

ASSIGNMENT

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Name of the Student	Shikhar singh
Reg. No	17ETCS002168
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Course Leader/s	Santhoshi Kumari

Declaration Sheet			
Student Name	Shikhar singh		
Reg. No	17ETCS002168		
Programme	B.Tech	Semester/Year	05/2017
Course Code	CSC304A		
Course Title	Computer Simulation		
Course Date		to	
Course Leader	Santhoshi Kumari		
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Solution to Question No. A:

A1.1 Introduction to discrete-time and continuous-time simulation:

Discrete time simulation is an appropriate approach for simulating systems whose state is discrete and changes at particular time point and then remains in that state for some time. For example, a system is the number of customers in a post office, the number of customers is discrete (integer) and the number of customers only changes when someone enters the post office or finishes its business at the counter.

Continuous time simulation is appropriate approach for systems with a continuous state that changes continuously over time. For example, a system is the amount of liquid in a tank and or its temperature. Such a system can be described by differential equations. Continuous simulation is a technique to solve these equations numerically.

A1.2 Identify and explain advantage and disadvantages of discrete event simulation and continuous event simulation of a system by taking suitable example:

Discrete Event Simulation has evolved as a powerful decision making tool after the appearance of fast and inexpensive computing capacity. Discrete event simulation enables the study of systems which are discrete, dynamic and stochastic. Discrete Event Simulation models are dynamic simulation models. Time evolvment plays an important role in the analyzed system. Stochastic simulation models are run several times to generate a distribution of outcomes that can be analyzed. Discrete Event Simulations are typically used to analysis queuing problems, although it fits to many different applications.

Pros:

- New protocols and different operating procedures or new methods can be analyzed in the simulation model. Meanwhile the real system is not disrupted by experiments.
- Phenomena can be speed up or slowed down in the simulation. An entire shift can be analyzed in minutes.
- The simulation model can be used to train students. The students make their decisions in the simulation model to learn and gain experience before operating the real system. When they make mistakes they can learn from this experience while the real system is not disrupted.

Cons:

- Discrete Event Simulation can be applied only if the simulation model can replicate the reality to a sufficient extent.
- Stochastic skills and an adequate level of experience and knowledge is needed for the creation of a simulation model.

- Like numerical mathematical models and traditional spreadsheet analysis, Discrete Event Simulation only provides estimations for the model outcomes.

Continuous Event Simulation is the basic approach to simulate the event history for each micro unit i.e. the timing of different types of events. In general, a random process is assumed to generate the events being considered, with the probability density for experiencing an event at a given point in time depending on a set of explanatory variables. These may include the state of the unit and the time since the last event of a given type.

For continuous time, the only pro is that continuous models are occasionally easier to work with using pen and paper mathematics, as the real data comes in discrete form, computers work in discrete units. Moreover, Continuous time is a special form of Discrete time.

A1.3 Stance taken, justification and Conclusion

Discrete time simulation and Continuous time simulation, both are useful in their respective domains. In the current usage of simulation, discrete time simulation is evolving rapidly as the simulation has become inexpensive, it doesn't effects the real-time systems, huge simulations can be analyzed in minutes, also real data for simulation comes in discrete units and it is much more efficient to perform simulation in computers than simulating using pen and paper, where a risk of mistake in calculation remains constant. Therefore, Discrete event simulation has become the general form of simulation now a days. So it is better to perform all simulations in discrete-time/discrete-event simulations.

Solution to Question No. B:**B1.1 Introduction:**

The given problem statement is the case of Monte Carlo simulation. Monte Carlo simulation is a technique which incorporates mathematical computation to model the probability of different outcomes in a process that cannot easily be predicted due to the intervention of random variables. It is a technique used to understand the impact of risk and uncertainty in prediction and forecasting models. This type of simulation helps one visualize most of the potential outcomes to have a better insight of the risks involved in the decision-making process.

This problem can be approached by Monte Carlo method because it has a frequency distribution which gives a range to different amount of rainfall. As the random number is provided, it will fall between these predefined ranges and hence makes the random event computational. Which means that the city forecast can be simulated and the whole event can be analyzed.

