

Mini-batch gradient descent

Batch vs. mini-batch gradient descent

Vectorization allows you to efficiently compute on m examples.

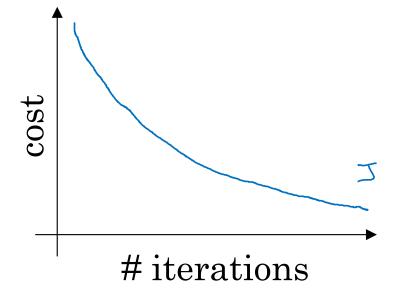
stop of qualit deat Mini-batch gradient descent (as ifmel 500) report 2 for t = 1,..., 5000 { Formal peop on X [ts]. $A_{CO} = a_{CO} \left(\frac{5}{5} c_{OJ} \right)$ $A_{CO} = a_{CO}$ Compute cost $J^{\ell\ell}_{\overline{J}} = \frac{1}{1000} \stackrel{\text{def}}{=} J(y,y) + \frac{\lambda}{211000} \stackrel{\text{E}}{=} ||W^{\ell\ell}||_F^2$. Backprop to compart gradults cort Jser (usy (xser) YEER)) 3 W:= W⁽²⁾ - ddw⁽²⁾, b⁽¹⁾ = b⁽¹⁾ - db⁽²⁾ "I epoch" poss through training set.



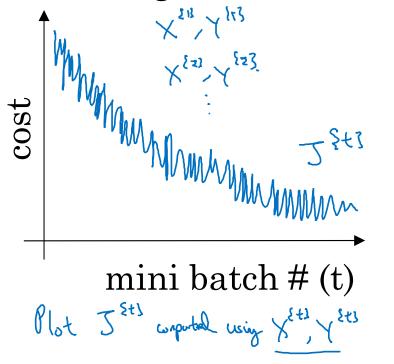
Understanding mini-batch gradient descent

Training with mini batch gradient descent

Batch gradient descent



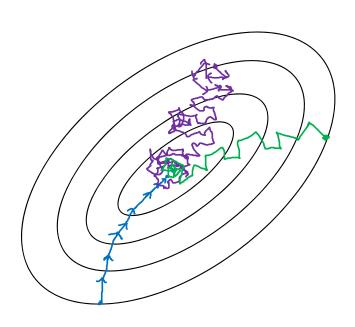
Mini-batch gradient descent



Choosing your mini-batch size

The mini-botth size = m: Sorth godner desch. $(X^{SIS}, Y^{SIS}) = (X, Y)$ The mini-botth size = 1: Stochaster graph descent. Every example is it our $(X^{SIS}, Y^{SIS}) = (X^{SIS}, Y^{SIS}) = (X^$

In practice: Social in-between I all m



Stochostic

gradent

legent

Lose spealup

from ventonitation

In-bothern

(min;hoth size

not too by/small)

Furleyt levery.

Vectorantian.

(n) 000)

· Mate poor without processing entire truly set.

Bostch

gradient desent

(min; harth size = m)

Two long per iteration

Choosing your mini-batch size

If small tray set: Use borth graher descent.

(m < 2500)

Typical mint-borth sizes:

(c) 64, 128, 256, 512

20 20 20 20 20

Male sue mintbook fit is CPU/GPU memony.

