常用积分公式

(-)含有 ax +b的积分 (a ≠ 0)

1.
$$\int \frac{dx}{ax + b} = \frac{1}{a} \ln |ax + b| + C$$

2.
$$\int (ax+b)^{\mu} dx = \frac{1}{a(\mu+1)} (ax+b)^{\mu+} + C (\mu \neq -1)$$

3.
$$\int \frac{x}{ax + b} dx = \frac{1}{a^2} (ax + b - b \ln |ax + b|) + C$$

6.
$$\int \frac{dx}{x^2(ax^+b)} = -\frac{1}{bx} + \frac{a}{b^2} \ln \left| \frac{ax^+b}{x} \right| + C$$

7.
$$\int \frac{x}{(ax + b)^2} dx = \frac{1}{a^2} (\ln |ax + b| + \frac{b}{ax + b}) + C$$

8.
$$\int \frac{x^2}{(ax+b)^2} dx = \frac{1}{a^3} (ax+b-2b \ln |ax+b-\frac{b^2}{ax+b}) + C$$

9.
$$\int \frac{dx}{x(ax+b)^2} = \frac{1}{b(ax+b)} - \frac{1}{b^2} \ln \left| \frac{ax+b}{x} \right| + C$$

10.
$$\int \sqrt{ax + b} dx = \frac{2}{3a} \sqrt{(ax + b)^3} + C$$

11.
$$\int x \sqrt{ax + b} dx = \frac{2}{15a^2} (3ax - 2b) \sqrt{(ax + b)^3} + C$$

12.
$$\int x^2 \sqrt{ax^+b} dx = \frac{2}{105a^3} (15a^2x^2 - 12abx^+8b^2) \sqrt{(ax^+b)^3} + C$$

13.
$$\int \frac{x}{\sqrt{ax+b}} dx = \frac{2}{3a^2} (ax-2b) \sqrt{ax+b} + C$$

14.
$$\int \frac{x^2}{\sqrt{ax+b}} dx = \frac{2}{15a^3} (3a^2x^2 - 4abx + 8b^2) \sqrt{ax+b} + C$$

16.
$$\int \frac{dx}{x^2 \sqrt{ax + b}} = -\frac{\sqrt{ax + b}}{bx} - \frac{a}{2b} \int \frac{dx}{x \sqrt{ax + b}}$$

17.
$$\int \frac{\sqrt{ax + b}}{x} dx = 2\sqrt{ax + b} + b \int \frac{dx}{x\sqrt{ax + b}}$$

18.
$$\int \frac{\sqrt{ax + b}}{x^2} dx = -\frac{\sqrt{ax + b}}{x} + \frac{a}{2} \int \frac{dx}{x\sqrt{ax + b}}$$

$$(\Xi)$$
含有 $x^2 \pm a^2$ 的积分

19.
$$\int \frac{dx}{x^2 + a^2} = \frac{1}{a} \arctan \frac{x}{a} + C$$

21.
$$\int \frac{dx}{x^2 - a^2} = \frac{1}{2a} \ln \left| \frac{x - a}{x + a} \right| + C$$

(四)含有
$$ax^2 + b(a > 0)$$
的积分

23.
$$\int \frac{x}{ax^2 + b} dx = \frac{1}{2a} \ln |ax^2 + b| + C$$

24.
$$\int \frac{x^2}{ax^2 + b} dx = \frac{x}{a} - \frac{b}{a} \int \frac{dx}{ax^2 + b}$$

25.
$$\int \frac{dx}{x(ax^2+b)} = \frac{1}{2b} \ln \frac{x^2}{|ax^2+b|} + C$$

26.
$$\int \frac{dx}{x^2(ax^2 + b)} = -\frac{1}{bx} - \frac{a}{b} \int \frac{dx}{ax^2 + b}$$

27.
$$\int \frac{dx}{x^3(ax^2+b)} = \frac{a}{2b^2} \ln \frac{|ax^2+b|}{x^2} - \frac{1}{2bx^2} + C$$

28.
$$\int \frac{dx}{(ax^2 + b)^2} = \frac{x}{2b(ax^2 + b)} + \frac{1}{2b} \int \frac{dx}{ax^2 + b}$$

