(NH <sub>3</sub> ) <sub>6</sub> ] <sup>3+</sup>	Q	2
С	[Fe(CN) <sub>6</sub> ] <sup>3-</sup>	R	4
D	[CoF <sub>6</sub> ] <sup>3-</sup>	S	1

(1) A-Q; B-P; C-R; D-S

(2) A-P; B-Q; C-S; D-R

(3) A-Q; B-P; C-S; D-R

(4) A-S; B-Q; C-P; D-R

#### Answer (3)

**Sol.**  $[Ni(NH_3)_6]^{2+}$  :  $sp^3d^2$  n=2

 $[Co(NH_3)_6]^{3+}$  :  $d^2sp^3$  n=0

 $[Fe(CN)_6]^{3-}$  :  $o^2 sp^3$  n = 1

 $[CoF_6]^{3-}$  :  $sp^3d^2$  n=4

 The correct order of nucleophilic substitution of following compounds with NaOH

(1) A > B > C > D

(2) D > C > A > B

(3) D > C > B > A

(4) A > B > D > C

#### Answer (2)

**Sol.** Nucleophilic of substitution rate depends on the presence of E.W.G at ortho and para position of benzene ring. Hence the correct order of nucleophilic substitution will be D > C > A > B.



11. Statement-1: Methyl orange is a weak acid

Statement-2: Benzenoid form of methyl orange is deeply coloured than quinonoid form

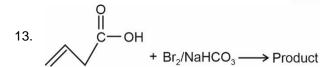
- (1) Statement-1 is correct and Statement-2 is wrong
- (2) Both the Statements-1 and Statement-2 are correct
- (3) Statement-1 is wrong and Statement-2 is correct
- (4) None of them

# Answer (1)

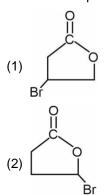
- **Sol.** Methyl orange is a weak acid. So, statement-1 is correct. In acidic medium, it exists in quinonoid form which is red in colour and in alkaline medium it exists in benzenoid form which is yellow in colour. Since red is more deeply coloured than yellow, Statement-2 is wrong.
- 12. Which of the following is correct?
  - (I) Photocurrent  $\alpha$  Intensity of photoelectrons
  - (II) Kinetic energy is dependent on frequency
  - (III) Kinetic energy is independent of frequency
  - (1) I, II only
  - (2) III, I only
  - (3) II only
  - (4) III only

#### Answer (1)

**Sol.** Photocurrent  $\alpha$  Intensity of incident light. Kinetic energy of electron is dependent on frequency of incident light.



Find out final product of this reaction



(4) None

#### Answer (1)

Sol.

$$OH \xrightarrow{Br_2} \xrightarrow{Br^+} NaHCO_3$$

$$OH \xrightarrow{O} OH$$

$$OH \xrightarrow{O} OH$$

14.

15.

16.

17.

18.

19.

20.

## SECTION - B

**Numerical Value Type Questions:** This section contains 10 questions. In Section B, attempt any five questions out of 10. The answer to each question is a **NUMERICAL VALUE.** For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to the second decimal place; e.g., 06.25, 07.00, –00.33, –00.30, 30.27, –27.30) using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.

21. Compounds of Xenon having one electron pair on central atom

XeO<sub>3</sub> XeOF<sub>2</sub> XeF<sub>4</sub> XeF<sub>5</sub>

Answer (01.00)

Sol. O have 1 lone pair on central atom

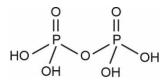
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22. What is the ratio of  $\sigma$  and  $\pi$  bonds in pyrophosphoric acid?

# Answer (06)

Sol. Pyrophosphoric acid is H<sub>4</sub>P<sub>2</sub>O<sub>7</sub>



 $\sigma$  bonds = 12

 $\pi$  bonds = 2

Ratio of  $\frac{\sigma}{\pi} = \frac{12}{2} = 6$ 

23. Find out oxidation number of central metal atom of Fe(CO)<sub>5</sub>, VO<sup>2+</sup> and WO<sub>3</sub>. Then calculate the sum of their oxidation states.