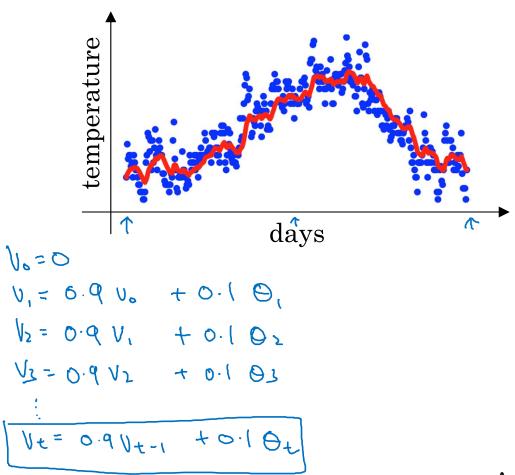
XXX, YXX, YXX



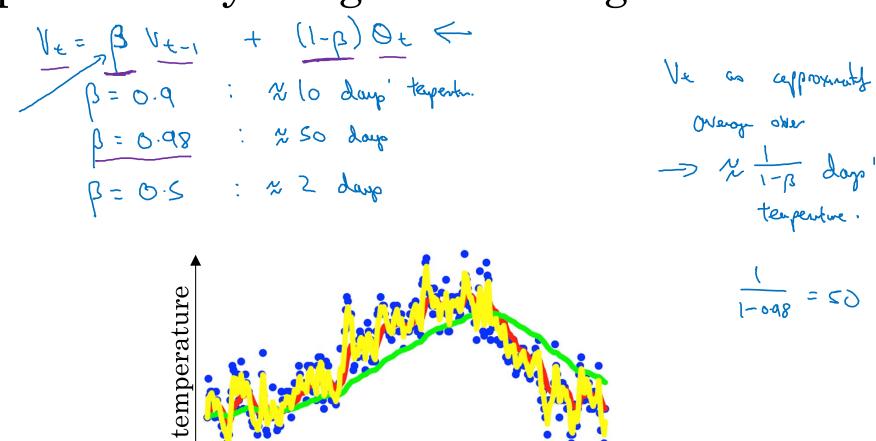
Exponentially weighted averages

Temperature in London

```
\theta_{1} = 40^{\circ}F \quad \text{fc} \leftarrow \theta_{2} = 49^{\circ}F \quad \text{gc}
\theta_{3} = 45^{\circ}F
\vdots
\theta_{180} = 60^{\circ}F \quad \text{Gc}
\theta_{181} = 56^{\circ}F
\vdots
```



Exponentially weighted averages



days



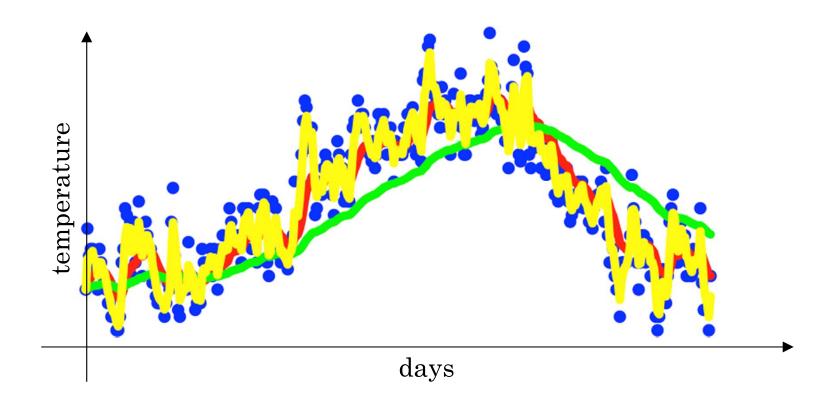
Understanding exponentially weighted averages

Exponentially weighted averages

$$v_t = \beta v_{t-1} + (1 - \beta)\theta_t$$



ک، ن



Exponentially weighted averages

Exponentially weighted averages
$$v_{t} = \beta v_{t-1} + (1-\beta)\theta_{t}$$

$$v_{100} = 0.9v_{99} + 0.1\theta_{100}$$

$$v_{99} = 0.9v_{98} + 0.1\theta_{99}$$

$$v_{98} = 0.9v_{97} + 0.1\theta_{98}$$
...
$$v_{100} = 0.9v_{98} + 0.1\theta_{99}$$

$$v_{100} = 0.9v_{99} + 0.1\theta_{98}$$

$$v_{100} = 0.9v_{99} + 0.1\theta_{99}$$

$$v_{100} = 0.9v_{99} + 0.1\theta_{100}$$

$$v_$$

Implementing exponentially weighted averages

$$v_0 = 0$$

 $v_1 = \beta v_0 + (1 - \beta) \theta_1$
 $v_2 = \beta v_1 + (1 - \beta) \theta_2$
 $v_3 = \beta v_2 + (1 - \beta) \theta_3$
...

$$V_{0} := 0$$
 $V_{0} := \beta v + (1-\beta) O_{1}$
 $V_{0} := \beta v + (1-\beta) O_{2}$
 $V_{0} := \beta v + (1-\beta) O_{2}$

>
$$V_0 = 0$$

Kapent ξ

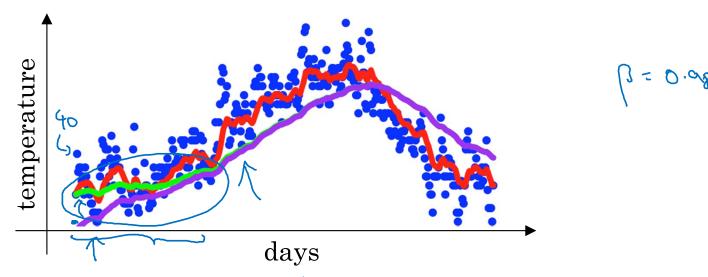
Cut next 0_{\pm}
 $V_0 := \beta V_0 + (1-\beta) 0_{\pm}$

