Homework 7 - Decision Tree

Shiloh Bradley 6/23/2020

Toyota Corolla

```
df <- read.csv("ToyotaCorolla2.csv")</pre>
head(df)
##
     Price Age
                  KM Fuel_Type HP Met_Color Automatic
                                                          cc Doors
## 1 13500
           23 46986
                         Diesel 90
                                                      0 2000
## 2 13750
           23 72937
                        Diesel 90
                                           1
                                                      0 2000
                                                                 3
                                                      0 2000
## 3 13950
            24 41711
                        Diesel 90
                                           1
                                                                 3
                                                      0 2000
## 4 14950
           26 48000
                        Diesel 90
                                           0
                                                                 3
## 5 13750
           30 38500
                        Diesel 90
                                                      0 2000
                                                                 3
## 6 12950 32 61000
                        Diesel 90
                                           0
                                                      0 2000
                                                                 3
     Quarterly_Tax Weight
## 1
                      1165
               210
## 2
               210
                      1165
               210
## 3
                     1165
## 4
               210
                      1165
## 5
               210
                      1170
## 6
               210
                      1170
summary(df)
##
        Price
                                                        Fuel_Type
                          Age
                                            ΚM
##
          : 4350
                    Min.
                            : 1.00
                                     Min.
                                            :
                                                       CNG
    1st Qu.: 8450
                    1st Qu.:44.00
                                     1st Qu.: 43000
                                                       Diesel: 155
    Median: 9900
                    Median :61.00
                                     Median : 63390
##
                                                       Petrol:1264
    Mean :10731
                    Mean
                           :55.95
                                     Mean : 68533
    3rd Qu.:11950
##
                    3rd Qu.:70.00
                                     3rd Qu.: 87021
    Max.
           :32500
                    Max.
                            :80.00
                                     Max.
                                            :243000
##
          ΗP
                      Met_Color
                                        Automatic
                                                               СС
##
  Min.
          : 69.0
                    Min.
                            :0.0000
                                      Min.
                                             :0.00000
                                                                : 1300
                                                         Min.
   1st Qu.: 90.0
                    1st Qu.:0.0000
                                      1st Qu.:0.00000
                                                         1st Qu.: 1400
  Median :110.0
                    Median :1.0000
                                      Median :0.00000
                                                         Median: 1600
## Mean
          :101.5
                    Mean
                            :0.6748
                                      Mean
                                              :0.05571
                                                         Mean
