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1 Greedy Algorithms

In [6]: $\# O(N \log N)$

Each step, choose the best local max. Fast, but proof of global optimum is often hard.

1.1 Disjoint Interval (Activity Selection)

Given a set of intervals, find largest set of disjoint intervals.

def disjoint_1(intervals):

```
intervals.sort(key=lambda (left, right):right)
biggest_so_far = None
answers = []
for (l, r) in intervals:
    if biggest_so_far is None or biggest_so_far <= l:
        answers.append((l, r))
        biggest_so_far = r
return answers</pre>
```

In [5]: assert disjoint_1([(1, 2), (3, 4), (2, 3), (1, 3)]) == [(1, 2), (2, 3), (3,

Proof of correctness: suppose we choose a sequence $a_1...a_n$, but there's a longer length sequence $b_1...b_m$, m > n. We know that $b_{1R} > a_{1R}$ by the selection algorithm. Then $a_1b_2...b_m$ is still optimal and disjoint. Then we compare a_2 with b_2 , a_3 with b_3 , etc. But then b_{n+1} should be choosable by the selection algorithm, and thus a contradiction so we know our algorithm is optimal.