B1.2 Simulation Table:

Statistics for two scenarios are mentioned in the problem statement.

1. if it rained on the previous day. (as shown in table 1.)
2. if it does not rain on the previous day. (as shown in table 2.)

The cumulative frequencies corresponding to each probability is to be found out for both the cases.

Now, after finding out the cumulative frequencies for the given probabilities, we can find out the range in which the random numbers fall into each of the given categories. The cumulative probability and the random number range is mentioned in both the table 1 and 2.

Table 1: stats if it rained on previous day

Rained on previous day			
Event	Probability	Cumulative probability	Random no. range
No Rain	0.50	0.50	0 – 50
1 cm rain	0.25	0.75	51 – 75
2 cm rain	0.15	0.90	76 – 90
3 cm rain	0.05	0.95	91 – 95
4 cm rain	0.03	0.98	96 – 98
5 cm rain	0.02	1.00	99 – 100

Table 2 : stats if it does not rain on the previous day.

Not Rained on previous day			
Event	Probability	Cumulative probability	Random no. range
No Rain	0.75	0.75	0 – 75
1 cm rain	0.15	0.90	76 – 90
2 cm rain	0.06	0.96	91 – 96
3 cm rain	0.04	1.00	97 – 100

Now, based upon the two tables mentioned above, the city weather is simulated for 10 days as shown in the table 3. This table consists of 5 columns which shows the number of days, the random digit chosen between 10 to 100, the event (if it rained or not), the amount of rainfall to actually occur and the explanation as to from which table the statistics are being referred.

NOTE: as per the question, it was assumed that it didn't rain on the day before the first day.

The random digits chosen for the simulation are as follows: -

49, 63, 86, 93, 69, 78, 51, 22, 12, 10.

Table 3: simulation table for 10 days.

Simulating the city weather for 10 days				
DAY	Random digit	EVENT (rain / no rain)	Amount Of rain (in cm)	explanation
1	49	No rain	0	No rain on the previous day. (assumption)
2	63	No rain	0	No rain on the 1 st day (table 2)
3	86	Rain	1	No rain on the 2 nd day (table 2)
4	93	Rain	3	Rained on the 3 rd day (table 1)
5	69	Rain	1	Rained on the 4 th day (table 1)
6	78	Rain	2	Rained on the 5 th day (table 1)
7	51	Rain	1	Rained on the 6 th day (table 1)
8	22	No rain	0	Rained on the 7 th day (table 1)
9	12	No rain	0	No rain on the 8 th day (table 2)
10	72	No rain	0	No rain on the 9 th day (table 2)

		Σ no. of days without rain = 5 days	Σ amount of rain = 8 cm	
--	--	--	-----------------------------------	--

B1.3 Result and Analysis

The random digits chosen for the problem were 49, 63, 86, 93, 69, 78, 51, 22, 12, 10.

The simulation table was made along with the details corresponding to each random digit and at the last, total number of days without rain and total amount of rainfall was calculated.

From the above table 3, the following things can be deduced: -

- Total rain during the time period of 10 days was **8 cms**.
- Total number of days the city lasted without rain in the time period of 10 days was **5 days**.
- Average rainfall each day = $\frac{\Sigma \text{ amount of rain each day}}{\text{total no. of days}} = \frac{8}{10} = \mathbf{0.8 \text{ cm}}$.
- Average time span it did not rain = $\frac{\Sigma \text{ total no. of days it does not rain}}{\text{total no. of days}} = \frac{5}{10} = \mathbf{0.5 \text{ day i.e. on an average it didn't rain for half a day}}$.

The accuracy of Monte Carlo method of simulating random distributions is analyzed.

Although Monte Carlo adds mathematical weightage to the analysis of risk factors involved in a system, it can be seen that the accuracy of some standard computer codes is overstated. It has been shown that increasing the accuracy of the Monte Carlo method by increasing the number of simulations is not economical because the time complexity of algorithm is inversely proportional to the squared relative error^[2]. Therefore, a new method of increasing the accuracy with a significant reduction in the number of simulations was developed. For the new method, the number of simulations and time complexity of algorithm are inversely proportional to the relative error.

