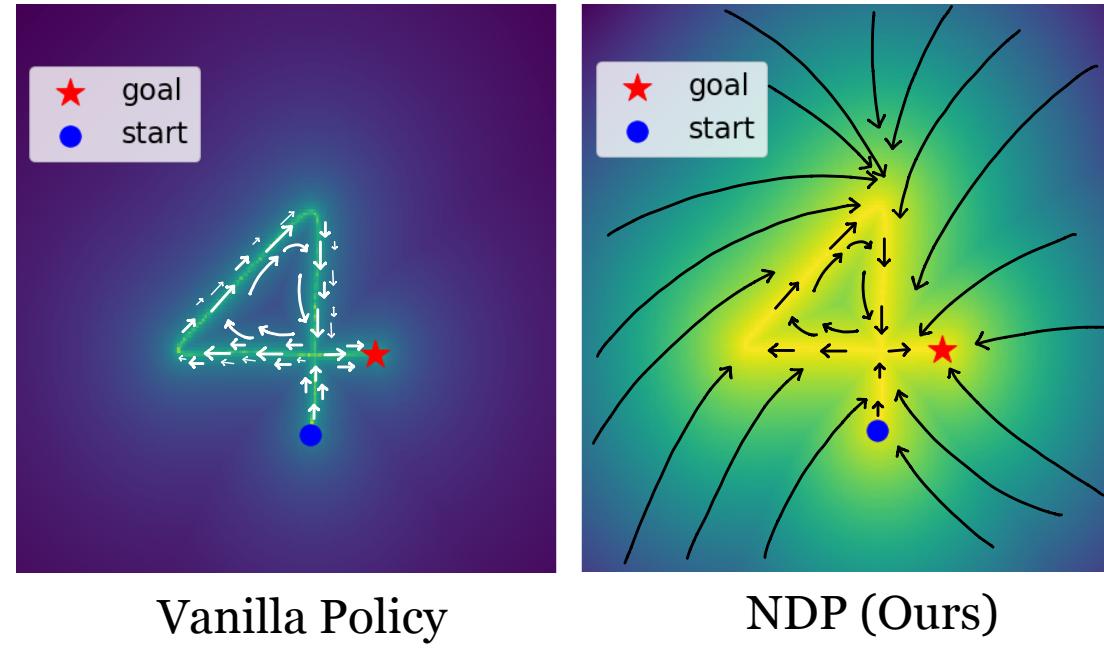


Neural Dynamic Policies for End-to-End Sensorimotor Learning



Shikhar Bahl, Mustafa Mukadam, Abhinav Gupta, Deepak Pathak





✓ Needs to reason in trajectory space





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✓ Needs to consider momentum and forces





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Needs Kinematics + Dynamics





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only reason at each timestep



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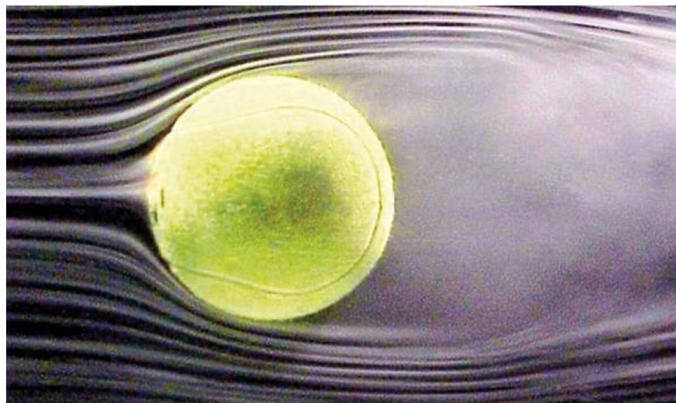


- ✗ Deep robot learning methods only reason at each timestep
- ✗ Only operate in raw action space (torque, joint angles, etc)

Can we build policies that reason directly in trajectory space?

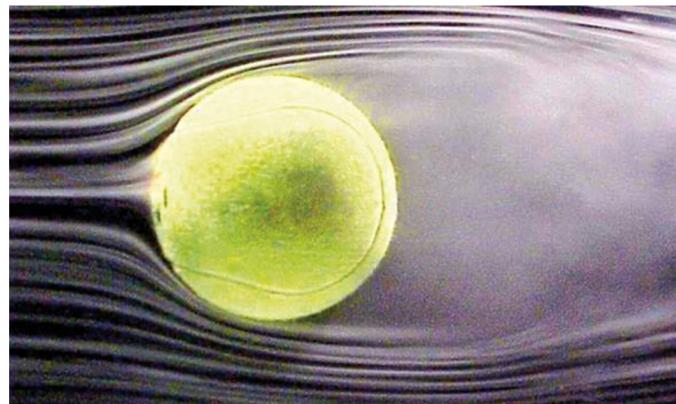
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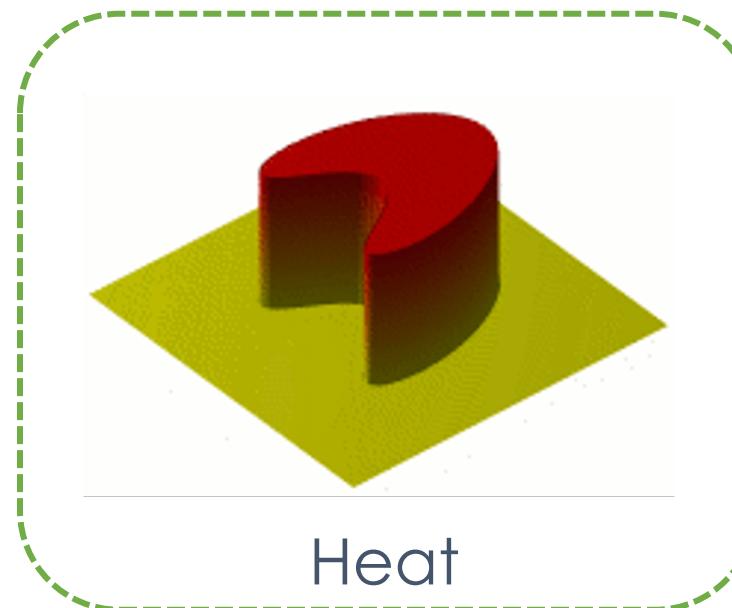


Fluids

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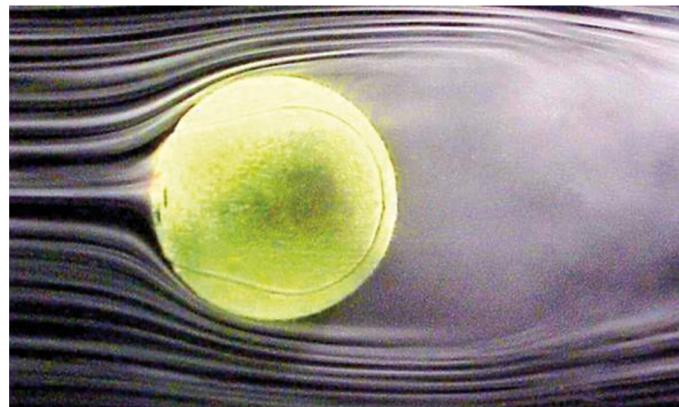


Fluids

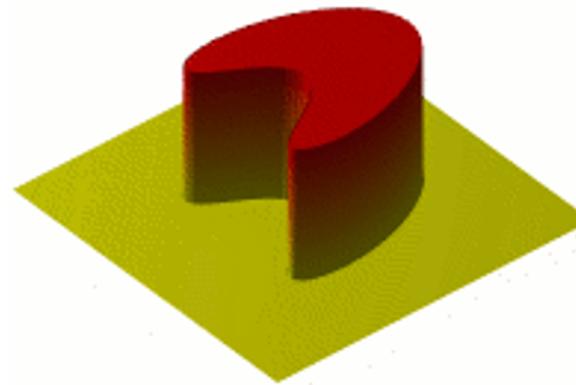


Heat

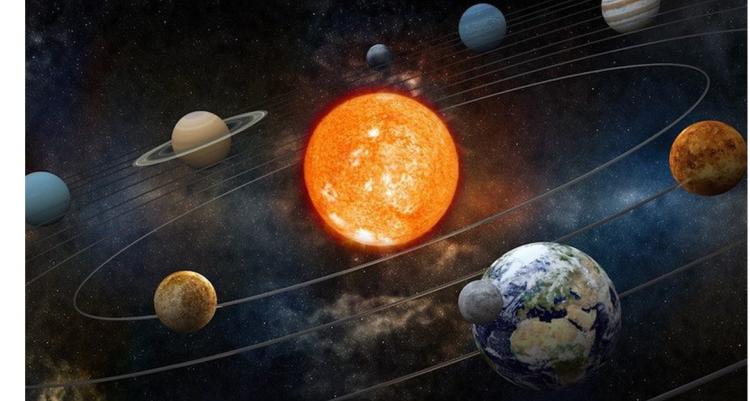
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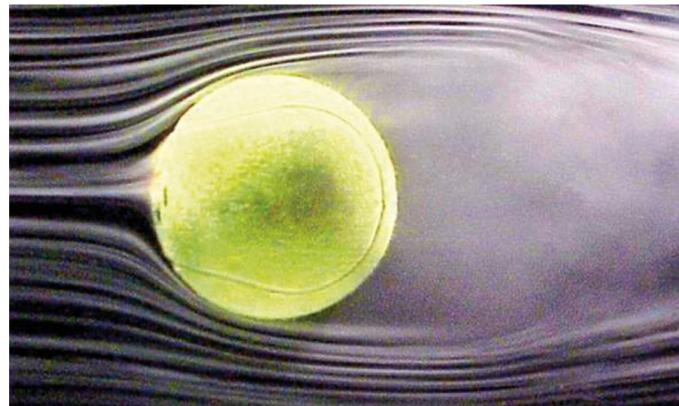


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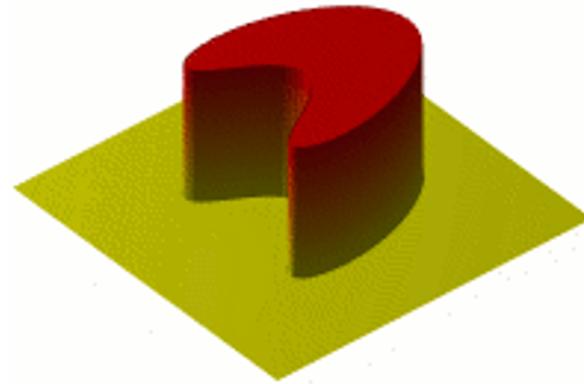


Gravity

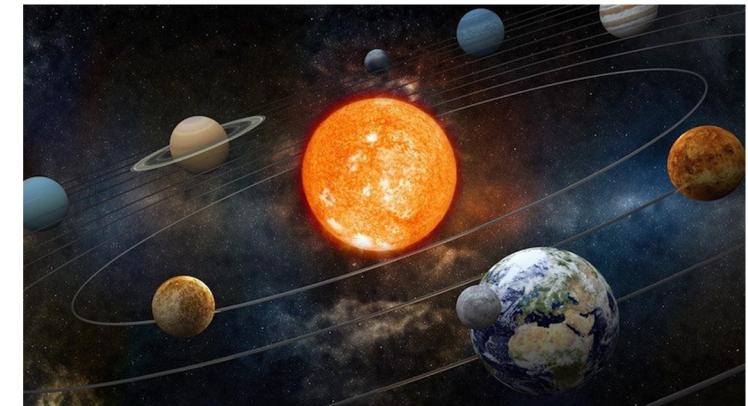
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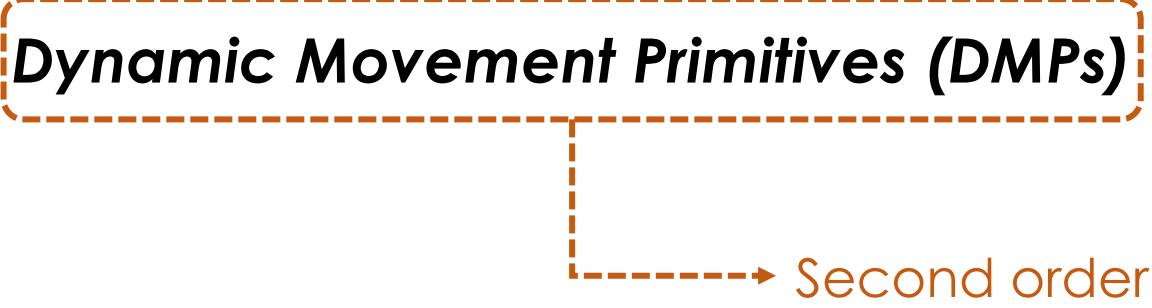
Gravity

Can we use the same formulation be used to describe the motion of a robot?

Popular in classical robotics: ***Dynamic Movement Primitives (DMPs)*** [Schaal, 2002]

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Second order dynamical system

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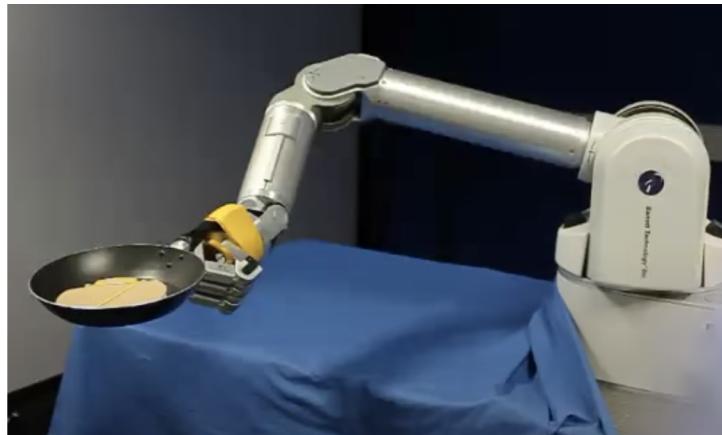
Second order dynamical system

Table Tennis



[Muelling et. al, 2013]

Pancake Flipping



[Kormushev et. al, 2010]

Letter Writing



[Steinmetz, 2014]

DMP-based Methods

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*Can handle dynamic tasks
but require sparse supervision (i.e. rewards)*

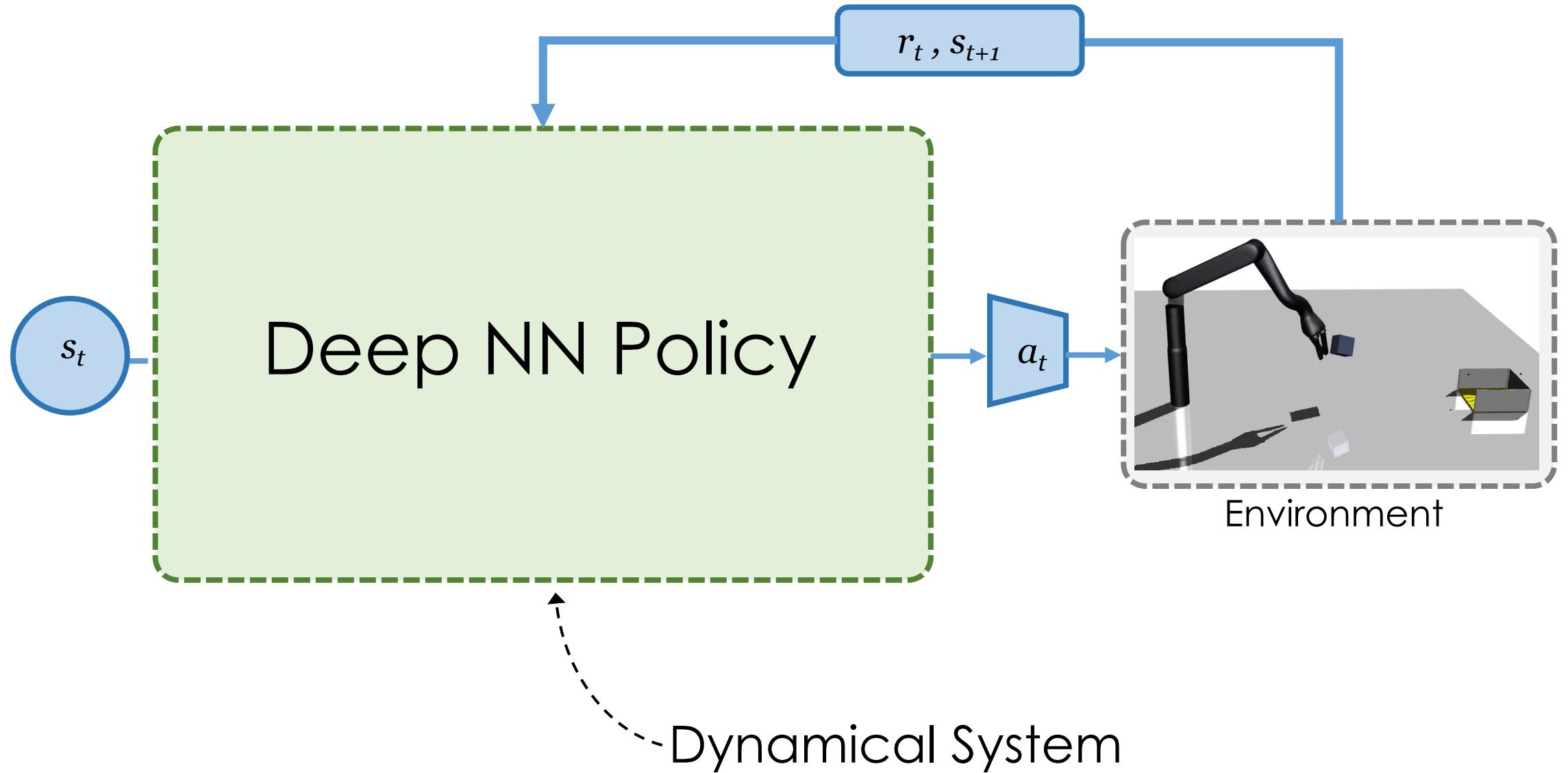
*Are sensitive to parameter tuning
and require dense supervision*

