Does Skill Abundance Still Matter? The Evolution of Comparative Advantage in the 21st Century*

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Abstract

This paper documents that skill-abundant countries no longer have a comparative advantage in skill-intensive sectors. While this empirical relationship was strong in the 1980s, it weakened in the 1990s and disappeared by the 2000s. The decline is only evident in countries and sectors with high automation, with the presence of offshoring not being a significant driver of the decline. Using a quantitative trade model incorporating both automation and offshoring, I confirm that observed changes in automation can account for the evolution of comparative advantage while observed changes in offshoring cannot. Through the lens of the same model, automation increases skill premia in high-automation, developed countries and increases welfare globally, while offshoring has smaller, more evenly distributed welfare gains.

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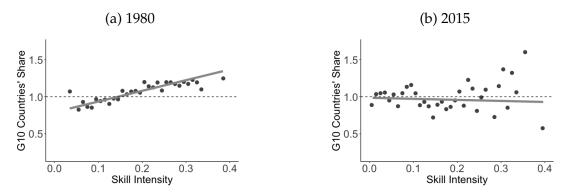
1 Introduction

One of the most influential ideas in international economics is the idea, developed by Eli Heckscher and Bertil Ohlin and later formalized by Paul Samuelson, that a country's skill abundance may shape its pattern of comparative advantage in skill-intensive sectors. Throughout the 20th century, it has played a central role in shaping classic debates about from the origins of growth miracles (Young, 1995; Ventura, 1997) to the relationship between globalization, technology, and inequality (Krugman, 1979; Leamer, 1984; Wood, 1994; Bernard et al., 1995). Did the emergence of China and other developing countries make the previous force more salient? Or, does the 21st century bring new technologies, such as automation, that reverse the previous patterns and make them less relevant?

In the first half of the paper, I document that skill-abundant countries no longer have a comparative advantage in skill-intensive sectors. Figure 1 shows this new fact in a parsimonious way. I plot the revealed comparative advantage of the G10 countries against the skill intensity of different products, where the revealed comparative advantage is defined as the G10's export share out of world export in each sector divided by their export share in all sectors, and the skill intensity is defined as the share of non-production worker's payroll share in valued added in the US data. Since G10 countries are skill-abundant, one may expect these countries to have relatively lower costs and, in turn, relatively higher exports in skill-intensive sectors. Panel 1a shows that this indeed is the case in 1980. By 2015, however, the relationship has entirely disappeared. Using a more systematic specification, I show that while this empirical relationship was present (Romalis, 2004; Morrow, 2010; Chor, 2010), it weakened in the 1990s and disappeared by the 2000s. In addition, I show that the importance of skill abundance in comparative advantage only disappeared in countries and sectors exposed to high automation.

In the second half of the paper, I develop a multi-sector, multi-factor trade model, in which both automation and offshoring affect the costs of production and, in turn, the relationship between the country's skill abundance and its exports in skill-intensive sectors. Using structural accounting exercises, I find that automation is the most plausible explanation for the evolution of comparative advantage in the last few decades. Through the lens of the same model, automation increases skill premia only in developed countries with high automation and increases in welfare in all countries. In contrast, offshoring leads to smaller, more equally distributed increases in skill premia and welfare in all countries.

Figure 1: G10's Export Shares in Skill-Intensive Sectors (Relative to Shares in All Sectors)



Notes: The figures show binned scatterplots of a G10's share of global exports in each sector divided by its share of aggregate global exports across 397 four-digit sectors with different skill intensities. The skill intensity is the shares of non-production workers' payroll in value-added in the US data. See Appendix B for the details.

Does Skill Abundance Still Matter? Expanding on the findings in Figure 1, Section 2 examines the importance of the country's skill abundance for comparative advantage in skill-intensive sectors in a more systematic manner. For every five years from 1980 to 2015, I regress bilateral trade flows at the exporter-importer-sector level on the interaction of an exporter's characteristics, skill abundance, and sector's characteristics, skill intensity. I control exporter-importer and importer-sector fixed effects. This specification follows the literature to reveal comparative advantage using bilateral trade flow data, relying on a multi-sector Eaton-Kortum model, such as Chor (2010), Costinot et al. (2012), and Levchenko and Zhang (2016). The fixed effects control trade pattern determinants specific to exporter-importer pairs, such as distances or trade agreements, as well as those specific to importer-sector pairs, such as tariffs or expenditure shares. My main variable of interest is the interaction of an exporter's skill abundance and a sector's skill intensity. If the coefficient of this interaction is positive, skill-abundant countries have a comparative advantage in skill-intensive sectors.

I find that, until the 1990s, skill-abundant countries used to specialize in skill-intensive sectors. This aligns with the papers that have found a positive coefficient and interpreted it as supportive of the Heckscher-Ohlin Theory (Romalis, 2004; Morrow, 2010; Chor, 2010). The novel finding is that the importance of skill abundance in comparative advantage weakened over time and eventually disappeared post-2000. This empirical finding is robust across the range of the specifications previously used in the literature, the measures of countries' skill abundance and sectors' skill intensity in 1980 for entire periods, or the data sources for trade flow.

A First Look at Mechanisms. Automation and offshoring have been two major technological trends in recent decades. Both of these trends have the potential to undo the relationship between a country's skill abundance and a sector's skill intensity in trade patterns because they substitute low-skill workers with machines or foreign intermediates, thus potentially reducing the role of domestic low-skill workers in production (Grossman and Rossi-Hansberg, 2008; Acemoglu and Restrepo, 2022b). They may also blur the mapping from skill abundance to relative costs across sectors with different skill intensities.

Section 3 empirically investigates these two specific channels—the rise of automation and offshoring—, as potential mechanisms behind the decline in the skill-abundance-driven comparative advantage. Using data on robot adoption, intermediate imports, and factor payment shares, I construct measures of automation share, the share of factor payment to machines, and offshoring shares, the share of foreign intermediates in total intermediates, by country, sector, and year. I then examine the heterogeneity in changes in comparative advantage across countries and sectors. My specifications allow the importance of skill abundance in comparative advantage to vary with the automation or offshoring shares.

First, the decline in the importance of a country's skill abundance in comparative advantage in a skill-intensive sector is more pronounced among countries and sectors with higher levels of automation, such as the automobile sectors in Germany and Japan. Second, among countries and sectors where automation levels are below the global median, such as the textile sectors in developing countries, skill abundance remains as important in 2015 as it was in the 1990s. Finally, there is little heterogeneity of the decline across countries and sectors with different degrees of offshoring and, what heterogeneity there suggests is that offshoring has strengthened, not weakened, the mapping from skill abundance to comparative advantage.

Theoretical Framework. The heterogeneity in Section 3 is qualitatively consistent with the story that automation, rather than offshoring, causes the decline in the importance of skill abundance in comparative advantage. In Section 4, I develop a model to clarify and quantify the effect of automation and offshoring on the evolution of comparative advantage. In particular, I develop a multi-sector, multi-factor Eaton-Kortum model that incorporates a task framework for automation (Acemoglu and Restrepo, 2022b) and offshoring (Grossman and Rossi-Hansberg, 2008).

¹The automobile sector is not skill-intensive. For example, the share of payroll allocated to skilled labor as a percentage of value added was 8%, placing it around the bottom 10 percentile in 1980, based on the Japanese Census of Manufacturers. The same is true for the US, where the share of payroll allocated to skilled labor as a percentage of value added was 11%, placing it around the bottom 25 percentile in 1980, based on the NBER CES Manufacturing Database.

In the model, exogenous increases in automation and offshoring decrease demand for low-skill labor given output, reducing the importance of the country's skill abundance in the unit cost function. Intuitively, this task displacement makes low-skill-scarce countries, such as Germany or Japan, remain competitive in low-skill-intensive sectors. For example, Germany automates or offshores its production processes in the automobile sector, allowing it to use machines or foreign intermediates instead of relying on its scarce production workers. This shift in production technology enables Germany to gain a comparative advantage in the automobile sector, making it harder for countries like Vietnam or Malaysia to compete even with their abundant production workers.

Quantitative Relevance. Using the model developed in Section 4, Section 5 quantifies the roles of automation and offshoring in the evolution of comparative advantage. To do so, I first calibrate the model to the economy in 1995 and simulate the model under three counterfactual scenarios, using the exact hat algebra (Dekle et al., 2008). Using the automation and offshoring shares constructed in Section 3, I consider the following three counterfactual scenarios: (a) only automation shares change from 1995 to 2008, (b) only offshoring shares change from 1995 to 2008, and (c) only automation and offshoring share change from 1995 to 2008. Other parameters, such as trade costs or final goods sectoral expenditure shares, are held constant at their levels in 1995.

Then, I run the same regression as in Section 2 using the model-generated data for each counterfactual scenario and compare the coefficients for the importance of skill abundance to those obtained from the actual data.

My key finding is that the model, incorporating both automation and offshoring shocks, can explain around 90% of the declines in the importance of skill abundance for comparative advantage observed in the data as found in Section 2. Furthermore, I find that automation, rather than offshoring, is the primary driver behind the decline. Specifically, without the advancements in automation since 1995, skill abundance would have remained important for comparative advantage in 2008.

Macro Implications. Having quantified the roles of automation and offshoring in the evolution of comparative advantage, I explore their macroeconomic implications beyond changes in export patterns, such as manufacturing shares, skill premia, and welfare across countries. To do so, I the model under the three counterfactual scenarios and examine the macroeconomic implications.

²My initial year is 1995 because the World Input-Output Database with multiple labor types, which I use, is only available from 1995.

First, I show that automation shifts tasks from low-skilled labor worldwide to high-skilled labor in high-income countries. This shift relocates manufacturing production from low-automation countries to high-automation, high-income countries. As a result, skill premia increase in high-automation countries, while they decrease in low-automation countries. Skill premia decrease in low-automation countries because they start to specialize in more low-skill intensive sectors, increasing demand for low-skill labor. The welfare effects are positive across all countries but are more pronounced in high-automation countries, such as Germany and Japan.

I further highlight that the impact of automation on skill premia and welfare depends on changes in comparative advantage. When trade elasticity is low, resulting in limited sectoral reallocation, skill premia rise in all countries because low-automation, skill-scarce countries do not specialize much in low-skill-intensive sectors. Additionally, the welfare effects become smaller across all countries due to reduced specialization. This implies that incorporating changes in comparative advantage and sectoral reallocation is crucial when analyzing the effects of automation on skill premia and welfare.

Second, I demonstrate that offshoring shifts tasks from low-skilled labor in skill-abundant countries to low-skilled labor in skill-scarce countries. The effects of offshoring on the manufacturing shares, skill premia, and welfare are smaller and more equally spread across countries compared to automation. This is because offshoring tends to occur more uniformly across countries.

Literature. First, this paper contributes to the large literature that empirically investigates the sources of comparative advantage (Leamer, 1984; Bowen et al., 1987; Trefler, 1993, 1995; Davis and Weinstein, 2001; Romalis, 2004; Schott, 2004; Nunn, 2007; Levchenko, 2007; Costinot, 2009; Morrow, 2010; Chor, 2010; Costinot et al., 2012; Davis and Dingel, 2020). These papers stress the importance of the Ricardian or Heckscher-Ohlin sources of comparative advantage before or in 2000, and almost none study how comparative advantage evolves over time.³ My paper offers a new fact that a country's skill abundance has become less important in comparative advantage in skill-intensive sectors over time and no longer matters after 2000. My paper also shows that automation is the most plausible explanation for this decline in the importance of a country's skill abundance.

³Some exceptions are Hanson et al. (2015) and Levchenko and Zhang (2016), which find the mean reversion or convergence of comparative advantage over time. My results show that the pattern of comparative advantage has not changed much for countries and sectors with lower levels of automation. Thus, unless mean reversion is systematically correlated with automation, it cannot explain my empirical facts entirely, and my results are complementary to the findings in Hanson et al. (2015) and Levchenko and Zhang (2016). Another related stream of the literature focusing on the changes in comparative advantage is the theoretical literature that studies endogenous comparative advantage, including Redding (1999).

Second, this paper contributes to the large literature on the interaction between trade and technology, pioneered by Krugman (1979) and Grossman and Helpman (1991). More specifically, my paper relates to the papers that embed high- and low-skilled labor into multi-sector quantitative trade models (Parro, 2013; Burstein et al., 2013; Caron et al., 2014; Burstein and Vogel, 2017; Burstein et al., 2019; Morrow and Trefler, 2022; Furusawa et al., 2022). Most of them are concerned with the implications of trade cost reduction or skill-biased technology on the skill premium. While I demonstrate the implications of changes in trade and technology for skill premium as well, my main focus is on the changes in trade patterns over time.

The closest paper is Morrow and Trefler (2022), which provide a model-based decomposition of how the differences in skill abundance across countries are absorbed into different factors. They find that within-industry skill intensities are more important than between-industry output mixes in 2006. I empirically confirm this and also highlight that the relationship between skill abundance and skill intensity was important before 2000. Moreover, my empirical and quantitative results suggest that automation is a plausible explanation for why differences in within-industry skill intensities across countries are important.

2 Skill Abundance as a Source of Comparative Advantage?

In this section, I examine how the interaction between skill abundance across countries and skill intensity across sectors shapes comparative advantages from 1980 to 2015.

2.1 Baseline Specification

Theoretical Motivation To motivate the regression that reveals the comparative advantage of countries across sectors with different skill intensities, I provide a quick review of a multi-sector Eaton Kortum (Eaton and Kortum, 2002) model, following Chor (2010) and Costinot et al. (2012).

