1. Consider the following algorithm for minimizing a function f:

$$x^{(k+1)} = x^{(k)} + \alpha_k d^{(k)},$$

where

$$\alpha_k = \arg\min_{\alpha} f(x^{(k)} + \alpha d^{(k)}).$$

Let  $g^{(k)} = \nabla f \left( x^{(k)} \right)$  (as usual). Suppose that f is quadratic with Hessian Q. We choose

$$d^{(k+1)} = \gamma_k g^{(k+1)} + d^{(k)},$$

and we wish the directions  $d^{(k)}$  and  $d^{(k+1)}$  to be Q-conjugate. Find a formula for  $\gamma_k$  in terms of  $d^{(k)}$ ,  $g^{(k+1)}$ , and Q.