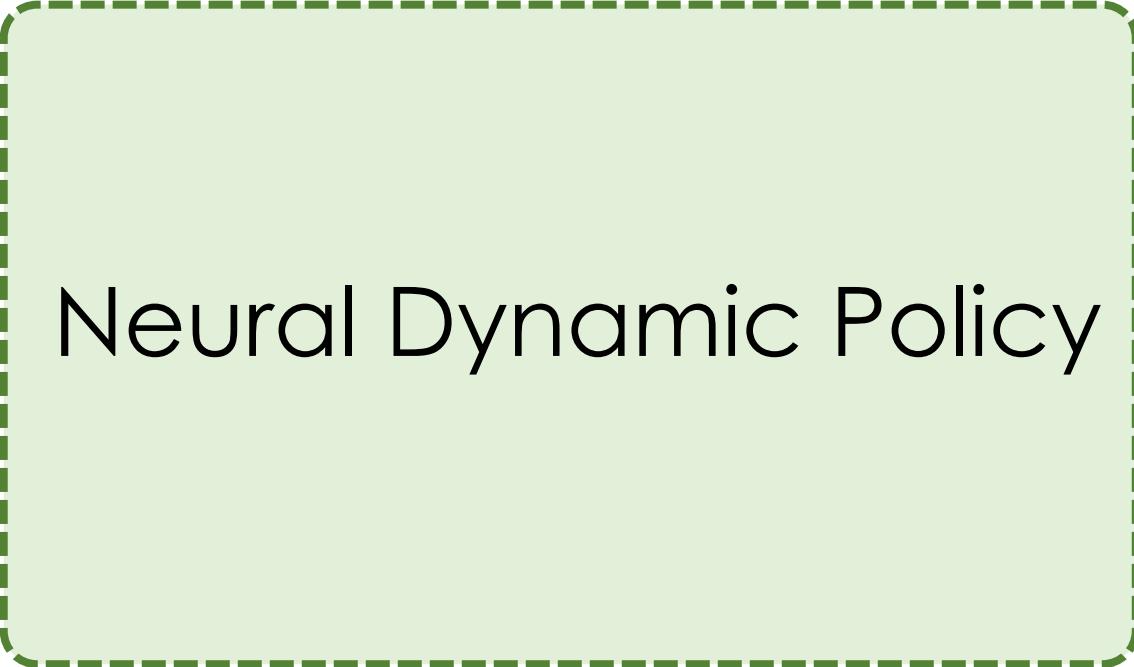
Do not scale to high dimensional inputs

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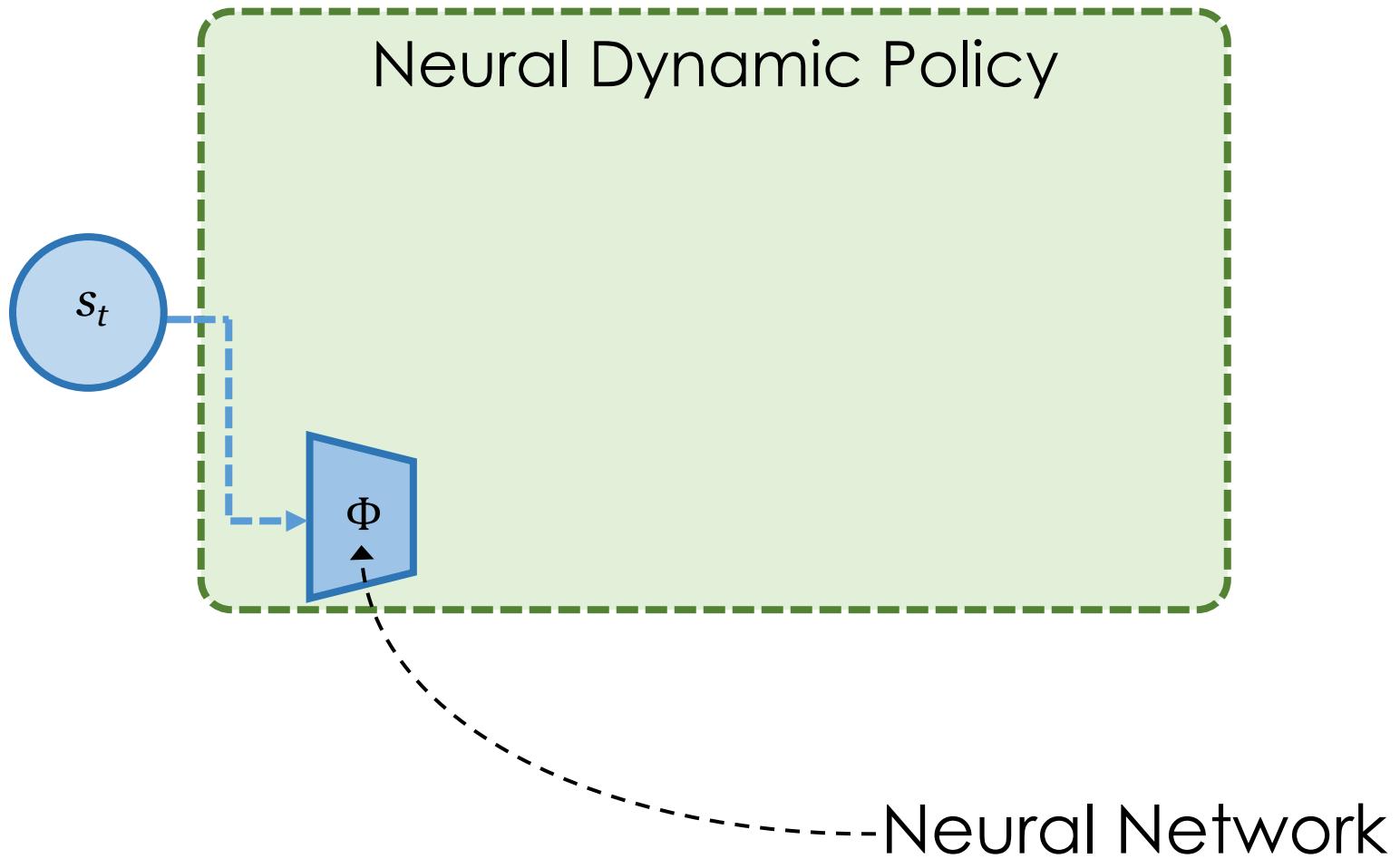
How can we bridge the gap between these two paradigms?

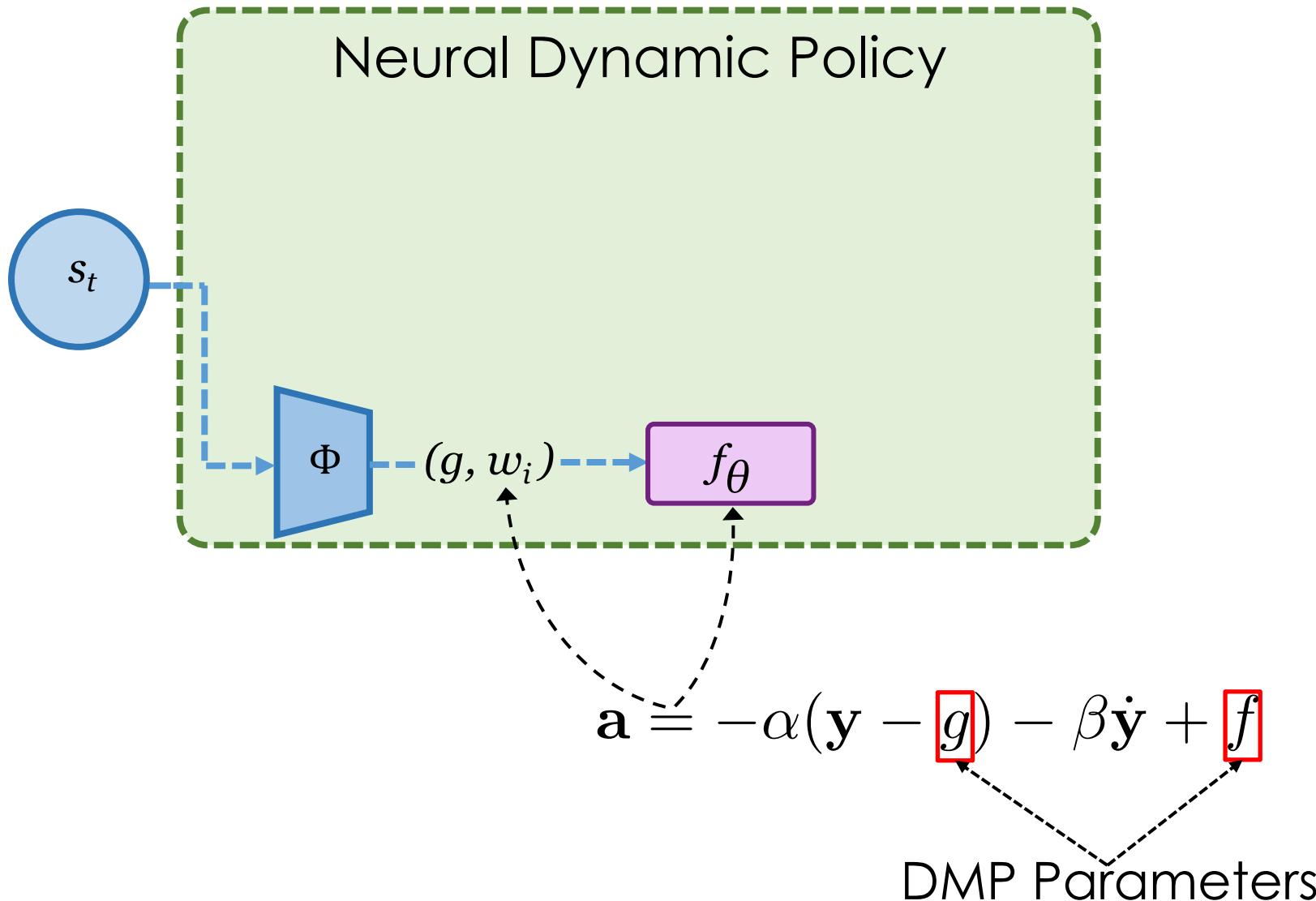
Difficulty with dynamic tasks

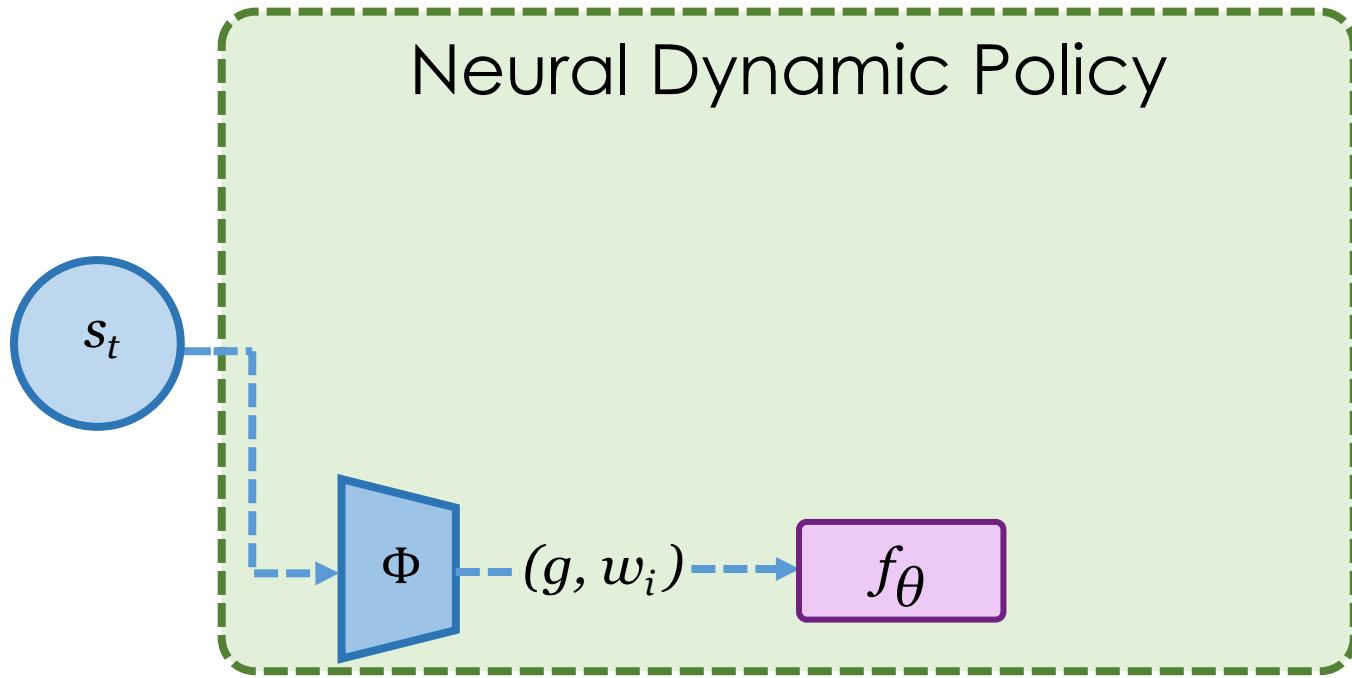




Neural Dynamic Policy

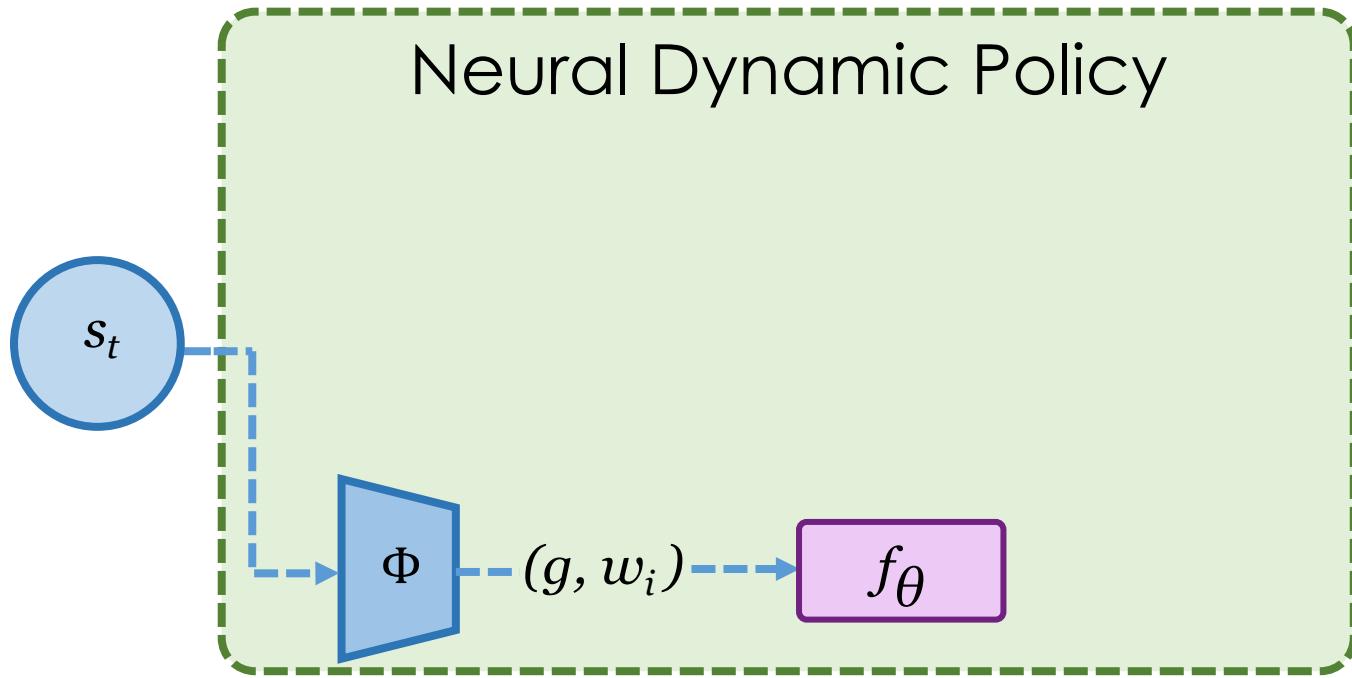






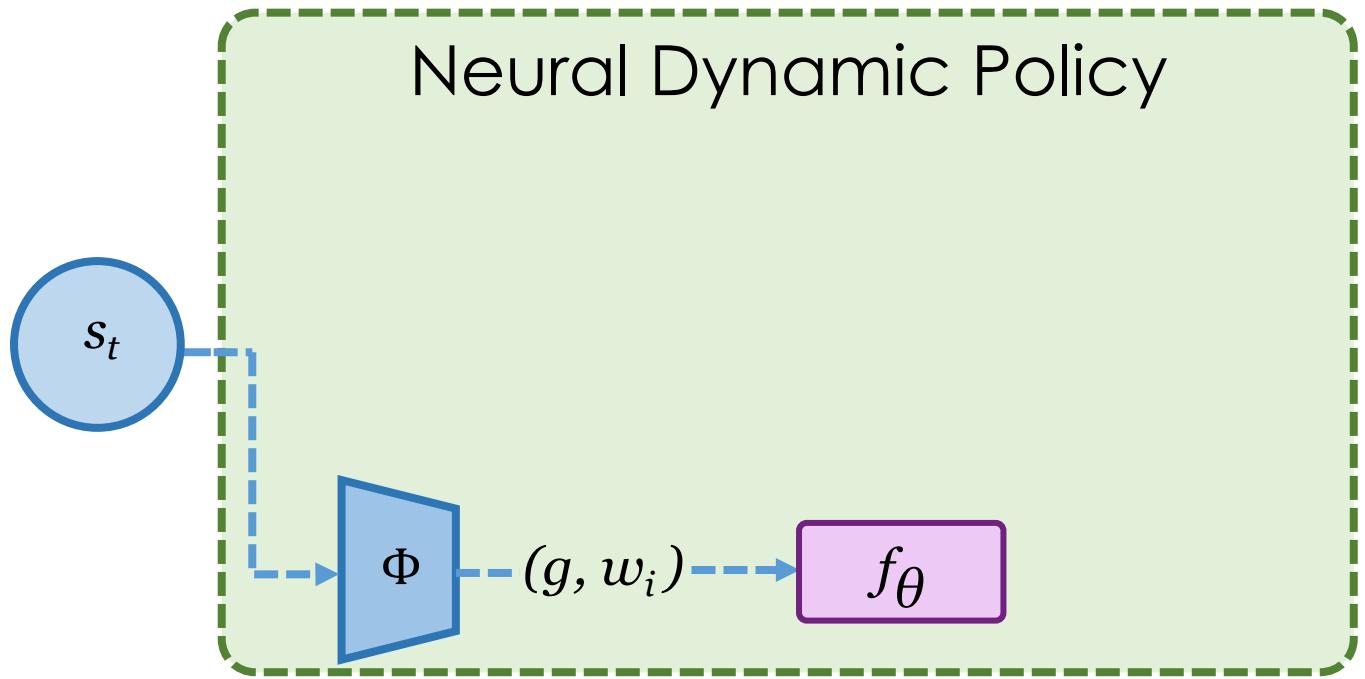
$$\mathbf{a} = -\alpha(\mathbf{y} - g) - \beta \dot{\mathbf{y}} + f$$

Robot position



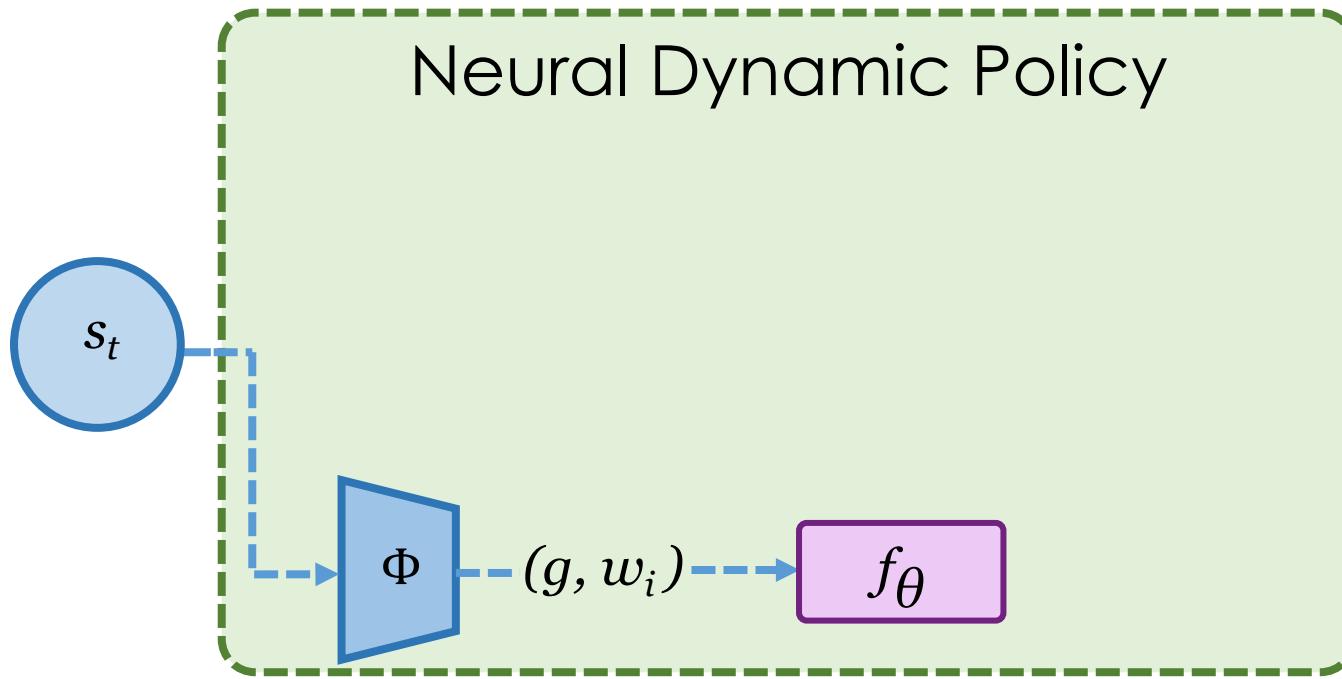
$$\mathbf{a} = -\alpha(\mathbf{y} - \boxed{g}) - \beta \dot{\mathbf{y}} + f$$