Suppose that bilateral exports from i to j in sector s can be expressed as

$$X_{i,j,s} = \frac{(c_{i,s}\tau_{i,j,s})^{-\theta}}{\sum_{l}(c_{l,s}\tau_{l,j,s})^{-\theta}}X_{j,s}$$
(1)

⁴There are also several theoretical papers discuss the roles of trade in the direction of technology, such as Wood (1994), Acemoglu and Zilibotti (2001), Acemoglu (2003), Thoenig and Verdier (2003), Epifani and Gancia (2008), and Loebbing (2022).

where $c_{i,s}$ is the unit production cost in country i in sector s, $\tau_{i,j,s}$ is the bilateral trade cost, $X_{i,s}$ is the total expenditure of country j in sector s, and $\theta > 0$ is the trade elasticity.

Following Costinot et al. (2012), assume that the trade cost takes the form of $\tau_{i,j,s} = \tau_{i,j} \cdot \tau_{j,s}$. The first part $\tau_{i,j}$ measures the trade costs specific to countries i and j, such as physical distance, use of common language, historical ties, or common membership in organizations. The second part $\tau_{j,s}$ measures the trade costs specific to destination j in sector s, such as tariffs imposed by country j on s.

Now, let's consider the unit production cost $c_{i,s}$, which takes the following form

$$c_{i,s} = (w_i^H)^{\alpha_s^H} (w_i^L)^{1-\alpha_s^H}$$

where w_i^H and w_i^L are wages of high-skill and low-skill workers, and α_s^H is the share of high-skill workers' payroll in value-added, which I call the sector's skill intensity.

Then, combining this unit cost function with equation (1) after taking the log, the bilateral trade flows can be written as follows:

$$\ln X_{i,j,s} = -\theta \ln \left(\alpha_s^H \times \ln \left(\frac{w_i^H}{w_i^L} \right) \right) + \eta_{i,j} + \eta_{j,s}, \tag{2}$$

where $\eta_{i,j}$ and $\eta_{j,s}$ are defined as follows:

$$\eta_{i,j} = - heta \ln w_i^L - heta \ln au_{i,j}, \quad \eta_{j,s} = - heta \ln au_{j,s} - \ln \left(\sum_l (c_{l,s} au_{l,j,s})^{- heta}
ight) + \ln X_{j,s}.$$

The specification (2) reveals the comparative advantage of countries with different relative skill premia, w_i^H/w_i^L , across sectors with different skill intensities, α_s^H . In particular, a country with a lower skill premium has higher exports in a sector with higher skill intensity, which is the classic prediction of the Factor Proportions Theory.

In a typical cross-country dataset, it is rare to observe skill prices. Thus, the previous studies in the literature (Romalis, 2004; Chor, 2010) use the relative skill abundance H_i/L_i , instead of skill premia, w_i^H/w_i^L and assume the negative correlation,

$$\operatorname{Corr}\left(\ln(H_i/L_i), \ln(w_i^H/w_i^L)\right) < 0.$$

This negative correlation means that skill-abundant countries have lower skill premia.

Then, the specification (2) becomes as follows:

$$\ln X_{i,j,s} = \beta_i \ln \left(\alpha_s^H \times \ln \left(\frac{H_i}{L_i} \right) \right) + \eta_{i,j} + \eta_{j,s}, \tag{3}$$

where

$$\beta_i = -\theta \cdot \frac{\operatorname{Cov}\left(\ln(H_i/L_i), \ln(w_i^H/w_i^L)\right)}{\operatorname{Var}\left(\ln(H_i/L_i)\right)} > 0.$$

This is the standard specification to reveal comparative advantage of countries with different relative skill abundance, H_i/L_i , across sectors with different skill intensities, α_s^H . We expect $\beta>0$ because skill-abundant (high H_i/L_i) countries have lower skill premia (low w_i^H/w_i^L) and thus lower unit costs and larger exports in skill-intensive (high α_s^H) sectors.⁵ As an illustration, compare two countries, the US and Bangladesh. Which country is relatively more efficient in producing high-skill-intensive goods, such as computers, than low-skill-intensive goods, such as clothes? We naturally expect that the US has a comparative advantage in more skill-intensive goods, in this case, computers. This is because producing computers requires designers or engineers with Ph.D. degrees and thus the computer sector has higher skill intensity α_s^H . This relationship between the country's skill abundance and the sectors' skill intensity means the US, with higher H_i/L_i , has lower unit production costs and larger exports in sectors with higher α_s^H , which implies that $\beta>0$.

2.2 Empirical Strategy

Building on the specification (3), my estimation equation takes as follows

$$X_{i,j,s,t} = \exp\left[\beta_t \left(\alpha_{s,t}^H \times \ln\left(\frac{H_{i,t}}{L_{i,t}}\right)\right) + \eta_{i,j,t} + \eta_{j,s,t}\right] + \varepsilon_{i,j,s,t},\tag{4}$$

where $X_{i,j,s,t}$ is the bilateral trade flow from country i to j in sector s at time t, $\alpha_{s,t}^H$ is the skill intensity in sector s at time t, $H_{i,t}$ and $H_{i,t}$ are the numbers of high-skilled workers and low-skilled workers in country i at time t, respectively, $\eta_{i,j,t}$ and $\eta_{j,s,t}$ are the origin-destination and destination-sector fixed effects, and $\theta_{i,j,s,t}$ is an error term. Following the literature standard, I use the exponential specification to adopt the Poisson Pseudo Maximum Likelihood (PPML) method following Silva and Tenreyro (2006) because the bilateral trade flows across sectors contain many zeros.

2.3 Data

My baseline empirical analysis uses bilateral trade flow data combined with sector-level factor intensity data and country-level factor endowment data.

⁵Note that the slope of the skill premium curve, Corr $(\ln(H_i/L_i), \ln(w_i^H/w_i^L))$, can be heterogeneous across countries. Thus, I keep the country index i in the coefficient β_i . In practice, if I run the bi-variate OLS, I will obtain the average of β_i across countries.

2.3.1 Data Sources

Bilateral Trade Flow The first main dataset is the bilateral trade flow data from the UN Comtrade data. The data contains annual imports and exports by detailed product code. I focus on manufacturing sectors because service trade data are available only after 2000. I convert SITC Rev.2 manufacturing products into US SIC 4-digit industry. I summarize the steps to construct the final dataset in Appendix A.

Factor Intensity The second main data is the factor intensity across sectors from the NBER-CES Manufacturing Industry Database (Becker et al., 2021).⁶ The data contains sector-level data on output, employment, and input costs. I compute factor payment shares of non-production workers out of total wage payments. This leads to skill intensity across 397 4-digit manufacturing sectors for each year.

Factor Endowment The third main data is factor endowment across countries from the Barro-Lee Educational Attainment Dataset (Barro and Lee, 2013), which is commonly used in the previous studies, including Hall and Jones (1999) and Romalis (2004). I construct a relative skill endowment, the ratio of college-educated people aged 25-64 relative to non-college-educated people aged 25-64.

2.3.2 Final Samples

Periods: Every 5 years 1980-2015 Since factor endowment data from the Barro-Lee Dataset are available only every five years, I use data from every 5 years from 1980 to 2015. This leaves me with 8 time periods in total. For the trade flow data, to eliminate fluctuations and to focus on long-run trends, I take a 3-year moving average around each year.

Countries: 52 countries First, I restrict samples of countries to those that have trade and factor endowment data covering all the periods from 1980 to 2015. Second, I restrict samples to those that have ever had imports and exports of more than 100 million USD (in 2015 value) at least once from 1980 to 2015 as in Atkin et al. (2021) to ensure that the

⁶I use the US data following the literature (Romalis, 2004; Nunn, 2007; Chor, 2010) because the results can be comparable with them and because the data are comparable across different periods within my paper. This is vital as my focus is on the changes in the coefficients over time.

⁷While the original data were up to 2010, the extended data to 2015, which I use, is available in their web page here.

smallest countries do not drive results. These restrictions led to 52 countries, and these 49 countries accounted for more than 98% of world exports in 1990.

Sectors: 397 sectors I use all 397 sectors (in the SIC 4 digits) available in the NBER-CES Manufacturing Industry Database (Becker et al., 2021).

2.4 Main Results: Declining Importance of Skills in Trade

2.4.1 Baseline Result

Figure 2 shows the estimates of β_t and its 95% confidence intervals based on heteroskedasticity robust standard errors clustered at the origin-sector level. The first finding is that the estimates had been positive until 1995. This means that the country-level skill endowments were the source of comparative advantage in skill-intensive sectors and that developing countries specialize in low-skill-intensive sectors. This result is consistent with the previous papers, which found that more skill-abundant countries specialize in skill-intensive sectors, including Chor (2010) using data of the 1980s, Romalis (2004), Levchenko (2007), and Nunn (2007) using data of the 1990s.

The second, and new, finding is that the estimates decreased over time and became insignificant by 1995. This suggests that skill abundance across countries has become less important for comparative advantage in skill-intensive sectors and is not as important as it used to be in 1980 to explain trade patterns.

2.4.2 Relationships to the Findings in the Previous Papers

While this paper is the first to show the evolution of comparative advantage over time by running the same specification (4) over time, several papers have used similar specifications at the cross-section level between the late 1980s and the late 1990s. Chor (2010) and Morrow (2010) find that skill abundance is important for comparative advantage in skill-intensive sectors in the late 1980s or the early 1990s, and Romalis (2004) shows it for the 1990s.

Relationships with Chor (2010). While the specification is almost identical to the one in Chor (2010), it is worthwhile to mention that there are two small differences. First, Chor (2010) did not partial out the origin-destination fixed effects and instead included several origin-destination (i, j) level variables, such as physical distance, common languages, or trade agreements, in the regression because the goal of Chor (2010) is to explore broader

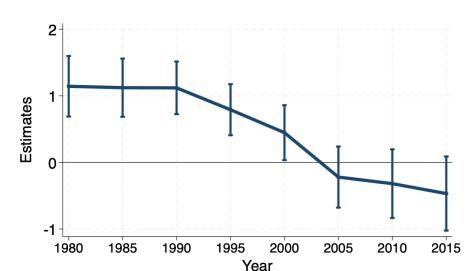


Figure 2: Estimates of Importance of Skill Abundance in Comparative Advantage

Note: The figures show the estimates of coefficients β_t in equation (4) in each point time separately. The bars indicate 95% confidence intervals based on heteroskedasticity-robust standard errors, clustered at the origin-sector level.

sources of comparative advantage. My specification of Equation (4) nonparametrically controls these origin-destination (i,j) level variables by the fixed effects, $\eta_{i,j,t}$, and focuses only on the variation at origin-sector (i,s) level. Second, Chor (2010) used the ratio of nonproduction workers in sector $\ln(H_s/L_s)$ instead of skill intensity α_s^H while Chor (2010) itself derives the specification and concludes that the right measure for the skill intensity is α_s^H . Nevertheless, the result is robust when I use the variable that Chor (2010) uses. Figure C.2 in Appendix C shows the result using the factor intensity definition of Chor (2010) and confirms that the coefficient decreases in the same manner. My results are consistent with their findings in these periods and, on top of it, provide the evolution of the relationship between the country's skill abundance and the sector's skill intensity over time.

Papers using Total Exports Other papers which adopted related specifications include Davis and Weinstein (2001), Romalis (2004), Nunn (2007), or Levchenko (2007). They ag-

⁸While the importance of skill abundance is not their main subject of interest, several papers report that skill abundance is one of the sources of comparative advantage along with the variables of their interests, including Nunn (2007) for the early 1990s, Levchenko (2007) for the 1990s, and Bombardini et al. (2012) for the 1990s.

⁹For Nunn (2007) and Levchenko (2007), the importance of skill abundance is not their main subject of interest. However, they include the interaction between the country's skill abundance and the sector's skill intensity as a covariate and show the importance of skill abundance in comparative advantage.

gregate bilateral trade flows to total exports at the origin-sector level and regress on different potential sources of comparative advantage. They also found that skill-abundant countries or regions have relatively larger exports in skill-intensive sectors at each point of time. Conceptually, their specifications and the specification in (4) are similar in that both focus on the variation at the origin-sector (i,s) level. Importantly, however, the specification (4) allows me to include the origin-destination fixed effects, $\eta_{i,j,t}$, and the destination-sector fixed effects, $\eta_{j,s,t}$. These fixed effects can isolate the effect of having neighborhood countries with particular sectoral preferences or policies. Nevertheless, the result is robust. Figure C.3 in Appendix C shows the result using the total exports at the origin-sector level as outcome variables as in Romalis (2004) and others and confirms that the coefficient decreases in the same manner.

2.4.3 Some Potential Explanations

Before exploring the potential hypotheses behind the decreases in β_t , I show that the finding is robust across different specifications and is inconsistent with some of the explanations. Figure 3 shows the results for various alternative specifications. All the panels show the same, decreasing trends over time.

Other Factor Endowments Figure 3a adds another term to consider capital intensity and capital endowment across countries as follows.

$$X_{i,j,s,t} = \exp\left[\beta_t \cdot \left(\alpha_{s,t}^H \times \ln\left(\frac{H_{i,t}}{L_{i,t}}\right)\right) + \beta_t^K \left(\alpha_{s,t}^K \times \ln\left(\frac{K_{i,t}}{L_{i,t}}\right)\right) + \eta_{i,j,t} + \eta_{j,s,t}\right] + \varepsilon_{i,j,s,t}, \quad (5)$$

Now, I use a value-added share of production labor for the skill intensity, $\alpha_{s,t}^H$, and a value-added share of capital for the capital intensity, $\alpha_{s,t}^K$. The data is from the NBER-CES Manufacturing Industry Database (Becker et al., 2021). To compute the capital to low-skilled labor ratio across countries, $K_{i,t}/L_{i,t}$, I use the real capital stock and employment Penn World Table (PWT) data from Feenstra et al. (2015) and combine it with the data from the Barro-Lee Dataset. Figure 3b further adds the interaction of the importance of institutions across sectors and rules of law across countries, following Nunn (2007). The patterns in Figure 3a and 3b are similar to the one in Figure 2 in that the skill becomes less important over the years and that the estimate has become insignificant after 2000.