(五)含有 $ax^2 + bx + c$ (a > 0)的积分

$$29. \int \frac{dx}{ax^{2} + bx + c} = \begin{cases} \frac{2}{\sqrt{4ac - b^{2}}} & arctan \frac{2ax + b}{\sqrt{4ac - b^{2}}} + C \\ \frac{1}{\sqrt{b^{2} - 4ac}} \ln \left| \frac{2ax + b - \sqrt{b^{2} - 4ac}}{2ax + b + \sqrt{b^{2} - 4ac}} \right| + C \quad (b^{2} > 4ac) \end{cases}$$

30.
$$\int \frac{x}{ax^2 + bx + c} dx = \frac{1}{2a} \ln |ax^2 + bx + c| - \frac{b}{2a} \int \frac{dx}{ax^2 + bx + c}$$

(六)含有
$$\sqrt{x^2 + a^2}$$
 (a > 0)的积分

31.
$$\int \frac{dx}{\sqrt{x^2 + a^2}} = \operatorname{arsh} \frac{x}{a} + C_1 = \ln(x + \sqrt{x^2 + a^2}) + C$$

32.
$$\int \frac{dx}{\sqrt{(x^2 + a^2)^3}} = \frac{x}{a^2 \sqrt{x^2 + a^2}} + C$$

33.
$$\int \frac{x}{\sqrt{x^2 + a^2}} dx = \sqrt{x^2 + a^2} + C$$

34.
$$\int \frac{x}{\sqrt{(x^2 + a^2)^3}} dx = -\frac{1}{\sqrt{x^2 + a^2}} + C$$

35.
$$\int \frac{x^2}{\sqrt{x^2 + a^2}} dx = \frac{x}{2} \sqrt{x^2 + a^2} - \frac{a^2}{2} \ln(x + \sqrt{x^2 + a^2}) + C$$

成功是必须的

36.
$$\int \frac{x^2}{\sqrt{(x^2 + a^2)^3}} dx = -\frac{x}{\sqrt{x^2 + a^2}} + \ln(x + \sqrt{x^2 + a^2}) + C$$

37.
$$\int \frac{dx}{x\sqrt{x^2 + a^2}} = \frac{1}{a} \ln \frac{\sqrt{x^2 + a^2} - a}{|x|} + C$$

38.
$$\int \frac{dx}{x^2 \sqrt{x^2 + a^2}} = -\frac{\sqrt{x^2 + a^2}}{a^2 x} + C$$

39.
$$\int \sqrt{x^2 + a^2} dx = \frac{x}{2} \sqrt{x^2 + a^2} + \frac{a^2}{2} \ln(x + \sqrt{x^2 + a^2}) + C$$

40.
$$\int \sqrt{(x^2 + a^2)^3} dx = \frac{x}{8} (2x^2 + 5a^2) \sqrt{x^2 + a^2} + \frac{3}{8} a^4 \ln(x + \sqrt{x^2 + a^2}) + C$$

41.
$$\int x \sqrt{x^2 + a^2} dx = \frac{1}{3} \sqrt{(x^2 + a^2)^3} + C$$

42.
$$\int x^2 \sqrt{x^2 + a^2} dx = \frac{x}{8} (2x^2 + a^2) \sqrt{x^2 + a^2} - \frac{a^4}{8} \ln(x + \sqrt{x^2 + a^2}) + C$$

43.
$$\int \frac{\sqrt{x^2 + a^2}}{x} dx = \sqrt{x^2 + a^2} + a \ln \frac{\sqrt{x^2 + a^2} - a}{|x|} + C$$

44.
$$\int \frac{\sqrt{x^2 + a^2}}{x^2} dx = -\frac{\sqrt{x^2 + a^2}}{x} + \ln(x + \sqrt{x^2 + a^2}) + C$$

(七)含有
$$\sqrt{x^2 - a^2}$$
 (a > 0)的积分

45.
$$\int \frac{dx}{\sqrt{x^2 - a^2}} = \frac{x}{|x|} \operatorname{arch} \frac{|x|}{a} + C_1 = \ln |x + \sqrt{x^2 - a^2}| + C$$

46.
$$\int \frac{dx}{\sqrt{(x^2 - a^2)^3}} = -\frac{x}{a^2 \sqrt{x^2 - a^2}} + C$$

47.
$$\int \frac{x}{\sqrt{x^2 - a^2}} dx = \sqrt{x^2 - a^2} + C$$

48.
$$\int \frac{x}{\sqrt{(x^2-a^2)^3}} dx = -\frac{1}{\sqrt{x^2-a^2}} + C$$

49.
$$\int \frac{x^2}{\sqrt{x^2 - a^2}} dx = \frac{x}{2} \sqrt{x^2 - a^2} + \frac{a^2}{2} \ln \left| x + \sqrt{x^2 - a^2} \right| + C$$