Goal position



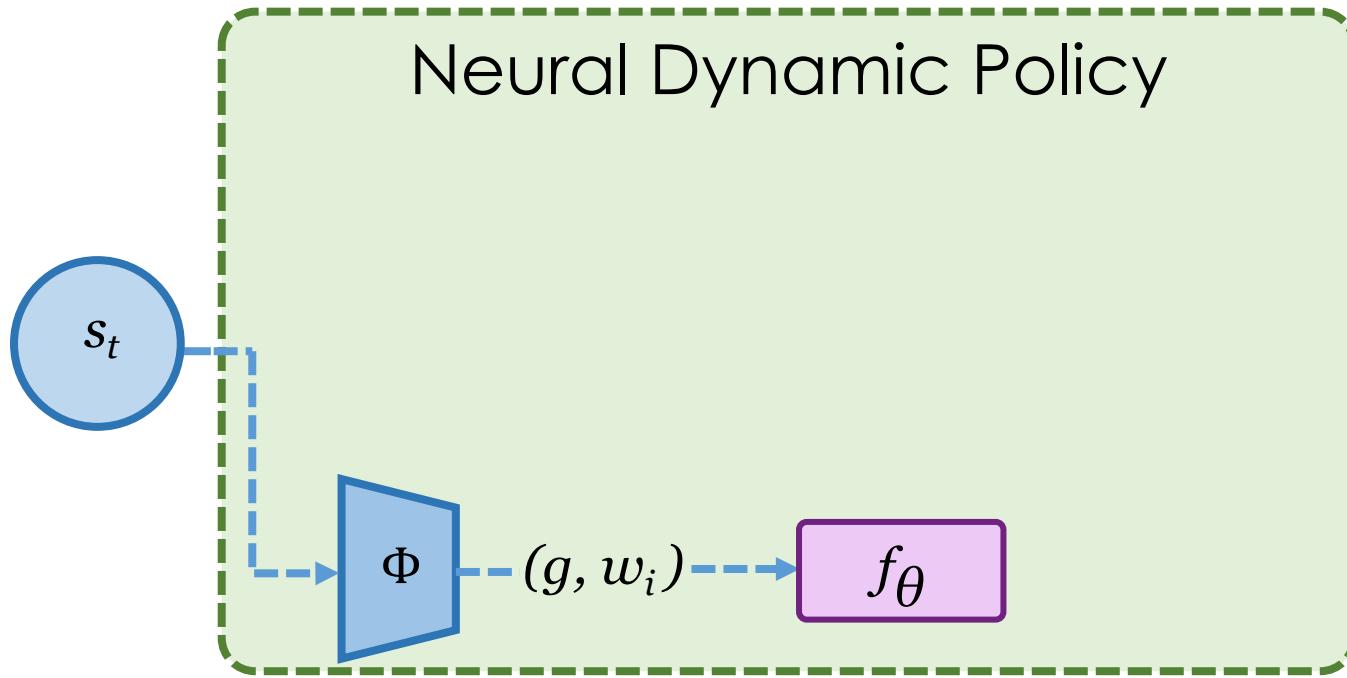
$$\mathbf{a} = -\alpha(\mathbf{y} - g) - \beta\dot{\mathbf{y}} + f$$

2nd Order Differential Equation in \mathbf{y}

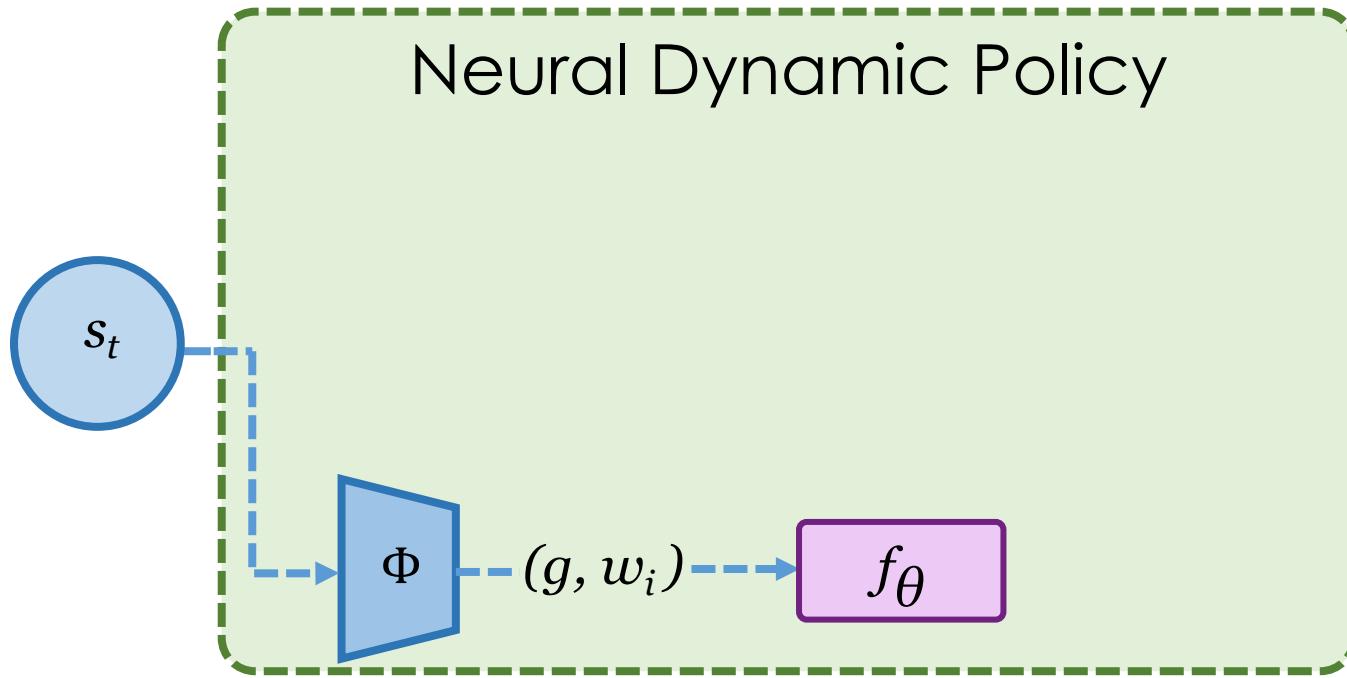


$$\mathbf{a} = -\alpha(\mathbf{y} - g) - \beta\dot{\mathbf{y}} + \boxed{f}$$

Forcing function

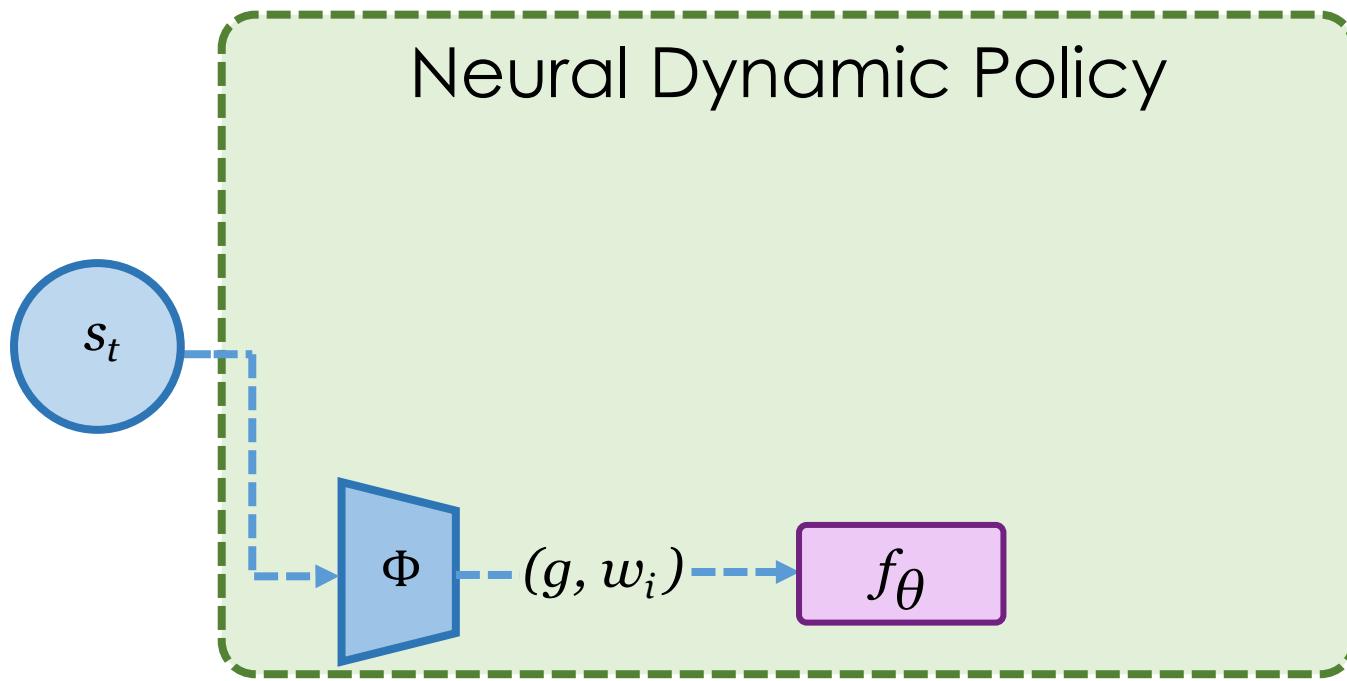


$$f(x) = \frac{\sum_{i=1}^N \Psi_i(x) w_i}{\sum_{i=1}^N \Psi_i(x)} x(g - y_0)$$



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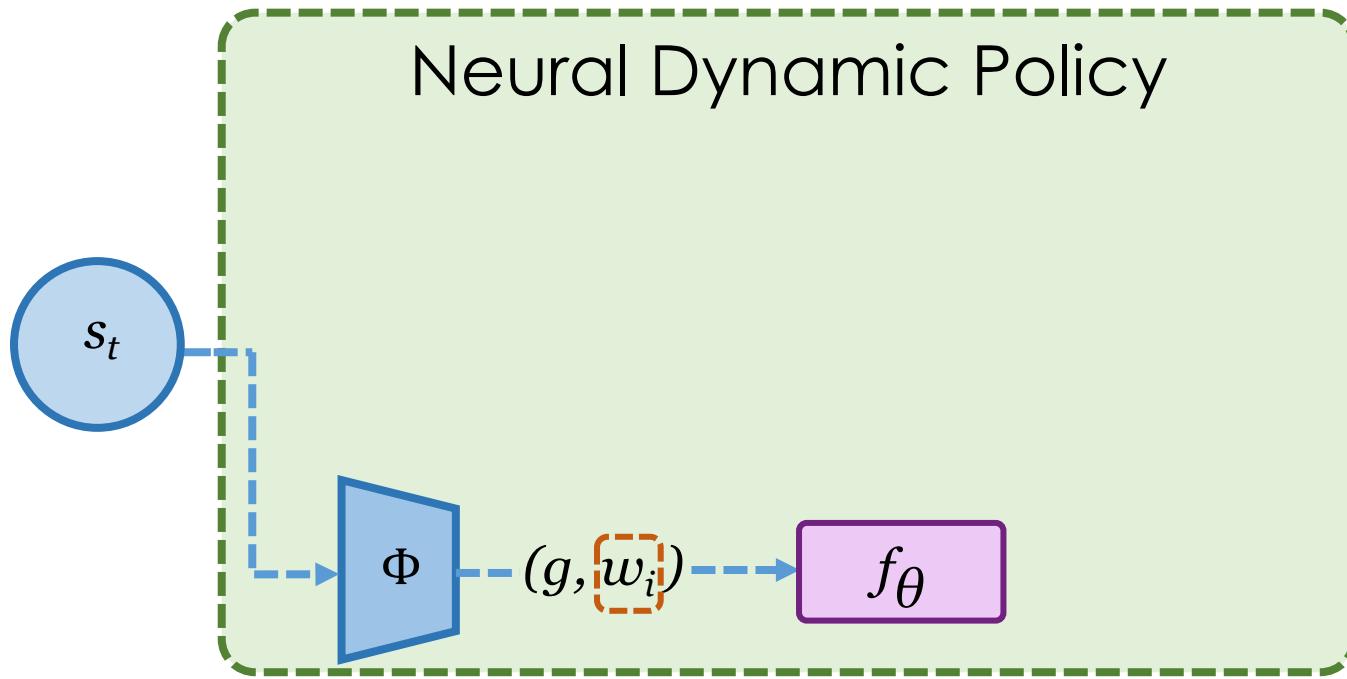
Radial Basis Function



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$\Psi_i(x) = \exp\left(-\frac{1}{2\sigma_i^2}(x - c_i)^2\right),$

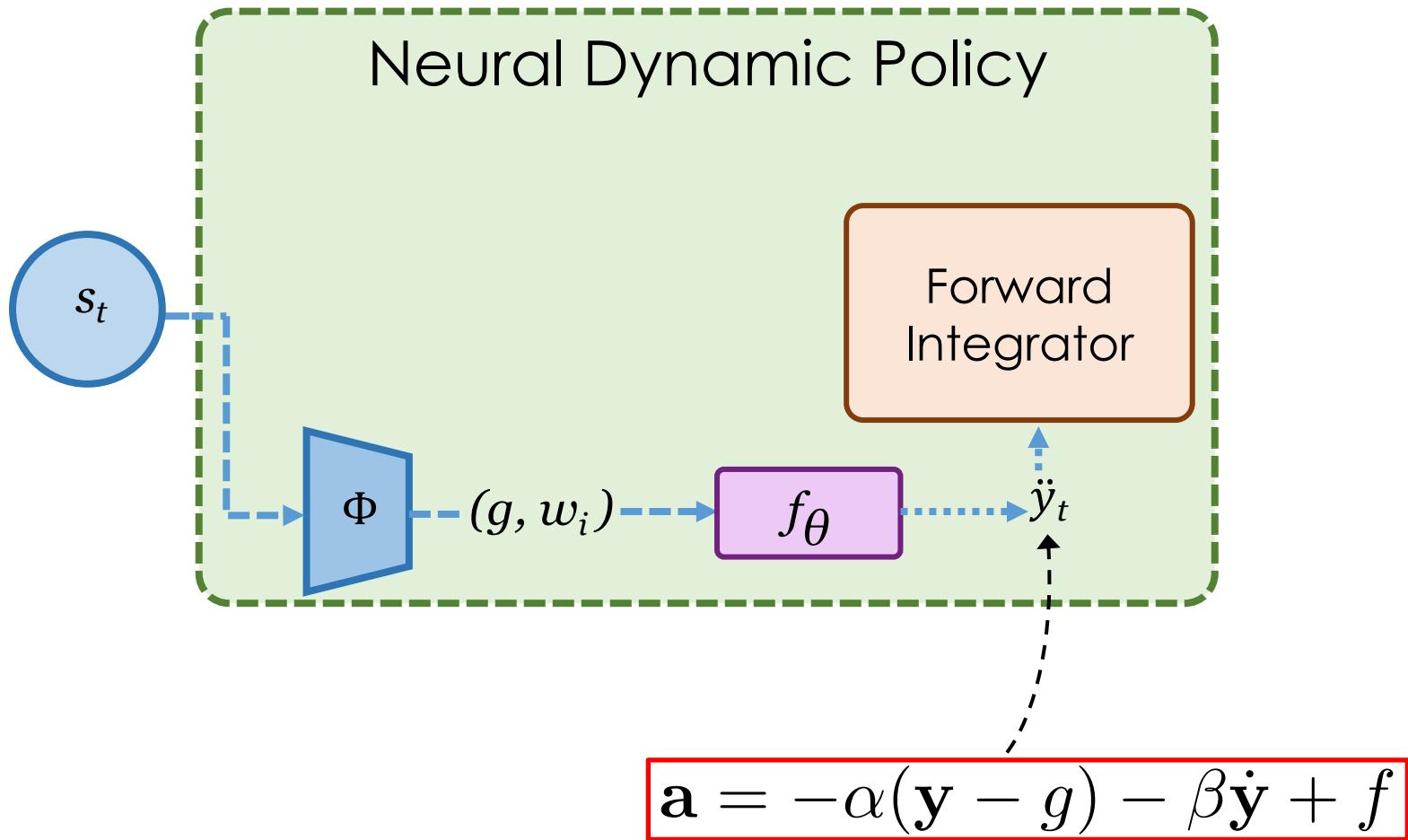
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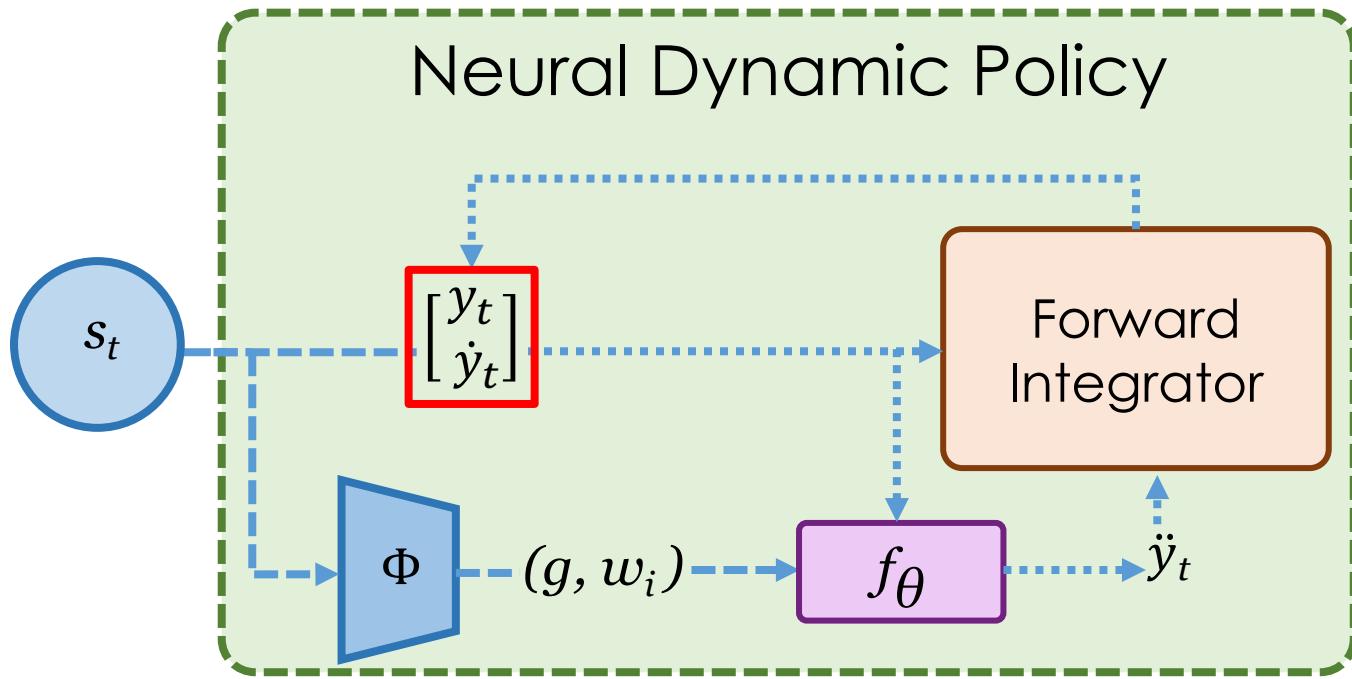