# Answer (10.00)

WO<sub>3</sub>

Sol. Compound Oxidation state of central metal atoms  $Fe(CO)_5 \qquad \qquad 0$   $VO^{2+} \qquad \qquad +4$ 

Sum of oxidation states = 0 + 4 + 6 = 10

24. How many of the following have five radial nodes?5s, 6s, 7s, 6p and 4p

+6

# Answer (01)

**Sol.** Radial nodes is given by (n - l - 1)

For 5s. Radial node = 4

For 6s, Radial node = 5

For 7s, Radial node = 6

For 6p, Radial node = 4

For 4p, Radial node = 2

25. In good quality cement ratio of lime total oxides of Si(SiO<sub>2</sub>), Aluminium(Al<sub>2</sub>O<sub>3</sub>) and Iron(Fe<sub>2</sub>O<sub>3</sub>) should be as close as possible to\_\_\_\_\_.

#### Answer (2)

Sol. Fact

Reference NCERT Page-304 NCERT.

26. The boiling points of two solvents X and Y are in the ratio 2:1 (in K) and their enthalpy of vaporisation is in the ratio 1:2. Find the ratio of elevation in boiling point when same moles of solute are added to same mass of both the solvents, if the molar mass of X is twice that of Y

# Answer (16.00)

Sol. 
$$K_{b} = \frac{RTb^{2}M}{1000\Delta H}$$

$$\frac{\left(K_{b}\right)_{x}}{\left(K_{b}\right)_{y}} = \frac{\left(Tb\right)_{x}^{2}}{\left(Tb\right)_{y}^{2}} \times \frac{M_{x}}{M_{y}} \times \frac{\left(\Delta H\right)_{y}}{\left(\Delta H\right)_{x}}$$

$$= \frac{4}{1} \times 2 \times 2 = 16$$

27.  $K_{sp}$  of BaSO<sub>4</sub> is 8 × 10<sup>-11</sup>. If the solubility in presence of 0.1 M CaSO<sub>4</sub> is X × 10<sup>-10</sup> M, Find X.

#### Answer (8)

**Sol.** 'X'  $\times$  10<sup>-10</sup>M, X is :

BaSO<sub>4</sub> 
$$\rightleftharpoons$$
 Ba<sup>+2</sup> + SO<sub>4</sub><sup>-2</sup> S S + 0.1  $\approx$  0.1

$$S \times 0.1 = 8 \times 10^{-11}$$
  
 $S = 8 \times 10^{-10}$ 

28. For As<sub>2</sub>S<sub>3</sub> colloidal solution, the coagulation value of AlCl<sub>3</sub> & NaCl are 0.09 and 50.04 respectively. If coagulation power of AlCl<sub>3</sub> is x times of NaCl then tell the value of x.

#### **Answer (556)**

Sol. For a given colloid

 $\frac{\text{Coagulation value of NaCl}}{\text{Coagulation value of AlCl}_3} =$ 

Coagulation power of AlCl<sub>3</sub> Coagulation power of NaCl

$$\frac{50.04}{0.09} = x$$

29.

30.



# **MATHEMATICS**

#### **SECTION - A**

**Multiple Choice Questions:** This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

#### Choose the correct answer:

1. The absolute difference of the coefficient of  $x^7$  and

 $x^9$  in the expansion of  $\left(2x + \frac{1}{2x}\right)^{11}$  is

- (1)  $11 \times 2^5$
- (2)  $11 \times 2^7$
- (3)  $11 \times 2^4$
- (4)  $11 \times 2^3$

# Answer (2)

**Sol.** 
$$T_{r+1} = {}^{11}C_r (2x)^{11-r} \left(\frac{1}{2x}\right)^r$$
$$= {}^{11}C_r \frac{2^{11-r}}{2^r} x^{11-2r}$$

$$11 - 2r = 7$$
 and  $11 - 2r = 9$   
 $r = 2$   $r = 1$ 

.: Coefficient of 
$$x^7$$
 is  ${}^{11}C_2 \frac{{(2)}^9}{2^2} = {}^{11}C_2 {(2)}^7$ 

Coefficient of 
$$x^9$$
 is  ${}^{11}C_1 \frac{{(2)}^{10}}{2} = {}^{11}C_1 {(2)}^9$ 

$${}^{11}C_2(2)^7 - 11 \times (2)^9$$
  
= 11 \times 2^7

- 2. Let  $f(x) = \{1, 2, 3, 4, 5, 6, 7\}$  the relation  $R = \{(x, y) \in A \times A, x + y = 7\}$  is
  - (1) Symmetric
  - (2) Reflexive
  - (3) Transitive
  - (4) Equivalence