                                                                : 1577
##
    3rd Qu.:110.0
                    3rd Qu.:1.0000
                                      3rd Qu.:0.00000
                                                         3rd Qu.: 1600
##
    Max.
           :192.0
                    Max.
                           :1.0000
                                              :1.00000
                                                         Max.
                                                                :16000
##
                    Quarterly_Tax
        Doors
                                          Weight
##
   Min.
           :2.000
                    Min. : 19.00
                                      Min.
                                              :1000
   1st Qu.:3.000
                    1st Qu.: 69.00
                                      1st Qu.:1040
  Median :4.000
                    Median: 85.00
                                      Median:1070
## Mean
           :4.033
                          : 87.12
                                      Mean
                                              :1072
                    Mean
    3rd Qu.:5.000
                    3rd Qu.: 85.00
                                      3rd Qu.:1085
  Max.
           :5.000
                            :283.00
                                              :1615
                    Max.
                                      Max.
M \leftarrow .25 * nrow(df)
#to be able to replicate the results, set initial seed for random
#number generator
set.seed(11317)
```

```
holdout <- sample(1:nrow(df), M, replace = F)</pre>
df.train <- df[-holdout, ] # Training set</pre>
df.test <- df[holdout, ]</pre>
                           # Test set
dim(df.train) # 1077 11
## [1] 1077 11
dim(df.test) # 359 11
## [1] 359 11
lm1 \leftarrow lm(Price \sim ...
         data = df.train)
summary(lm1)
##
## Call:
## lm(formula = Price ~ ., data = df.train)
## Residuals:
##
       Min
                      Median
                                           Max
                 1Q
                                   3Q
## -10455.9 -743.2
                     -39.2
                                683.9
                                        6880.7
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  -5.926e+03 1.370e+03 -4.326 1.66e-05 ***
                  -1.244e+02 2.993e+00 -41.560 < 2e-16 ***
## Age
                  -1.623e-02 1.489e-03 -10.901 < 2e-16 ***
## KM
## Fuel_TypeDiesel 1.104e+03 4.394e+02 2.514
                                                 0.0121 *
## Fuel_TypePetrol 2.857e+03 4.352e+02 6.563 8.22e-11 ***
                   2.283e+01 4.021e+00 5.679 1.74e-08 ***
## HP
## Met_Color
                   4.373e+01 8.695e+01 0.503 0.6151
## Automatic
                   3.792e+02 1.789e+02 2.119
                                                  0.0343 *
## cc
                  -2.157e-02 9.109e-02 -0.237
                                                  0.8129
                 -2.619e+01 4.534e+01 -0.578
## Doors
                                                  0.5636
## Quarterly_Tax 1.199e+01 1.850e+00 6.485 1.36e-10 ***
## Weight
                  1.753e+01 1.327e+00 13.207 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1314 on 1065 degrees of freedom
## Multiple R-squared: 0.8634, Adjusted R-squared: 0.862
## F-statistic: 612.1 on 11 and 1065 DF, p-value: < 2.2e-16
vif(lm1)
##
                    GVIF Df GVIF<sup>(1/(2*Df))</sup>
## Age
                1.875729 1
                                   1.369573
## KM
                2.041341 1
                                   1.428755
## Fuel_Type
                6.903487 2
                                   1.620941
## HP
                2.177556 1
                                   1.475654
## Met_Color
                1.020219 1
                                   1.010059
## Automatic
                1.083180 1
                                   1.040759
## cc
                1.181299 1
                                   1.086876
## Doors
                1.168824 1
                                   1.081122
```