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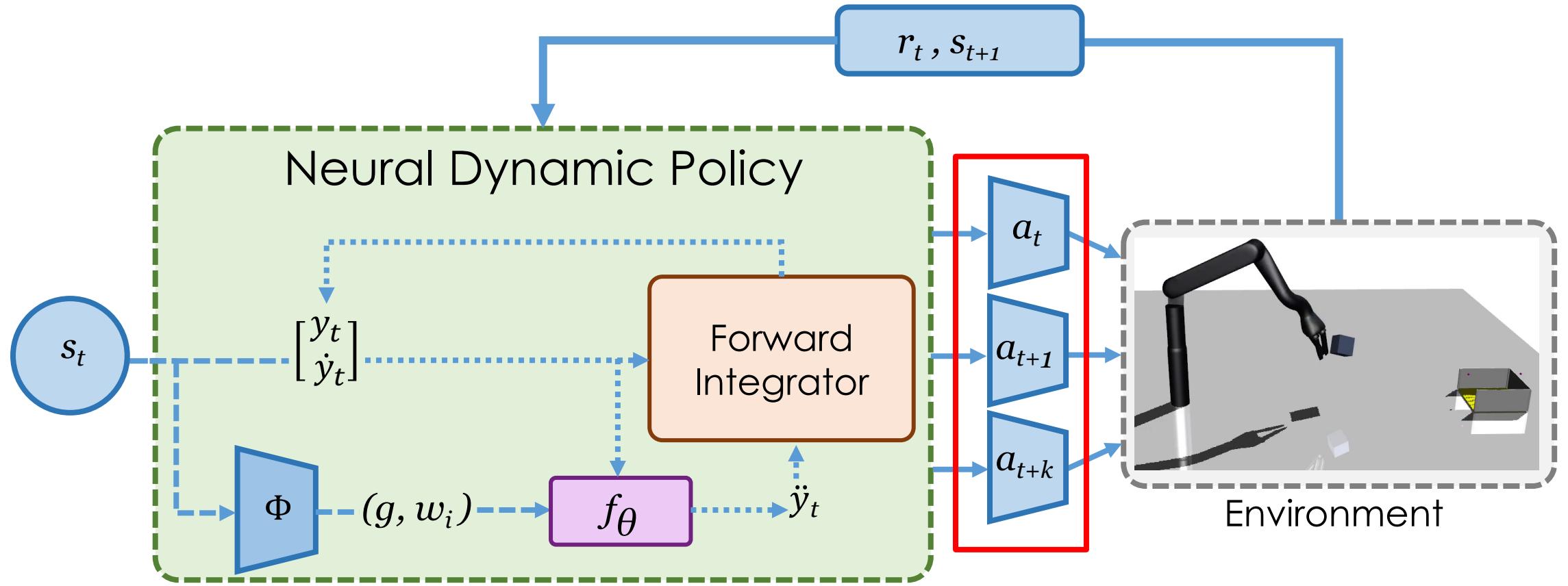
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Weight of RBF



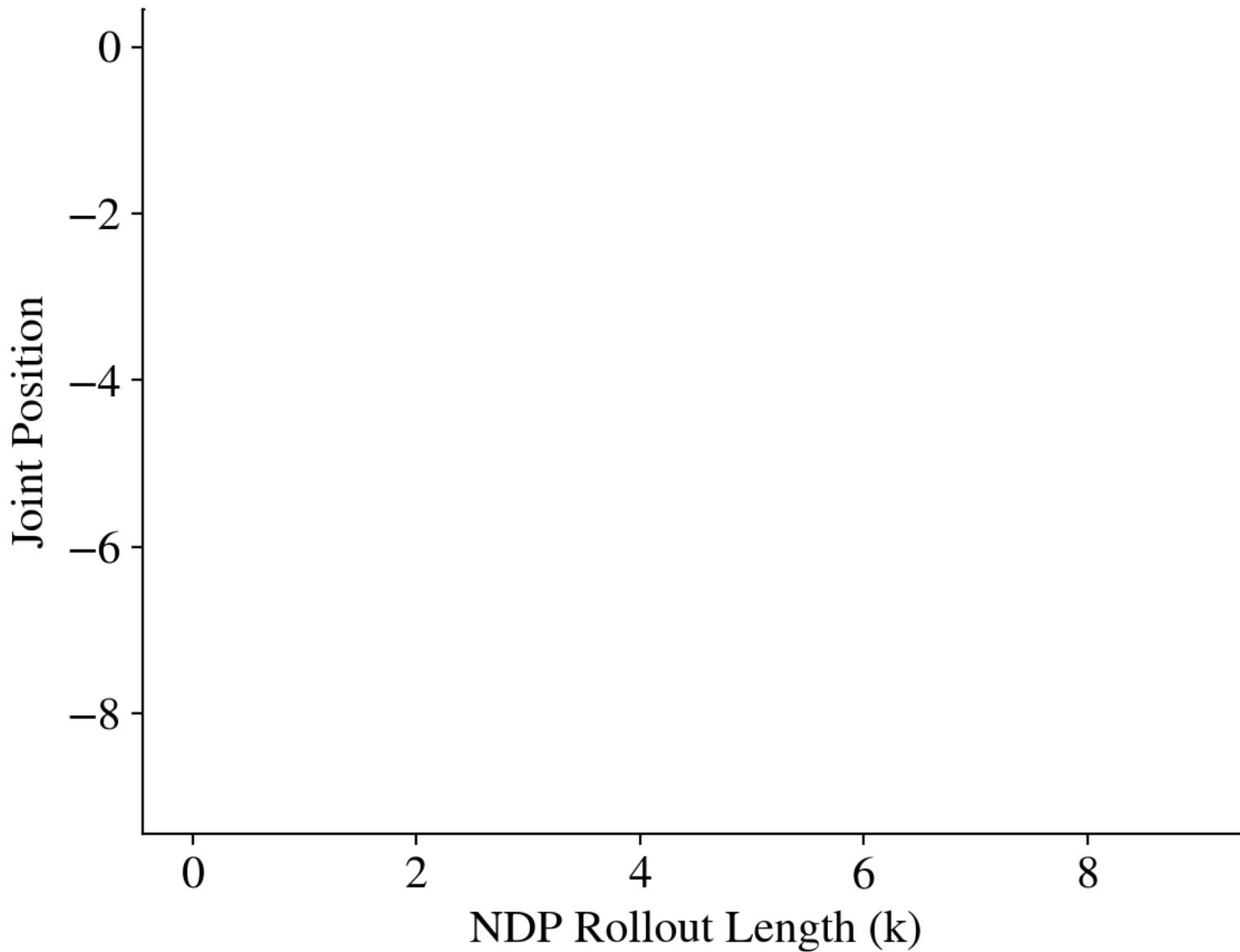


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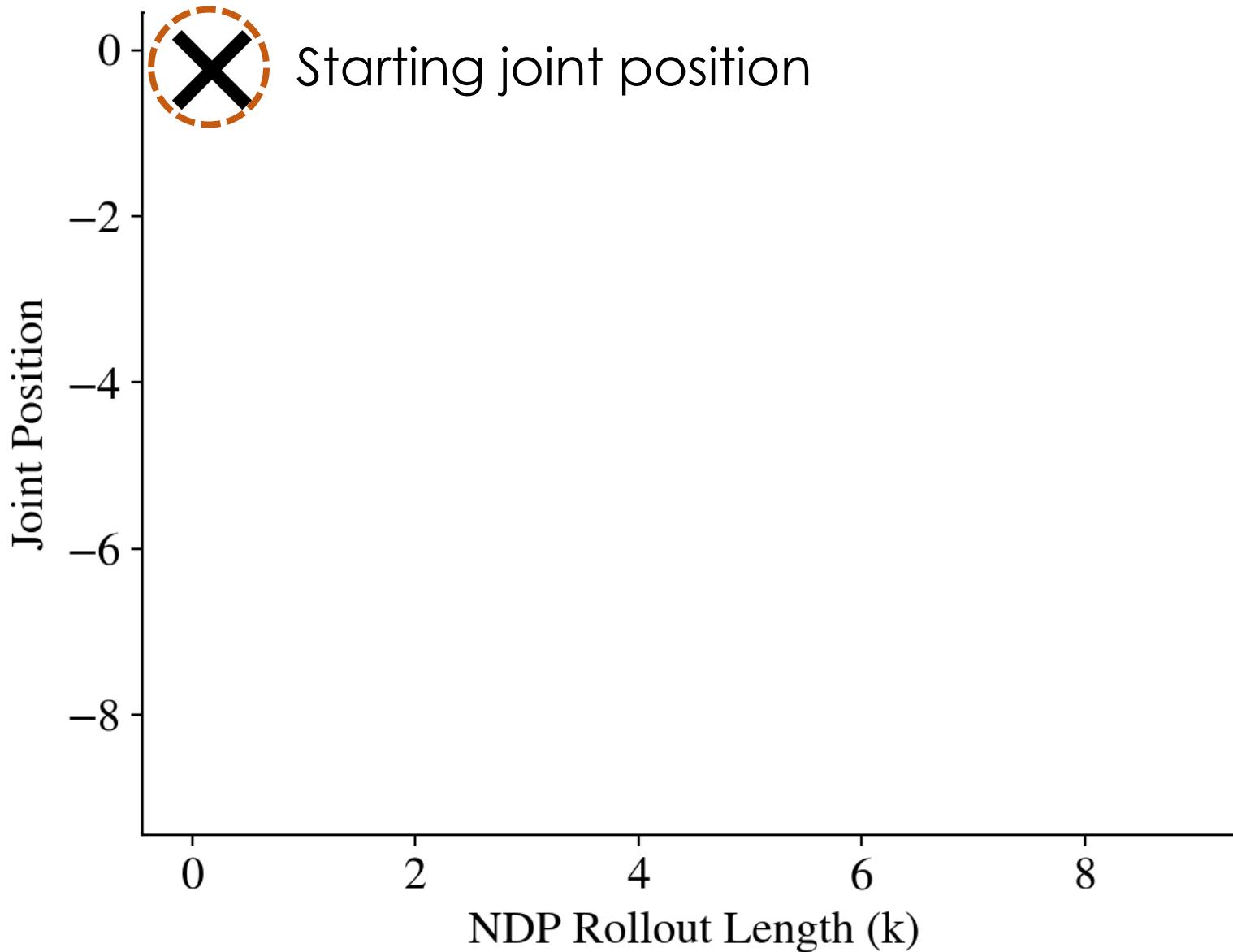


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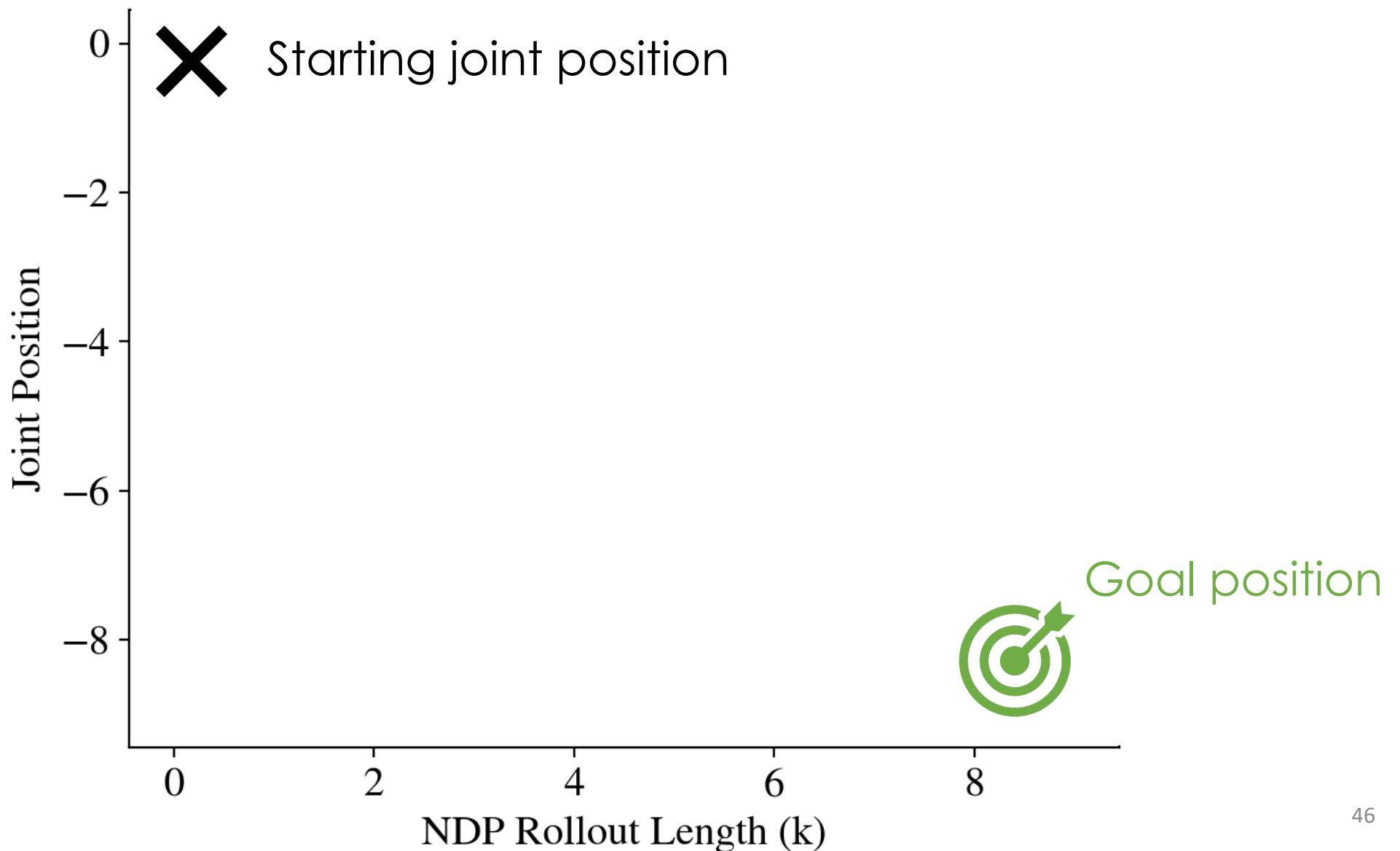
NDPs Intuition



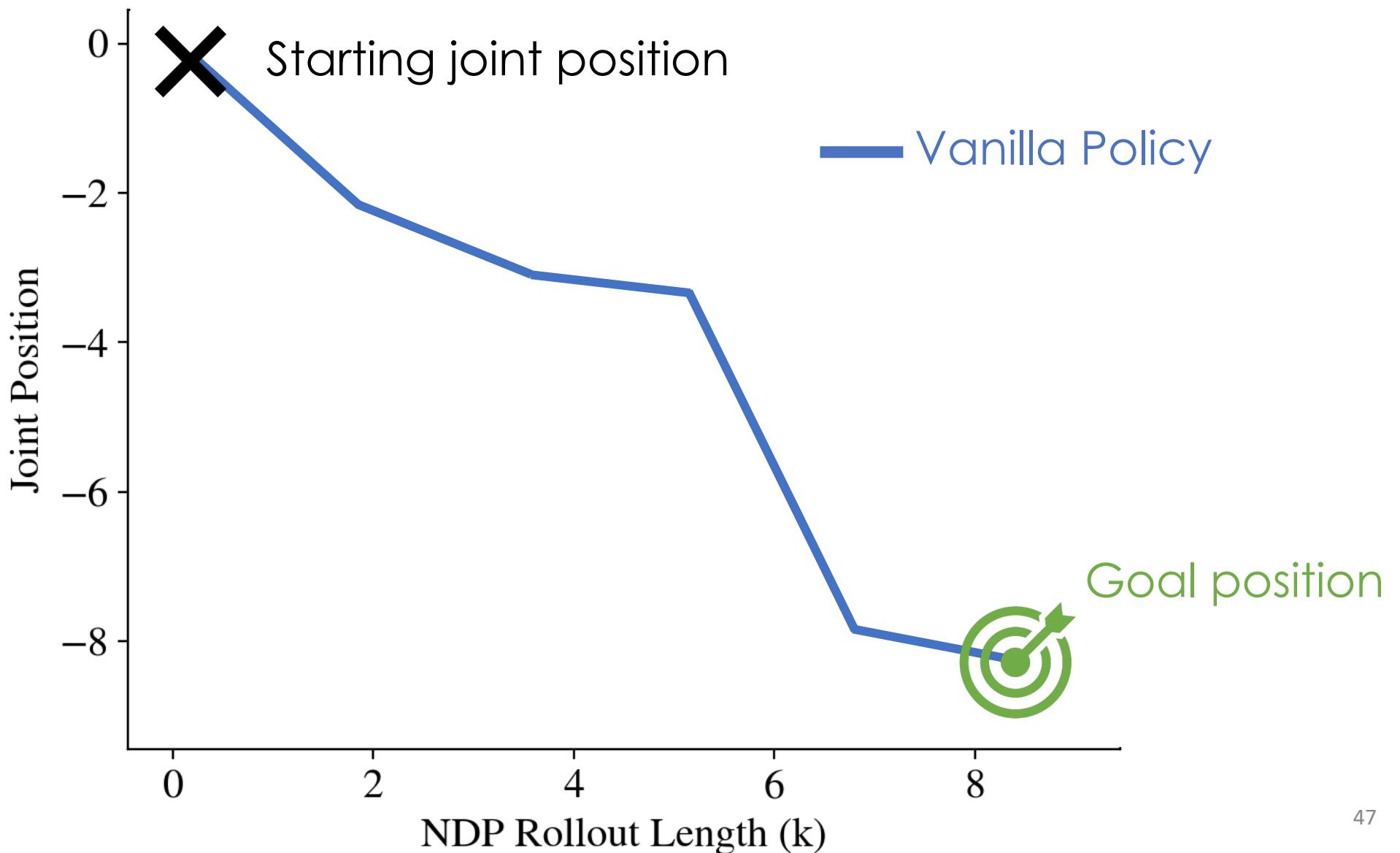
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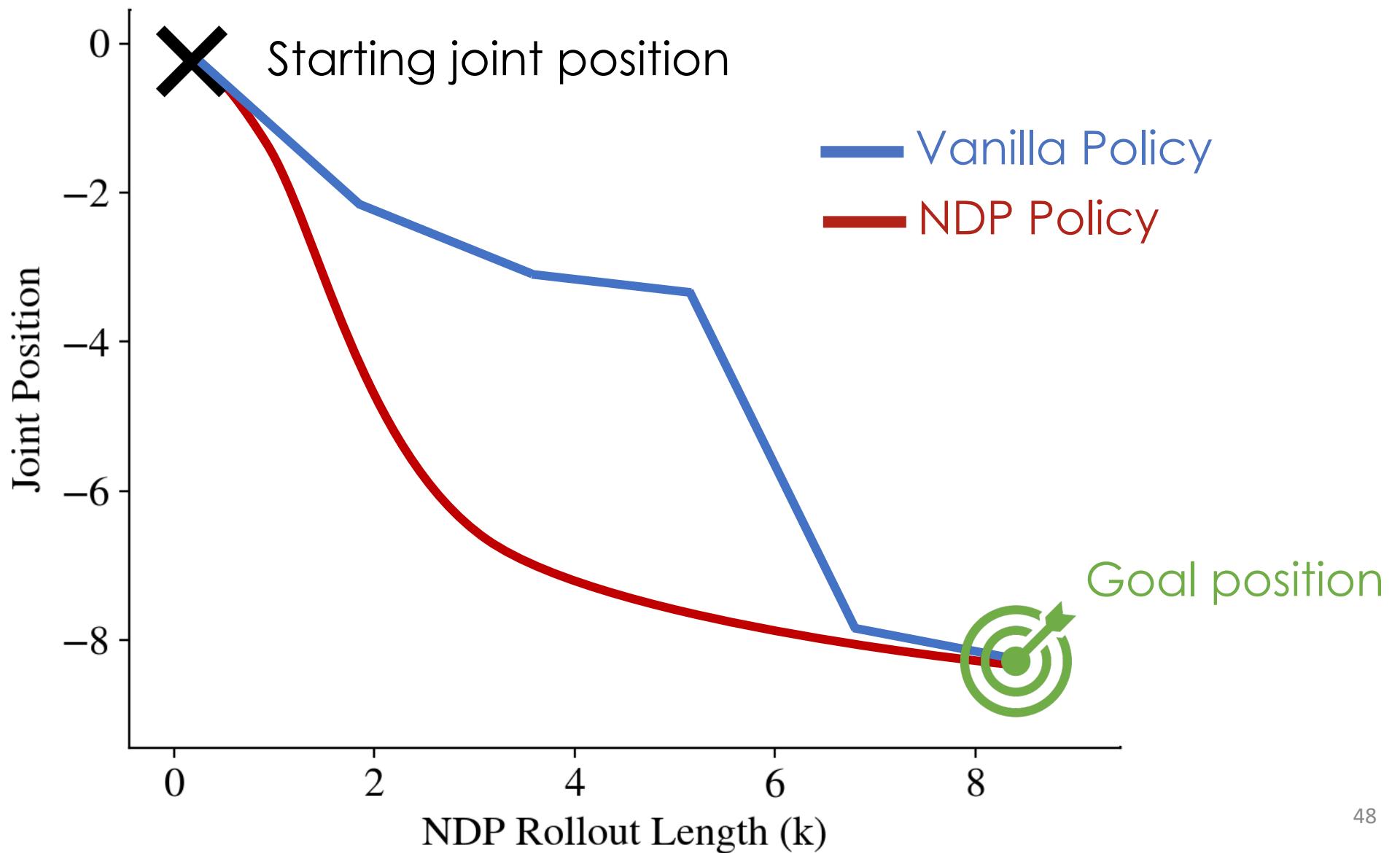
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RL Algorithm