#### Answer (1)

**Sol.** 
$$x + y = 7$$
  
 $y = 7 - x$   
 $R = \{(1, 6), (2, 5), (3, 4), (4, 3), (5, 2), (6, 1)\}$ 

- $\therefore (a, b) \in R \Rightarrow (b, a) \in R.$
- :. Relation is symmetric

- The number of words with or without meaning can be formed from the word MATHEMATICS where C, S not come together is
  - (1)  $\frac{9}{8} \times 10!$
- (2)  $\frac{1}{8} \times 10!$
- (3)  $\frac{5}{8} \times 10!$
- (4)  $\frac{1}{2} \times 10!$

# Answer (1)

**Sol.** Total words = 
$$\frac{11!}{2!2!2!}$$

When C and S are together =  $\frac{10!}{2!2!2!} \times 2!$ 

∴ Required number of words = 
$$\frac{11!}{(2!)^3} - \frac{10!}{(2!)^3} \times 2!$$
  
=  $\frac{10!}{8} [11-2]$   
=  $\frac{9}{8} \times 10!$ 

- 4. Let  $a_n = 5 + 8 + 14 + 23 + \dots$  upto n terms. If  $S_n = \sum_{k=1}^n a_k$ , then  $S_{30} a_{40}$  is equal to
  - (1) 78025
  - (2) 12800
  - (3) 11600
  - (4) 12100

#### Answer (1)

**Sol.** 
$$a_n = 5 + 8 + 14 + \dots T_n$$

$$\frac{a_n = 5 + 8 + 14... + T_{n-1} + T_n}{0 = 5 + \underbrace{3 + 6 + 9 + ....}_{(n-1) \text{ terms}} - T_n}$$

$$\Rightarrow T_n = 5 + \left(\frac{n-1}{2}\right) (6 + (n-2)3) = 5 + \frac{3}{2}(n-1)^n$$

$$5 + \frac{3}{2}n^2 - \frac{3}{2}n$$

$$\Rightarrow \frac{1}{2} \Big( 10 + 3n^2 - 3n \Big)$$

$$T_n = \frac{1}{2} \left( 3n^2 - 3n + 10 \right)$$

# JEE (Main)-2023: Phase-2 (08-04-2023)-Evening



$$a_n = \sum T_n = \frac{1}{2} \left[ \frac{3 \cdot (n)(n+1)(2n+1)}{6} - \frac{3 \cdot (n)(n+1)}{2} + 10n \right]$$
$$= \frac{1}{2} (n) \left( \frac{(n+1)(2n+1)}{2} - \frac{3(n+1)}{2} + 100 \right)$$

$$a_n = \frac{n}{4} \left( 2n^2 + 3n + 1 - 3n - 3 + 20 \right)$$
$$= \frac{n}{4} \left( 2n^2 + 18 \right) = \frac{n}{4} \left( n^2 + 9 \right)$$

$$a_{40} = \frac{40}{2} (1600 + 9) = 1609 \times 20 = 32180$$

$$S_n = \sum a_n = \frac{1}{2} \left[ \left( \frac{(n)(n+1)}{2} \right)^2 + \frac{9 \cdot (n)(n+1)}{2} \right]$$

$$S_{30} = \frac{1}{2} \left( \left( \frac{30 \times 3}{2} \right)^2 + \frac{9}{2} (30)(31) \right)$$
$$= \frac{1}{2} (216225 + 4185)$$
$$= 110205$$

$$S_{30} - a_{40} = 78025$$

The equation  $ax^2 + bx + c = 0$  has roots  $\alpha$  and  $\beta$ .

Then find 
$$\lim_{x \to \frac{1}{\alpha}} \frac{1 - \cos(cx^2 + bx + a)}{2(1 - \alpha x)^2}$$
 is

(1) 
$$\frac{c^2(\alpha-\beta)^2}{4\alpha^4\beta^2}$$
 (2)  $\frac{c^2(\alpha-\beta)^2}{\alpha^4\beta^2}$ 

$$(2) \frac{c^2(\alpha-\beta)^2}{\alpha^4\beta^2}$$

(3) 
$$\frac{c^2(\alpha-\beta)^2}{2\alpha^4\beta^2}$$
 (4)  $\frac{c^2(\alpha-\beta)^2}{4\alpha^2\beta^2}$ 

$$(4) \quad \frac{c^2(\alpha-\beta)^2}{4\alpha^2\beta^2}$$

# Answer (1)

Sol. 
$$\lim_{x \to \frac{1}{\alpha}} \frac{2\sin^2\left(\frac{cx^2 + bx + a}{2}\right)}{2\alpha^2\left(x - \frac{1}{\alpha}\right)^2}$$

$$=\frac{c^2(\alpha-\beta)^2}{4\alpha^2\beta^2}$$

- 6.  $\theta \in (0, 2\pi)$  and  $\frac{1+2i\sin\theta}{1-i\sin\theta}$  is purely imaginary then the value of  $\theta$  is
  - (1)  $\pi$

