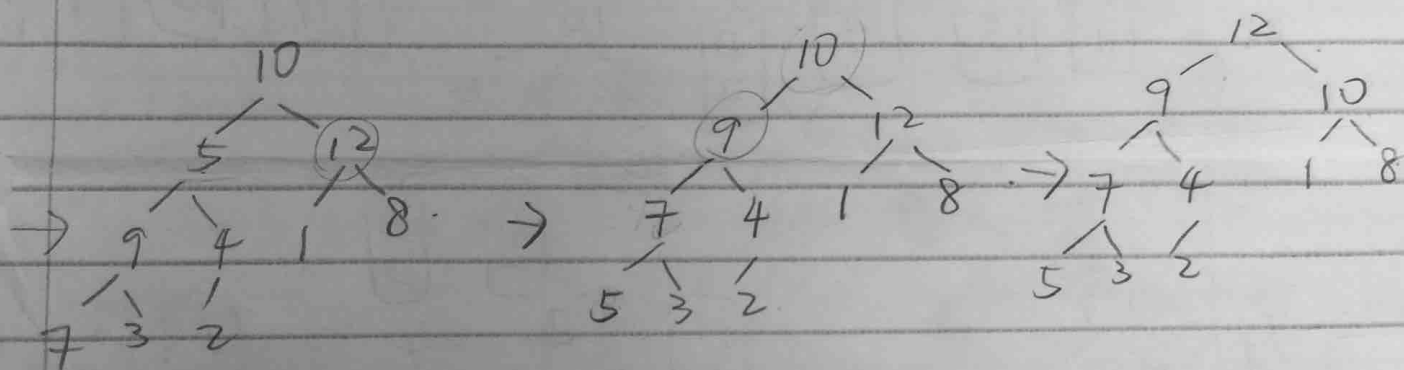
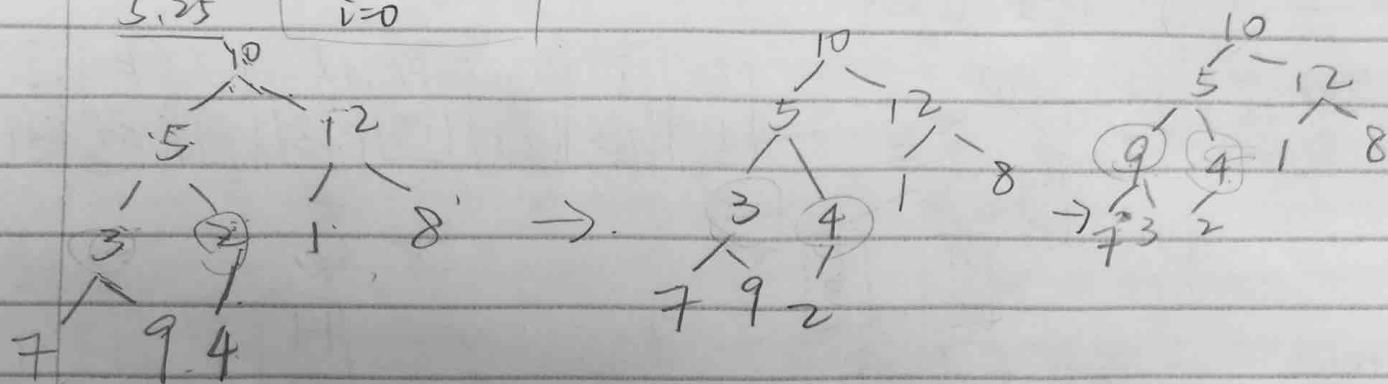


5.23

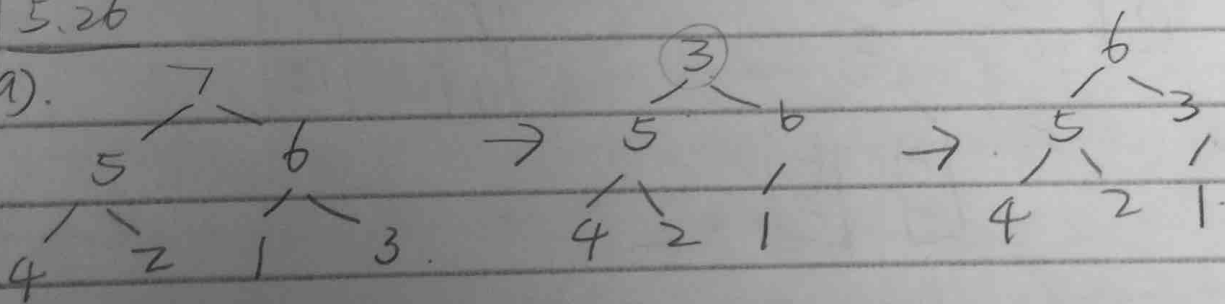
$$\begin{aligned} \circ \min &= \sum_{i=0}^{h-1} 2^i + 1 \\ \circ \max &= \sum_{i=0}^h 2^i \end{aligned}$$

