

MODULE *RWSet*

CONSTANTS *Key*, *Version*, *Value*, *NULL*

$State \triangleq [Key \rightarrow (Value \cup NULL)]$

CONSTANTS *Operation*

CONSTANTS *Apply*(-, -, -)

ASSUME $\forall s0 \in State, s1 \in State, f \in Operation : Apply(s0, f, s1) \in \text{BOOLEAN}$

$Deterministic(f) \triangleq$
 $\forall s0, s1, s2 \in State : Apply(s0, f, s1) \wedge Apply(s0, f, s2) \Rightarrow s1 = s2$

CONSTANT *WriteSet*, *ComputeWS*(-, -), *Commit*(-, -)
ASSUME $\forall s1, s2 \in State : ComputeWS(s1, s2) \in WriteSet$
ASSUME $\forall s \in State, ws \in WriteSet : Commit(s, ws) \in State$
ASSUME $\forall s1, s2 \in State : Commit(s1, ComputeWS(s1, s2)) = s2$

CONSTANTS *Simulate*(-, -, -)

ASSUME $\forall s0, f, rw : Simulate(s0, f, rw) \in \text{BOOLEAN}$

$$\begin{aligned}
SefetyOfWriteSet &\triangleq \text{TRUE} \\
SefetyOfReadSet &\triangleq \text{TRUE} \\
SafetyOfSimulation &\triangleq SefetyOfWriteSet \wedge SefetyOfReadSet
\end{aligned}$$

$$\begin{aligned}
ReadSetOK(s, ruset) &\triangleq \text{TRUE} \quad s \text{ satisfies } ruset \text{ condition (= MVCC condition)} \\
ApplyTx(s1, f, s2) &\triangleq \text{TRUE} \quad f(s1) = s2 \\
ApplyWriteSet(s1, ruset, s2) &\triangleq \text{TRUE} \quad \text{committing } WriteSet \text{ } ruset \text{ at state } s1 \text{ results in state } s2
\end{aligned}$$

$$\begin{aligned}
SafetyOfCommit &\triangleq \forall ss0, ss1, s, s1, s2 \in State, f, ruset \in RWSet : \\
Simulate(ss0, f, ss1, ruset) &\wedge ReadSetOK(s, ruset) \wedge ApplyTx(s, f, s1) \wedge ApplyWriteSet(s, ruset, s2) \Rightarrow s1 = s2
\end{aligned}$$