Solution to Question No. 3:**B2.1 Introduction to problem solving approach:**

An ATM simulation system can be described as discrete single server queueing system. Which means that service requests are going to be at discrete point in time i.e. a state change (event) is going to be unique and discontinuous. Also, only once machine (ATM) is handling all the requests hence it is a single server system. Discrete event simulation is generally carried out by a software designed in high level programming languages such as Pascal, C++, or any specialized simulation language. Following are the five key features –

1. Entities – These are the representation of real elements like the parts of machines.
2. Relationships – It means to link entities together.
3. Simulation Executive – It is responsible for controlling the advance time and executing discrete events.
4. Random Number Generator – It helps to simulate different data coming into the simulation model.
5. Results & Statistics – It validates the model and provides its performance measures.

Simulation of a single server queueing system:

A queue is the combination of all the entities in the system being served and those waiting for their turn. The central element of the system is a server, which provides service to the connected devices or items. Items request to the system to be served, if the server is idle. Then, it is served immediately, else it joins a waiting queue. After the task is completed by the server, the item departs. A simple queueing system can be represented by the following figure:

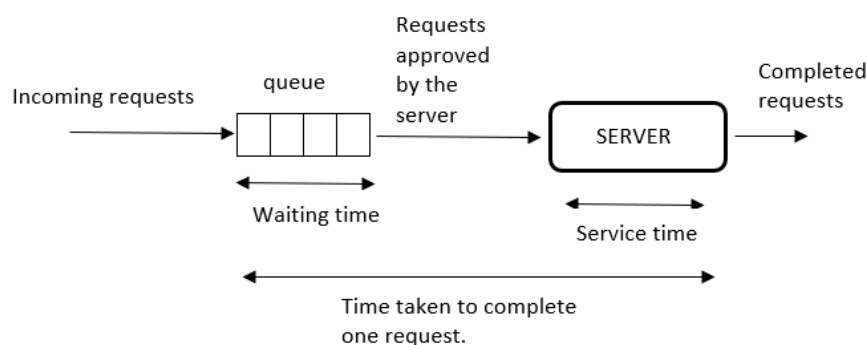


Figure 1: a single server queueing system.

As all the requests will be made randomly by people, hence each person is going to make request one by one at each point of time. Other will have to be in a queue until the person who reaches first, completes the service. Thus, the working of this system is based on FIFO (First in First Out) algorithm.

B2.2 Implementation:

As mentioned in the problem statement, the simulation is to be performed for 12 hours i.e. 720 mins in total. The interarrival time of the incoming customer (service request) is going to be chosen randomly between 1 to 4 mins and service time for each request will be between 1 to 6 min.

ALGORITHM:

1. Record the interarrival time and update the arrival time of the request and send the request to the server for computation.

2. Check whether the server is idle or not.
 - a. If the server is idle, start the service and update the start time.
 - b. If the server is not idle, push the service in the queue and wait for the ongoing service to end.
3. Add service time to the arrival time to get the end time of service.
4. Note down the difference of arrival time and service end time to get time spent by each request in the system.
5. Note down the waiting time of each service while in queue.
6. Note down the server idle time.
7. Repeat steps 1 to 7 until last request arrives.
8. After the last request, stop the simulation and compute the output stats i.e.
 - a. Total Idle time of the ATM machine (server).
 - b. Average waiting time of a customer.
 - c. Average service time.
 - d. Average time between arrivals.
 - e. Average time a customer spends in the system.
 - f. Percentage utilization of the whole system.

$$\text{Percentage utilization} = \frac{\sum(\text{average service time})}{\sum(\text{average interarrival time})} * 100$$

