

## STAT511 HW#8

**Reading:** Read Chapter 10 of Ott & Longnecker  
**See Canvas Calendar for Due Date.**

40 points total, 2 points per problem part unless otherwise noted.

1. Suppose  $Y$  is a binomial random variable with  $n = 22$  and  $\pi = 0.72$ . Compute the following.
  - A. Mean and standard deviation of  $Y$ .
  - B.  $P(Y \leq 16)$
  - C.  $P(Y < 16)$
  - D.  $P(16 \leq Y < 18)$
  - E.  $P(Y = 18)$
  - F.  $P(Y \geq 18)$
  - G. The normal approximation to  $P(Y \geq 18)$  without continuity correction.
  - H. The normal approximation to  $P(Y \geq 18)$  with continuity correction.
2. In a sample of 75 randomly selected students, 51 of them are STEM majors. Express all answers to the following questions as proportions. For this question, do the calculations “by hand”.
  - A. Give an estimate for the proportion of students who are STEM majors.
  - B. Provide a 95% confidence interval for the true proportion of students who are STEM majors. Use the large sample normal approximation (slide 13 of the CH10 notes).
  - C. Conduct a hypothesis test (using the large sample normal approximation) with  $\alpha=0.05$  to test  $H_A: \pi > 0.5$ . Give the  $Z$  test statistic,  $p$ -value, and conclusion (**4pts**).
3. A factory manager decided to estimate the proportion of defective items. A random sample of 60 items was inspected and it was found that 10 of them are defective.
  - A. Give an estimate for the proportion of defective items.
  - B. Using R, calculate a **90%** confidence interval for the true proportion of defective items using the normal approximation. NOTES: (1) Use `correct=TRUE` (default). (2) The R CI will not match a hand calculation for this problem because R uses a different formula.
  - C. Using R, calculate a **90%** confidence interval for the true proportion of defective items using the exact binomial method.
  - D. Is the sample size large enough for the normal approximation to be valid? Justify your response using the “better” criteria discussed in the notes.
4. A researcher is planning to run a one-way ANOVA to compare 4 different pesticides used on apple trees. The response variable is yield. The researcher wishes to calculate the sample size needed (e.g. number of trees per treatment) to achieve a power level of 0.90 given several different conjectured alternatives. Assume the researcher will have an equal number of trees for each treatment, and believes the standard deviation (within treatment) is  $\sigma = 10$  units. The different conjectured alternatives are:

- i.  $\mu_1 = 55, \mu_2 = 45, \mu_3 = 45, \mu_4 = 35$
- ii.  $\mu_1 = 50, \mu_2 = 50, \mu_3 = 40, \mu_4 = 40$
- iii.  $\mu_1 = 50, \mu_2 = 50, \mu_3 = 45, \mu_4 = 35$

- A. What sample size do you recommend to the researcher for each of the above scenarios? **(6 pts)** **Note:** Round your sample size UP to the next integer value!
- B. Notice that the conjectured means in the three different scenarios all sum to 180, yet you should have found that quite different sample sizes were needed to achieve a power of 0.90. Which scenario requires the largest sample size? Explain why it requires the largest sample size. It helps to think about the null hypothesis for the ANOVA F-test.