(2) 0

(3)  $2\pi$ 

(4)  $\frac{\pi}{4}$ 

# Answer (4)

Sol. Real part has to be zero

$$\Rightarrow \frac{1 - 2\sin^2\theta}{1 + \sin^2\theta} = 0$$

$$\sin^2 \theta = \frac{1}{2}$$

$$\theta = n\pi \pm \frac{\pi}{4}, n \in I$$

$$\theta = \frac{\pi}{4}, \frac{5\pi}{4}, \frac{3\pi}{4}$$

- 7. The statement  $(p \land (\sim q)) \lor (\sim p)$  is equivalent to
  - (1)  $p \wedge q$
- (3)  $p \vee q$
- (4)  $\sim p \wedge \sim q$

#### Answer (2)

**Sol.** 
$$(p \land (\sim q)) \lor (\sim p)$$

$$= (p \vee \sim p) \wedge (\sim q \vee \sim p)$$

$$= T \wedge (\sim q \vee \sim p)$$

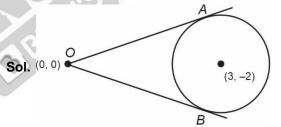
$$= \sim q \vee \sim p$$

From O(0, 0), two tangents OA and OB are drawn to a circle  $x^2 + y^2 - 6x + 4y + 8 = 0$ , then the equation of circumcircle of  $\triangle OAB$ .

(1) 
$$x^2 + y^2 - 3x + 2y = 0$$
 (2)  $x^2 + y^2 + 3x - 2y = 0$ 

(3) 
$$x^2 + y^2 + 3x + 2y = 0$$
 (4)  $x^2 + y^2 - 3x - 2y = 0$ 

# Answer (1)



(0, 0) and (3, -2) are diametric end points

$$(x-0)(x-3) + (y-0)(y+2) = 0$$

$$x^2 + y^2 - 3x + 2y = 0$$

The mid points of side of a triangle are (0, 1), (1, 0), 9. (1, 1), where incentre is D. A parabola  $y^2 = 4ax$ passes through D whose focus is  $(\alpha + \beta\sqrt{2}, 0)$  then

$$\frac{\beta^2}{\alpha}$$
 is

(1)  $\frac{1}{2}$ 

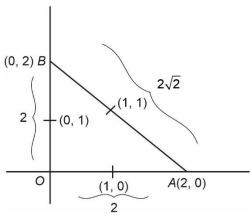
(2) 2

(3)  $\frac{1}{8}$ 

(4) 4

#### Answer (3)

Sol.



: Mid-point is (0, 1), (1, 0) and (1, 1)

$$I = \left(\frac{4}{4 + 2\sqrt{2}}, \frac{4}{4 + 2\sqrt{2}}\right)$$

$$y^2 = 4ax$$

 $y^2 = 4ax$  passes through I

$$\left(\frac{4}{4+2\sqrt{2}}\right)^2 = 4a\left(\frac{4}{4+2\sqrt{2}}\right) \Rightarrow a = \frac{1}{4+2\sqrt{2}}$$

Focus = (a, 0)

$$=\left(\frac{1}{4+2\sqrt{2}},\,0\right)$$

$$=\left(\frac{4-2\sqrt{2}}{8},0\right)$$

$$\alpha = \frac{4}{8} = \frac{1}{2}, \ \beta = \frac{-2}{8} = \frac{-1}{4}$$

$$\frac{\beta^2}{\alpha} = \frac{1}{8}$$

- 10. Let  $R = \{a, b, c, d, e\}$  and  $S = \{1, 2, 3, 4\}$ . Then number of onto functions  $f(x) : R \rightarrow S$  such that  $f(a) \neq 1$  is
  - (1) 240
- (2) 180
- (3) 204
- (4) 216

#### Answer (2)

Sol. Total number of onto functions

$$=\frac{5!}{3!2!}\times 4!$$

Now, when f(a) = 1

$$\frac{4!}{2!2!} \times 3! + 4!$$

 $\therefore$  Required functions = 240 - 36 - 24

# 11. A parabola with focus (3, 0) and directrix x = -3. Points P and Q lie on the parabola and their ordinates are in the ratio 3:1. The point of intersection of tangents drawn at points P and Q lies on the parabola