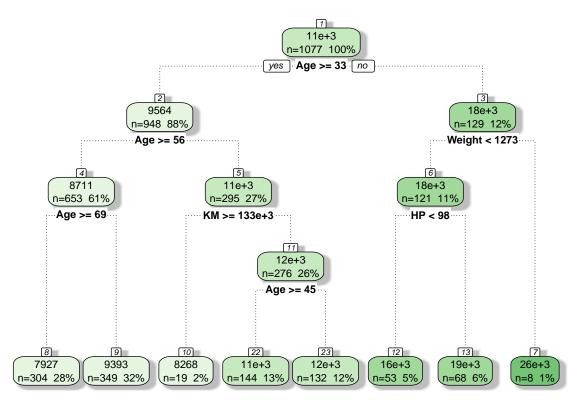
```
## Quarterly_Tax 3.492318 1 1.868774
## Weight 3.017700 1 1.737153
```

There aren't any variables with VIF greater than 5, so we don't need to worry about those.

We will just worry about dropping insignificant values instead.

```
lm2 <- lm(Price ~ . -Met_Color -cc -Doors, data = df.train)</pre>
summary(lm2)
##
## Call:
## lm(formula = Price ~ . - Met_Color - cc - Doors, data = df.train)
## Residuals:
##
       Min
                 1Q
                                   ЗQ
                                            Max
                      Median
## -10329.8
             -747.5
                       -57.7
                                 686.9
                                         6923.8
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  -5.756e+03 1.343e+03 -4.286 1.99e-05 ***
                  -1.244e+02 2.988e+00 -41.637 < 2e-16 ***
## Age
                  -1.632e-02 1.483e-03 -11.008 < 2e-16 ***
## KM
## Fuel_TypeDiesel 1.108e+03 4.334e+02 2.558 0.0107 *
## Fuel_TypePetrol 2.837e+03 4.339e+02 6.538 9.65e-11 ***
                   2.291e+01 3.927e+00 5.835 7.13e-09 ***
## HP
## Automatic
                   3.857e+02 1.763e+02 2.187 0.0289 *
## Quarterly_Tax 1.191e+01 1.843e+00 6.465 1.54e-10 ***
## Weight
                  1.729e+01 1.259e+00 13.728 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1313 on 1068 degrees of freedom
## Multiple R-squared: 0.8634, Adjusted R-squared: 0.8623
## F-statistic: 843.5 on 8 and 1068 DF, p-value: < 2.2e-16
vif(lm2)
##
                    GVIF Df GVIF^(1/(2*Df))
                1.874295 1
                                   1.369049
## Age
## KM
                2.028835 1
                                   1.424372
## Fuel_Type
                6.395945 2
                                   1.590289
## HP
                2.081820 1
                                   1.442851
## Automatic
                1.054496 1
                                   1.026887
## Quarterly_Tax 3.474634 1
                                   1.864037
## Weight
                2.723620 1
                                   1.650340
lmF <- lm2
pred.lmF_test <- predict(lmF, df.test)</pre>
reslmF_test <- df.test$Price - pred.lmF_test
R_train <- cor(df.train$Price, lmF$fitted.values)</pre>
R_train2 <- R_train**2</pre>
MSE.lmF_train <- sum(lmF$residuals**2)/nrow(df.train)</pre>
```

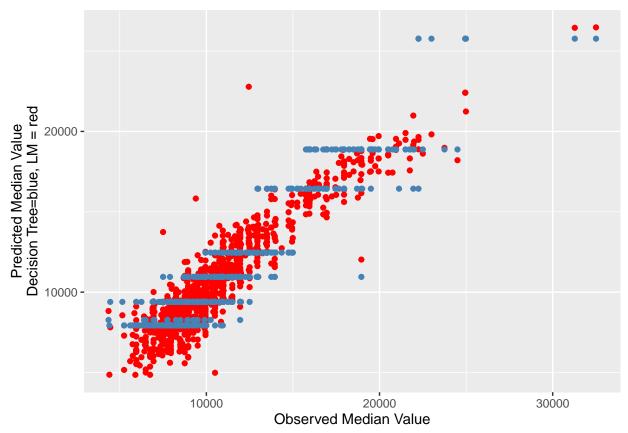
```
RMSE.lmF_train <- sqrt(MSE.lmF_train)</pre>
R_test <- cor(df.test$Price, pred.lmF_test)</pre>
R_test2 <- R_test**2</pre>
MSE.lmF_test <- sum(reslmF_test**2)/nrow(df.test)</pre>
RMSE.lmF_test <- sqrt(MSE.lmF_test)</pre>
RMSE <- c(RMSE.lmF_train, RMSE.lmF_test)</pre>
R2 <- c(R_train2, R_test2)
df.lmF <- rbind.data.frame(RMSE, R2)</pre>
colnames(df.lmF) <- c("training", "test")</pre>
rownames(df.lmF) <- c("RMSE.LM", "R_Square.LM")</pre>
df.lmF
##
                   training
                                     test
## RMSE.LM
               1307.2017712 1346.4283848
## R_Square.LM
                  0.8633596
                               0.8805802
fit <- rpart(Price ~ . -Met_Color -cc -Doors, data = df.train, method = "anova")</pre>
rpart.plot(fit)
                                         11e + 3
                                         100%
                                 18e+3
                  9564
                  88%
                                                                  12%
               Age >= 56
                                                            Weight < 1273
      8711
                                                         18e+3
                             11e+3
      61%
                             27%
                                                          11%
   Age >= 69
                        KM >= 133e+3
                                                        HP < 98
                                     12e+3
                                     26%
                                  Age >= 45
           9393
                      8268
                                                                        26e+3
 7927
                               11e+3
                                          12e+3
                                                    16e+3
                                                              19e+3
 28%
           32%
                      2%
                                13%
                                          12%
                                                     5%
                                                                6%
                                                                          1%
fancyRpartPlot(fit)
```