50.
$$\int \frac{x^2}{\sqrt{(x^2 - a^2)^3}} dx = -\frac{x}{\sqrt{x^2 - a^2}} + \ln x + \sqrt{x^2 - a^2} + C$$

51.
$$\int \frac{dx}{x\sqrt{x^2-a^2}} = \frac{1}{a} \arccos \frac{a}{|x|} + C$$

52.
$$\int \frac{dx}{x^2 \sqrt{x^2 - a^2}} = \frac{\sqrt{x^2 - a^2}}{a^2 x} + C$$

53.
$$\int \sqrt{x^2 - a^2} dx = \frac{x}{2} \sqrt{x^2 - a^2} - \frac{a^2}{2} \ln \left| x + \sqrt{x^2 - a^2} \right| + C$$

54.
$$\int \sqrt{(x^2 - a^2)^3} dx = \frac{x}{8} (2x^2 - 5a^2) \sqrt{x^2 - a^2} + \frac{3}{8} a^4 \ln \left| x + \sqrt{x^2 - a^2} \right| + C$$

55.
$$\int x \sqrt{x^2 - a^2} dx = \frac{1}{3} \sqrt{(x^2 - a^2)^3} + C$$

56.
$$\int x^2 \sqrt{x^2 - a^2} dx = \frac{x}{8} (2x^2 - a^2) \sqrt{x^2 - a^2} - \frac{a^4}{8} \ln |x + \sqrt{x^2 - a^2}| + C$$

57.
$$\int \frac{\sqrt{x^2 - a^2}}{x} dx = \sqrt{x^2 - a^2} - a \arccos \frac{a}{|x|} + C$$

(八)含有
$$\sqrt{a^2-x^2}$$
 (a > 0)的积分

59.
$$\int \frac{dx}{\sqrt{a^2 - x^2}} = \arcsin \frac{x}{a} + C$$

60.
$$\int \frac{dx}{\sqrt{(a^2 - x^2)^3}} = \frac{x}{a^2 \sqrt{a^2 - x^2}} + C$$

61.
$$\int \frac{x}{\sqrt{a^2 - x^2}} dx = -\sqrt{a^2 - x^2} + C$$

62.
$$\int \frac{x}{\sqrt{(a^2 - x^2)^3}} dx = \frac{1}{\sqrt{a^2 - x^2}} + C$$

63.
$$\int \frac{x^2}{\sqrt{a^2 - x^2}} dx = -\frac{x}{2} \sqrt{a^2 - x^2} + \frac{a^2}{2} \arcsin \frac{x}{a} + C$$

64.
$$\int \frac{x^2}{\sqrt{(a^2 - x^2)^3}} dx = \frac{x}{\sqrt{a^2 - x^2}} - \arcsin \frac{x}{a} + C$$

65.
$$\int \frac{dx}{x\sqrt{a^2-x^2}} = \frac{1}{a} \ln \frac{a-\sqrt{a^2-x^2}}{|x|} + C$$

66.
$$\int \frac{dx}{x^2 \sqrt{a^2 - x^2}} = -\frac{\sqrt{a^2 - x^2}}{a^2 x} + C$$

67.
$$\int \sqrt{a^2 - x^2} dx = \frac{x}{2} \sqrt{a^2 - x^2} + \frac{a^2}{2} \arcsin \frac{x}{a} + C$$

68.
$$\int \sqrt{(a^2 - x^2)^3} dx = \frac{x}{8} (5a^2 - 2x^2) \sqrt{a^2 - x^2} + \frac{3}{8} a^4 \arcsin \frac{x}{a} + C$$

69.
$$\int x \sqrt{a^2 - x^2} dx = -\frac{1}{3} \sqrt{(a^2 - x^2)^3} + C$$

70.
$$\int x^2 \sqrt{a^2 - x^2} dx = \frac{x}{8} (2x^2 - a^2) \sqrt{a^2 - x^2} + \frac{a^4}{8} \arcsin \frac{x}{a} + C$$

71.
$$\int_{x}^{\sqrt{a^2 - x^2}} dx = \sqrt{a^2 - x^2} + a \ln \frac{a - \sqrt{a^2 - x^2}}{|x|} + C$$

