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0.0.1 Asymptotic Notation

$$\begin{array}{l} \text{Fact: } f(n) \in o(g(n)) \iff \lim_{n \to \infty} f(n)/g(n) = 0 \\ \omega \iff = \infty \\ \Theta \iff = C \neq \infty, 0 \\ \text{Use L'Hopital's Rule.} \\ \text{Useful: } a^{\log_b n} = n^{\log_b a} \end{array}$$

 $\begin{array}{l} \sum i = \Theta(n^2) \text{ (arithmetic series)} \\ \sum c^i = \Theta(c^n) \text{ (geometric series)} \\ \sum 1/i = \Theta(\log n) \text{ (harmonic series)} \\ \log(n!) = n\log n - \Theta(n) \text{ (harmonic series)} \text{ (Stirling formula)} \\ \Theta(\sum \log(n/i)) = \Theta(\sum (\log n - \log i)) = \Theta(n\log n - (n\log n - \Theta(n))) = \Theta(n) \\ T(n) = 2T(n/2) + n^2 = \Theta(N^2) \end{array}$