

$$\begin{aligned}
P(x; \mu, \sigma^2) &= \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x-\mu)^2}{2\sigma^2}} \\
&= \frac{1}{\sqrt{2\pi}} \frac{1}{\sigma} e^{-\frac{(x-\mu)^2}{2\sigma^2}} \\
&= \frac{1}{\sqrt{2\pi}} e^{\ln \frac{1}{\sigma}} e^{-\frac{(x-\mu)^2}{2\sigma^2}} \\
&= \frac{1}{\sqrt{2\pi}} e^{-\ln(\sigma) - \frac{(x-\mu)^2}{2\sigma^2}} \\
&= \frac{1}{\sqrt{2\pi}} e^{-\frac{x^2}{2\sigma^2} + \frac{\mu x}{\sigma^2} - \frac{\mu^2}{2\sigma^2} + \ln(\frac{1}{\sigma})} \\
&= \frac{1}{\sqrt{2\pi}} e^{\begin{bmatrix} \frac{\mu}{\sigma^2} & -\frac{1}{2\sigma^2} \end{bmatrix} \begin{bmatrix} x & x^2 \end{bmatrix}^T - \left(\frac{\mu^2}{2\sigma^2} + \ln \sigma \right)}
\end{aligned}$$

For

$$P(x; \mu, \sigma^2) = \frac{1}{\sqrt{2\pi}} e^{\begin{bmatrix} \frac{\mu}{\sigma^2} & -\frac{1}{2\sigma^2} \end{bmatrix} \begin{bmatrix} x & x^2 \end{bmatrix}^T - \left(\frac{\mu^2}{2\sigma^2} + \ln \sigma \right)} \quad (1)$$

In Eq 1, counting measure is $1/\sqrt{2\pi}$, natural parameter η is $\begin{bmatrix} \frac{\mu}{\sigma^2} & -\frac{1}{2\sigma^2} \end{bmatrix}$, sufficient statistics $t(x)$ are $\begin{bmatrix} x & x^2 \end{bmatrix}$, $a(\eta)$ is $\left(\frac{\mu^2}{2\sigma^2} + \ln \sigma \right)$.

$$\begin{aligned}
\eta_1 &= \frac{\mu}{\sigma^2} \\
\eta_2 &= -\frac{1}{2\sigma^2}
\end{aligned}$$

Thus,

$$\mu = \frac{\eta_1}{-2\eta_2}$$

And,

$$\begin{aligned}
a(\eta) &= \left[\frac{\left(\frac{\eta_1}{2\eta_2} \right)^2}{2 \left(\frac{1}{-2\eta_2} \right)^2} + \ln \sqrt{\frac{1}{-2\eta_2}} \right] = -\frac{1}{2} \eta_1^2 \frac{1}{2\eta_2} - \frac{1}{2} \ln(-2\eta_2) \\
&= \frac{\eta_1^2}{4\eta_2} - \frac{1}{2} \ln(-2\eta_2)
\end{aligned}$$