72.
$$\int \frac{\sqrt{a^2 - x^2}}{x^2} dx = -\frac{\sqrt{a^2 - x^2}}{x} - \arcsin \frac{x}{a} + C$$

(九)含有
$$\sqrt{\pm ax^2 + bx + c}$$
 (a > 0)的积分

73.
$$\int \frac{dx}{\sqrt{ax^2 + bx + c}} = \frac{1}{\sqrt{a}} \ln \left| 2ax + b + 2\sqrt{a}\sqrt{ax^2 + bx + c} \right| + C$$

74.
$$\int \sqrt{ax^2 + bx + c} dx = \frac{2ax + b}{4a} \sqrt{ax^2 + bx + c}$$

$$+\frac{4ac-\frac{2}{b}}{8\sqrt{a^3}}\ln 2x + b + 2\sqrt{a}\sqrt{\frac{2}{a}x + bx}$$
 c+ C

75.
$$\int \frac{x}{\sqrt{ax^2 + bx + c}} dx = \frac{1}{a} \sqrt{ax^2 + bx + c}$$

$$-\frac{b}{2\sqrt{a^3}} \ln |a| x + b + 2 a |a| |a| x + b x | c+ C$$

76.
$$\int \frac{dx}{\sqrt{c + bx - ax^2}} = -\frac{1}{\sqrt{a}} \arcsin \frac{2ax - b}{\sqrt{b^2 + 4ac}} + C$$

77.
$$\int \sqrt{c + bx - ax^2} dx = \frac{2ax - b}{4a} \sqrt{c + bx - ax^2} + \frac{b^2 + 4ac}{8\sqrt{a^3}} \arcsin \frac{2ax - b}{\sqrt{b^2 + 4ac}} + C$$

78.
$$\int \frac{x}{\sqrt{c + bx - ax^2}} dx = -\frac{1}{a} \sqrt{c + bx - ax^2} + \frac{b}{2\sqrt{a^3}} \arcsin \frac{2ax - b}{\sqrt{b^2 + 4ac}} + C$$

(十)含有
$$\sqrt{\pm \frac{x-a}{x-b}}$$
 或 $\sqrt{(x-a)(b-x)}$ 的积分

79.
$$\int \sqrt{\frac{x-a}{x-b}} dx = (x-b)\sqrt{\frac{x-a}{x-b}} + (b-a)\ln(\sqrt{|x-a|} + \sqrt{|x-b|}) + C$$

80.
$$\int \sqrt{\frac{x-a}{b-x}} dx = (x-b)\sqrt{\frac{x-a}{b-x}} + (b-a)\arcsin\sqrt{\frac{x-a}{b-x}} + C$$

81.
$$\int \frac{dx}{\sqrt{(x-a)(b-x)}} = 2\arcsin\sqrt{\frac{x-a}{b-x}} + C \quad (a < b)$$

(十一)含有三角函数的积分

83.
$$\int \sin x dx = -\cos x + C$$

84.
$$\int \cos x dx = \sin x + C$$

85 .
$$\int \tan x dx = -\ln |\cos x| + C$$

86.
$$\int \cot x dx = \ln |\sin x| + C$$

87.
$$\int \sec x dx = \ln \left| \tan \left(\frac{\pi}{4} + \frac{x}{2} \right) \right| + C = \ln \left| \sec x + \tan x \right| + C$$

88.
$$\int \csc x dx = \ln \left| \tan \frac{x}{2} \right| + C = \ln \left| \csc x - \cot x \right| + C$$

89 .
$$\int \sec^2 x dx = \tan x + C$$

90.
$$\left[\csc^2 x dx = -\cot x + C\right]$$

91.
$$\int \sec x \tan x dx = \sec x + C$$

92.
$$\int \csc x \cot x dx = -\csc x + C$$

93.
$$\int \sin^2 x dx = \frac{x}{2} - \frac{1}{4} \sin 2x + C$$

94.
$$\int \cos^2 x dx = \frac{x}{2} + \frac{1}{4} \sin 2x + C$$

95.
$$\int \sin^n x dx = -\frac{1}{n} \sin^{n-1} x \cos x + \frac{n-1}{n} \int \sin^{n-2} x dx$$

96.
$$\int \cos^n x dx = \frac{1}{n} \cos^{n-4} x \sin x + \frac{n-1}{n} \int \cos^{n-2} x dx$$