Code implementation:

```
package single_server_system;

/**
 *
 * @author shikhar
 */
import java.util.Random;
import java.util.Scanner;

public class Single_server_system {

    |
    public static void main(String[] args) {

        Scanner in = new Scanner (System.in);

        Random rand = new Random();

        System.out.printf("Simulating the ATM Machine ...\\n");

        int request=0;
        int total=0;

        int[] iat=new int[10000], st =new int[10000],at= new int[10000],ss= new int[10000];

        int[] se = new int[10000], wait =new int[10000], idle = new int[10000], tcss = new int[10000];

        double sumwait=0.00, sumidle=0.00,sumservice=0.00,sumiat=0.00, sumtcss=0.00;

        se[0]=0;

        System.out.printf("Reqno \tIAT \tST \tAT \tSS \tSE \tTCSS \twait \tidle\\n");
```

Figure 2: source code

```

for(int i=1;se[i-1]<=720;i++)
{
    iat[i] = rand.nextInt(4)+1; //random number generation
    st[i] = rand.nextInt(6)+1; //random number generation
    total += iat[i]; // cummilative sum
    at[i]=total; //initilization
    if((at[i]-se[i-1])>=0)
        ss[i]=at[i]; //check and then initilize start time
    else
        ss[i]=se[i-1];

    se[i]=ss[i]+st[i]; //calculating service end
    wait[i]=ss[i]-at[i]; //calculating wait time
    idle[i]=ss[i]-se[i-1]; //calculating idle time
    tcss[i] = se[i]-at[i]; // calculating the time a customer spends in a system
    sumwait+=wait[i]; // calculating total wait time
    sumidle+=idle[i]; // calculating idle wait time
    sumservice+=st[i]; // calculating total service time
    sumiat+=iat[i]; // calculating total inter arrival time
    sumtcss+=tcss[i]; // calculating total time a customer spends in system
}

```

Figure 3: source code (updating various fields)

```

System.out.printf("%d \t%d \t%d \t%d \t%d \t%d \t%d \t%d \t%d\n",i,iat[i],st[i],at[i],ss[i],se[i],tcss[i],wait[i],idle[i]);
request=i; // updating flag for the last request.
}

```

Figure 4: source code (printing the details in a tabular format.)

```

System.out.printf("\nThe total number of requests processed: %d",request);
System.out.printf("\nAverage waiting time of a customer: %f\n",(sumwait/request));
System.out.printf("Idle time of the ATM machine: %f\n",sumidle);
System.out.printf("Average service time: %f\n",(sumservice/request));
System.out.printf("Average time between arrivals: %f\n", sumiat/request);
System.out.printf("Average time customer spends in the system: %f\n", sumtcss/request);
System.out.printf("Percentage utilization of the system: %f \n", sumiat*100/sumservice);

```

Figure 5: source code (computing and printing output stats.)

All the figures mentioned above are the different functionalities of the program.

B2.3 Results and analysis:

The program was run and successfully executed, which yielded the following output: -

```
run:
Simulating the ATM Machine ...
Reqno  IAT  ST  AT  SS  SE  TCSS  wait  idle
1      3    3    3    3    6    3    0    3
2      3    1    6    6    7    1    0    0
3      3    3    9    9   12    3    0    2
4      4    6   13   13   19    6    0    1
5      2    5   15   19   24    9    4    0
6      4    1   19   24   25    6    5    0
7      2    3   21   25   28    7    4    0
8      2    4   23   28   32    9    5    0
9      4    5   27   32   37   10    5    0
10     3    4   30   37   41   11    7    0
11     2    2   32   41   43   11    9    0
12     1    2   33   43   45   12   10    0
13     3    1   36   45   46   10    9    0
14     4    3   40   46   49    9    6    0
15     3    1   43   49   50    7    6    0
16     3    6   46   50   56   10    4    0
17     3    4   49   56   60   11    7    0
18     4    4   53   60   64   11    7    0
19     1    5   54   64   69   15   10    0
20     2    5   56   69   74   18   13    0
21     2    5   58   74   79   21   16    0
22     1    1   59   79   80   21   20    0
23     1    2   60   80   82   22   20    0
24     1    2   61   82   84   23   21    0
25     4    6   65   84   90   25   19    0
26     2    2   67   90   92   25   23    0
27     2    3   69   92   95   26   23    0
28     1    1   70   95   96   26   25    0
29     1    1   71   96   97   26   25    0
30     4    2   75   97   99   24   22    0
31     2    6   77   99  105   28   22    0
32     1    2   78  105  107   29   27    0
33     3    1   81  107  108   27   26    0
34     3    5   84  108  113   29   24    0
35     1    5   85  113  118   33   28    0
```