Rattle 2020-Jun-24 19:18:11 Shiloh

```
pred.train_dt <- predict(fit, newdata = df.train)</pre>
pred.test_dt <- predict(fit, newdata = df.test)</pre>
MSE.train_dt <- sum((pred.train_dt - df.train$Price)**2)/nrow(df.train)
RMSE.train_dt <- sqrt(MSE.train_dt)</pre>
MSE.test_dt <- sum((pred.test_dt - df.test$Price)**2)/nrow(df.test)</pre>
RMSE.test_dt <- sqrt(MSE.test_dt)</pre>
r.train_dt <- cor(df.train$Price, pred.train_dt)</pre>
RMSE_dt <- c(RMSE.train_dt, RMSE.test_dt)</pre>
r.test_dt <- cor(df.test$Price, pred.test_dt)</pre>
r_dt <- c(r.train_dt, r.test_dt)</pre>
r2_dt <- r_dt**2
df.dt <- rbind.data.frame(RMSE_dt, r2_dt)</pre>
colnames(df.dt) <- c("training","test")</pre>
rownames(df.dt) <- c("RMSE.DT", "R_Square.DT")</pre>
round(df.dt,2)
##
                training
## RMSE.DT
                 1329.75 1443.30
## R_Square.DT
                     0.86
                              0.86
df.train <- cbind.data.frame(df.train$Price, lmF$fitted.values, pred.train dt)
colnames(df.train) <- c("Price_obs", "Price_lm.pred", "Price_dt.pred")</pre>
df.test <- cbind.data.frame(df.test$Price, pred.lmF_test, pred.test_dt)</pre>
colnames(df.test) <- c("Price_obs", "Price_lm.pred", "Price_dt.pred")</pre>
```

```
p.train1 <- ggplot(df.train, aes(x = Price_obs)) +
   geom_point(aes(y = Price_lm.pred), color = "red") +
   geom_point(aes(y = Price_dt.pred), color = "steelblue") +
   xlab("Observed Median Value") +
   ylab("Predicted Median Value\nDecision Tree=blue, LM = red")
p.train1</pre>
```



Charles Book Club

```
df <- read.csv("Charles_BookClub.csv", header = TRUE)

M <- .25 * nrow(df)
#to be able to replicate the results, set initial seed for random
#number generator
set.seed(11317)
holdout <- sample(1:nrow(df), M, replace = F)

df.train <- df[-holdout,]  # Training set
df.test <- df[holdout,]  # Test set
dim(df.train) # 1500 18

## [1] 1500 18

dim(df.test) # 500 18</pre>
```

