

## Quick Review

- Ductility: Ability of a material to be permanently deformed without breaking when a force is applied.

$$\% \text{ elongation} = \frac{l_f - l_0}{l_0} \times 100$$

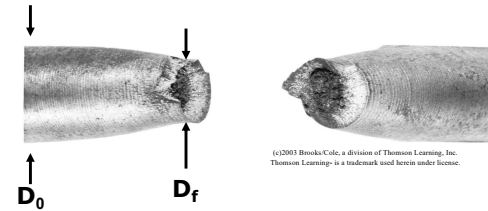
$$\% \text{ reduction in area} = \frac{A_0 - A_f}{A_0} \times 100$$

### Example:

- Initial diameter of bar  $D_0 = 12.5 \text{ mm}$
- Final diameter at the fracture surface  $D_f = 9.85 \text{ mm}$

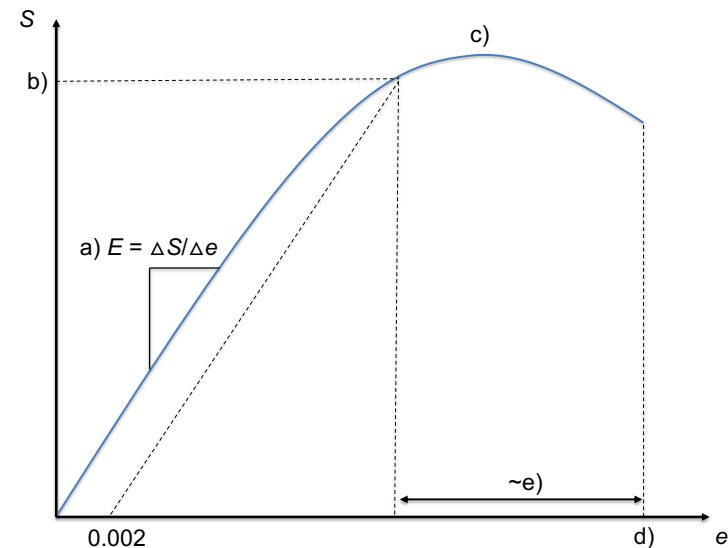
$$\begin{aligned} \bullet \text{ \% RA} = ? \quad \%RA &= \frac{A_0 - A_f}{A_0} \\ &= \frac{\pi(12.5\text{mm}/2)^2 - \pi(9.85\text{mm}/2)^2}{\pi(12.5\text{mm}/2)^2} \\ &= 0.379 = 37.9\% \end{aligned}$$

Measure  $D_0$  prior to testing



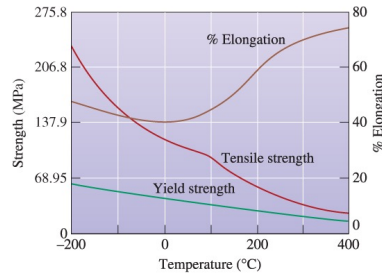
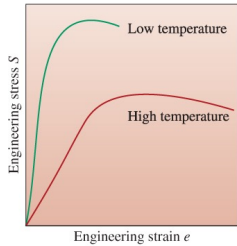
- Exercise: Sketch an engineering stress-strain curve for a metal and show the following on the curve:

- Elastic Modulus
- 0.2% offset yield strength
- The point at which necking happens
- The strain at the breaking point
- The permanent strain at the breaking point (i.e. failure)



## Quick Review

- As temperature increases:
  - YS, UTS,  $E$  decrease
  - Ductility increases



- Due to ( $\uparrow$  or  $\downarrow$ ):
  - \_\_\_ dislocation density
  - \_\_\_ grain size
  - \_\_\_ point defect density

**Example:** Calculate the engineering and true stresses/strains for an Al-alloy rod (12.83 mm initial diameter, 50.8 mm initial length) that is subjected to a 35.584 kN load, resulting in a 12.46 mm diameter and 3.05 mm increase in length.

$$A_0 = \pi \left( \frac{12.83 \text{ mm}}{2} \right)^2 = 129.3 \text{ mm}^2$$

$$S = \frac{F}{A_0} = \frac{35.584 \text{ kN}}{129.3 \text{ mm}^2} = \frac{35.584 \times 10^3 \text{ N}}{129.3 \times 10^{-6} \text{ m}^2} = 275 \text{ MPa}$$

$$l_0 = 50.8 \text{ mm}$$

$$F = 35.584 \text{ kN}$$

$$\Delta l = 3.05 \text{ mm}$$

$$e = \frac{\Delta l}{l_0} = \frac{3.05 \text{ mm}}{50.8 \text{ mm}} = 0.06$$

$$\sigma = S(1 + e) = 275 \text{ MPa}(1.06) = 291.5 \text{ MPa} \text{ is the true stress}$$

