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May 24, 2016

0.0.1 Asymptotic Notation

Fact:
$$f(n) \in o(g(n)) \iff \lim_{n \to \infty} f(n)/g(n) = 0$$

 $\omega \iff = \infty$
 $\Theta \iff = C \neq \infty, 0$
Use L'Hopital's Rule.
Useful: $a^{\log_b n} = n^{\log_b a}$

 $\begin{array}{l} \sum i = \Theta(n^2) \text{ (arithmetic series)} \\ \sum c^i = \Theta(c^n) \text{ (geometric series)} \\ \sum 1/i = \Theta(\log n) \text{ (harmonic series)} \\ \log(n!) = n\log n - \Theta(n) \text{ (harmonic series)} \text{ (Stirling formula)} \\ \Theta(\sum \log(n/i)) = \Theta(\sum (\log n - \log i)) = \Theta(n\log n - (n\log n - \Theta(n))) = \Theta(n) \\ T(n) = 2T(n/2) + n^2 = \Theta(N^2) \end{array}$