¹⁰I divide real capital stock by the number of non-college-educated people, which is computed from employment in PWT multiplied by the share of non-college-educated people in the Barro-Lee Dataset.

Weights One concern is that some of the small countries drive the results and do not describe trade patterns in the world. Figure 3c weighs each observation by the total volumes of exports in each year at the country level. Nonetheless, the result has not changed.

Unobserved Heterogeneity at Aggregated Sectoral Level Figure 3d controls the fixed effects at the level of origin countries and 2-digit sectors. This specification controls unobserved heterogeneity at the level of origin countries and 2-digit sectors and focuses on the variations of skill intensity within 2-digit sectors. The pattern is still unaffected.

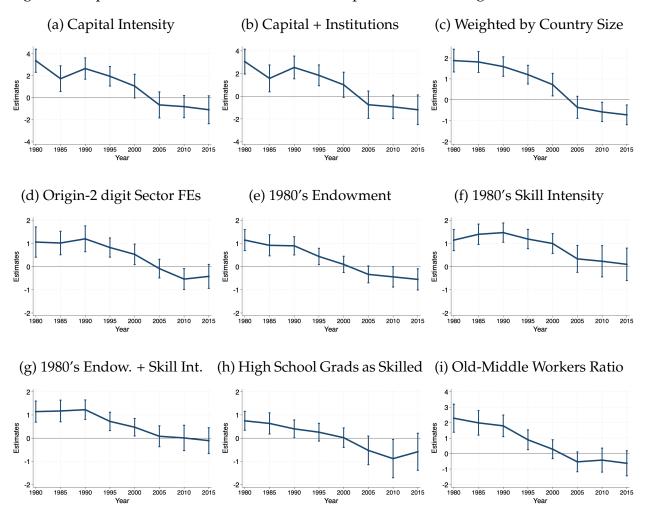
Fixing Factor Endowment and/or Intensity Data as of 1980 One may think that decreasing $\hat{\beta}_t$ can be just a result of increases in measurement errors in the running variable. For example, as the cohort size of the college-educated increases, unobserved heterogeneity, such as school quality, can become more heterogeneous within the college-educated. To address this concern, I fix the running variable, using data as of 1980, for all the sample years. Figure 3e uses factor endowments across countries in 1980 for the entire sample period. Figure 3f uses factor intensity across sectors in 1980 for the entire sample period. Figure 3g uses factor endowments across countries and factor intensity across sectors in 1980 for the entire sample period. Using 1980's skill intensity in Figure 3f and 3g widens the confidence intervals, but the patterns are still the same.

Alternative Skill Endowment Measures Figure 3h uses high school graduates to others for skilled to non-skilled labor ratio, using the same data source (Barro and Lee, 2013). Figure 3i uses the old-to-middle workers ratio for skilled to non-skilled labor ratio from Acemoglu and Restrepo (2022a). The time-series patterns hold with these alternative measures.

3 Potential Hypotheses: Heterogeneous Evolution by Automation and Offshoring

The result in Figure 2 suggests that skill endowments become less important as a source of comparative advantage. In this section, I explore the potential hypotheses behind this trend. In particular, I focus on two factors: automation and offshoring. I construct measures of automation and offshoring by countries, sectors, and years. I then examine the heterogeneity in changes in β_t , depending on the degrees of automation and sectors.

Figure 3: Importance of Skill Abundance in Comparative Advantage: Robustness Check



Notes: The figures show the estimates of coefficients β_t in equation (4) in each point time separately under various specifications. The bars indicate 95% confidence intervals based on heteroskedasticity-robust standard errors, clustered at the origin-sector level. Figure 3a adds the interaction of capital intensity and capital endowments as an additional control. Figure 3b further adds institution intensity and institution endowment terms as in Nunn (2007). Figure 3c weighs counties by total exports in each year. Figure 3d controls fixed effects at the level of a pair of the origin country and the 2-digit sector. Figure 3e replaces skill endowments in each year with those in 1980. Figure 3f replaces skill intensities in each year with those in 1980. Figure 3h replaces skill endowments based on college graduation with those based on high school graduates. Figure 3i replaces skill endowments with the old-to-middle worker's ratio in Acemoglu and Restrepo (2022a).

While I present a formal analysis in Section 4, I briefly explain why automation and offshoring can change the roles of skill endowments in trade patterns. Automation replaces production workers who complete routine tasks with machines. This task displacement allows firms to rely on machines instead of routine occupation workers, and domestic labor endowment can become less relevant for comparative advantage. Similarly, offshoring replaces domestic factors, including labor, with foreign factors. This displacement allows firms to rely on foreign factors, and domestic factor endowments will become less relevant for trade.

3.1 Trends in Automation and Offshoring

Before going into the analyses, I give a quick overview of the trends in automation and offshoring during the period. As Figure 4 shows, automation and offshoring have been rising since 1990. Figure 4a shows the robots per thousand industry workers from Acemoglu and Restrepo (2022a). The number of robots per thousand workers increased from 0.63 in 1993 to 3.47 in 2014 on average across all countries in my sample, but the increase was more pronounced among labor-scarce countries, such as Germany or South Korea. Figure 4b shows the share of imports in total intermediate uses from the World Input-Output Database (Timmer et al., 2015). The share of imports in intermediates, which I call offshoring share hereafter, increased from 40% in 1995 to 50% in 2011 on average across all countries, but the levels and the changes of offshoring shares are heterogeneous across countries. South Korea's offshoring share is stable at around 20% while Germany's offshoring share increased from 33% in 1995 to 50% in 2011. The US offshoring share also increased by 11% points, but the levels were still low at 26% in 2011.

3.2 Specifications for Heterogeneity

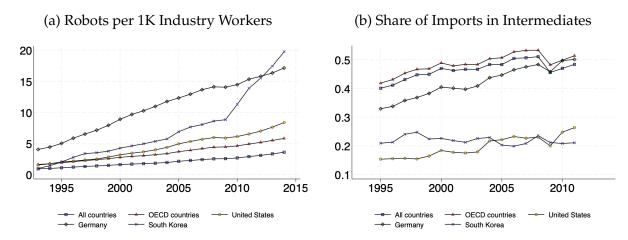
In this section, I allow the importance of skill abundance, β_t in equation (4), to depend on the degrees of automation and offshoring, $\beta_{i,s,t}$, for each country i and sector s as in the following specification.

$$X_{i,j,s,t} = \exp\left[\beta_{i,s,t} \cdot \left(\alpha_{s,t}^{H} \times \ln\left(\frac{H_{i,t}}{L_{i,t}}\right)\right) + \eta_{i,j,t} + \eta_{j,s,t}\right] + \varepsilon_{i,j,s,t},\tag{6}$$

To explore the heterogeneity, I adopt two specifications for the key parameter to estimate, $\beta_{i,s,t}$, that varies across countries and sectors.¹¹

¹¹Note that the analyses in this section only capture cross-sectional differences of the exposure to automa-

Figure 4: Automation and Offshoring



Notes: The figures show the trends in automation and offshoring. The left panel shows the number of robots per thousand industry workers from Acemoglu and Restrepo (2022a). The data is originally from the IFR (for robot data) and the ILO (for worker data). The right panel shows the share of imports in intermediates from the World Input-Output Database Release 2013 (Timmer et al., 2015).

Trend by Groups using Time-Invariant Dummy Variables The first specification defines high- and low-automation and high- and low-offshoring groups for countries and sectors and runs regressions where the coefficient $\beta_{i,s,t}$ depends on the dummy variables. In particular, we model $\beta_{i,s,t}$ in equation (6) as

$$\beta_{i,s,t} = \underbrace{\beta_t^0}_{\text{Base Group}} + \underbrace{\sum_{g \in G} \beta_t^g \cdot \mathbb{1}((i,s) \in g),}_{\text{Heterogeneous Trends}}$$
(7)

where *g* is a group of countries and sectors by the degree of automation and offshoring. Since we fix which group each country-sector pair belongs to over time, this specification reveals the differential trends by groups of the degrees of automation and offshoring.

I consider four dummies for groups, high-automation country, high-automation sector, high-offshoring country, and high-offshoring sector. For automation, I define a country as a high-automation country if the number of robot stocks in 2014 from the IFR data is above the median. I define each 4-digit sector as a high-automation sector if it falls into one of the following 2-digit broad sectors: Electronic & Other Electric Equipment sector, Transportation Equipment sector, and Plastic Chemical sectors as high-automation sec-

tion or offshoring and importantly, do not consider the general equilibrium effects, including the effects coming from changes in skill premia.

tors.¹² For offshoring, I define a country and a sector as a high-offshoring country or a high-offshoring sector if the increases in the offshoring shares from 1982 to 2017 are above the median. I compute the offshoring shares as the share of import in total intermediate uses, using the US BEA Input-Output Table and World Input-Output Database (WIOD) (Timmer et al., 2015), following Feenstra and Hanson (1996). In particular, I construct offshoring share by country, sector, and year as

$$\text{Offshoring Share}_{i,s,t} = \frac{\text{Imported Intermediates}_{i,t}}{\text{Total Intermediates}_{i,t}} \times \frac{\text{Imported Intermediates}_{US,s,t}}{\text{Total Intermediates}_{US,t}}$$

where Imported Intermediates $_{i,t}$ is the value of imported intermediates of country i in year t from the WIOD, Total Intermediates $_{i,t}$ is the value of total intermediate uses of country i in year t from the WIOD, Imported Intermediates $_{US,s,t}$ is the value of imported intermediates in the US in 4-digit sector s in year t from the US BEA Input-Output Table, and Total Intermediates $_{US,t}$ is the value of total intermediate uses in the US in year t from the US BEA Input-Output Table.

Trends and Levels using Time-Variant Continuous Variables The second specification constructs continuous measures of automation and offshoring across countries, sectors, and years. In particular, we model $\beta_{i,s,t}$ in equation (6) as

$$\beta_{i,s,t} = \beta^0 + \beta^1 \cdot t + \beta^{\text{Auto}} \text{Automation Share}_{i,s,t} + \beta^{\text{Ofs}} \text{Offshoring Share}_{i,s,t}.$$
 (8)

Automation Share i,s,t is the share of automation capital, such as machines and equipment, in country i, sector s, and year t, which is the factor payment share for automation capital to the sum of the payments for automation capital and low-skilled labor.

Automation Share_{i,s,t}
$$\equiv \frac{p_{i,s,t}^M M_{i,s,t}}{p_{i,s,t}^M M_{i,s,t} + w_{i,t}^L L_{i,s,t}}$$
, (9)

where $p_{i,s,t}^M M_{i,s,t}$ is factor payment for automation capital and $w_{i,t}^L L_{i,s,t}$ is the total payroll for low-skilled workers. This is the standard definition to measure the degree of automation in the task framework literature (Acemoglu and Restrepo, 2022b). The challenge here is that there is no data source for payments to automation capital, $p_{i,s,t}^M M_{i,s,t}$ across countries and sectors. Therefore, I construct it by combining (1) time-invariant capital income $p_{i,s,t0}^K K_{i,s,t0}$ at the country-sector (2-digit) level from the WIOD data, (2) time-invariant

¹²I follow this strategy because the robot data is only available at the level of 2-digit broad sectors, and these three 2-digit broad sectors have a share of 79% of the total number of robots in all sectors in 2014.

equipment-to-capital ratio at the sector (4-digit) level from the NBER CES data in the US, and (3) time-variant robot adoption data at the country-sector (2-digit) level from the IFR data. In particular, I construct $p_{i,s,t}^M M_{i,s,t}$ as

$$p_{i,s,t}^{M}M_{i,s,t} = \underbrace{p_{i,s,t0}^{K}K_{i,s,t0}}_{\text{Country}\times 2\text{-digit Sector}} \cdot \underbrace{\frac{p_{US,s,t0}^{M}M_{US,s,t0}}{p_{US,s,t0}^{K}K_{US,s,t0}}}_{\text{4-digit Sector}} \cdot \underbrace{\frac{p_{i,s,t}^{R}R_{i,s,t}}{p_{i,s,t0}^{R}R_{i,s,t0}}}_{\text{Country}\times 2\text{-digit Sector}\times \text{Year}}$$

Offshoring Share $_{i,s,t}$ is the share of import in total intermediate uses as in the first specification.

Compared to the first specification, this specification includes the levels of the degrees of automation and offshoring that vary over time. This feature allows the importance of skill abundance to depend not on the relative but the absolute levels of automation and offshoring.

3.3 Results

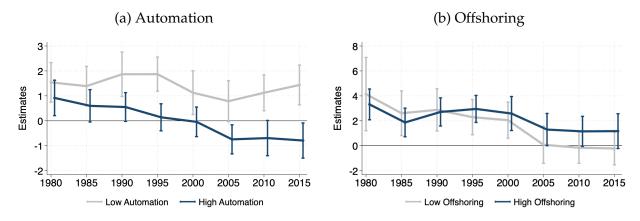
3.3.1 Trends by Groups using Time-Invariant Dummy Variables

I first start results with the first specification using time-invariant dummy variables. Figure 5a shows the result for automation. I estimate (7) for automation, and the gray line shows the time path of $\widehat{\beta}_t^0$, the coefficient for the low-automation group. The navy line shows the time path of $\widehat{\beta}_t^0 + \sum_{g \in G_{\text{Auto}}} \widehat{\beta}_t^g$ where G_{Auto} is a set of groups, high-automation countries and high-automation sectors. I compute the confidence intervals using the delta method. The result in Figure 5a shows that the importance of skill abundance decreased more in countries or sectors exposed to more automation as shown in the navy line. More importantly, the gray line does not go down over time, which means that skill abundance is still as important as in the 1980s for the countries and sectors with below-median exposure to automation.