Algorithm 1 Training NDPs for RL

Require: Policy π , k NDP rollout length, g low-level inverse controller

for 1, 2, ... episodes **do**

for $t = 0, k, \dots$, until end of episode **do**

$w, g = \Phi(s_t)$

Robot y_t, \dot{y}_t from s_t (pos, vel)

for $m = 1, \dots, M$ (integration steps) **do**

Estimate \dot{x}_m via (2) and update x_m

Estimate $\ddot{y}_{t+m}, \dot{y}_{t+m}, y_{t+m}$ via (4), (5)

$a_{t+n} = g(y_{t+m}, y_{t+m-1})$

Apply action a_{t+n} to get s_{t+n+1}

Store transition (s, a, s', r)

end for

Compute Policy gradient ∇_θ

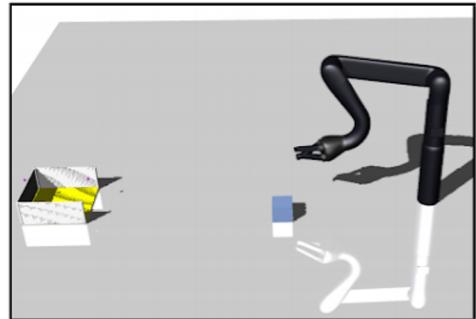
$\theta \leftarrow \theta + \eta \nabla_\theta J$

end for

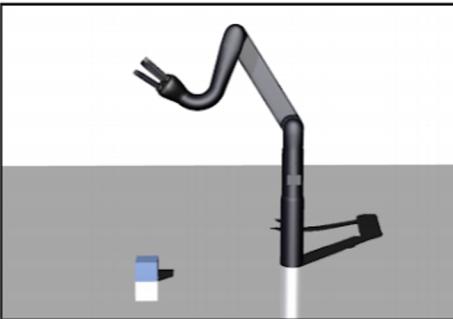
end for

Results

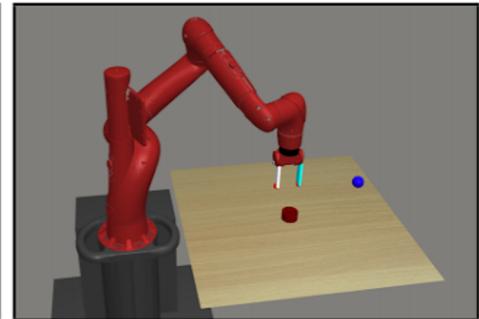
Reinforcement Learning



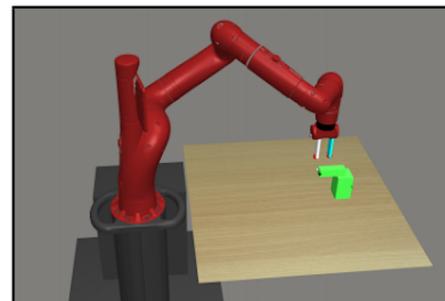
(a) Throwing



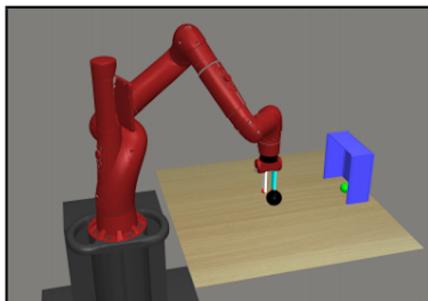
(b) Picking



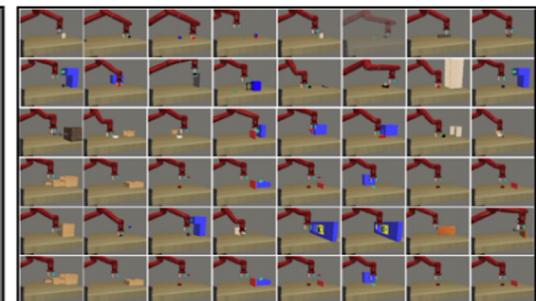
(c) Pushing



(d) Faucet Open

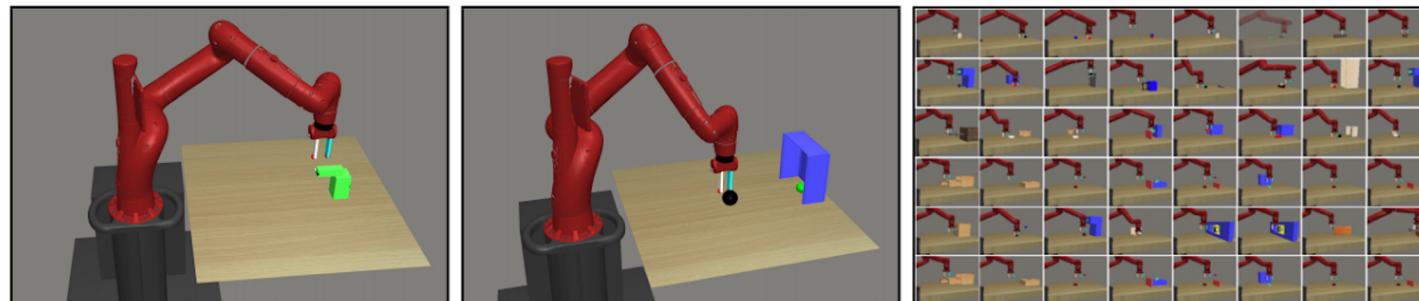
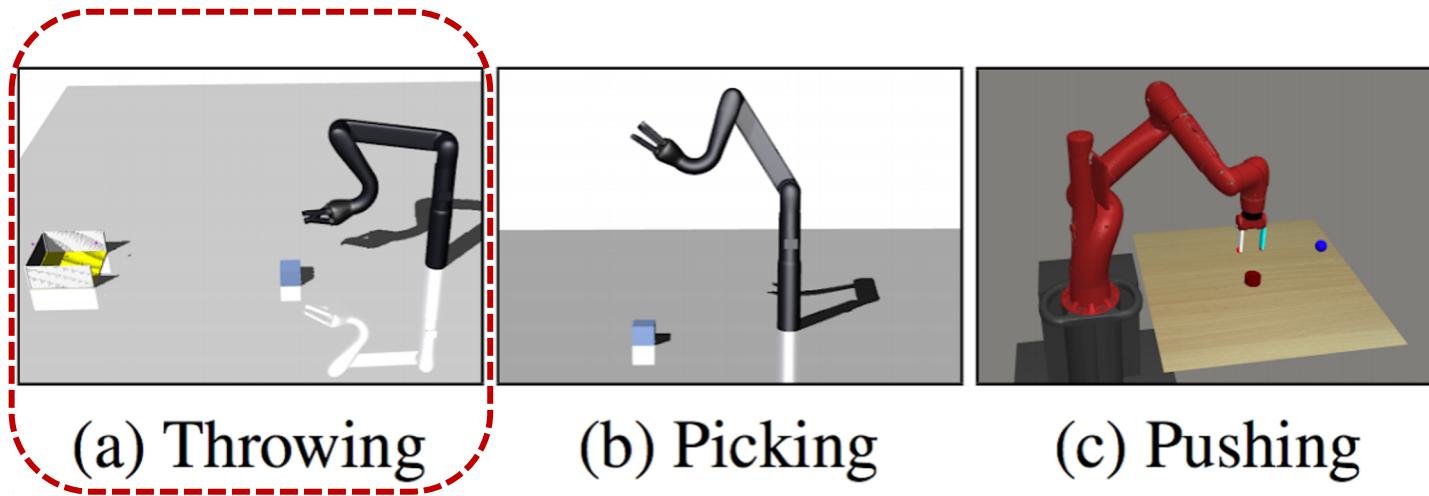


(e) Soccer

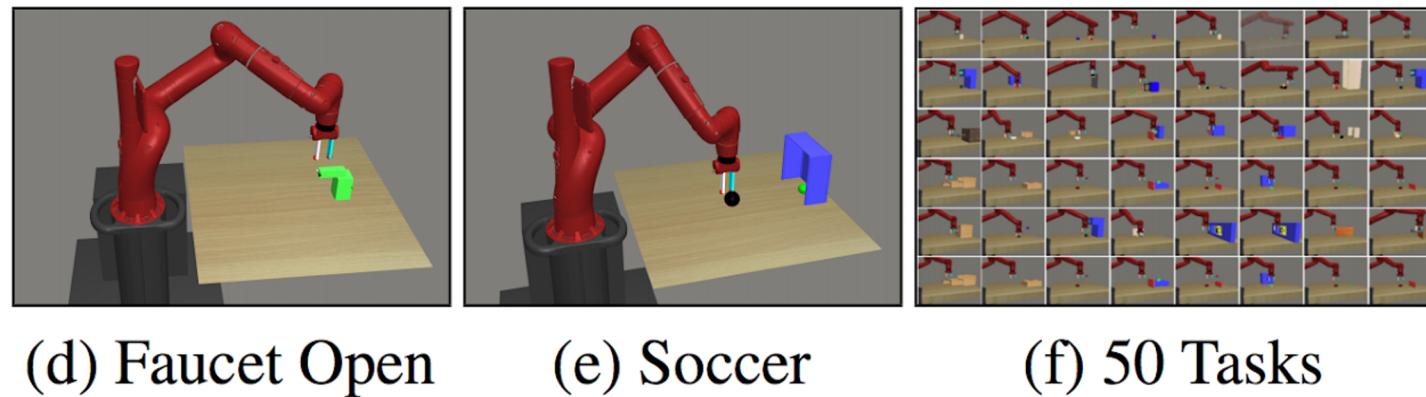
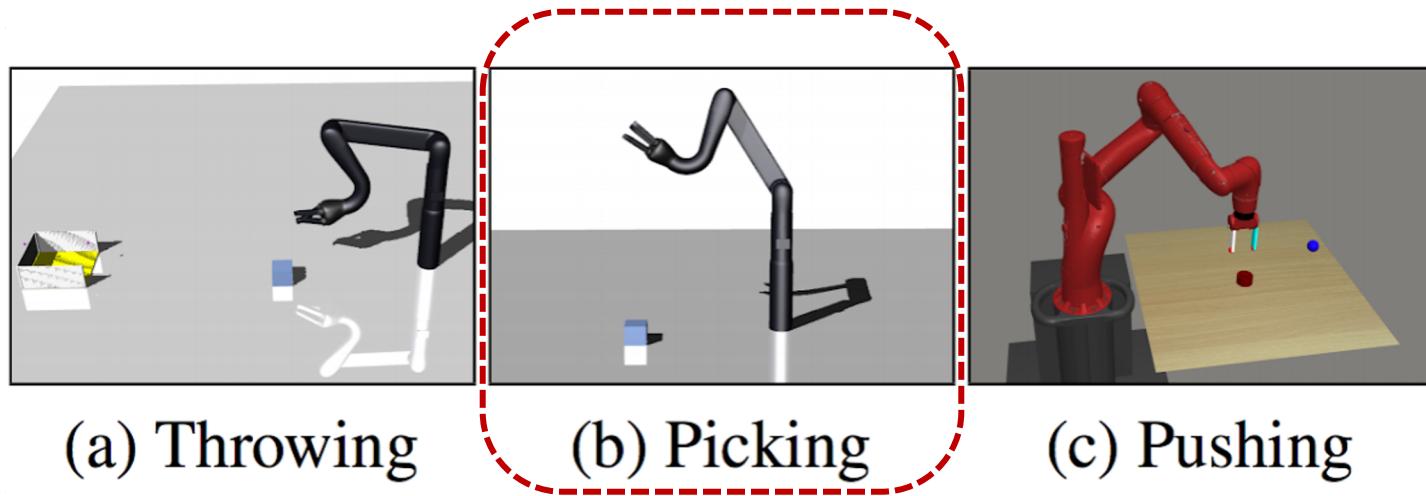


(f) 50 Tasks

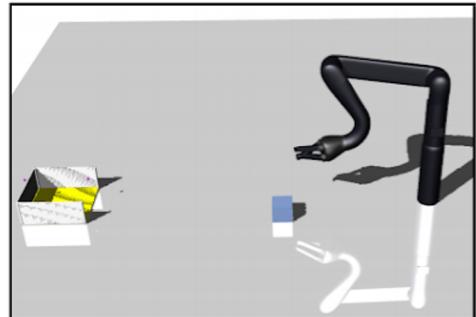
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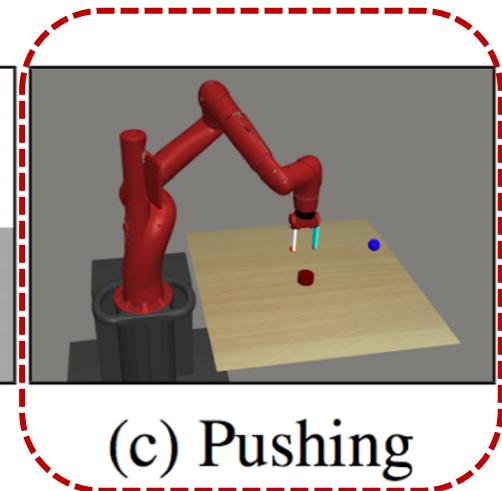
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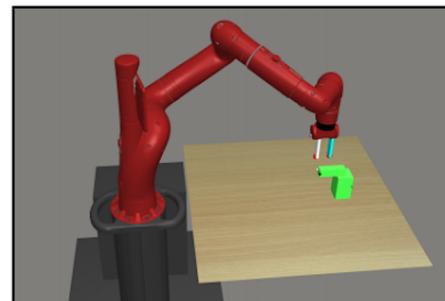
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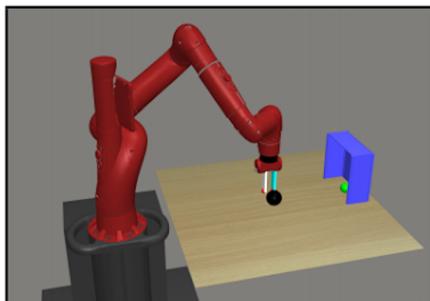
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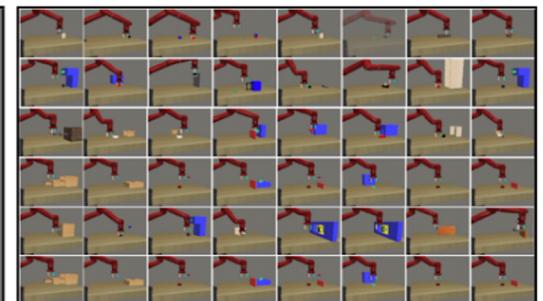
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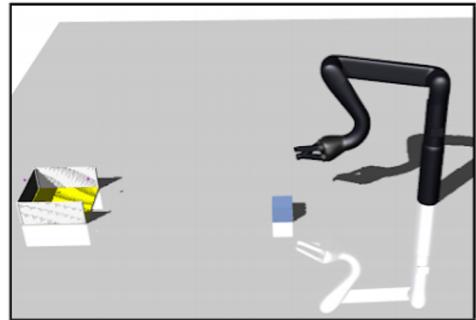


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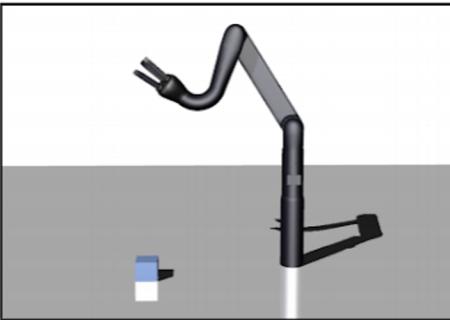


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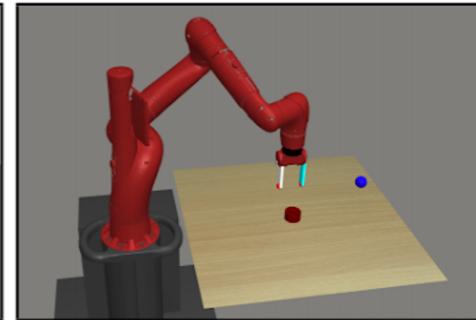
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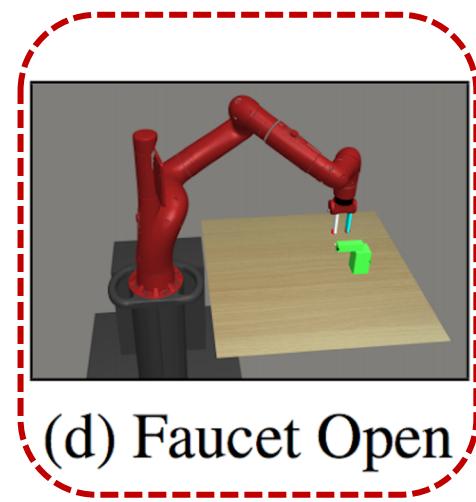
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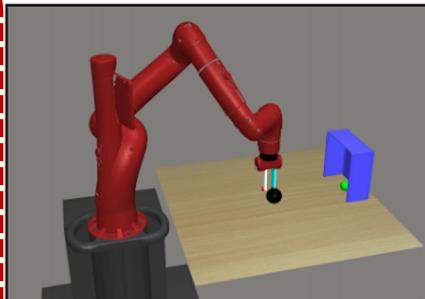
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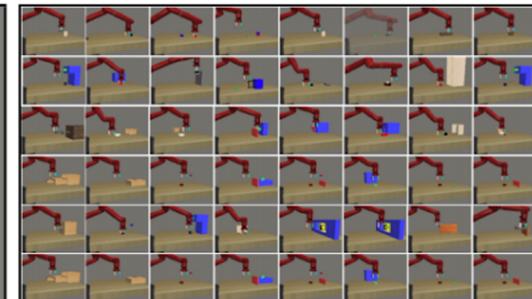
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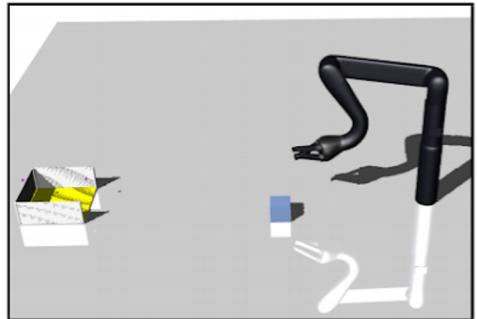