(1) 
$$y^2 = 16x$$

(2) 
$$y^2 = 4x$$

(3) 
$$y^2 = 8x$$

(4) 
$$x^2 = 4y$$

#### Answer (1)

**Sol.** Given parabola  $y^2 = 12x$ 

$$P(3t_1^2, 6t_1), Q(3t_2^2, 6t_2)$$

$$\frac{t_1}{t_2} = 3 \implies t_1 = 3t_2 \qquad \qquad \dots (i)$$

Let point of intersection be (h, k)

$$h = 3t_1t_2$$
 ...(ii

and 
$$k = 3(t_1 + t_2)$$
 ...(iii)

(i) and (iii) 
$$\Rightarrow t_2 = \frac{k}{12}$$

(ii) 
$$\Rightarrow h = 9t_2^2 = 9 \times \frac{k^2}{144} \Rightarrow k^2 = 16h$$

$$\Rightarrow y^2 = 16x$$

12. In probability distribution for discrete variable x = 0, 1, 2 ...  $P(x = x) = k(x + 1) \cdot 3^{-x}$ . The probability of  $P(x \ge 2)$  is equal to

(1) 
$$\frac{5}{18}$$

(2) 
$$\frac{10}{18}$$

(3) 
$$\frac{20}{27}$$

(4) 
$$\frac{7}{27}$$

#### Answer (4)

**Sol.**  $\Sigma P = 1$ 

$$\Rightarrow k(1 + 2.3^{-1} + 3.3^{-2} + ....) = 1$$

Let 
$$S = 1 + \frac{2}{3} + \frac{3}{3^2} + \dots$$

$$\frac{\frac{S}{3} = \frac{1}{3} + \frac{2}{3^2} + \dots}{\frac{2S}{3} = 1 + \frac{1}{3} + \frac{1}{3^2} + \dots} = \frac{1}{1 - \frac{1}{3}} = \frac{3}{2}$$

$$\Rightarrow S = \frac{9}{4}$$

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$$\therefore k \cdot \frac{9}{4} = 1 \Rightarrow k = \frac{4}{9}$$

Now 
$$P(x \ge 2) = 1 - P(x = 0, 1)$$

$$=1-\left(k+k.\frac{2}{3}\right)$$

$$=1-\frac{5k}{3}$$

$$=1-\frac{5}{3}.\frac{4}{9}$$

$$=\frac{7}{27}$$

13. If 
$$f(x) = \begin{cases} 3x^2 + k\sqrt{x+1} & 0 < x < 1 \\ 3mx^2 + k^2 & x \ge 1 \end{cases}$$
 is

differentiable at x > 1 then  $\frac{8f'(8)}{f'(\frac{1}{8})}$  is for  $k \ne 0$ 

- (1) 309
- (2) 311
- (3) 306
- (4) 305

### Answer (1)

**Sol.** 
$$f(x) = \begin{cases} 3x^2 + k\sqrt{x+1} & 0 < x < 1 \\ 3mx^2 + k^2 & x \ge 1 \end{cases}$$

$$3 + k\sqrt{2} = 3m + k^2$$
 ...(i

$$f'(x) = \begin{cases} 6x + \frac{k}{2\sqrt{x+1}} & 0 < x < 1\\ 6mx & x \ge 1 \end{cases}$$

$$6 + \frac{k}{2\sqrt{2}} = 6m$$
 ...(ii)

$$3 + k\sqrt{2} = 3 + \frac{k}{4\sqrt{2}} + k^2$$

$$k = 0 \text{ or } \frac{7\sqrt{2}}{8}$$

If 
$$k = 0$$

If 
$$k = \frac{7\sqrt{2}}{8}$$

$$m = \frac{103}{96}$$

(Rejected)

Now, 
$$\frac{8f'(8)}{f'\left(\frac{1}{8}\right)} = \frac{48m}{\frac{6}{8} + \frac{k}{2\sqrt{\frac{9}{8}}}} = \frac{48m}{\frac{6}{8} + \frac{\sqrt{2}k}{3}}$$

$$\frac{8f'(8)}{f'\left(\frac{1}{8}\right)} = 309$$

- 14.
- 15.
- 16.
- 17.
- 18.
- 19.
- 20.