Figure 5b shows that the importance of skill abundance decreased both in high- and low-offshoring groups and exhibits no significant heterogeneity across countries or sectors exposed to offshoring in different degrees.

Discussion These heterogeneous results suggest that explanations common across countries and sectors may not explain the observed decline in $\hat{\beta}_t$ entirely. For example, Hanson et al. (2015) and Levchenko and Zhang (2016) show the mean reversion or convergence in comparative advantage over time. While they can potentially explain the decreasing

Figure 5: Estimates of Importance of Skill Abundance in Comparative Advantage: Trends by Groups using Time-Invariant Dummy Variables



Notes: The figures show the estimates of the importance of skill abundance in comparative advantage in skill-intensive sectors. The left panel shows the estimates from (7) for low-automation and high-automation groups. The gray line shows the time path of $\widehat{\beta_t^0}$, the coefficient for the low-automation group. The navy line shows the time path of $\widehat{\beta_t^0} + \sum_{g \in G_{\text{Auto}}} \widehat{\beta_t^g}$ where G_{Auto} is a set of groups, high-automation countries and high-automation sectors. The right panel shows the estimates from (7) for low-offshoring and high-offshoring groups. The gray line shows the time path of $\widehat{\beta_t^0}$, the coefficient for the low-offshoring group. The navy line shows the time path of $\widehat{\beta_t^0} + \sum_{g \in G_{\text{Ofs}}} \widehat{\beta_t^g}$ where G_{Ofs} is a set of groups, high-offshoring countries and high-offshoring sectors. In both panels, the 95% confidence intervals are computed using the delta method.

importance of a country's skill abundance in comparative advantage in skill-intensive sectors for all countries and sectors, I show that the pattern is heterogeneous across countries and sectors with different exposures to automation. More importantly, my results show that the pattern of comparative advantage has not changed much for countries and sectors with lower levels of automation. Thus, unless mean reversion is systematically correlated with automation and offshoring, it cannot explain my empirical facts entirely. Therefore, my results are complementary to and not inconsistent with the findings in Hanson et al. (2015) and Levchenko and Zhang (2016).

3.3.2 Trends and Levels using Time-Variant Continuous Variables

The second specification is to use the time-variant continuous variables as in Equation 8. The use of the WIOD data makes the sample smaller, and the final sample is 26 countries, 393 4-digit sectors, and three periods, 1995, 2000, and 2005. Table 1 shows the results. All columns include the interaction between the exporter's skill abundance and the sector's skill intensity as the running variable, "Skill Term", $\alpha_{s,t}^H \times \ln(H_{i,t}/L_{i,t})$. All columns also control the interaction between the "Skill Term" and linear time trend. Column (1) shows

that the coefficient on the "Skill Term" is 1.17, implying that a country's skill abundance was an important source of comparative advantage in skill-intensive sectors in 1995, the beginning sample period. The coefficient of the interaction between the "Skill Term" and the linear trend is -1.18, implying that the importance is decreasing over time. Since there are three periods, 1995, 2000, and 2005, this means that the skill abundance used to be important in comparative advantage in skill-intensive sectors in 1995 and no longer matter in 2000. Column (2) adds the interaction between the "Skill Term" and automation shares. The coefficient is -3.18, meaning that higher automation makes the skill abundance less important. Column (3) adds the interaction between the "Skill Term" and offshoring shares. The coefficient is 0.47 with a standard error 0.43, implying that there is no large heterogeneity across countries and sectors with different offshoring shares. Column (4) adds both automation shares and offshoring shares to incorporate the correlation between automation and offshoring shares. The coefficient on the interaction between the "Skill Term" and automation shares is -3.05, which is close to the one in Column (2). This means that the heterogeneity in the importance of skill abundance based on different levels of automation is robust after controlling offshoring shares.

Table 1: Importance of Skill Abundance in Comparative Advantage: Roles of Automation and Offshoring, Continuous Measures

	Dep. Var. Log Trade Flow			
	(1)	(2)	(3)	(4)
Skill Term	1.17	2.36	1.00	2.23
	(0.53)	(0.62)	(0.58)	(0.69)
x Automation Share		-3.18		-3.05
		(1.04)		(1.05)
x Offshoring Share			0.47	0.24
			(0.43)	(0.41)
x Linear Trend	-1.18	-1.06	-1.18	-1.07
	(0.17)	(0.16)	(0.17)	(0.16)
Observations	1,528,800	1,528,800	1,523,612	1,523,612
Origin-Dest-Year FE	\checkmark	\checkmark	\checkmark	\checkmark
Dest-Sector-Year FE	\checkmark	\checkmark	\checkmark	\checkmark

Notes: The table shows the results for the importance of skill abundance in comparative advantage, based on the specification for β_t in equation (8). The dependent variable is the bilateral trade flow. All columns include the interaction between the exporter's skill abundance and the sector's skill intensity, "Skill Term", as the running variable. All columns also control the interaction between "Skill Term" and linear time trend. Columns (2) and (4) include the interaction between "Skill Term" and the automation share. Columns (3) and (4) include the interaction between "Skill Term" and the offshoring share. All the columns include origin-exporter-year fixed effects and importer-sector fixed effects. The standard errors are in parentheses and clustered at the exporter-sector level.

These results are robust if I drop the linear time trend or if I add the interaction between the sector's capital intensity and the country's capital abundance as in (5). Table D.1 and D.2 in Appendix D, respectively.

4 Trade Model with Automation and Offshoring

In this section, I develop a quantitative trade model with automation and offshoring to quantify the mechanisms and to draw implications for macroeconomic outcomes, such as manufacturing shares, skill premia, and welfare. The model builds on a multi-country, multi-sector, multi-factor Eaton-Kortum model. In particular, I embed the task framework of Acemoglu and Restrepo (2018) and Acemoglu and Restrepo (2022a) into a quantitative trade model with input-output linkages of Caliendo and Parro (2015).

4.1 The Model

There are I countries and S sectors. I denote countries by i and j and sectors by r and s. Countries differ in primary factor endowments—high-skilled H_i and low-skilled labor L_i . These labor endowments are the only primary factors in this model. Sectors differ in factor shares as explained later. All markets are perfectly competitive and both types of labor are freely mobile across sectors but not across countries.

4.1.1 Final Goods Demand

The demand side is a version of standard multi-sector Eaton-Kortum trade models as in Costinot et al. (2012).

Assume that trade frictions take the form of the standard iceberg trade cost, $\tau_{ij,s}^F \ge 1$ for final goods s exported from country i to j, bilateral exports from country i to j in sector s, X_{ijs} can be expressed as

$$X_{ij,s} = \pi_{ij,s}^F \cdot \mu_{j,s} \left(w_j^L L_j + w_j^H H_j \right)$$

where trade share of final goods, $\pi_{ij,s}^F$ is given by

$$\pi_{ij,s}^{F} = \frac{(c_{i,s}\tau_{ij,s}^{F})^{-\theta}}{\sum_{l}(c_{l,s}\tau_{li,s}^{F})^{-\theta}},$$
(10)

where $\mu_{j,s}$ is the expenditure share of country j in sector s with $\sum_s \mu_{j,s} = 1$, and $w_j^L L_j + w_j^H H_j$ is the aggregate income of country j. θ is the trade elasticity.

4.1.2 Production Technology

Compared to the standard multi-sector, multi-factor Eaton-Kortum model, the key difference is the unit production $\cos c_{i,s}$, incorporating automation and offshoring. Specifically, the production side follows the task framework developed by Acemoglu and Restrepo (2018), extended to incorporate two types of labor by Acemoglu and Restrepo (2022a), and generalized to include multiple factors within the task framework by Acemoglu and Restrepo (2022b).

Gross output in sector s in country i is produced by combining high-skilled labor $H_{i,s}$ and production task composites $T_{i,s}$ produced by low-skilled labor, machines, domestic intermediates, and foreign intermediates.¹³ The gross production function is

$$Y_{i.s} = (H_{i.s})^{\alpha_s^H} \cdot (T_{i.s})^{1-\alpha_s^H},$$

where α_s^H is the factor share of high-skilled labor. Goods produced can be used as final goods, intermediate goods, or capital. ¹⁴

Production Task Following Acemoglu and Restrepo (2022b), tasks are combined as follows:

$$T_{i,s} = \exp\left(\int_0^1 \ln T_{i,s}(z)dz\right).$$

Task $T_{i,s}(z)$ can be produced either by low-skill labor, machines, or intermediates:

$$T_{i,s}(z) = A^{M} \psi_{i,s}^{M}(z) M_{i,s}(z) + A^{L} \psi_{i,s}^{L}(z) L_{i,s}(z) + A^{XD} \psi_{i,s}^{XD}(z) X D_{i,s}(z) + A^{XF} \psi_{i,s}^{XF}(z) X F_{i,s}(z),$$
(11)

where $M_{i,s}(z)$, $L_{i,s}(z)$, $XD_{i,s}(z)$, $XF_{i,s}(z)$ are machines, low-skill labor, domestic intermediates, and foreign intermediates. A^M , A^L , A^{XD} , and A^{XF} are factor-augmented technology, which makes each factor more productive equally across tasks. $\psi^M_{i,s}(z)$, $\psi^L_{i,s}(z)$, $\psi^{XD}_{i,s}(z)$ are task-specific productivity components, which determine the specialization patterns of each factor across tasks. This becomes zero for factors that cannot perform a task.

¹³Here, the machine includes equipment and excludes structures, such as buildings.

¹⁴This unitary elasticity of substitution across high-skilled labor and task composites follows Acemoglu and Restrepo (2022a). This is for simplicity and to highlight the substitution across low-skilled labor and automation or offshoring.

Demand for machines, low-skilled labor, and intermediates across tasks within a country-sector pair (i, s) add up to aggregate factor inputs at a country-sector level,

$$\int_0^1 L_{i,s}(z)dz = L_{i,s}, \quad \int_0^1 M_{i,s}(z)dz = M_{i,s}, \quad \int_0^1 XD_{i,s}(z)dz = XD_{i,s}, \quad \int_0^1 XF_{i,s}(z)dz = XF_{i,s}.$$

4.1.3 Supply and Price of Machines and Intermediates

Final outputs can be used either as final consumption, machines, or intermediates. Machines and foreign intermediates can be sourced from different countries and sectors with trade costs, and the setup is similar to the intermediate supply structure in Caliendo and Parro (2015). Here, I only show the price indices and trade shares of machines and intermediates, which are relevant for solving the equilibrium.¹⁵

First, machine price, $w_{i,s}^{M}$, is given by

$$w_{i,s}^{M} = \prod_{r} \left(\frac{w_{i,rs}^{M}}{\alpha_{i,rs}^{M}} \right)^{\alpha_{i,rs}^{M}}, \tag{12}$$

where $w_{i,rs}^M$ is the price of machines used in country i and sector s sourced from r and $\alpha_{i,rs}^M$ is the input-output coefficient for machines with $\sum_r \alpha_{i,rs}^M = 1$.

The price of machines in country i and sector s sourced from sector r is given by

$$w_{i,rs}^M = \left(\sum_j (c_{j,r} \tau_{ji,r}^M)^{-\theta}\right)^{-1/\theta}.$$

Also, the share of machines used in country i sourced from country j is

$$\pi_{ji,r}^{M} = \frac{(c_{j,r}\tau_{ji,r}^{M})^{-\theta}}{\sum_{l}(c_{l,r}\tau_{li,r}^{M})^{-\theta}}.$$
(13)

Second, the price of domestic intermediates is given by the Cobb-Douglas aggregate of unit costs across sourcing sectors r as follows

$$w_{i,s}^{XD} = \prod_{r} \left(\frac{c_{i,r}}{\alpha_{i,rs}^X} \right)^{\alpha_{i,rs}^X} , \tag{14}$$

where $\alpha_{i,rs}^X$ is the input-output coefficient for intermediates with $\sum_r \alpha_{i,rs}^X = 1$.

¹⁵The detail is in Appendix E.

Finally, the price of foreign intermediates is given by

$$w_{i,s}^{XF} = \prod_{r} \left(\frac{w_{i,rs}^{XF}}{\alpha_{i,rs}^{X}} \right)^{\alpha_{i,rs}^{X}}, \tag{15}$$

where

$$w_{i,rs}^{XF} = \left(\sum_{j \neq i} (c_{j,r} au_{ji,r}^X)^{- heta}
ight)^{-1/ heta}$$
 ,

and the share of foreign intermediates used in country i in sector r from country j is given by

$$\pi_{ji,r}^{XF} = \frac{(c_{j,r}\tau_{ji,r}^X)^{-\theta}}{\sum_{l \neq i} (c_{l,r}\tau_{li,r}^X)^{-\theta}}.$$
 (16)

4.1.4 Market Clearing Conditions

Goods Market Clearing Output in country i and sector s, $Y_{i,s}$, can be used as final consumption, machines service, or intermediates. Thus, the good market clearing condition is as follows

$$Y_{i,s} = \underbrace{\sum_{j} \pi_{ij,s}^{F} \mu_{j,s}(w_{j}^{L}L_{j} + w_{j}^{H}H_{j})}_{\text{Final Consumption in } j} + \underbrace{\sum_{j} \sum_{r} \pi_{ij,r}^{M} \alpha_{j,sr}^{M} (1 - \alpha_{r}^{H}) \Gamma_{j,r}^{M} Y_{j,r}}_{\text{Machine Service in } j - r}$$

$$+ \underbrace{\sum_{r} \alpha_{i,sr}^{X} (1 - \alpha_{r}^{H}) \Gamma_{i,r}^{XD} Y_{i,r}}_{\text{Domestic Intermediates in } i - r} + \underbrace{\sum_{j} \sum_{r} \pi_{ij,r}^{X} \alpha_{j,sr}^{X} (1 - \alpha_{r}^{H}) \Gamma_{j,r}^{XF} Y_{j,r}}_{\text{Foreign Intermediates in } j \neq i) - r}$$

$$(17)$$

Labor Market Clearing The labor market clearing condition is standard as follows.

$$w_i^L L_i = \sum_s (1 - \alpha_s^H) \Gamma_{i,s}^L Y_{i,s}$$

$$w_i^H H_i = \sum_s \alpha_s^H Y_{i,s}$$
(18)

4.2 Equilibrium

Definition 4.1. A *decentralized equilibrium* is defined as consumption, investment, an allocation of tasks, and sourcing plans of intermediates in which

(i) A representative household in each country chooses consumption to maximize utility subject to budget constraint

- (ii) Firms choose factor demand and allocation of tasks to maximize profits
- (iii) Goods and factor markets clear

Proposition 4.1. *The equilibrium exists and is unique.*

Proof. The model is a variant of the Eaton-Kortum model Eaton and Kortum (2002) with intermediates so that the model is within the universal gravity framework of Allen et al. (2020).