Andrew Ng



Bias correction in exponentially weighted average

Bias correction



$$v_{t} = \beta v_{t-1} + (1 - \beta)\theta_{t}$$

$$v_{0} = 0$$

$$v_{1} = 0.98 v_{0} + 0.02 \Theta_{1}$$

$$v_{2} = 0.98 v_{1} + 0.02 \Theta_{2}$$

$$= 0.98 \times 0.02 \times \Theta_{1} + 0.02 \Theta_{2}$$

$$= 0.0196 \Theta_{1} + 0.02 \Theta_{2}$$

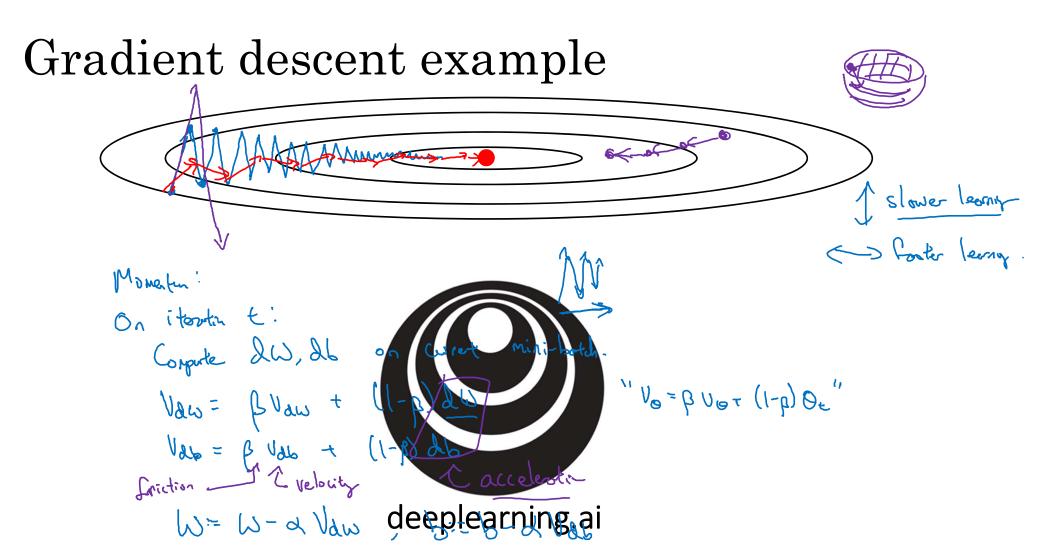
$$\frac{1-\beta^{t}}{1-\beta^{t}}$$

$$t=2: 1-\beta^{t} = 1-(0.98)^{2} = 0.0396$$

$$\frac{V_{2}}{0.0396} = 0.0396$$



Gradient descent with momentum



Implementation details

On iteration *t*:

Compute dW, db on the current mini-batch

$$\rightarrow v_{dW} = \beta v_{dW} + M \beta dW$$

$$v_{db} = \beta v_{db} + (1 - \beta) \underline{db}$$

$$W = W - \alpha v_{dW}, \ b = b - \alpha v_{db}$$

Hyperparameters:
$$\alpha, \beta$$

$$\beta = 0.9$$
Overlose on lose 100 graduits



RMSprop

RMSprop W., Wz, W2 On iteration t: Compute du, de on count mini-both Saw = B2 Saw + (1-P2) dw? = small \Rightarrow Sab = β_2 Sab + $(1-\beta_2)$ db^2 < large W:= W- & dw < b:= b-2 db < JSab+E < Z=10-8



Adam optimization algorithm

Adam optimization algorithm

Hyperparameters choice:

$$\rightarrow$$
 d: needs to be tune
 \rightarrow β : 0.9 \longrightarrow (dw)
 \rightarrow β : 0.999 \longrightarrow (dw²)
 \rightarrow Σ : 10-8