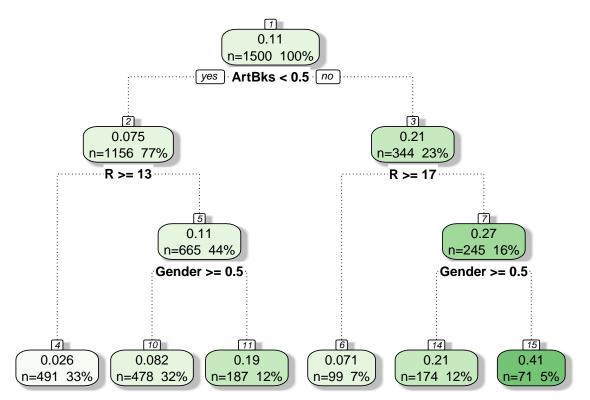
```
lm1 \leftarrow lm(Florence \sim .,
          data = df.train)
# summary(lm1)
vif(lm1)
##
          Seq.
                       ID.
                                Gender
                                                 М
                                                             R.
                                                                         F
## 3499.030319 3498.938281
                              1.005187
                                          1.382630
                                                      3.365684
                                                                 25.170685
   FirstPurch
                 ChildBks
                             YouthBks
                                           CookBks
                                                      DoltYBks
                                                                    RefBks
##
     10.205032
                  3.404586
                              1.964167
                                          3.628549
                                                      2.237993
                                                                  2.068220
##
       ArtBks
                  GeogBks
                              ItalCook ItalHAtlas
                                                       ItalArt
                  2.623941
##
      2.108610
                              1.666955
                                          1.487643
                                                      1.648895
Remove variables with VIF greater than 5.
lm2 <- lm(Florence ~ . -Seq. -ID. -FirstPurch, data = df.train)</pre>
summary(lm2)
##
## Call:
## lm(formula = Florence ~ . - Seq. - ID. - FirstPurch, data = df.train)
##
## Residuals:
##
       Min
                  1Q
                      Median
                                    30
                                            Max
## -0.62351 -0.13810 -0.07681 0.00542 1.04590
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.620e-01 3.057e-02 5.299 1.34e-07 ***
## Gender
              -8.415e-02 1.658e-02 -5.075 4.36e-07 ***
## M
               4.476e-06 8.682e-05
                                      0.052 0.958887
## R
              -3.673e-03 1.243e-03 -2.955 0.003172 **
## F
               3.597e-02 1.016e-02 3.539 0.000414 ***
## ChildBks
              -5.388e-02 1.371e-02 -3.929 8.91e-05 ***
## YouthBks
              -5.287e-02 1.772e-02 -2.983 0.002899 **
## CookBks
              -6.264e-02 1.330e-02 -4.712 2.69e-06 ***
## DoltYBks
              -6.587e-02 1.532e-02 -4.300 1.82e-05 ***
## RefBks
               -8.097e-03 1.851e-02 -0.438 0.661795
               9.221e-02 1.782e-02
## ArtBks
                                       5.174 2.60e-07 ***
## GeogBks
              1.894e-02 1.518e-02
                                      1.248 0.212399
## ItalCook
               9.575e-03 2.500e-02
                                       0.383 0.701795
## ItalHAtlas 1.719e-03 4.530e-02
                                       0.038 0.969743
## ItalArt
               4.078e-02 4.200e-02
                                       0.971 0.331718
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2895 on 1485 degrees of freedom
## Multiple R-squared: 0.1291, Adjusted R-squared: 0.1209
## F-statistic: 15.73 on 14 and 1485 DF, p-value: < 2.2e-16
vif(lm2)
##
       Gender
                                                 ChildBks
                      М
                                 R
                                                            YouthBks
##
     1.004759
               1.378995
                           1.890931 22.052163
                                                 3.340340
                                                            1.935618
##
                                                 GeogBks
     CookBks
               DoltYBks
                            RefBks
                                        ArtBks
                                                            ItalCook
               2.208253
                          2.008012
                                     2.072295
##
     3.543613
                                                2.548580
                                                          1.659966
```

```
## ItalHAtlas ItalArt
## 1.466824 1.644772
```