4.2.1 Task Share

One of the most important objects in this theoretical framework is task share, which represents task allocation across factors. Cost minimization leads to the following allocation:

$$\mathcal{T}_{i,s}^{F} = \left\{ z : \frac{w_{i}^{F}}{\psi_{i,s}^{F}(z) \cdot A^{F}} = \min_{F' \in \{L,M,XD,XF\}} \frac{w_{i}^{F'}}{\psi_{i,s}^{F'}(z) \cdot A^{F'}} \right\}$$

for each factor $F \in \{L, M, XD, XF\}$, where $\mathcal{T}_{i,s}^F$ are sets of tasks allocated to factor F.

Tasks are allocated to the factor, which is the most efficient to complete the task. As in Acemoglu and Restrepo (2022b), when a task can be produced at the same unit cost by different factors, I assume it is allocated to labor, machines, and then domestic intermediates as a tie-breaking rule.¹⁶

Given these task allocation rules, I define the task share as follows

$$\Gamma^L_{i,s} = \int_{\mathcal{T}^L_{i,s}} dz, \quad \Gamma^M_{i,s} = \int_{\mathcal{T}^M_{i,s}} dz, \quad \Gamma^{XD}_{i,s} = \int_{\mathcal{T}^{XD}_{i,s}} dz, \quad \Gamma^{XF}_{i,s} = \int_{\mathcal{T}^{XF}_{i,s}} dz,$$

where these quantities are the measures of the sets, $\mathcal{T}_{i,s}^L$, $\mathcal{T}_{i,s}^M$, $\mathcal{T}_{i,s}^{XD}$, $\mathcal{T}_{i,s}^{XF}$.

In this theoretical framework, automation and offshoring are isomorphic and captured by increases in $\Gamma^{M}_{i,s}$ and $\Gamma^{XF}_{i,s}$, respectively. These changes in task share decrease the task share of low-skilled workers, $\Gamma^{L}_{i,s}$.

This framework nests the previous papers in the task framework. The papers on automation literature, such as Acemoglu and Restrepo (2020) or Acemoglu and Restrepo (2022b), assume that there is no intermediate, $\Gamma^{XD}_{i,s} = \Gamma^{XF}_{i,s} = 0$, and focus on task allocations across labor (potentially multi types) and machines. Grossman and Rossi-Hansberg (2008), which studies the effects of offshoring on factor prices, assumes that there is no capital and that intermediates are supplied only from abroad, $\Gamma^{M}_{i,s} = \Gamma^{XD}_{i,s} = 0$, and the foreign intermediates are produced only using foreign labor.

¹⁶This simplifies the exposition and has no substantial consequences.

Unit Production Cost Consequently, the unit production cost in country *i* sector *s* can be written as follows:

$$c_{i,s} = \Lambda_s \cdot (w_i^H)^{\alpha_s^H} \cdot \left[\left(\frac{w_{i,s}^M}{\Gamma_{i,s}^M} \right)^{\Gamma_{i,s}^M} \cdot \left(\frac{w_i^L}{\Gamma_{i,s}^L} \right)^{\Gamma_{i,s}^L} \cdot \left(\frac{w_{i,s}^{XD}}{\Gamma_{i,s}^{XD}} \right)^{\Gamma_{i,s}^{XD}} \cdot \left(\frac{w_{i,s}^{XF}}{\Gamma_{i,s}^{XF}} \right)^{\Gamma_{i,s}^{XF}} \right]^{1-\alpha_s^H}$$
(19)

where Λ_s is

$$\Lambda_s = (\alpha_s^H)^{-\alpha_s^H} (1 - \alpha_s^H)^{\alpha_s^H - 1}.$$

4.2.2 Characterization of Equilibrium

Having established the task shares and the unit production cost, I can now characterize the equilibrium as follows.

Definition 4.2. A decentralized equilibrium consists of a vector of wages $\{w_i^H, w_i^L\}$ that satisfies the following systems of equations.

- (i) Given the vector of wages, prices of machines, prices of intermediates, and unit production costs are jointly pinned down by (12), (14), (15), and (19),
- (ii) Given unit costs in each country and sector, trade shares for final goods, machines, and intermediates are determined by (10), (13), and (16),
- (iii) Goods and labor markets clear by (17) and (18).

4.3 Changes in Comparative Advantage

After characterizing the equilibrium, I can now show how automation and offshoring affect comparative advantage.

In this section, I just focus on automation, by setting $\Gamma_{is}^{XD} = \Gamma_{is}^{XF} = 0$.

Proposition 4.2. (Changes in Comparative Advantage due to Automation) Assume that machines are non-tradable and produced only by sector s = R. Also, assume that the automation share in country i and sector s satisfied $\Gamma^M_{i,s} = \Gamma^M_i \cdot \Gamma^M_s$ for all i, s. Then, the trade flow follows

$$\ln X_{i,j,s} = -\theta \left(1 - \overline{\alpha_R^H} \Gamma_{i,s}^M \right) \left[\alpha_s^H \times \ln \left(\frac{w_i^H}{w_i^L} \right) \right] - \theta \overline{\alpha_R^H} \Gamma_{i,s}^M \ln \left(\frac{w_i^H}{w_i^L} \right) + \eta_{i,j} + \eta_{j,s}, \quad (20)$$

where $\overline{\alpha_R^H}$ is the skill intensity in machine-producing sector s = R.

This equation (20) extends the expression (2), which was the trade flow equation without automation. The first additional component is $-\overline{\alpha_R^H}\Gamma_{i,s}^M$ in front of the interaction term. I call this the displacement term, which is increasing in $\Gamma_{i,s}^M$. When $\Gamma_{i,s}^M$ (automation share) increases, the interaction term between the sector's skill intensity and the country's relative wage (skill premium) becomes smaller. This means that automation gives a comparative advantage to the countries with lower skill premia (skill-abundant countries), such as Germany, in low-skill-intensive sectors, such as the automobile sector.

The second component is $-\theta \overline{\alpha_R^H} \Gamma_{i,s}^M \frac{w_i^H}{w_i^L}$ which is the comparative advantage of countries with lower skill premium in high automation sectors, regardless of the sector's skill intensity α_s^H .

Proposition 4.3. (Changes in $\hat{\beta}$ due to Automation) Consider the following regression.

$$\ln X_{i,j,s} = \beta_i \left[\alpha_s^H \times \ln \left(H_i / L_i \right) \right] + \delta \cdot \Gamma_{i,s}^M \ln \left(H_i / L_i \right) + \eta_{i,j} + \eta_{j,s} + \varepsilon_{i,j,s}$$

Suppose that $\Gamma_{i,s}^M = \Gamma$ for all i, s. Then, increases in Γ (automation) decreases $\hat{\beta}_i$ (importance of skill abundance for comparative advantage in skill-intensive sectors), where

$$\widehat{\beta}_i = \theta \left(1 - \overline{\alpha_R^H} \cdot \Gamma \right) \times \frac{\phi}{Var\left(\ln(H_i/L_i) \right)}, \quad \phi \equiv Cov\left(\ln(H_i/L_i), \ln(w_i^L/w_i^H) \right)$$

if
$$\phi > 0$$
 and $\frac{d\phi}{d\Gamma} < 0$.

The first assumption, $\phi > 0$, means that skill-abundant countries have lower skill premia. The second assumption, $d\phi/d\Gamma$, means that automation increases skill premia more in skill-abundant (developed) countries.¹⁷

Under these assumptions, this proposition characterizes the effect of automation on the importance of skill abundance for comparative advantage in skill-intensive sectors, which I show the decline in Section 2. This specification is consistent with the specification for the heterogeneous effects in (8).

This proposition shows that automation can decrease $\hat{\beta}_i$ via (i) the displacement effect in sectors with automation, which I study in Section 3 and (ii) the general equilibrium effect, that is, a decrease in ϕ regardless of the levels of automation in each sector, which is absent in Section 3. The quantitative results in Section 5 incorporate this general equilibrium effect and evaluate the full quantitative implications of automation and offshoring.

¹⁷These assumptions are verified in the quantitative section.

4.4 Changes in Skill Premium

Before going to the quantitative section, I show how automation and offshoring affect skill premia across countries.

Proposition 4.4. (Changes in Skill Premium due to Automation and Offshoring) Changes in skill premium can be decomposed into task displacement and sectoral reallocation terms as follows:

$$\widetilde{w_{i}^{H}} - \widetilde{w_{i}^{L}} = - \underbrace{\sum_{s} \zeta_{i,s}^{L} \cdot \widetilde{\Gamma_{i,s}^{L}}}_{\text{Task Displacement}} + \underbrace{\sum_{s} \left(\zeta_{i,s}^{H} - \zeta_{i,s}^{L} \right) \cdot \widetilde{Y_{i,s}}}_{\text{Sectoral Reallocation}}, \tag{21}$$

where $\widetilde{X} \equiv dX/X$ and $\zeta_{i,s}^H$ and $\zeta_{i,s}^L$ are sectoral share in payroll for each labor type as follows:

$$\zeta_{i,s}^{H} = \frac{\alpha_{s}^{H} Y_{i,s}}{\sum_{r} \alpha_{r}^{H} \cdot Y_{i,r}} = \frac{w_{i}^{H} H_{i,s}}{\sum_{r} w_{i}^{H} H_{i,r}}, \quad \zeta_{i,s}^{L} = \frac{(1 - \alpha_{s}^{H}) \cdot \Gamma_{i,s}^{L} \cdot Y_{i,s}}{\sum_{r} (1 - \alpha_{r}^{H}) \cdot \Gamma_{i,r}^{L} \cdot Y_{i,r}} = \frac{w_{i}^{L} L_{i,s}}{\sum_{r} w_{i}^{L} L_{i,r}}.$$

This proposition shows how skill premium changes in response to automation or off-shoring, which leads to decreases in labor share, $\Gamma^L_{i,s}$. The first term captures the task displacement effect. Automation and offshoring in this model decrease the task share of low-skill labor $\Gamma^L_{i,s}$. This decreases the relative demand for low-skill labor in the economy. The second term captures the sectoral reallocation effect. Automation and offshoring can change the output in that country and sector. If automation or offshoring increases output in that sector, the relative demand for high-skill to low-skill labor increases if that sector relatively relies more on high-skill labor than low-skill labor, $\zeta^H_{i,s} > \zeta^L_{i,s}$. The second term highlights the importance of changes in comparative advantage when considering the effects of automation or offshoring on skill premium, which I come back to in the quantitative analysis.

5 Quantitative Analysis

In this section, I study the quantitative importance of automation and offshoring for changes in comparative advantage and the implications for structural change and welfare. First, I explain the data, the calibration strategy, and the counterfactual exercises I run. Second, I show how much automation and offshoring affect comparative advantage by running the same regression (4) in Section 2 using the data generated under counter-

factual scenarios. Finally, I explore the quantitative implications for skill premia, manufacturing shares, and welfare across countries.

5.1 Data and Calibration

My main dataset for the quantitative analysis is the WIOD data (Timmer et al., 2015). I use 36 countries, plus the rest of the world and 18 2-digit sectors. Note that in this exercise, the sectoral coverage differs from the analysis in Section 2. I used 396 4-digit sic manufacturing sectors in Section 2 while I use 18 sectors, including service sectors here.¹⁸

I use the exact hat algebra following Dekle et al. (2008), which does not require me to calibrate productivity levels across countries and sectors or trade costs across exporters, importers, and sectors. The only parameter I need to calibrate is the trade elasticity, θ , and I set it to be 5, which is standard (Anderson and Van Wincoop, 2004; Arkolakis et al., 2012).

For the benchmark year t_0 , I directly feed trade shares, π_{i,j,s,t_0} , expenditure shares, μ_{i,s,t_0} , factor shares, $\{\alpha_{s,t_0}^H, \Gamma_{i,s,t_0}^L, \Gamma_{i,s,t_0}^M, \Gamma_{i,s,t_0}^{XP}, \Gamma_{i,s,t_0}^{XF}\}$, factor endowments, $\{L_i, H_i\}$, and the total factor payments by labor types, $\{w_i^L L_i, w_i^H H_i\}$ from the WIOD (Timmer et al., 2015). The input-output coefficients for intermediates and machines, $\alpha_{i,rs}^X$ and $\alpha_{i,rs}^M$, are from Ding (2022). $\alpha_{i,rs}^{20}$

Since the WIOD with labor compensation by multiple labor types is only available between 1995 and 2008, I choose 1995 as the benchmark year, t_0 .