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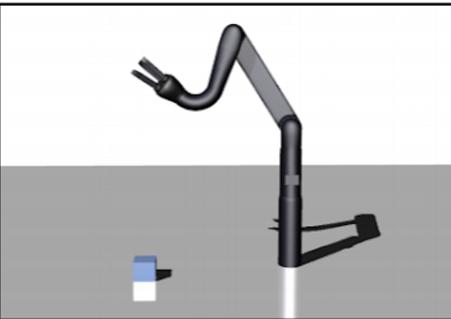


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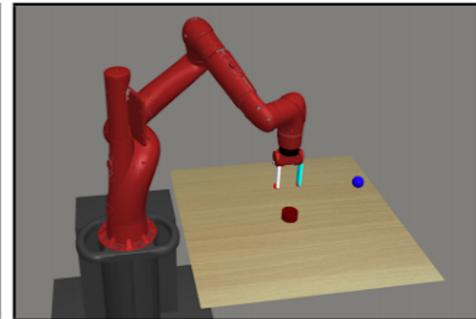
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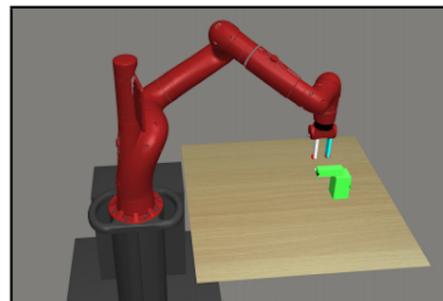
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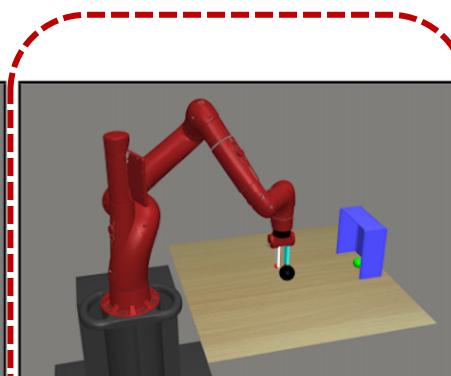
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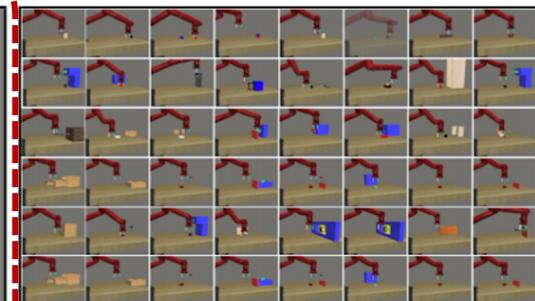
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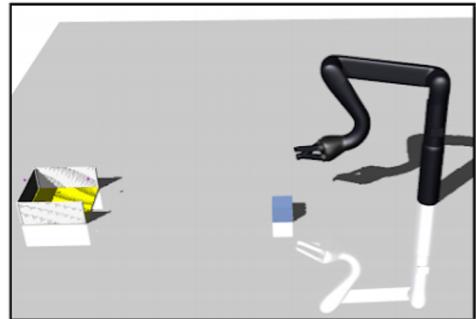


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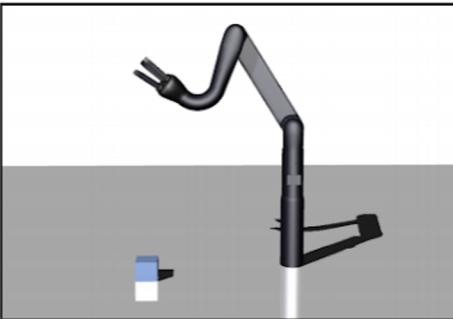


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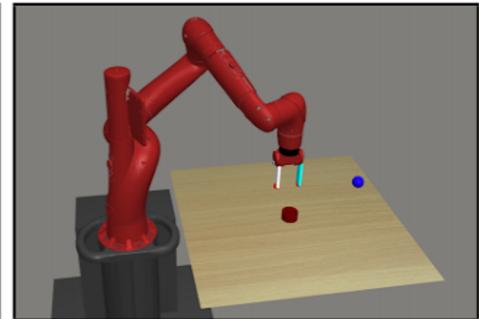
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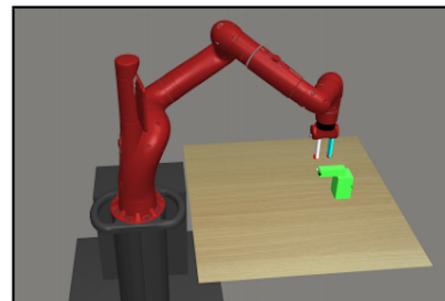
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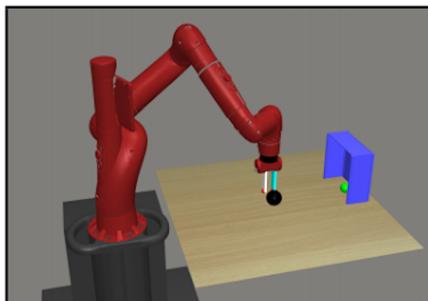
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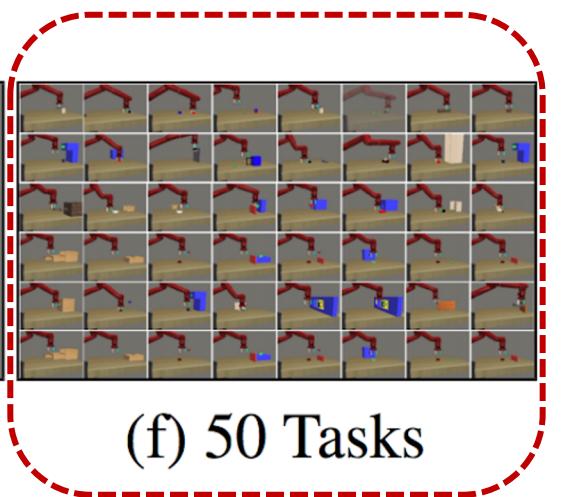
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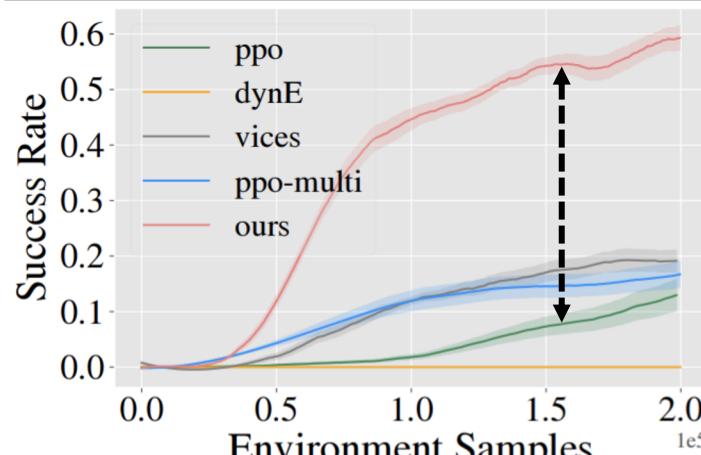


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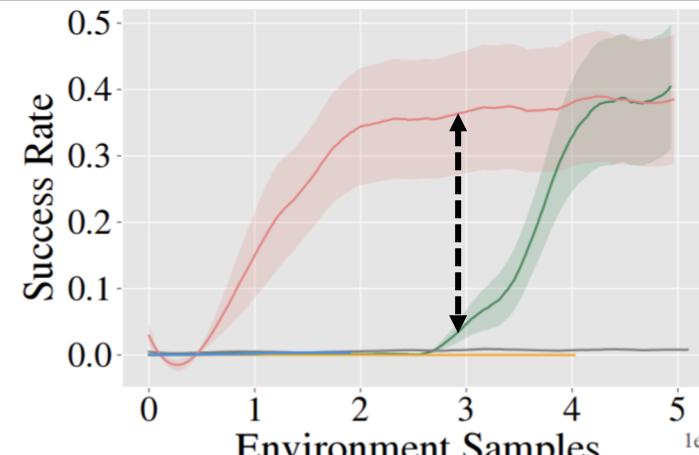


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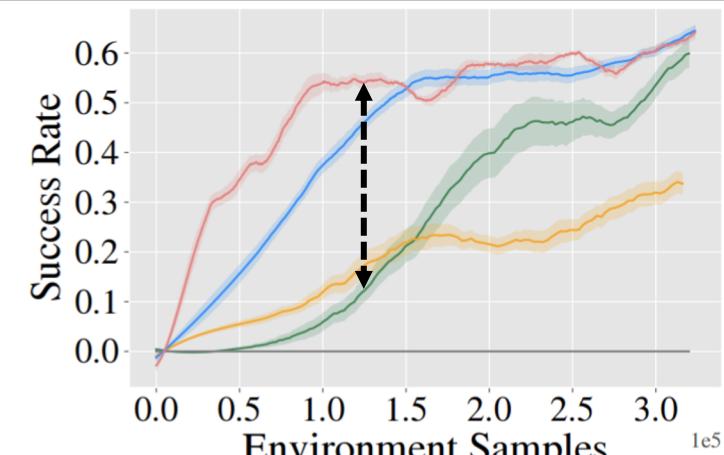
RL: Results



