Kähler reduction by a complex Lie group

Shing Tak Lam

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Let M a Kähler manifold, G a compact Lie group acting on M, with

1. G acting on M in a Hamiltonian way, with moment map $\mu : M \to \mathfrak{g}^*$,

2. G acting on M isometrically.

3. G acting freely on $\mu^{-1}(0)$.

Then we have that $\mu^{-1}(0)/G$ is a Kähler manifold. Suppose $G^{\mathbb{C}}$ is a complexification of G.