5.2 Exact Hat Algebra

I avoid explicitly calibrating the factor-specific productivity, A^F , exporter-sector-factor-task specific productivity, $\psi^F_{i,s}(z)$, and trade costs $\tau^F_{ij,s}$, $\tau^M_{ij,s}$, $\tau^X_{ij,s}$, by solving the model in percent changes from the observed equilibrium in 1995 using the exact hat algebra method pioneered by Dekle et al. (2008). This method implicitly calibrates those parameters to ex-

¹⁸The original WIOD data has 35 sectors, and I aggregate service sectors into two aggregate sectors, high-skilled service and low-skilled service sectors. High-skilled service sectors consist of Post and telecommunications, Financial Intermediation, Real Estate Activities, and Renting of m&eq and Other Business Activities. The remaining service sectors are categorized as low-skilled service sectors. I drop Education, Health and Social Work, Other Community, Social and Personal Services, and Private Households with Employed Persons because of missing values in many countries.

¹⁹The original WIOD data has three types of labor, low-skilled, middle-skilled, and high-skilled. I combine low-skilled and middle-skilled as low-skilled labor.

²⁰Ding (2022) constructs a novel dataset on inter-sectoral capital service flow. I use the input-output coefficient for capital for the ones for machines in my paper. I covert the input-output coefficients at the bilateral level to the use-country level by taking the median.

actly match the factor payments in each country and trade shares. Details are in Appendix F

5.3 Changes in Comparative Advantage

5.3.1 Overview

In this subsection, I quantify the roles of automation and offshoring in the changes in comparative advantage, observed in Section 2. To do so, I first assume that the model economy is at the level of the benchmark year, 1995. Then, using the exact hat algebra, I consider three scenarios, (1) only the path of automation share, $\Gamma^{M}_{i,s,t'}$, changes over time, (2) only the path of offshoring share, $\Gamma^{XF}_{i,s,t'}$ changes over time, and (3) only the paths of automation share and offshoring share change over time. I then, for each scenario, run the same regression as in (4) as follows:

$$\ln X_{i,j,s,t} = \beta_t \left[\alpha_{s,t_0}^H \times \ln \left(\frac{H_{i,t_0}}{L_{i,t_0}} \right) \right] + \eta_{i,j,t} + \eta_{j,s,t} + \varepsilon_{i,j,s,t}.$$

I compare the estimates of β_t under different counterfactual scenarios with the estimates obtained from the real data in the WIOD.

Note that I fix the skill intensity and factor endowments at the level of 1995 in this counterfactual exercise. Therefore, the only time-varying variable in this regression is the trade flows, which the model generates under different counterfactual scenarios.

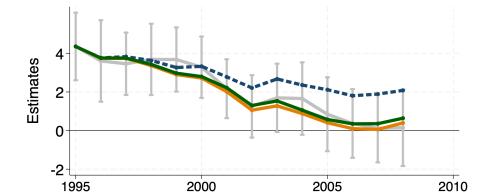
5.3.2 Result

Figure 6 shows the results for the importance of skill abundance in comparative advantage in the different counterfactual scenarios. To start with, the gray line shows the estimates of $\hat{\beta}$ in the WIOD as in the data. Consistent with the findings in Section 2 where I used more detailed data from different sources, the importance of the skill abundance decreased over time.

The orange line shows the estimates based on the generated data under the counter-factual scenario where I only change the automation share over time. The time trend almost perfectly explains the path from the data, which implies that changes in automation can explain the evolution of comparative advantage well. This is surprising because I do not target any moments for automation after the benchmark year, 1995.

The navy line shows the estimates based on the generated data under the counterfactual case where only the offshoring share changes over time. While the estimate is decreasing over time, it cannot explain the change in the estimates based on the data (the gray line).

Finally, the green line shows the estimates under the case where only automation and offshoring shares change. It almost matches the path of the case with only automation. This implies that offshoring does not have a strong, additional force to decrease the importance of skill abundance in comparative advantage on top of automation.



Year

Only Automation

Automation + Offshoring

Figure 6: Counterfactual: Importance of Skill Abundance in Comparative Advantage

Notes: The figures show the importance of skill abundance in comparative advantage in the different counterfactual scenarios. The gray line is the path of the estimates $\hat{\beta}$ using the WIOD with the 95% confidence interval cluster at the exporter-sector level. The orange line is the one when I only change automation share $\Gamma^{M}_{i,s,t}$ (and corresponding changes in $\Gamma^{L}_{i,s,t}$) as in the data and fix everything else at the levels in 1995. The navy line is the one when I only change offshoring share $\Gamma^{XF}_{i,s,t}$ (and corresponding changes in $\Gamma^{L}_{i,s,t}$) as in the data and fix everything else at the levels in 1995. The green line is the one when I only change automation share $\Gamma^{M}_{i,s,t}$ and offshoring share $\Gamma^{XF}_{i,s,t}$ (and corresponding changes in $\Gamma^{L}_{i,s,t}$) and fix everything else at the levels in 1995.

Data

--- Only Offshoring

5.4 Macro Implications

The previous subsection shows how automation and offshoring affect comparative advantage. In this subsection, I investigate the implications for macroeconomic aggregates, such as manufacturing output shares within each country, skill premia, and welfare across countries. To do so, I again assume that the model economy is at the level of the benchmark year, 1995. Then, I use the exact hat algebra to consider the following counterfactual cases, (1) automation shares are at the level of 1995 and (2) offshoring shares are at the level of 1995.

5.4.1 Manufacturing Output Shares within Each Country

First, I study the effect of automation and offshoring on manufacturing output shares within each country. Figure 7a shows the result for automation. The horizontal axis shows the country-level average increases in the automation share between 1995 and 2008. The vertical axis shows the country-level changes in the share of manufacturing output in total output between 1995 and 2008. Each dot represents a country. The result shows two groups of countries. The first group is a group of high-automation countries, such as Germany and Japan, which increase manufacturing output shares. For instance, Germany increases the manufacturing output share by 13% pt as it increases the automation share in each sector by 13% pt on average. The second group is a group of low-automation countries, such as the US, China, and India, which decrease their manufacturing shares. This indicates that automation shifts manufacturing production from low-automation countries to high-automation countries.

Figure 7b shows the result for offshoring. The horizontal axis now shows the country-level average increases in the offshoring share between 1995 and 2008. Compared to the results for automation, the effects of offshoring are small for most countries.

(a) Automation (b) Offshoring Changes in MFG Output Share (% pt) Changes in MFG Output Share (% pt) 20 •DEU 10 •JPN CHN 5 10 15 5 10 15 20 25 Avg. Increases in Automation Share (1995-2008, % pt) Avg. Increases in Offshoring Share (1995-2008, % pt)

Figure 7: Changes in Manufacturing Output Share within Each Country

Notes:Both panels show the changes in manufacturing output share in total output in each country in response to automation (Figure 7a) and offshoring (Figure 7b) from 1995 to 2008. The horizontal axis shows the country-level average increases in the automation share (Figure 7a) or the offshoring share (Figure 7b) between 1995 and 2008. In both panels, the vertical axis shows the changes in manufacturing output share in total output in each country. Each dot represents a country.

5.4.2 Skill Premium

I then explore the implications of automation and offshoring for skill premia. Figure 8 shows the results. Figure 8a shows the changes in skill premia across countries when only automation shares changes since 1995. The horizontal axis shows the country-level average increases in the automation share between 1995 and 2008, and the vertical axis shows the changes in skill premia across countries. There are two takeaways from this figure. First, there is a positive association between automation and increases in skill premia. This is consistent with the intuition that automation increases the relative demand for high-skilled labor to low-skilled labor. Second, while high-automation countries, such as Germany and Japan, increased skill premia, other countries decreased skill premia. These low-automation countries indeed reallocated resources to more low-skill-intensive sectors, and the relative demand for low-skilled workers increased, leading to declines in skill premia.

Figure 8b shows the result for offshoring. The horizontal axis shows the country-level average increases in the offshoring share between 1995 and 2008, and the vertical axis shows the changes in skill premia across countries. Compared to automation, the effect is modest, although the magnitude of the increases in offshoring shares is larger than those in automation shares.

(a) Automation (b) Offshoring 30 30 Increases in Skill Premium (% pt) ncreases in Skill Premium (% pt) 20 •DEU 10 •.IPN -10 Ó 5 10 15 5 10 15 25 Avg. Increases in Automation Share (1995-2008, % pt) Avg. Increases in Offshoring Share (1995-2008, % pt)

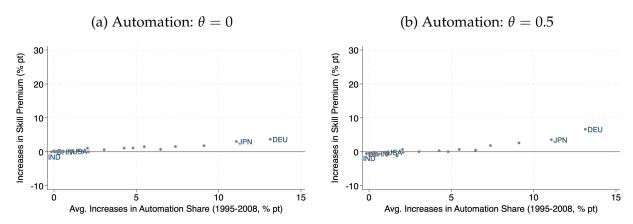
Figure 8: Changes in Skill Premia

Notes: Both panels show the changes in skill premia across countries in response to automation (Figure 8a) and offshoring (Figure 8b) from 1995 to 2008. The horizontal axis shows the country-level average increases in the automation share (Figure 8a) or the offshoring share (Figure 8b) between 1995 and 2008. In both panels, the vertical axis shows the changes in skill premia across countries. Each dot represents a country.

To investigate the roles of this sectoral reallocation, Figure 9a shows the effects of automation on skill premia when the trade share is fixed ($\theta = 0$). In this case, the output

shares in each country and sector are fixed because the expenditure shares are fixed by the Cobb-Douglass assumption on the final goods expenditure shares. The result in 9a shows that skill premia increased in all of the countries, which is consistent with the standard arguments in closed economies (Katz and Murphy, 1992; Acemoglu and Restrepo, 2022b). Figure 9b shows the results when $\theta = 0.5$ where the output is not fixed, but the trade elasticity is lower than the baseline $\theta = 5.0$. Still, skill premia increase in all of the countries. This highlights that sectoral reallocation via trade has important implications for the effects of automation on skill premia.

Figure 9: Changes in Skill Premia due to Automation with Different Trade Elasticity

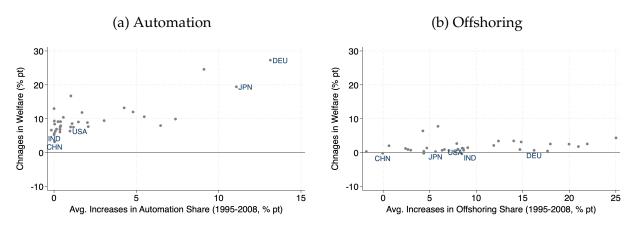


Notes: Both panels show the changes in skill premia across countries in response to automation from 1995 to 2008. The horizontal axis shows the country-level average increases in the automation share between 1995 and 2008. In both panels, the vertical axis shows the changes in skill premia across countries. Each dot represents a country. Figure 9a shows the results when the trade elasticity is zero ($\theta = 0.0$) so that the trade shares are fixed. Figure 9b shows the results when only automation shares change since 1995 when the trade elasticity is 0.5 ($\theta = 0.5$) so that the trade shares are lower than the baseline value ($\theta = 5.0$). Each dot represents a country.

5.4.3 Welfare

Finally, I examine the welfare effect of automation and offshoring across countries. Here, welfare change is the real consumption, which is equal to the real labor income, $(w_i^L L_i + w_i^H H_i)/P_i$ where P_i is the consumer price index for country i. Figure 10a shows the changes in welfare when only the automation shares change. All countries benefit from automation, and those with more automation increase welfare more. For instance, Germany with around 14% increases in automation enjoys about 30% increases in welfare. Figure 10b shows the results for offshoring. Again, all countries benefit from offshoring while there is not much heterogeneity in gains across countries.

Figure 10: Changes in Welfare



Notes: Both panels show the changes in welfare across countries in response to automation (Figure 10a) and offshoring (Figure 10b) from 1995 to 2008. The horizontal axis shows the country-level average increases in the automation share (Figure 10a) or the offshoring share (Figure 10b) between 1995 and 2008. In both panels, the vertical axis shows the changes in welfare across countries. Each dot represents a country.

Again, I examine how the effects depends on the trade elasticity. Figure 11 shows the results when the trade elasticity is 0.0 or 0.5. Compared to the results in Figure 10a, the welfare effects are smaller in these figures. For instance, when $\theta=0.0$, the welfare effects of automation for India, which is a low-automation country, is around 0% pt while it was 5% pt when $\theta=5.0$. This implies that the positive spillover from automation in high-automation countries becomes muted. This highlights that incorporating trade is important when considering the effect of automation on welfare across countries.

Figure 11: Welfare Effects of Automation with Different Trade Elasticity



Notes: Both panels show the changes in welfare across countries in response to automation from 1995 to 2008. The horizontal axis shows the country-level average increases in the automation share between 1995 and 2008. In both panels, the vertical axis shows the changes in welfare across countries. Figure 11a shows the results when only automation shares change since 1995 when the trade elasticity is zero ($\theta = 0.0$) so that the trade shares are fixed. Figure 11b shows the results when only automation shares change since 1995 when the trade elasticity is 0.5 ($\theta = 0.5$) so that the trade shares are lower than the baseline value ($\theta = 5.0$). Each dot represents a country.

6 Conclusion

In this paper, I document new facts about the evolution of comparative advantage and draw implications for macroeconomic variables. Empirically, I find that a country's skill abundance has become less important for comparative advantage in skill-intensive sectors over time. I show that automation is quantitatively more important in explaining these patterns than offshoring. Moreover, I show that automation in developed countries can lead to shifts in manufacturing production from developing to developed countries. Automation benefits rich countries more while offshoring benefits countries more equally.

References

Acemoglu, Daron (2003) "Patterns of skill premia," *The Review of Economic Studies*, 70 (2), 199–230.

Acemoglu, Daron and Pascual Restrepo (2018) "The race between man and machine: Implications of technology for growth, factor shares, and employment," *American Economic Review*, 108 (6), 1488–1542.