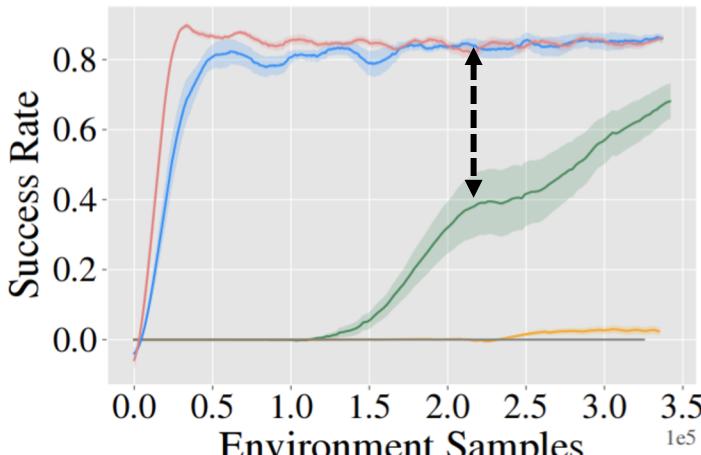
(a) Throwing



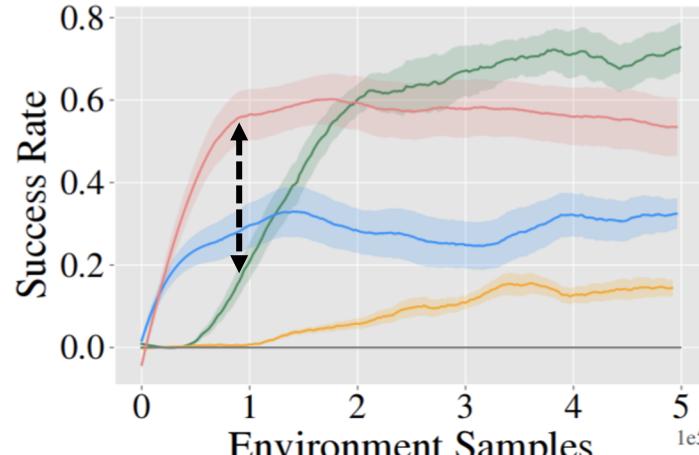
(b) Picking



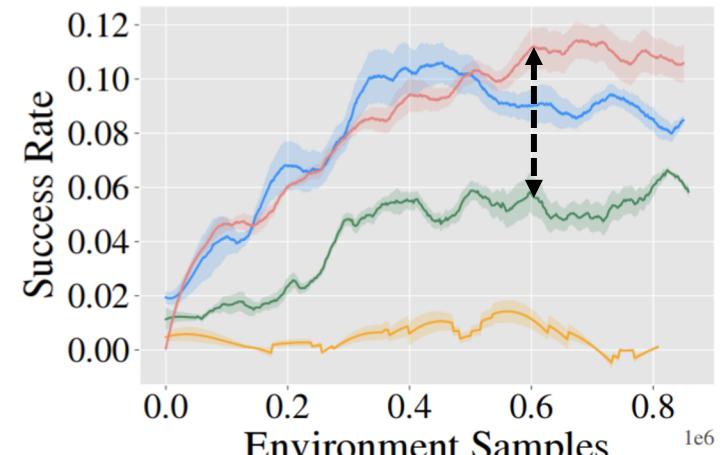
(c) Pushing



(d) Faucet Open

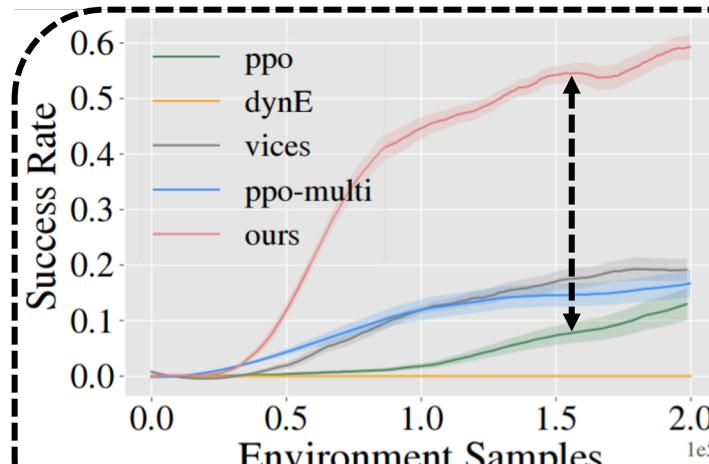


(e) Soccer

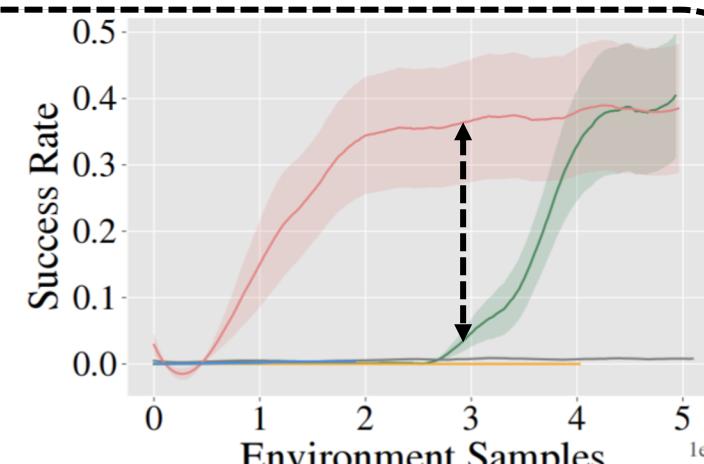


(f) Joint 50 MetaWorld Tasks

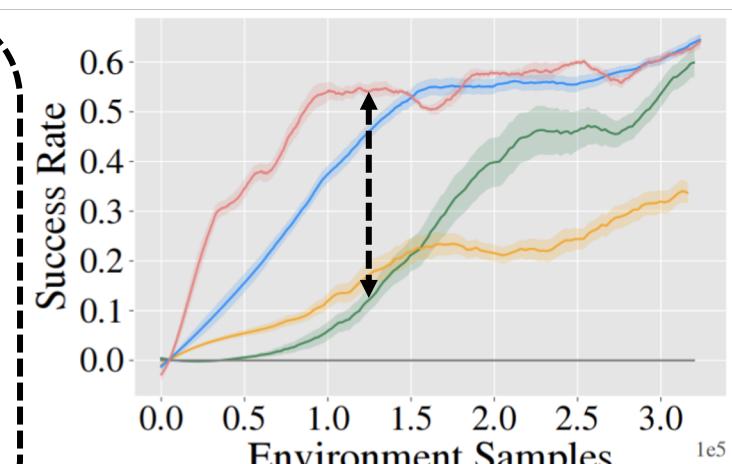
RL: Results



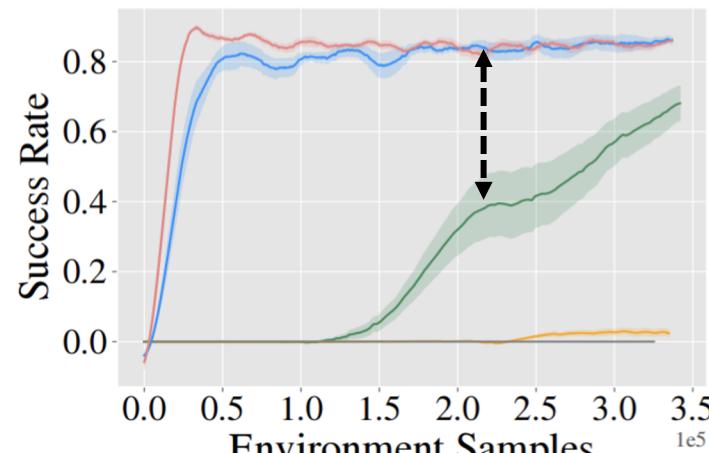
(a) Throwing



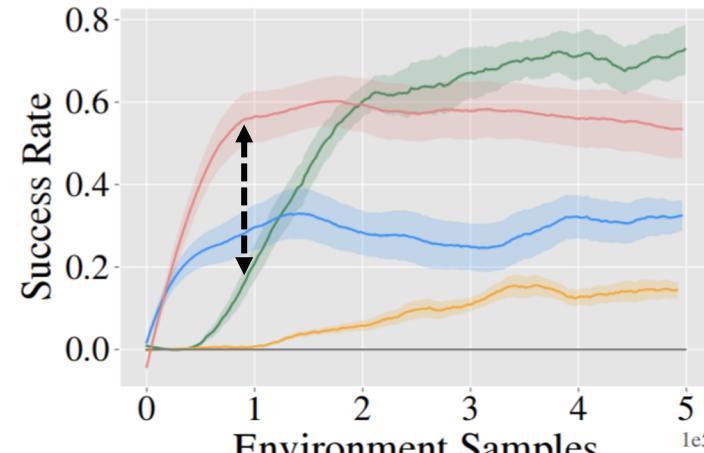
(b) Picking



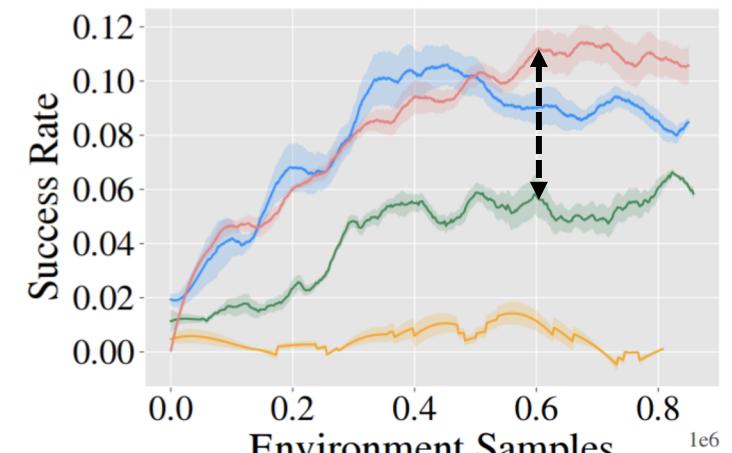
(c) Pushing



(d) Faucet Open

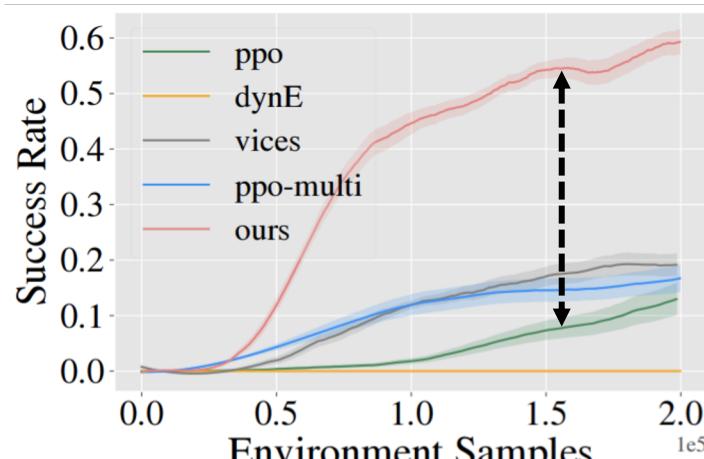


(e) Soccer

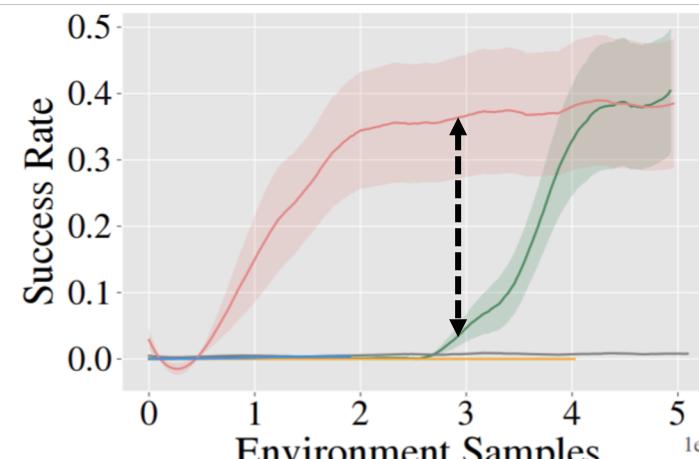


(f) Joint 50 MetaWorld Tasks

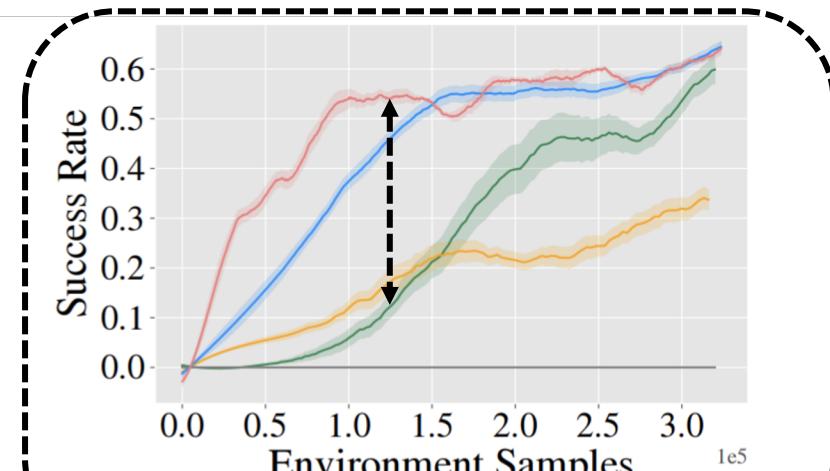
RL: Results



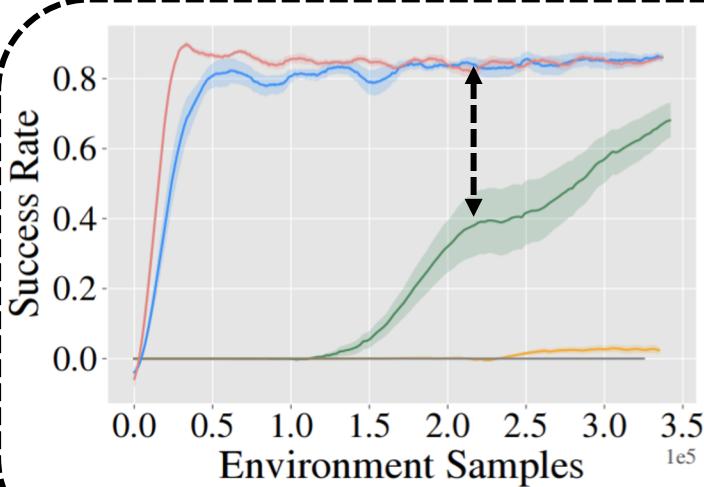
(a) Throwing



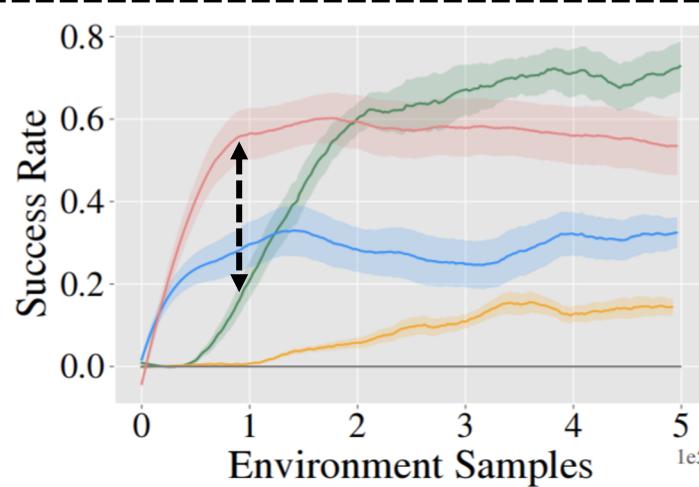
(b) Picking



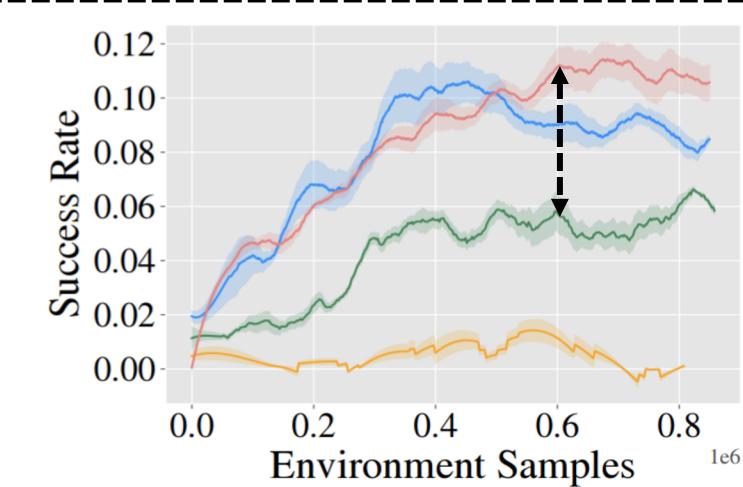
(c) Pushing



(d) Faucet Open



(e) Soccer

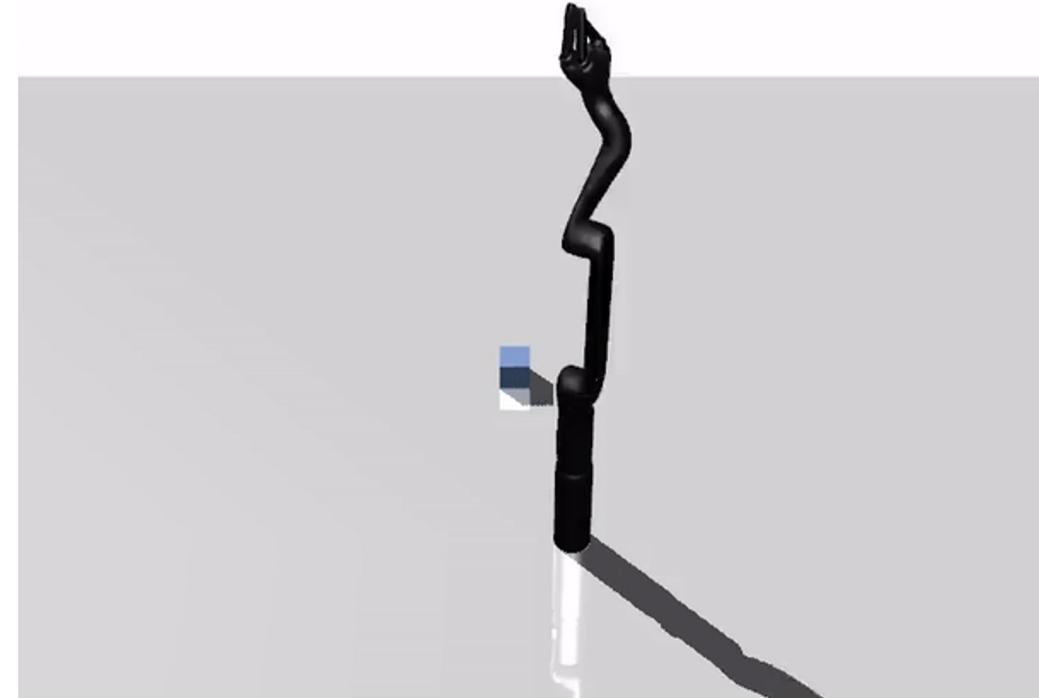


(f) Joint 50 MetaWorld Tasks

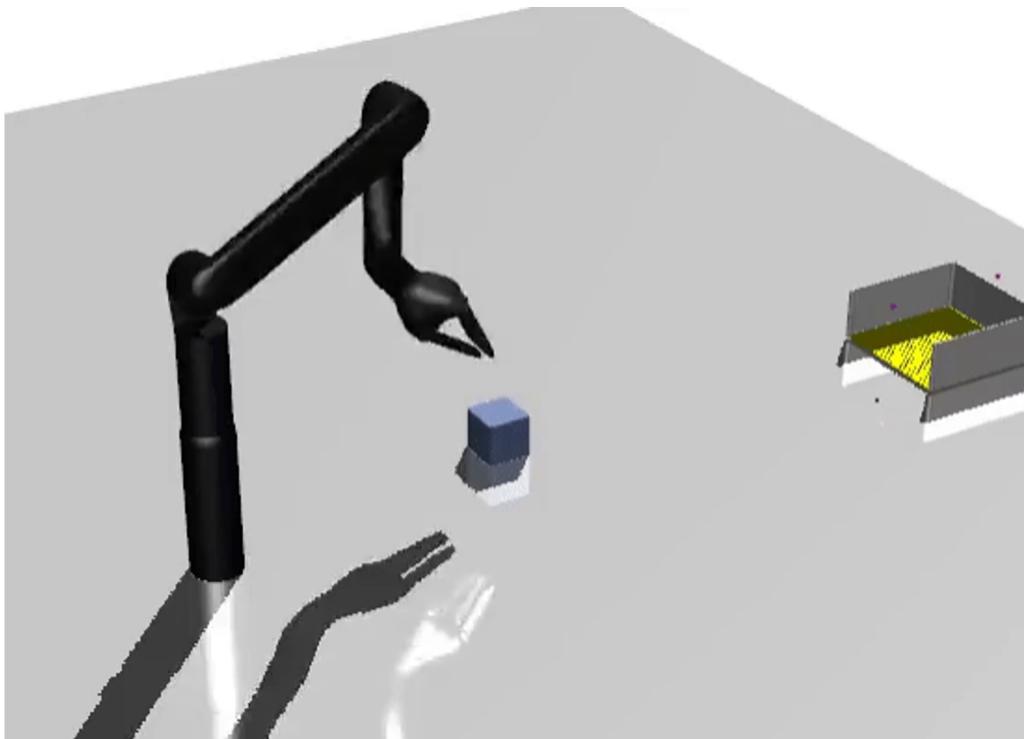
NDP (ours)



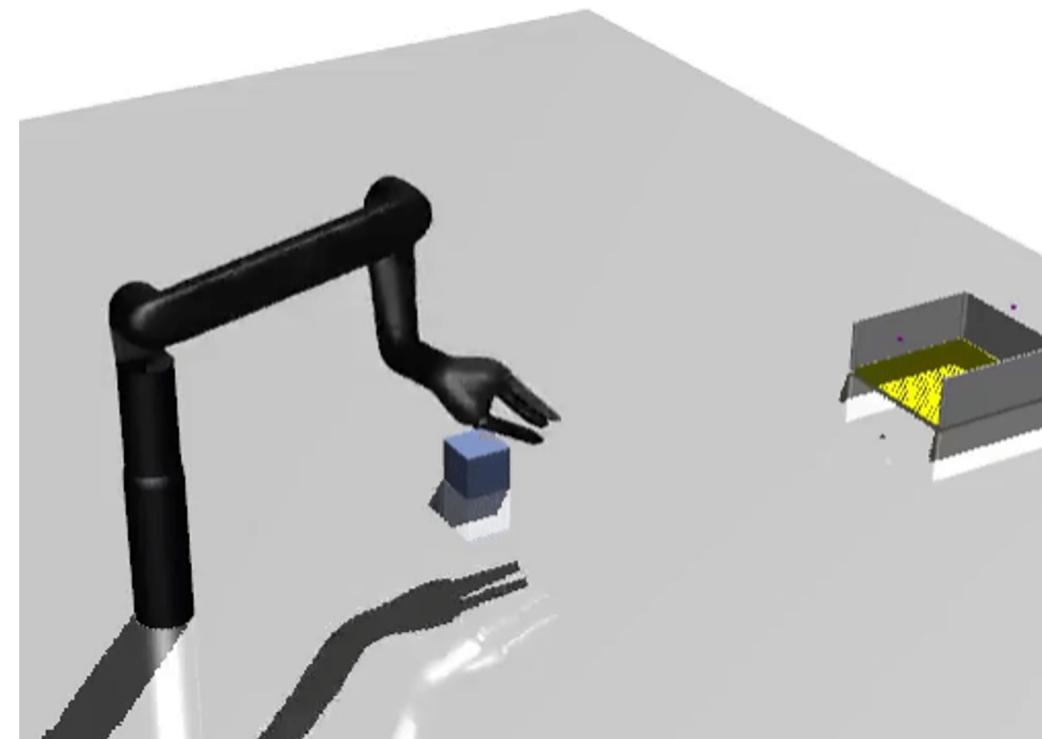
PPO-Multi (Baseline)



NDP (ours)

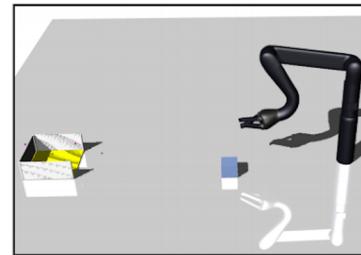


PPO-Multi (Baseline)

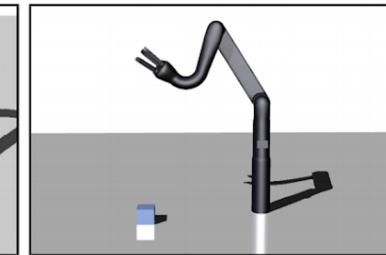


Imitation Learning

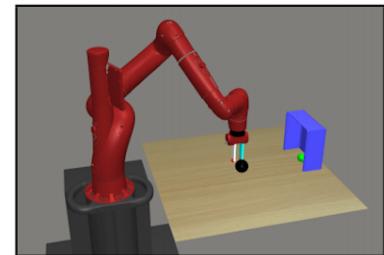
Method	NN	NDP (ours)
Throw	0.528 ± 0.262	0.642 ± 0.246
Pick	0.672 ± 0.074	0.408 ± 0.058
Push	0.002 ± 0.004	0.208 ± 0.049
Soccer	0.885 ± 0.016	0.890 ± 0.010
Faucet	0.532 ± 0.231	0.790 ± 0.059