Remove insignificant variables.

```
lmF <- lm(Florence ~ . -Seq. -ID. -FirstPurch -M -RefBks -GeogBks -ItalCook -ItalHAtlas -ItalArt, data
summary(lmF)
##
## lm(formula = Florence ~ . - Seq. - ID. - FirstPurch - M - RefBks -
      GeogBks - ItalCook - ItalHAtlas - ItalArt, data = df.train)
##
## Residuals:
##
      Min
               1Q
                    Median
                               3Q
## -0.62292 -0.14093 -0.07659 0.00674 1.04768
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.151279 0.023282 6.498 1.11e-10 ***
## Gender
            ## R
             ## F
## ChildBks
            ## YouthBks -0.058811 0.016050 -3.664 0.000257 ***
## CookBks
            -0.065665 0.011190 -5.868 5.42e-09 ***
            ## DoltYBks
             ## ArtBks
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2894 on 1491 degrees of freedom
## Multiple R-squared: 0.1266, Adjusted R-squared: 0.1219
## F-statistic:
                27 on 8 and 1491 DF, p-value: < 2.2e-16
vif(lmF)
                        F ChildBks YouthBks CookBks DoltYBks
##
## 1.003253 1.346521 8.591445 2.547548 1.589178 2.512888 1.741012 1.570854
pred.lmF_test <- predict(lmF, df.test)</pre>
reslmF_test <- df.test$Florence - pred.lmF_test
R_train <- cor(df.train$Florence, lmF$fitted.values)</pre>
R train2 <- R train**2
MSE.lmF_train <- sum(lmF$residuals**2)/nrow(df.train)</pre>
RMSE.lmF_train <- sqrt(MSE.lmF_train)</pre>
R_test <- cor(df.test$Florence, pred.lmF_test)</pre>
R_test2 <- R_test**2</pre>
MSE.lmF_test <- sum(reslmF_test**2)/nrow(df.test)</pre>
RMSE.lmF_test <- sqrt(MSE.lmF_test)</pre>
RMSE <- c(RMSE.lmF_train, RMSE.lmF_test)</pre>
R2 <- c(R_train2, R_test2)
df.lmF <- rbind.data.frame(RMSE, R2)</pre>
```

```
colnames(df.lmF) <- c("training", "test")</pre>
rownames(df.lmF) <- c("RMSE.LM", "R_Square.LM")</pre>
df.lmF
##
                training
                              test
               0.2884960 0.2986055
## RMSE.LM
## R_Square.LM 0.1265513 0.1194512
fit <- rpart(Florence ~ . -Seq. -ID. -FirstPurch -M -RefBks -GeogBks -ItalCook -ItalHAtlas -ItalArt,
             data = df.train, method = "anova")
rpart.plot(fit)
                                 100%
                        yes - ArtBks < 1-no
            0.075
          R >= 13
                                                      R >= 17^{-}
                   Gender = 1
                                                              Gender = 1
 0.026
               0.082
                              0.19
                                            0.071
                                                                         0.41
 33%
                32%
                              12%
                                             7%
                                                           12%
                                                                          5%
fancyRpartPlot(fit)
```



Rattle 2020-Jun-24 19:18:14 Shiloh

```
pred.train_dt <- predict(fit, newdata = df.train)</pre>
pred.test_dt <- predict(fit, newdata = df.test)</pre>
MSE.train_dt <- sum((pred.train_dt - df.train$Florence)**2)/nrow(df.train)
RMSE.train_dt <- sqrt(MSE.train_dt)</pre>
MSE.test_dt <- sum((pred.test_dt - df.test$Florence)**2)/nrow(df.test)</pre>
RMSE.test_dt <- sqrt(MSE.test_dt)</pre>
r.train_dt <- cor(df.train$Florence, pred.train_dt)</pre>
RMSE_dt <- c(RMSE.train_dt, RMSE.test_dt)</pre>
r.test_dt <- cor(df.test$Florence, pred.test_dt)</pre>
r_dt <- c(r.train_dt, r.test_dt)</pre>
r2_dt <- r_dt**2
df.dt <- rbind.data.frame(RMSE_dt, r2_dt)</pre>
colnames(df.dt) <- c("training","test")</pre>
rownames(df.dt) <- c("RMSE.DT", "R_Square.DT")</pre>
round(df.dt,2)
##
                training test
## RMSE.DT
                     0.29 0.31
## R_Square.DT
                     0.09 0.04
df.train <- cbind.data.frame(df.train$Florence, lmF$fitted.values, pred.train dt)
colnames(df.train) <- c("Florence_obs", "Florence_lm.pred", "Florence_dt.pred")</pre>
df.test <- cbind.data.frame(df.test$Florence, pred.lmF test, pred.test dt)</pre>
colnames(df.test) <- c("Florence_obs", "Florence_lm.pred", "Florence_dt.pred")</pre>
```

```
p.train1 <- ggplot(df.train, aes(x = Florence_obs)) +
    geom_point(aes(y = Florence_lm.pred), color = "red") +
    geom_point(aes(y = Florence_dt.pred), color = "steelblue") +
    xlab("Observed Median Value") +
    ylab("Predicted Median Value\nDecision Tree=blue, LM = red")
p.train1</pre>
```