- ——— (2020) "Robots and jobs: Evidence from US labor markets," *Journal of Political Economy*, 128 (6), 2188–2244.
- ——— (2022a) "Demographics and automation," *The Review of Economic Studies*, 89 (1), 1–44.
- ——— (2022b) "Tasks, automation, and the rise in US wage inequality," *Econometrica*, 90 (5), 1973–2016.
- Acemoglu, Daron and Fabrizio Zilibotti (2001) "Productivity differences," *The Quarterly Journal of Economics*, 116 (2), 563–606.
- Allen, Treb, Costas Arkolakis, and Yuta Takahashi (2020) "Universal gravity," *Journal of Political Economy*, 128 (2), 393–433.
- Anderson, James E and Eric Van Wincoop (2004) "Trade costs," *Journal of Economic literature*, 42 (3), 691–751.
- Arkolakis, Costas, Arnaud Costinot, and Andrés Rodríguez-Clare (2012) "New trade models, same old gains?" *American Economic Review*, 102 (1), 94–130.

- Atkin, David, Arnaud Costinot, and Masao Fukui (2021) "Globalization and the Ladder of Development: Pushed to the Top or Held at the Bottom?" Technical report, National Bureau of Economic Research.
- Autor, David, David Dorn, and Gordon H Hanson (2013) "The China syndrome: Local labor market effects of import competition in the United States," *American Economic Review*, 103 (6), 2121–68.
- Barro, Robert J and Jong Wha Lee (2013) "A new data set of educational attainment in the world, 1950–2010," *Journal of Development Economics*, 104, 184–198.
- Becker, Randy, Wayne Gray, and Jordan Marvakov (2021) "NBER-CES Manufacturing Industry Database (1958-2018, version 2021a)," https://www.nber.org/research/data/nber-ces-manufacturing-industry-database, Last accessed 2023-01-30.
- Bernard, Andrew B, J Bradford Jensen, and Robert Z Lawrence (1995) "Exporters, jobs, and wages in US manufacturing: 1976-1987," *Brookings papers on economic activity. Microeconomics*, 1995, 67–119.
- Bombardini, Matilde, Giovanni Gallipoli, and Germán Pupato (2012) "Skill dispersion and trade flows," *American Economic Review*, 102 (5), 2327–2348.
- Bowen, Harry P, Edward E Leamer, and Leo Sveikauskas (1987) "Multicountry, Multifactor Tests of the Factor Abundance Theory," *The American Economic Review*, 77 (5), 791–809.
- Burstein, Ariel, Javier Cravino, and Jonathan Vogel (2013) "Importing skill-biased technology," *American Economic Journal: Macroeconomics*, 5 (2), 32–71.
- Burstein, Ariel, Eduardo Morales, and Jonathan Vogel (2019) "Changes in between-group inequality: computers, occupations, and international trade," *American Economic Journal: Macroeconomics*, 11 (2), 348–400.
- Burstein, Ariel and Jonathan Vogel (2017) "International trade, technology, and the skill premium," *Journal of Political Economy*, 125 (5), 1356–1412.
- Caliendo, Lorenzo and Fernando Parro (2015) "Estimates of the Trade and Welfare Effects of NAFTA," *The Review of Economic Studies*, 82 (1), 1–44.
- Caron, Justin, Thibault Fally, and James R Markusen (2014) "International trade puzzles: A solution linking production and preferences," *The Quarterly Journal of Economics*, 129 (3), 1501–1552.

- Chor, Davin (2010) "Unpacking sources of comparative advantage: A quantitative approach," *Journal of International Economics*, 82 (2), 152–167.
- Costinot, Arnaud (2009) "On the origins of comparative advantage," *Journal of International Economics*, 77 (2), 255–264.
- Costinot, Arnaud, Dave Donaldson, and Ivana Komunjer (2012) "What goods do countries trade? A quantitative exploration of Ricardo's ideas," *The Review of Economic Studies*, 79 (2), 581–608.
- Davis, Donald R. and Jonathan I. Dingel (2020) "The comparative advantage of cities," *Journal of International Economics*, 123 (C), 10.1016/j.jinteco.2020.10.
- Davis, Donald R and David E Weinstein (2001) "An account of global factor trade," *American Economic Review*, 91 (5), 1423–1453.
- Dekle, Robert, Jonathan Eaton, and Samuel Kortum (2008) "Global Rebalancing with Gravity: Measuring the Burden of Adjustment.," *IMF Staff Papers*, 55 (3).
- Ding, Xiang (2022) "Capital Services in Global Value Chains," Technical report.
- Eaton, Jonathan and Samuel Kortum (2002) "Technology, geography, and trade," *Econometrica*, 70 (5), 1741–1779.
- Epifani, Paolo and Gino Gancia (2008) "The skill bias of world trade," *The Economic Journal*, 118 (530), 927–960.
- Feenstra, Robert C and Gordon H Hanson (1996) "Globalization, outsourcing, and wage inequality," *The American Economic Review*, 86 (2), 240.
- Feenstra, Robert C, Robert Inklaar, and Marcel P Timmer (2015) "The next generation of the Penn World Table," *American Economic Review*, 105 (10), 3150–82.
- Feenstra, Robert C and John Romalis (2014) "International prices and endogenous quality," *The Quarterly Journal of Economics*, 129 (2), 477–527.
- Furusawa, Taiji, Shoki Kusaka, and Yoichi Sugita (2022) "The Impacts of AI, Robots, and Globalization on Labor Markets: Analysis of a Quantitative General Equilibrium Trade Model," in *Robots and AI*, 123–149: Routledge.
- Grossman, Gene M and Elhanan Helpman (1991) "Trade, knowledge spillovers, and growth," *European economic review*, 35 (2-3), 517–526.

- Grossman, Gene M and Esteban Rossi-Hansberg (2008) "Trading tasks: A simple theory of offshoring," *American Economic Review*, 98 (5), 1978–1997.
- Hall, Robert E and Charles I Jones (1999) "Why do some countries produce so much more output per worker than others?" *The Quarterly Journal of Economics*, 114 (1), 83–116.
- Hanson, Gordon H, Nelson Lind, and Marc-Andreas Muendler (2015) "The dynamics of comparative advantage," Technical report, National bureau of economic research.
- Katz, Lawrence F and Kevin M Murphy (1992) "Changes in relative wages, 1963–1987: supply and demand factors," *The Quarterly Journal of Economics*, 107 (1), 35–78.
- Krugman, Paul (1979) "A model of innovation, technology transfer, and the world distribution of income," *Journal of political economy*, 87 (2), 253–266.
- Leamer, Edward E. (1984) Sources of International Comparative Advantage: Theory and Evidence: MIT Press.
- Levchenko, Andrei A (2007) "Institutional quality and international trade," *The Review of Economic Studies*, 74 (3), 791–819.
- Levchenko, Andrei A and Jing Zhang (2016) "The evolution of comparative advantage: Measurement and welfare implications," *Journal of Monetary Economics*, 78, 96–111.
- Loebbing, Jonas (2022) "An elementary theory of directed technical change and wage inequality," *The Review of Economic Studies*, 89 (1), 411–451.
- Morrow, Peter M (2010) "Ricardian–Heckscher–Ohlin comparative advantage: Theory and evidence," *Journal of International Economics*, 82 (2), 137–151.
- Morrow, Peter M and Daniel Trefler (2022) "How do endowments determine trade? quantifying the output mix, factor price, and skill-biased technology channels," *Journal of International Economics*, 137 (C).
- Nunn, Nathan (2007) "Relationship-specificity, incomplete contracts, and the pattern of trade," *The Quarterly Journal of Economics*, 122 (2), 569–600.
- OECD (2010) ""Main Economic Indicators complete database", Main Economic Indicators (database) Consumer Price Index: All Items for the United States [US-ACPIALLAINMEI]," http://dx.doi.org/10.1787/data-00052-en, Retrieved from FRED, Federal Reserve Bank of St. Louis; https://fred.stlouisfed.org/series/USACPIALLAINMEI, February 18, 2023.

- Parro, Fernando (2013) "Capital-skill complementarity and the skill premium in a quantitative model of trade," *American Economic Journal: Macroeconomics*, 5 (2), 72–117.
- Redding, Stephen (1999) "Dynamic comparative advantage and the welfare effects of trade," Oxford Economic Papers, 51 (1), 15–39.
- Romalis, John (2004) "Factor proportions and the structure of commodity trade," *American Economic Review*, 94 (1), 67–97.
- Schott, Peter K (2004) "Across-product versus within-product specialization in international trade," *The Quarterly Journal of Economics*, 119 (2), 647–678.
- Silva, JMC Santos and Silvana Tenreyro (2006) "The log of gravity," *The Review of Economics and Statistics*, 641–658.
- Thoenig, Mathias and Thierry Verdier (2003) "A theory of defensive skill-biased innovation and globalization," *American Economic Review*, 93 (3), 709–728.
- Timmer, Marcel P, Erik Dietzenbacher, Bart Los, Robert Stehrer, and Gaaitzen J De Vries (2015) "An illustrated user guide to the world input–output database: the case of global automotive production," *Review of International Economics*, 23 (3), 575–605.
- Trefler, Daniel (1993) "International factor price differences: Leontief was right!," *Journal of Political Economy*, 101 (6), 961–987.
- ———— (1995) "The case of the missing trade and other mysteries," *The American Economic Review*, 1029–1046.
- Ventura, Jaume (1997) "Growth and interdependence," *The Quarterly Journal of Economics*, 112 (1), 57–84.
- Wood, Adrian (1994) *North-South trade, employment and inequality: changing fortunes in a skill-driven world*: Clarendon Press.
- Young, Alwyn (1995) "The tyranny of numbers: confronting the statistical realities of the East Asian growth experience," *The quarterly journal of economics*, 110 (3), 641–680.

A Data Construction

A.1 Bilateral Trade Flow Data

First, I take the bilateral trade flow data from the UN Comtrade data.²¹ I take annual values of traded goods from 1964 to 2016 across 4-digit SITC product categories in SITC Rev. 2. I convert all trade flows into real 2015 US dollars using the US CPI from OECD (2010).

Second, using the cleaner provided by Feenstra and Romalis (2014), I construct bilateral trade flow data at the SITC Rev.2, 4-digit level across origin and destination pairs over time. This step gives primacy to importer's reports over exporter's reports where available, corrects values where UN values are known to be inaccurate, and accounts for re-exports of Chinese goods through Hong Kong.²²

Third, I combine countries, which reunify or report jointly for subsets of years in the database. I combined East and West Germany before the reunification, Belgium and Luxembourg; the islands that formed the Netherlands Antilles; North and South Yemen; and Sudan and South Sudan.

Fourth, I convert the data at the 4-digit SITC Rev.2 classification into the 4-digit SIC categories. I first map the 4-digit SITC data into the 6-digit HS 1996/2002 classification using the crosswalk provided by the United Nations. I then covert it into 4-digit SIC categories using the crosswalk by Autor et al. (2013).²³ ²⁴

Finally, to remove fluctuations at annual frequency, I take moving averages over three years. For instance, to get trade flows in 2000, I take averages of the values in 1999, 2000, and 2001.

A.2 Automation and Offshoring Data

My primary measure for automation is robot adoption data from the International Federation of Robots (IFR). It is available across countries and 2-digit sectors. For country groups, I take the countries with the number of robots in 2014 above the median as high-automation countries and the rest as low-automation countries. These high-automation countries include Japan, the US, China, South Korea, Germany, and others and have a

²¹Bulk downloads are available on their United Nation's web page here.

²²Their cleaner is available here.

²³The crosswalk is available in the UNSD web page here.

²⁴The crosswalk is available in David Dorn's web page here. sic87dd is an industry classification, which Autor et al. (2013) slightly modified the SIC 4-digit code in 1987 to make the classification time-consistent. See Autor et al. (2013) for details.

share of 99% of the world total. For sector groups, I take the Electronic & Other Electric Equipment sector, Transportation Equipment sector, and Plastic Chemical sector as the high-automation sectors and the rest as low-automation sectors.

My primary measure for offshoring is the share of foreign intermediate inputs, following Feenstra and Hanson (1996). For country groups, I use the data from World Input-Output Database (Timmer et al., 2015), the Long-run WIOD covering the period 1965-2000 and the Release 2016 covering the period 2000-2014. I compute the increases in the offshoring share from 1980 to 2014 and take countries above the median value of the increase in offshoring share. For sector groups, I use the US Input-Output Table as in Feenstra and Hanson (1996). I convert 6-digit sectoral categories in the IO Table into 4-digit sic codes, which I use in this paper. Since the Input-Output Table is published every five years between 1982 and 2017, I compute the increases in the offshoring share from 1982 to 2017 and take sectors above the median value of the increase in offshoring share.

B Details for Figure 1

B.1 Details on Data Construction and Definition

Definition G10 countries are Belgium, Canada, France, Germany, Italy, Japan, Netherlands, Sweden, Switzerland, the United Kingdom, and the United States.

Export data is from the UN Comtrade Data. The skill intensity is defined as the share of non-production workers' payroll in total value-added in each sector in the US from the NBER CES Manufacturing Database (Becker et al., 2021).

B.2 Robustness

Figure B.1 shows the figures for the evolution of revealed comparative advantage of G10 countries between 1965 and 2015, for every five years. It shows that the revealed comparative advantage in skill-intensive sectors is gradually weakening but that the speed has accelerated in the 2000s.