Adam: Adaptiv moment estimation

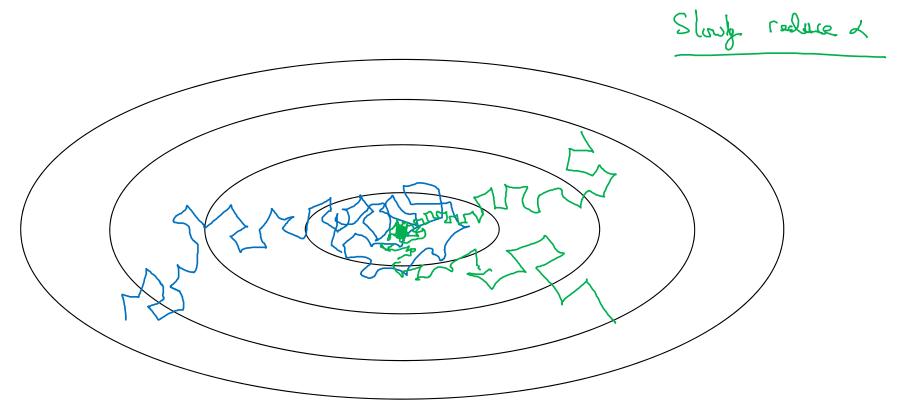


Adam Coates



Learning rate decay

Learning rate decay



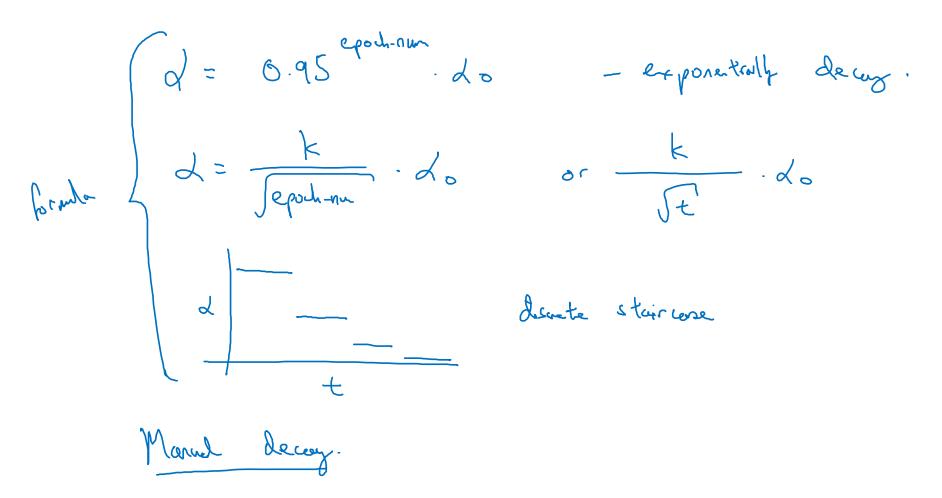
Learning rate decay

apoch = 1 pass throgh dort.

Epoch	2
	0.1
2	0.67
3	6.5
4	D. 4
•	-

X 813 (X 821)	
	> epoch 1
do = 0.2 decep. rete = 1	

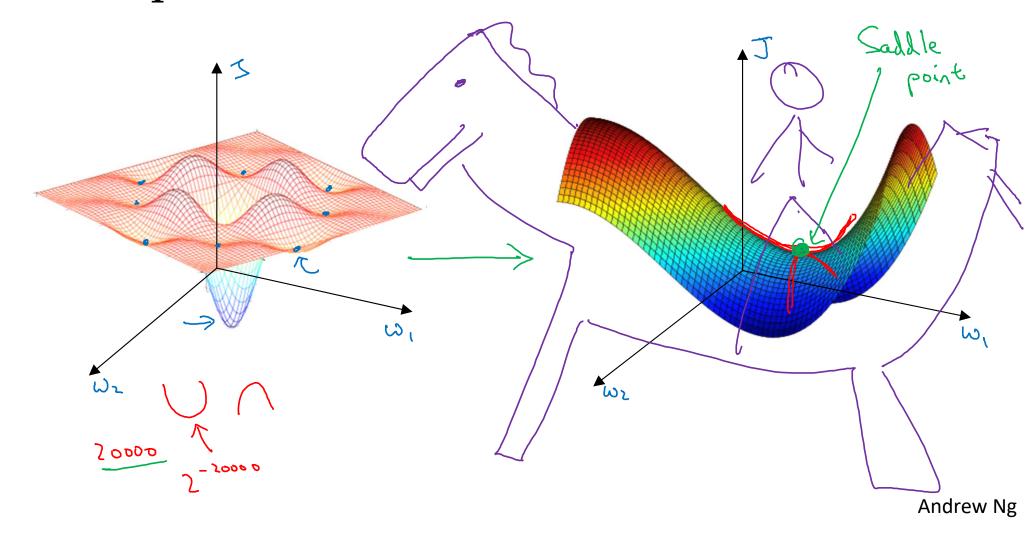
Other learning rate decay methods



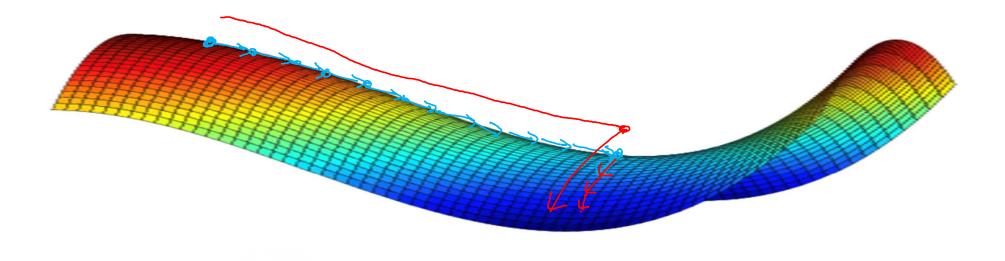


The problem of local optima

Local optima in neural networks



Problem of plateaus



- Unlikely to get stuck in a bad local optima
- Plateaus can make learning slow