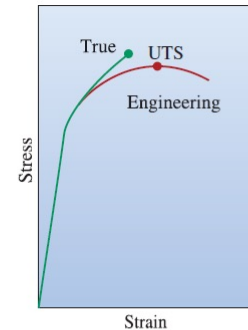
$$\varepsilon = \ln(1 + e) = \ln(1.06) = 0.058 \text{ is the true strain}$$

## Quick Review

- True stress and strain: based on instantaneous specimen dimensions

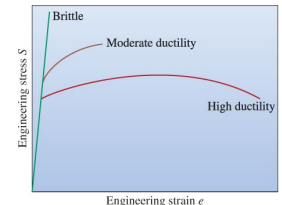
$$\text{True stress} = \sigma = \frac{F}{A} \quad \text{True strain} = \varepsilon = \int_{l_0}^l \frac{dl}{l} = \ln\left(\frac{l}{l_0}\right) = \ln\left(\frac{A_0}{A}\right)$$

$$\sigma = S(1 + e) \quad \varepsilon = \ln(1 + e)$$

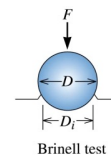


## Quick Review

- Very brittle materials
  - YS=UTS=Fracture strength

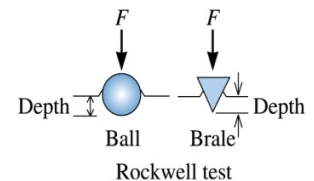


- Hardness test: measure of resistance to penetration by a hard indenter
  - Brinell, Rockwell, etc.



$$BHN = \frac{2F}{\pi D \left[ D - \sqrt{D^2 - D_i^2} \right]}$$

$F$  = applied load, kg  
 $D$  = diameter of indenter, mm  
 $D_i$  = diameter of impression



- A Brinell hardness test is performed using an indenter with a diameter of 10 mm and a load of 450 kg, resulting in an indentation of 3.7 mm on an Al-alloy. What is the BHN of the alloy?

$$BHN = \frac{2F}{\pi D \left[ D - \sqrt{D^2 - D_i^2} \right]}$$

$F = 450 \text{ kg}$   
 $D = 10 \text{ mm}$   
 $D_i = 3.7 \text{ mm}$

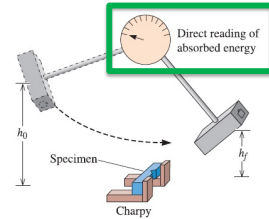
$$BHN = \frac{2(450 \text{ kg})}{\pi(10 \text{ mm}) \left[ 10 \text{ mm} - \sqrt{(10 \text{ mm})^2 - (3.7 \text{ mm})^2} \right]}$$

$$= \frac{900 \text{ kg}}{\pi(10 \text{ mm})[0.71 \text{ mm}]}$$

$$= 40.4 \text{ kg/mm}^2 \text{ (or 40.4 HB)}$$

- Measurements from a Charpy test (10 kg pendulum) on samples of a steel are provided. Calculate the impact energy for each test.

Temp [C]	$h_0$ [m]	$h_f$ [m]	Impact energy [J]
-196	0.50	0.46	3.9
-25	0.50	0.45	4.9
0	0.50	0.38	11.8
20	0.50	0.19	30.4
100	0.50	0.09	40.2



$$E = \text{mass} \times g \times (h_0 - h_f)$$

$$E = (10 \text{ kg})(9.81 \text{ m/s}^2)(0.50 \text{ m} - 0.46 \text{ m})$$

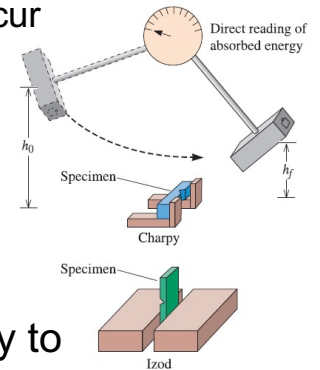
$$E = 3.9 \text{ J}$$

## Quick Review

- Metals/alloys more brittle for high strain rates (impacts)
  - Insufficient time for slip to occur

- Impact tests:

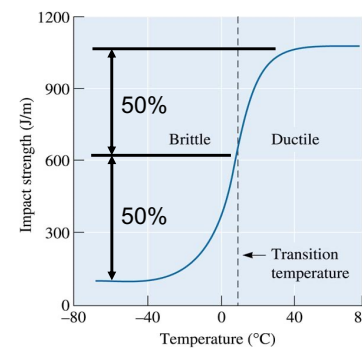
- Izod
- Charpy



- Impact toughness: the ability to withstand an impact blow

## Quick Review

- Impact tests can identify the ductile-to-brittle transition temperature (DBTT)



- Want DBTT \_\_\_\_\_  $T_{\text{operating}}$  (< or > ?)

## Midterm review suggestions

- Review all lecture slides
- Review all study questions
  - Note ones you find challenging
- Review the “key concepts” in weekly summaries
  - Try explaining to yourself or someone else
- Review formula sheet
  - Explain each formula to yourself
- Attempt old exams provided on LEARN
  - Review solutions, identify material to review