Figure 6: simulation of first 35 requests made.

```
182     1    4   478   636   640   162   158    0
183     2    1   480   640   641   161   160    0
184     4    5   484   641   646   162   157    0
185     2    6   486   646   652   166   160    0
186     4    6   490   652   658   168   162    0
187     3    2   493   658   660   167   165    0
188     3    5   496   660   665   169   164    0
189     1    6   497   665   671   174   168    0
190     4    6   501   671   677   176   170    0
191     2    6   503   677   683   180   174    0
192     3    1   506   683   684   178   177    0
193     4    6   510   684   690   180   174    0
194     1    4   511   690   694   183   179    0
195     3    5   514   694   699   185   180    0
196     3    3   517   699   702   185   182    0
197     4    1   521   702   703   182   181    0
198     3    3   524   703   706   182   179    0
199     4    3   528   706   709   181   178    0
200     2    5   530   709   714   184   179    0
201     2    6   532   714   720   188   182    0
```

```
The total number of requests processed: 201
Average waiting time of a customer: 90.820896
Idle time of the ATM machine: 4.000000
Average service time: 3.587065
Average time between arrivals: 2.651741
Average time customer spends in the system: 94.407960
Percentage utilization of the system: 73.925104
BUILD SUCCESSFUL (total time: 0 seconds)
```

Figure 7: simulation of the last 20 requests along with the output stats.

The output shown in the figures above consists of a tabular format where different columns indicate different attributes of the simulation table, which are as follows: -

- Reqno. : request number
- IAT : interarrival time
- ST : Service time
- AT : arrival time
- SS : service start
- SE : service end
- TCSS : time spent by customer in the system
- Wait : waiting time (time spent by the customer in the queue.)
- Idle : idle time (number of minutes the server remained idle as it didn't receive any request.)

The simulation was done till 12 hours i.e. 720 mins and during this time, a total of 201 service requests were successfully completed. All the service requests after 720th min were dismissed. And the customer whose service end time exceeds 720 mins was also dismissed.

Also, the following output statistics were computed: -

- Total number of requests processed : 201
- Average waiting time of a customer : 90.820896 mins
- Idle time of the ATM machine : 4.00 mins
- Average service time : 3.587065 mins
- Average time between arrivals : 2.651741 mins
- Average time a customer spends in the system : 94.407960 mins
- Percentage utilization of the system : 73.9251 %

The single server queuing system is the simplest queuing system in use. It has many advantages like reducing queue flow traffic, providing the users (services, users etc. Here, customers) a more relaxed environment etc. But it has its own disadvantages which sometimes, far outreach the advantages. The price to avail the system will be expensive and the system software has the tendency to crash and be corrupted. Moreover, the cost of maintenance will consume a part of the business profit. Also, one limitation is the possibility that the waiting space may in fact be limited. Another possibility is that arrival rate is state dependent. That is, potential customers are discouraged from entering the queue if they observe a long line at the time they arrive. Another practical limitation of the model is that the arrival process is not stationary. It is quite possible that the service station would experience peak periods and slack periods during which the arrival rate is higher.

1. https://en.wikipedia.org/wiki/Monte_Carlo_method#Monte_Carlo_and_random_numbers
2. "Accuracy and efficiency of Monte Carlo method" – Julius Goodman
https://inis.iaea.org/collection/NCLCollectionStore/_Public/19/047/19047359.pdf
3. https://www.academia.edu/35688542/Queue_Management_Systems_Characteristics_Advantages_and_Application