Figure B.1: Revealed Comparative Advantage of G10 Countries in Skill-Intensive Sectors: Different Years

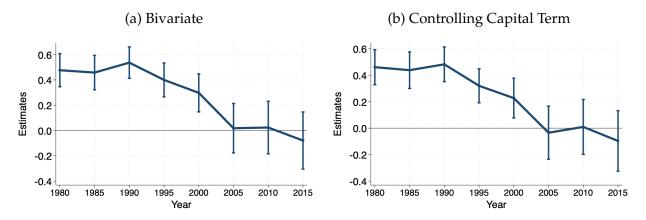


Notes: The figures show binned scatter-plots of revealed comparative advantage, a country's share of global exports in a sector divided by its share of aggregate global exports, for G10 countries across 397 four-digit sectors with different skill intensities, which I define as the share of non-production workers' payroll in value-added in the US each year. Export data is from the Comtrade database, and skill intensity data is from the US NBER CES Manufacturing Database (Becker et al., 2021). G10 countries are Belgium, Canada, France, Germany, Italy, Japan, Netherlands, Sweden, Switzerland, United Kingdom, and the United States.

C Robustness Checks for Section 2

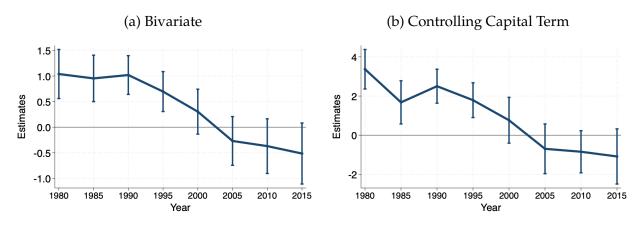
This section shows the robustness of the result presented in Section 2.

Figure C.2: Estimates of Importance of Skills in Comparative Advantage: Specification of Chor (2010)



Note: The figures show the estimates of coefficients β_t in equation (4) in each point time separately. The skill intensity measure is the log factor used in each sector in the US, $\ln(H_s/L_s)$, as in Chor (2010), instead of the skill intensity in the main specification. The bars indicate 95% confidence intervals based on heteroskedasticity-robust standard errors, clustered at the origin-sector level.

Figure C.3: Estimates of Importance of Skills in Comparative Advantage: Specification of Romalis (2004)



Note: The figures show the estimates of coefficients β_t using a total export as an outcome in each point time separately. The bars indicate 95% confidence intervals based on heteroskedasticity-robust standard errors, clustered at the origin-sector level.

D Robustness Checks for Section 3

This section shows the robustness of the result presented in Section 3. In particular, I provide two versions of robustness checks for Table 1.

Table D.1 shows the results without the linear trend. As before, the estimates of the coefficients on the interaction between the "Skill Term" and the automation share are negative and have similar magnitudes around -3. Moreover, since I do not include time trends, the quantitative importance of automation in the change in $\hat{\beta}_t$ is easy to understand. Let's focus on Column (2). Suppose that a country-sector pair has zero automation. Then, $\hat{\beta}_0 = 1.08$ with the standard error of 0.60. Then, suppose that the automation share is 33%, which is about the top 25 percentile value in 2015. This leads to $\hat{\beta}_t = 1.08 - 3.41 \times 0.33 \approx -0.05$, implying that the skill abundance is not important for the comparative advantage for country-sector pairs with the automation shares higher than the top 25 percentile value.

Table D.1: Importance of Skill Abundance in Comparative Advantage: Roles of Automation and Offshoring, Continuous Measures, Without the Linear Time Trend

	Dep. Var. Log Trade Flow				
	(1)	(2)	(3)	(4)	
Skill Term	-0.37	1.08	-0.54	0.94	
	(0.50)	(0.60)	(0.55)	(0.67)	
x Automation Share		-3.41		-3.27	
		(1.03)		(1.04)	
x Offshoring Share			0.49	0.25	
			(0.43)	(0.41)	
Observations	1,528,800	1,528,800	1,523,612	1,523,612	
Origin-Dest-Year FE	\checkmark	\checkmark	\checkmark	\checkmark	
Dest-Sector-Year FE	\checkmark	\checkmark	\checkmark	\checkmark	

Notes: The table shows the results for the importance of skill abundance in comparative advantage, based on the specification for β_t in equation (8). The dependent variable is the bilateral trade flow. All columns include the interaction between the exporter's skill abundance and the sector's skill intensity, "Skill Term", as the running variable. Columns (2) and (4) include the interaction between "Skill Term" and the automation share. Columns (3) and (4) include the interaction between "Skill Term" and the offshoring share. All the columns include origin-exporter-year fixed effects and importer-sector fixed effects. The standard errors are in parentheses and clustered at the exporter-sector level.

Table D.2 shows the results when I control the interaction between the exporter's capital abundance and the sector's capital intensity. Again, the magnitudes of the coefficient that represents the role of automation in the importance of skill abundance for comparative advantage are similar, which are around -3.0.

Table D.2: Importance of Skill Abundance in Comparative Advantage: Roles of Automation and Offshoring, Continuous Measures, With Capital Term

	Dep. Var. Log Trade Flow				
	(1)	(2)	(3)	(4)	
Skill Term	2.34	3.44	2.22	3.39	
	(0.58)	(0.66)	(0.63)	(0.73)	
x Automation Share		-3.00		-2.94	
		(1.03)		(1.04)	
x Offshoring Share			0.33	0.12	
			(0.42)	(0.41)	
x Linear Trend	-1.11	-1.00	-1.11	-1.01	
	(0.18)	(0.17)	(0.18)	(0.17)	
Capital Term	1.20	1.18	1.19	1.17	
	(0.26)	(0.25)	(0.26)	(0.25)	
Observations	1,528,800	1,528,800	1,523,612	1,523,612	
Origin-Dest-Year FE	\checkmark	\checkmark	\checkmark	\checkmark	
Dest-Sector-Year FE	\checkmark	\checkmark	\checkmark	\checkmark	

Notes: The table shows the results for the importance of skill abundance in comparative advantage, based on the specification for β_t in equation (8). The dependent variable is the bilateral trade flow. All columns include the interaction between the exporter's skill abundance and the sector's skill intensity, "Skill Term", and the interaction between the exporter's capital abundance and the sector's capital intensity, "Capital Term", as the running variables. Columns (2) and (4) include the interaction between "Skill Term" and the automation share. Columns (3) and (4) include the interaction between "Skill Term" and the offshoring share. All the columns include origin-exporter-year fixed effects and importer-sector fixed effects. The standard errors are in parentheses and clustered at the exporter-sector level.

E Theory Appendix

E.1 Supply of Machines and Intermediates

Here, I explain how machines and intermediates are sourced from different countries and sectors.

Machines Firms can either use domestic or foreign machines. The machine used in the country i and sector s is the combination of the machines sourced from different sectors.

$$M_{i,s} = \prod_{r} M_{i,rs}^{\alpha_{i,rs}^M},$$

where $M_{i,rs}$ is the machine sourced from sector r, and $\alpha_{i,rs}^M$ is the input-output coefficient for machines, which sums up to one as $\sum_r \alpha_{i,rs}^M = 1$.

The machine sourced from sector r can be sourced from domestic or foreign suppliers. Following the Caliendo and Parro (2015) for intermediates, producers of composite machines in country j and sector r supply $M_{j,r}^S$ at minimum cost by purchasing machine from the lowest cost suppliers across countries. This leads to the usual Eaton-Kortum style price aggregates as in (13).

Domestic Intermediates Firms combine intermediates from different sectors with the input-output coefficient for intermediates $\alpha_{i,rs}^X$, which sums up to one as $\sum_r \alpha_{i,rs}^X = 1$. $\alpha_{i,rs}^X$ is the cost share of intermediates from sector r when producing goods s in country i.

Then, the domestic intermediates used in country i and sector s are given by

$$XD_{i,s} = \prod_{r} XD_{i,rs}^{\alpha_{i,rs}^X}.$$

Foreign Intermediates Firms can also have access to foreign intermediates. Across sectors,

$$XF_{i,s} = \prod_{r} (XF_{i,rs})^{\alpha_{i,rs}^X},$$

where $\alpha_{i,rs}^{X}$ is the input-output coefficient for intermediates.

Following Caliendo and Parro (2015), the price of foreign intermediates follows (16).

F Exact Hat Algebra

In this paper, I follow Dekle et al. (2008) to use the exact hat algebra to focus on changes of variables. Here I show the equilibrium conditions, in hat notations, that is $\hat{X} = X'/X$, where X' is a new value in a counterfactual equilibrium for a variable X.

The equilibrium in changes can be characterized by the changes in wages $\{\widehat{w}_i^{\widehat{H}}, \widehat{w}_i^{\widehat{L}}\}$ where the following systems of equations holds.

Labor Demand

$$\begin{split} w_i^L L_i \widehat{w_i^L} \widehat{L}_i &= \sum_s (\Gamma_{i,s}^L)' \cdot (1 - \alpha_s^H) \cdot (Y_{i,s})' \\ w_i^H H_i \widehat{w_i^H} \widehat{H}_i &= \sum_s \alpha_s^H \cdot (Y_{i,s})' \end{split}$$

Goods Market Clearing

$$\begin{split} (Y_{i,s})' &= \sum_{j} \pi^{F}_{ij,s} \widehat{\pi^{F}_{ij,s}} \mu_{j,s} \left(w^{L}_{i} L_{i} \widehat{w^{L}_{i}} \widehat{L}_{i} + w^{H}_{i} H_{i} \widehat{w^{H}_{i}} \widehat{H}_{i} \right) \\ &+ \sum_{j} \sum_{r} \pi^{M}_{ij,r} \widehat{\pi^{M}_{ij,r}} \alpha^{M}_{j,sr} (1 - \alpha^{H}_{r}) (\Gamma^{M}_{j,r})' (Y_{j,r})' \\ &+ \sum_{r} \alpha^{X}_{i,sr} (1 - \alpha^{H}_{r}) (\Gamma^{XD}_{i,r})' (Y_{i,r})' \\ &+ \sum_{j} \sum_{r} \pi^{X}_{ij,r} \widehat{\pi^{X}_{ij,r}} \alpha^{X}_{j,sr} (1 - \alpha^{H}_{r}) (\Gamma^{XF}_{j,r})' (Y_{j,r})' \end{split}$$

Trade Shares

$$\widehat{\pi_{j,i,r}^F} = \frac{(\widehat{c_{j,r}}\widehat{\tau_{j,i,r}^F})^{1-\sigma}}{\sum_{l} \pi_{l,i,r}^F (\widehat{c_{l,r}}\widehat{\tau_{l,i,r}^F})^{1-\sigma}}, \quad \widehat{\pi_{j,i,r}^M} = \frac{(\widehat{c_{j,r}}\widehat{\tau_{j,i,r}^M})^{1-\sigma}}{\sum_{l} \pi_{l,i,r}^M (\widehat{c_{l,r}}\widehat{\tau_{l,i,r}^M})^{1-\sigma}}, \quad \widehat{\pi_{j,i,r}^{XF}} = \frac{(\widehat{c_{j,r}}\widehat{\tau_{j,i,r}^X}})^{1-\sigma}}{\sum_{l \neq j} \pi_{l,i,r}^{XF} (\widehat{c_{l,r}}\widehat{\tau_{l,i,r}^X})^{1-\sigma}}$$

Unit Cost

$$\begin{split} \widehat{c_{i,s}} &= (\widehat{w_i^H})^{\alpha_s^H} \cdot (\widehat{w_{i,s}^T})^{1-\alpha_s^H}, \\ \widehat{w_{i,s}^T} &= \prod_{f = \{M,L,XD,XF\}} \cdot \left(\frac{\widehat{w_i^f}}{\widehat{A^f}\Gamma_{i,s}^f}\right)^{\Gamma_{i,s}^f} \times (\Pi_{i,s}^M)^{(\Gamma_{i,s}^M)' - \Gamma_{i,s}^M} \cdot (\Pi_{i,s}^{XF})^{(\Gamma_{i,s}^{XF})' - \Gamma_{i,s}^{XF}} \end{split}$$

where $\Pi^{M}_{i,s}$ and $\Pi^{XF}_{i,s}$ are cost saving from automation and offshoring, which are exogenous variables.

Machine Price

$$\widehat{w_{i,s}^M} = \prod_r \left(\frac{\widehat{w_{i,rs}^M}}{\alpha_{i,rs}^M} \right)^{\alpha_{i,rs}^M}, \quad \widehat{w_{i,rs}^M} = \left(\sum_j (\widehat{c_{j,r}} \widehat{\tau_{ji,r}^M})^{-\theta} \right)^{-1/\theta}$$

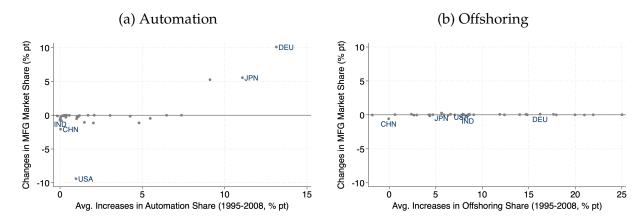
Intermediate Price

$$\widehat{w_{i,s}^{XD}} = \prod_{r} \left(\frac{\widehat{c_{i,r}}}{\alpha_{i,rs}^{X}} \right)^{\alpha_{i,rs}^{X}}, \quad \widehat{w_{i,s}^{XF}} = \prod_{r} \left(\frac{\widehat{w_{i,rs}^{XF}}}{\alpha_{i,rs}^{X}} \right)^{\alpha_{i,rs}^{X}}, \quad \widehat{w_{i,rs}^{XF}} = \left(\sum_{j \neq i} (\widehat{c_{j,r}} \widehat{\tau_{ji,r}^{X}})^{-\theta} \right)^{-1/\theta}.$$

G Additional Quantitative Results

G.1 Manufacturing Market Share in the World

Figure G.4: Changes in Manufacturing Market Share in the World



Notes: Figures G.4a and G.4b show the changes in manufacturing market shares in the world.