97.
$$\int \frac{dx}{\sin^n x} = -\frac{1}{n-1} \cdot \frac{\cos x}{\sin^{n-1} x} + \frac{n-2}{n-1} \int \frac{dx}{\sin^{n-2} x}$$

98.
$$\int \frac{dx}{\cos^n x} = \frac{1}{n-1} \cdot \frac{\sin x}{\cos^{n-4} x} + \frac{n-2}{n-1} \int \frac{dx}{\cos^{n-2} x}$$

99.
$$\int \cos^m x \sin^n x dx = \frac{1}{m+n} \cos^{m+1} x \sin^{n+1} x + \frac{m-1}{m+n} \int \cos^{m-2} x \sin^n x dx$$
$$= -\frac{1}{m+n} \cos^{m+1} x \sin^{n+1} x + \frac{n-1}{m+n} \int \cos^m x \sin^{n-2} x dx$$

100.
$$\int \sin ax \cos bx dx = -\frac{1}{2(a+b)} \cos(a+b)x - \frac{1}{2(a-b)} \cos(a-b)x + C$$

101.
$$\int \sin ax \sin bx dx = -\frac{1}{2(a+b)} \sin(a+b) x + \frac{1}{2(a-b)} \sin(a-b) x + C$$

102.
$$\int \cos ax \cos bx dx = \frac{1}{2(a+b)} \sin(a+b)x + \frac{1}{2(a-b)} \sin(a-b)x + C$$

103.
$$\int \frac{dx}{a + b \sin x} = \frac{2}{\sqrt{a^2 - b^2}} \arctan \frac{a \tan \frac{x}{2} + b}{\sqrt{a^2 - b^2}} + C \quad (a^2 > b^2)$$

105.
$$\int \frac{dx}{a + b \cos x} = \frac{2}{a + b} \sqrt{\frac{a + b}{a - b}} \arctan(\sqrt{\frac{a - b}{a + b}} \tan \frac{x}{2}) + C \quad (a^2 > b^2)$$

107.
$$\int \frac{dx}{a^2 \cos^2 x + b^2 \sin^2 x} = \frac{1}{ab} \arctan(\frac{b}{a} \tan x) + C$$

108.
$$\int \frac{dx}{a^2 \cos^2 x - b^2 \sin^2 x} = \frac{1}{2ab} \ln \left| \frac{b \tan x + a}{b \tan x - a} \right| + C$$

109.
$$\int x \sin ax dx = \frac{1}{a^2} \sin ax - \frac{1}{a} x \cos ax + C$$

110.
$$\int x^2 \sin ax dx = -\frac{1}{a}x^2 \cos ax + \frac{2}{a^2}x \sin ax + \frac{2}{a^3}\cos ax + C$$

111.
$$\int x \cos ax dx = \frac{1}{a^2} \cos ax + \frac{1}{a} x \sin ax + C$$

112.
$$\int x^2 \cos ax dx = \frac{1}{a} x^2 \sin ax + \frac{2}{a^2} x \cos ax - \frac{2}{a^3} \sin ax + C$$

113.
$$\int \arcsin \frac{x}{a} dx = x \arcsin \frac{x}{a} + \sqrt{a^2 - x^2} + C$$

114.
$$\int x \arcsin \frac{x}{a} dx = (\frac{x^2}{2} - \frac{a^2}{4}) \arcsin \frac{x}{a} + \frac{x}{4} \sqrt{a^2 - x^2} + C$$

115.
$$\int x^2 \arcsin \frac{x}{a} dx = \frac{x^3}{3} \arcsin \frac{x}{a} + \frac{1}{9} (x^2 + 2a^2) \sqrt{a^2 - x^2} + C$$

116.
$$\int \arccos \frac{x}{a} dx = x \arccos \frac{x}{a} - \sqrt{a^2 - x^2} + C$$

117.
$$\int x \arccos \frac{x}{a} dx = (\frac{x^2}{2} - \frac{a^2}{4}) \arccos \frac{x}{a} - \frac{x}{4} \sqrt{a^2 - x^2} + C$$

118.
$$\int x^2 \arccos \frac{x}{a} dx = \frac{x^3}{3} \arccos \frac{x}{a} - \frac{1}{9} (x^2 + 2a^2) \sqrt{a^2 - x^2} + C$$