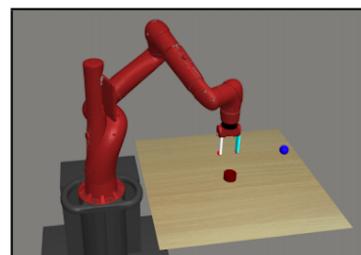
(a) Throwing



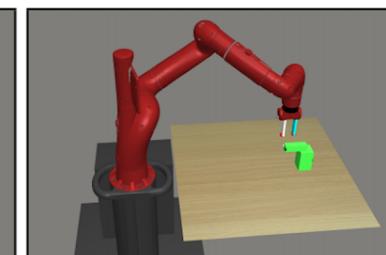
(b) Picking



(e) Soccer



(c) Pushing



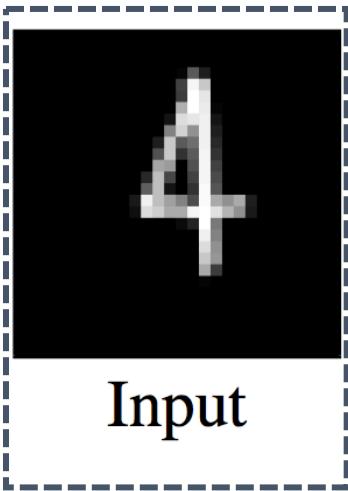
(d) Faucet Open

NDPs from Images

Digit Writing

Image of desired digit

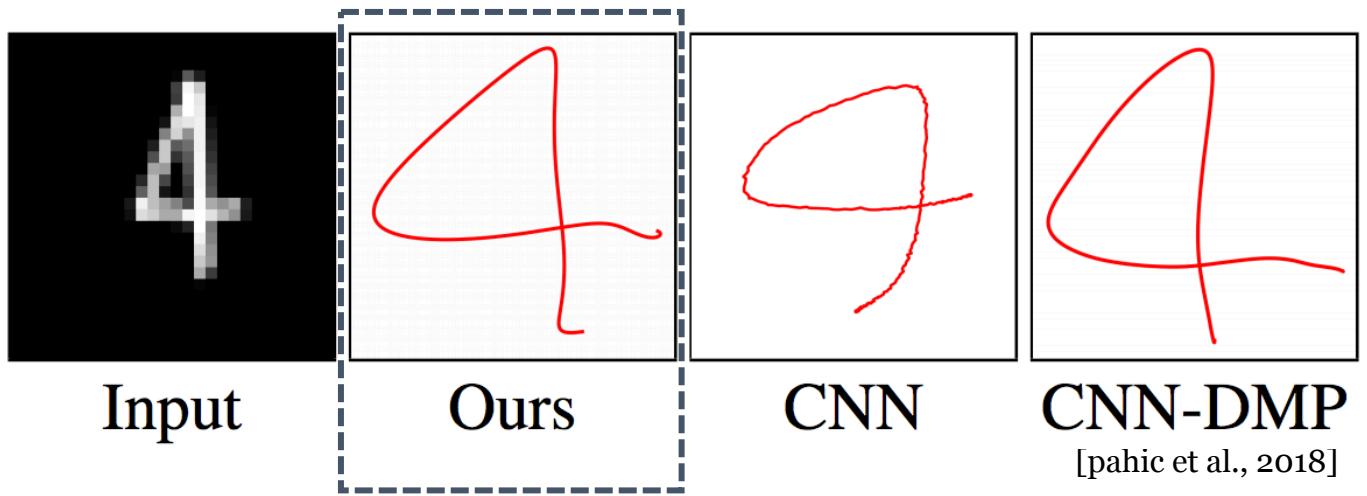
Output: end-effector positions



Digit Writing

Image of desired digit

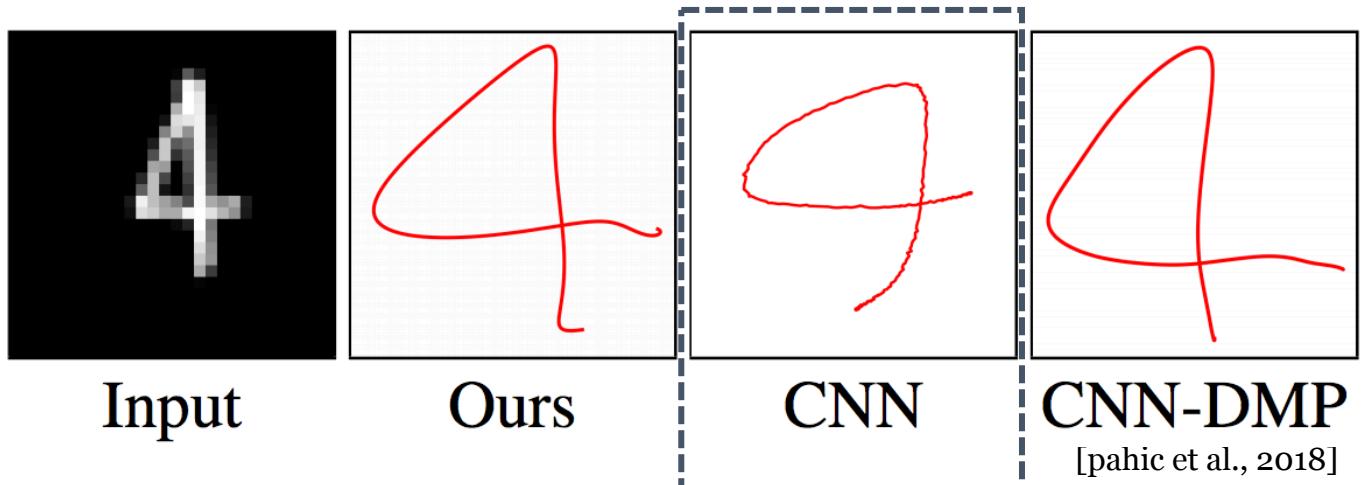
Output: end-effector positions



Digit Writing

Image of desired digit

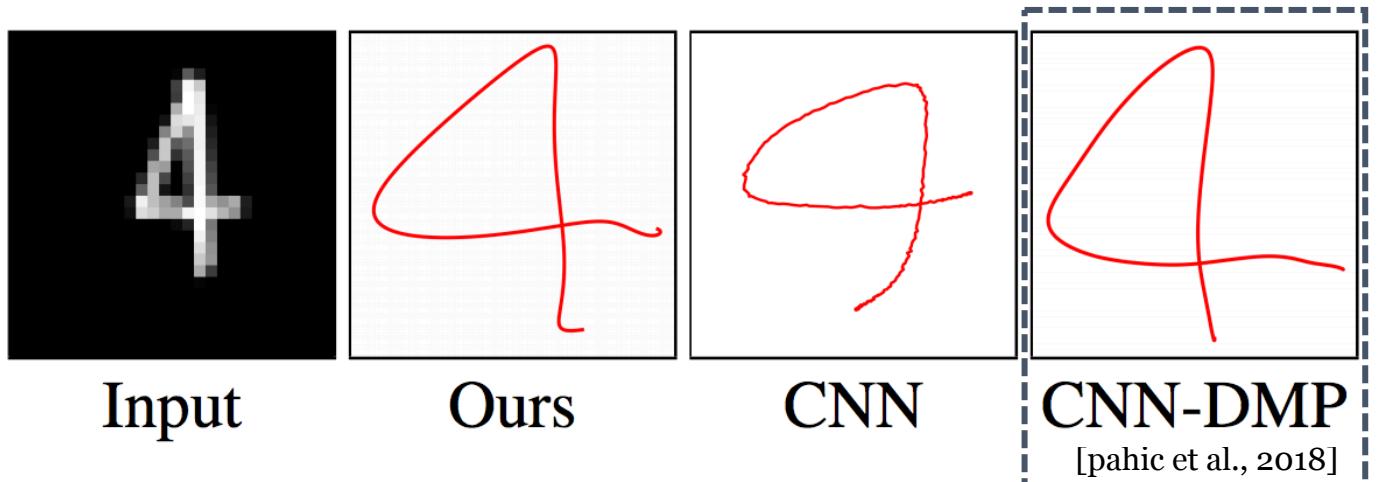
Output: end-effector positions



Digit Writing

Image of desired digit

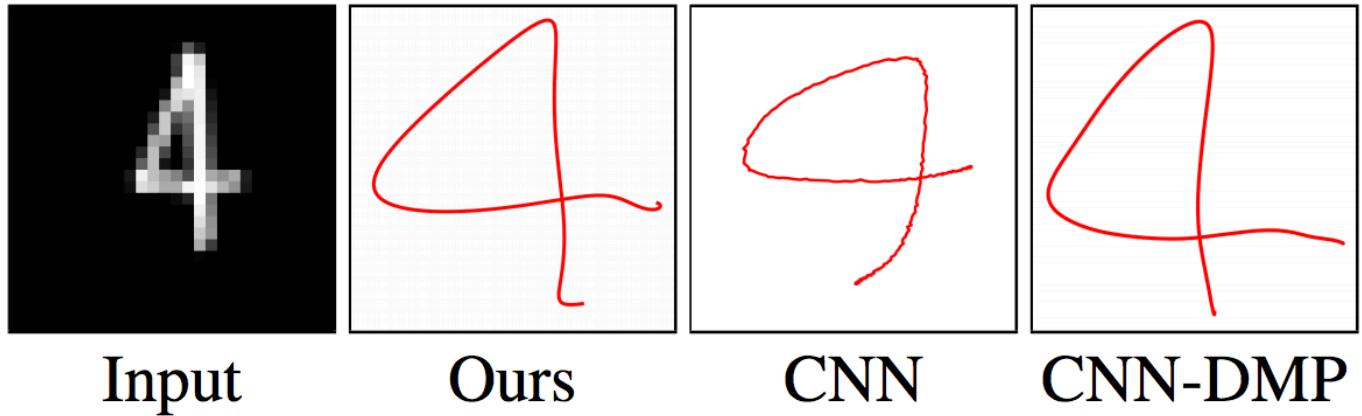
Output: end-effector positions



Digit Writing

Image of desired digit

Output: end-effector positions



NDP has smoother and more accurate reconstruction

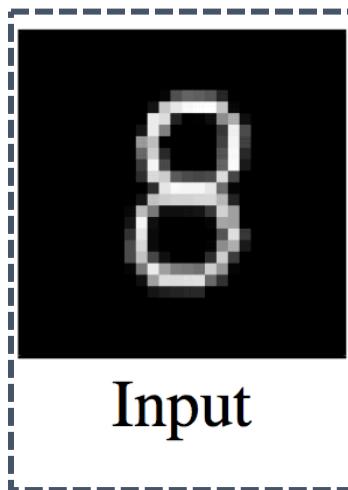
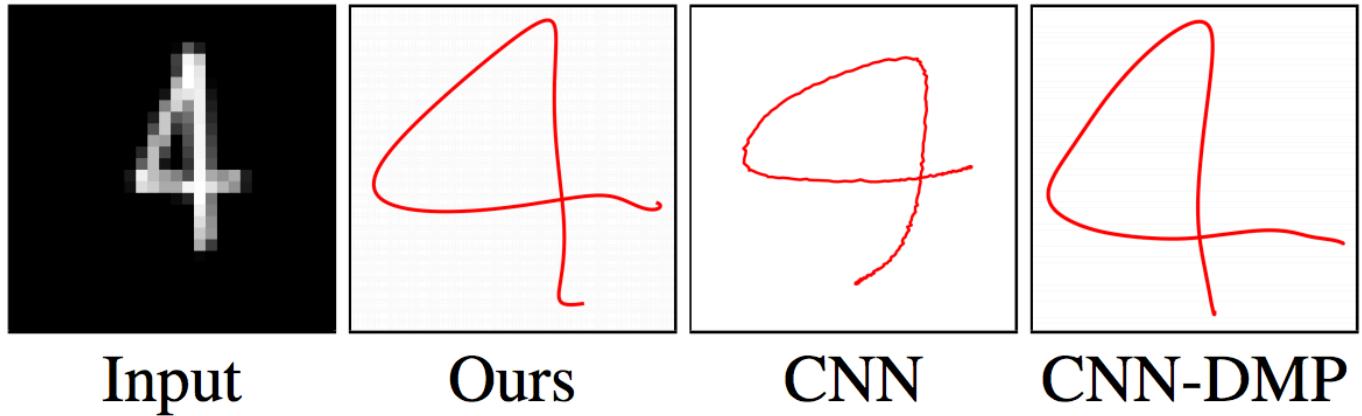
Digit Writing

Image of desired digit

Output: end-effector positions



NDP has smoother and more accurate reconstruction



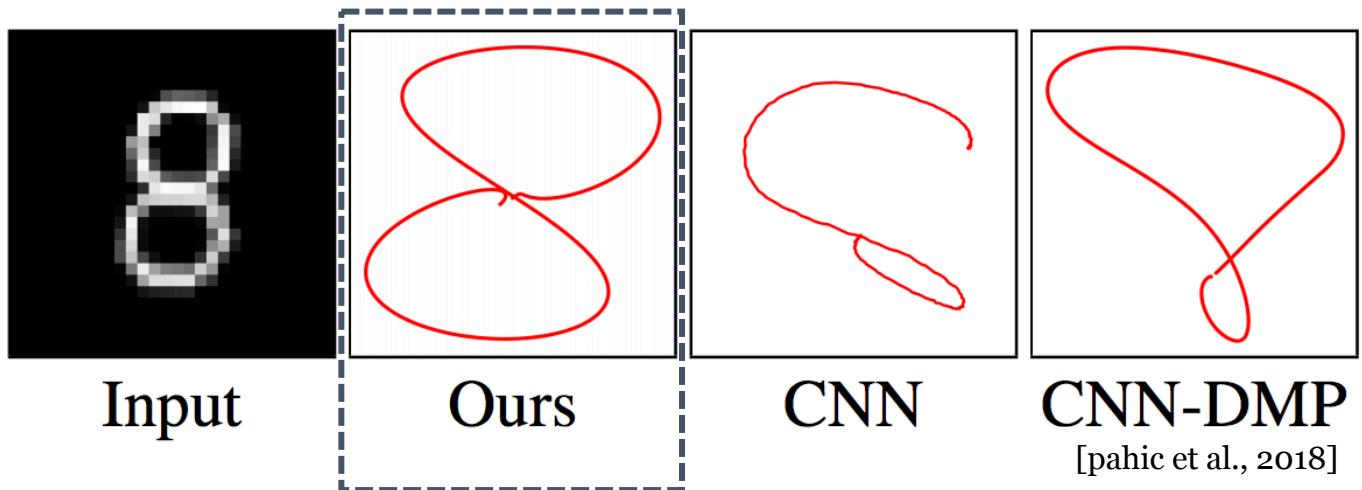
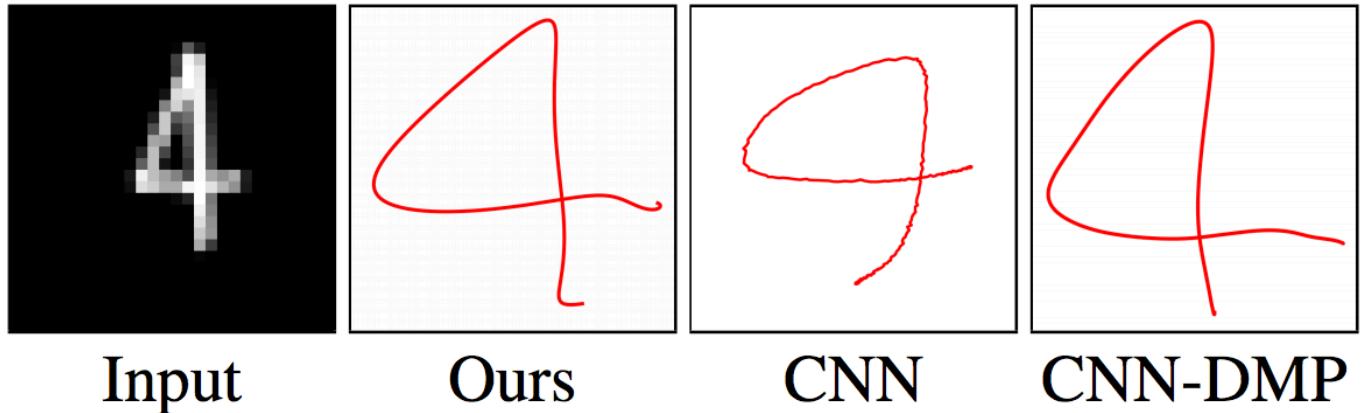
Digit Writing

Image of desired digit

Output: end-effector positions



NDP has smoother and more accurate reconstruction



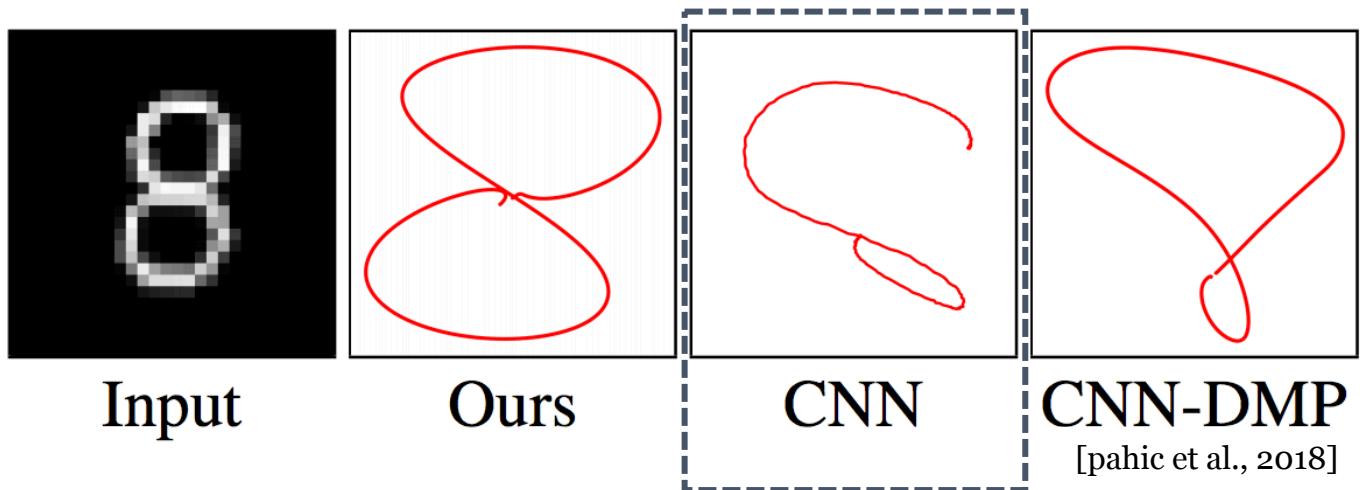
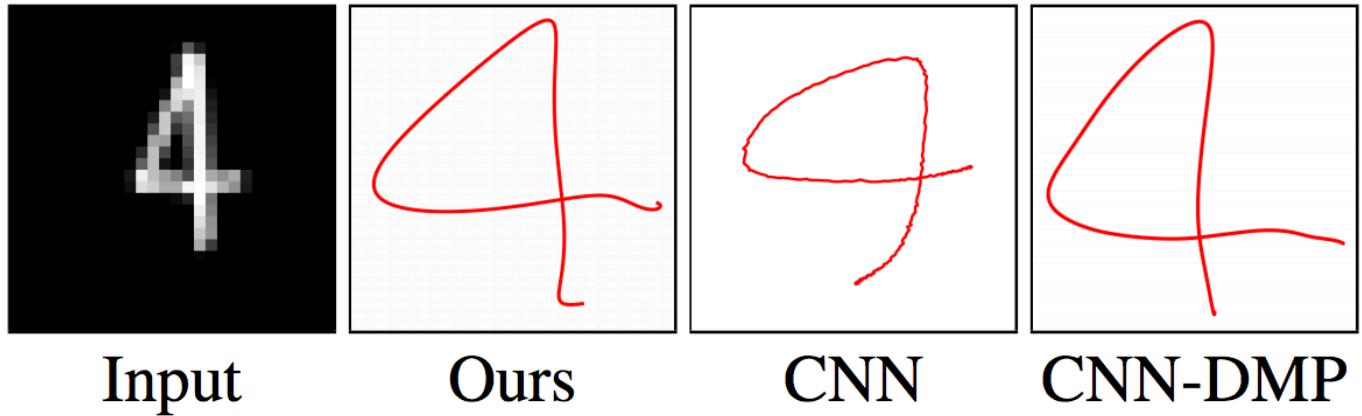
Digit Writing

Image of desired digit

Output: end-effector positions



NDP has smoother and more accurate reconstruction



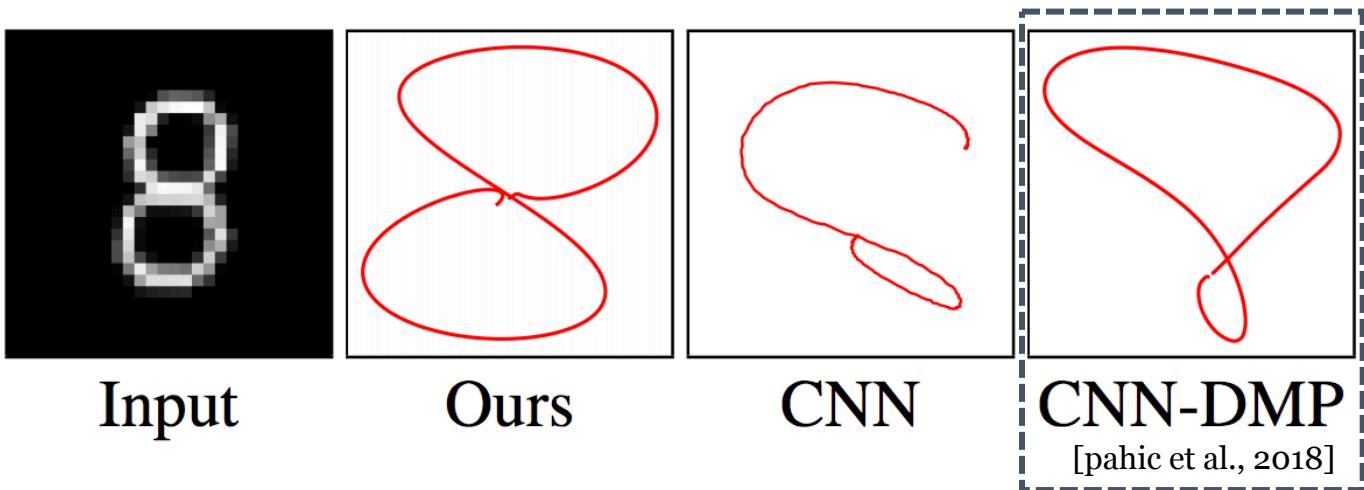
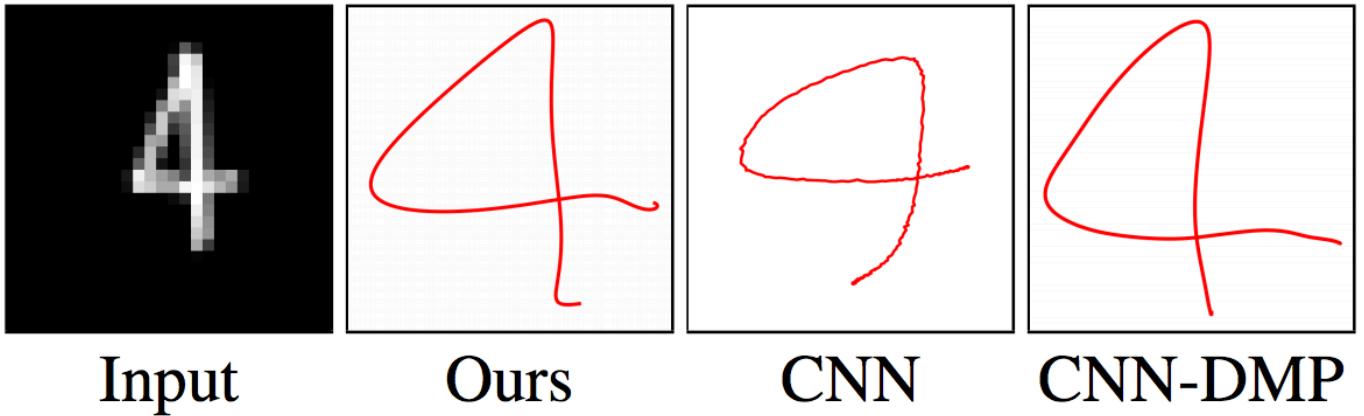
Digit Writing

Image of desired digit

Output: end-effector positions



NDP has smoother and more accurate reconstruction



Summary

NDPs are modeled after **dynamical systems** in nature

Reason at a **trajectory level** + **physically plausible** paths

Keep **advantages** of deep learning (adaptability, learning from visual inputs, etc)

Can easily be integrated in end-to-end setups

Strong performance in Reinforcement Learning and Imitation Learning, especially dynamic tasks

Thanks for Watching!

For paper and code:

shikharbahl.github.io/neural-dynamic-policy