#### **SECTION - B**

**Numerical Value Type Questions:** This section contains 10 questions. In Section B, attempt any five questions out of 10. The answer to each question is a **NUMERICAL VALUE.** For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to the second decimal place; e.g., 06.25, 07.00, -00.33, -00.30, 30.27, -27.30) using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.

21. The area of quadrilateral having vertices as (1, 2), (5, 6), (7, 6), (-1, -6)

#### Answer (24)

Sol. Area = 
$$\frac{1}{2}$$
  $\begin{bmatrix} 1 & 7 & 2 \\ 5 & 7 & 6 \\ 7 & 7 & 6 \\ -1 & 7 & -6 \\ 1 & 2 \end{bmatrix}$   
=  $\frac{1}{2}$   $[6 + 30 - 42 - 2 - 10 - 42 + 6 + 6]$   
=  $\frac{1}{2}$   $[48] = 24$ 

22. The value of 
$$\int_{0}^{2.4} [x^2] dx$$
 is  $\alpha + \beta \sqrt{2} + \gamma \sqrt{3} + \delta \sqrt{5}$  then  $(a + b + c + d + e)$  is equal to

#### Answer (06)

**Sol.** 
$$\int_{0}^{2.4} [x^{2}] dx = \int_{0}^{1} 0 dx + \int_{1}^{\sqrt{2}} 1 dx + \int_{\sqrt{2}}^{\sqrt{3}} 2 dx + \int_{\sqrt{3}}^{\sqrt{4}} 3 dx + \int_{\sqrt{4}}^{\sqrt{5}} 4 dx + \int_{\sqrt{5}}^{2.4} 5 dx$$
$$= (\sqrt{2} - 1) + 2(\sqrt{3} - \sqrt{2}) + 3(\sqrt{4} - \sqrt{3}) + 4(\sqrt{5} - \sqrt{4}) + 5(2.4 - \sqrt{5})$$

$$=9-\sqrt{2}-\sqrt{3}-\sqrt{5}$$

$$\alpha = 9$$
,  $\beta = -1$ ,  $\gamma = -1$ ,  $\delta = -1$ 

$$\therefore \quad \alpha + \beta + \gamma + \delta = 6$$

23. 
$$\frac{dx}{dy} - \frac{3\sin y}{\cos y \left(\ln \cos y\right)} x = \frac{\sin y}{\left(\ln \cos y\right)^2 \cos y}$$
 and

$$x\left(\frac{\pi}{3}\right) = \frac{1}{2\ln 2}, x\left(\frac{\pi}{6}\right) = \frac{1}{\ln(m) - \ln(n)}$$
 then the value

of mn is

# Answer (12)

**Sol.** 
$$I = e \int \frac{-3 \sin y}{\cos y (\ln \cos y)} dy$$

Put ln(cos y) = t

$$\frac{-1}{\cos y}\sin y \ dy = dt$$

$$=e\int \frac{3}{t}dt$$

$$= (\ln \cos y)^3$$

$$x(\ln\cos y)^3 = \int \frac{\sin y}{\cos y} \ln\cos y \ dy$$

$$x(\ln\cos y)^3 = \frac{-(\ln(\cos y))^2}{2} + C$$

$$x\left(\frac{\pi}{3}\right) = \frac{1}{2\ln 2}$$

$$\Rightarrow$$
  $C = 0$ 

$$\therefore x = -\frac{1}{2\ln(\cos y)}$$

$$x\left(\frac{\pi}{6}\right) = \frac{1}{\ln 4 - \ln 3}$$

$$m = 4$$

$$n = 3$$

24. If *m* is the number of solution of  $x^2 - 12x + 31 + [x] = 0$  and *n* be the number of solution of  $x^2 - 5|_{X+2}| - 4 = 0$ , then the value of  $m^2 + mn + n^2$  is

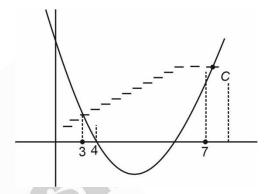
# Answer (19)

**Sol.** 
$$x^2 - 12x + 31 - [x] = 0$$

$$x^2 - 12x + 31 = [x]$$

$$(x-6)^2-5=[x]$$

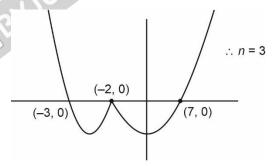
So, by graph



.. Two points of intersects

$$m = 2$$

$$x^2 - 5|_{X-2}|_{-4} = 0$$



$$m^2 + mn + n^2 = 4 + 6 + 9 = 19$$