119.
$$\int \arctan \frac{x}{a} dx = x \arctan \frac{x}{a} - \frac{a}{2} \ln(a^2 + x^2) + C$$

120.
$$\int x \arctan \frac{x}{a} dx = \frac{1}{2} (a^2 + x^2) \arctan \frac{x}{a} - \frac{a}{2} x + C$$

121.
$$\int x^2 \arctan \frac{x}{a} dx = \frac{x^3}{3} \arctan \frac{x}{a} - \frac{a}{6} x^2 + \frac{a^3}{6} \ln(a^2 + x^2) + C$$

(十三)含有指数函数的积分

122.
$$\int a^{x} dx = \frac{1}{\ln a} a^{x} + C$$

123.
$$\int e^{ax} dx = \frac{1}{a} e^{ax} + C$$

124.
$$\int xe^{ax} dx = \frac{1}{a^2} (ax - 1)e^{ax} + C$$

125.
$$\int x^n e^{ax} dx = \frac{1}{a} x^n e^{ax} - \frac{n}{a} \int x^{n-1} e^{ax} dx$$

126.
$$\int xa^{x}dx = \frac{x}{\ln a}a^{x} - \frac{1}{(\ln a)^{2}}a^{x} + C$$

127.
$$\int x^n a^x dx = \frac{1}{\ln a} x^n a^x - \frac{n}{\ln a} \int x^{n-4} a^x dx$$

128.
$$\int e^{ax} \sin bx dx = \frac{1}{a^2 + b^2} e^{ax} (a \sin bx - b \cos bx) + C$$

129.
$$\int e^{ax} \cos bx dx = \frac{1}{a^2 + b^2} e^{ax} (b \sin bx + a \cos bx) + C$$

(十四)含有对数函数的积分

132.
$$\int \ln x dx = x \ln x - x + C$$

133.
$$\int \frac{dx}{x \ln x} = \ln |\ln x| + C$$

134.
$$\int x^n \ln x dx = \frac{1}{n+1} x^{n+1} (\ln x - \frac{1}{n+1}) + C$$

135.
$$\int (\ln x)^n dx = x(\ln x)^n - n \int (\ln x)^{n-1} dx$$

136.
$$\int x^{m} (\ln x)^{n} dx = \frac{1}{m+1} x^{m+1} (\ln x)^{n} - \frac{n}{m+1} \int x^{m} (\ln x)^{n-1} dx$$

(十五)含有双曲函数的积分

137.
$$\int shxdx = chx + C$$

138.
$$\int chxdx = shx + C$$

139 .
$$\int thxdx = \ln chx + C$$

140.
$$\int sh^2 x dx = -\frac{x}{2} + \frac{1}{4} sh2x + C$$

141.
$$\int ch^2 x dx = \frac{x}{2} + \frac{1}{4} sh2x + C$$

(十六)定积分

142.
$$\int_{-\pi}^{\pi} \cos nx dx = \int_{-\pi}^{\pi} \sin nx dx = 0$$

143.
$$\int_{-\pi}^{\pi} \cos mx \sin nx dx = 0$$

144.
$$\int_{-\pi}^{\pi} \cos mx \cos nx dx = \begin{cases} 0, & m \neq n \\ \pi, & m = n \end{cases}$$

成功是必须的

145.
$$\int_{-\pi}^{\pi} \sin mx \sin nx dx = \begin{cases} 0, & m \neq n \\ \pi, & m = n \end{cases}$$

146.
$$\int_0^{\pi} \sin mx \sin nx dx = \int_0^{\pi} \cos mx \cos nx dx = \begin{cases} 0, & m \neq n \\ \frac{\pi}{2}, & m = n \end{cases}$$

147.
$$I_n = \int_0^{\pi} \sin^n x dx = \int_0^{\pi} \cos^n x dx$$

$$I_n = \frac{n-1}{n} I_{n-2}$$

$$I_n = \frac{n-1}{n} \cdot \frac{n-3}{n-2} \cdot \prod_{n=1}^{\infty} \frac{4-2}{5-3} \quad (n为大于 1的正奇数), I_1 = 1$$

$$I_n = \frac{n-1}{n} \cdot \frac{n-3}{n-2} \cdot \prod_{n=2}^{\infty} \frac{3}{4} \cdot \frac{1}{2} \cdot \frac{\pi}{2} \quad (n为正偶数), I_0 = \frac{\pi}{2}$$