5.25

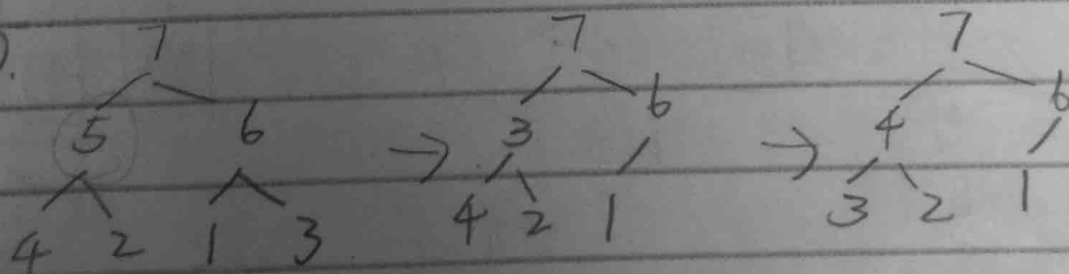


5.26

(a).

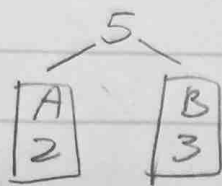


(b).



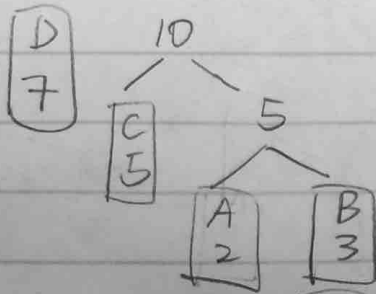
5.28

Step 1:



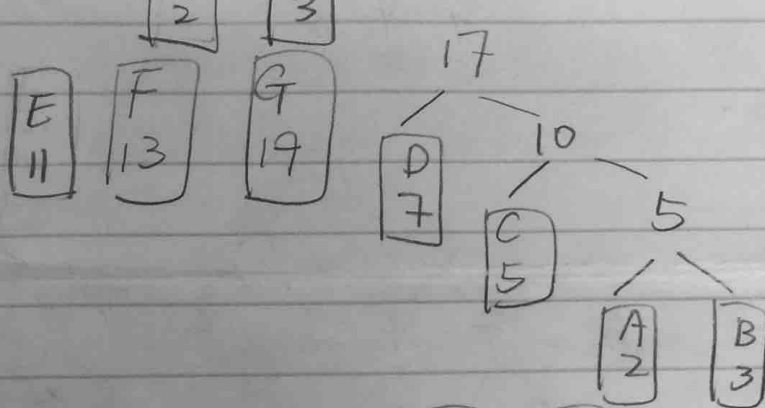
C	D	E	F	G	H	I	J	K	L
5	7	11	13	17	19	23	31	37	41

Step 2:



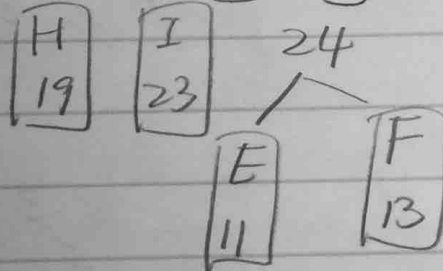
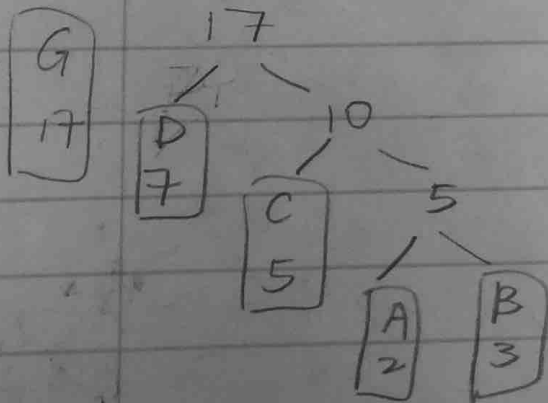
E	F	G	H	I	J	K	L
11	13	17	19	23	31	37	41

Step 3:



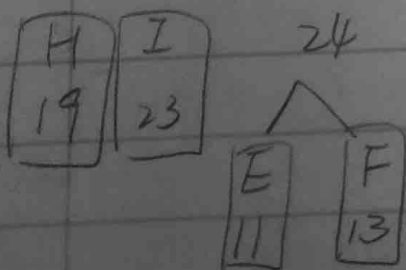
H	I	J	K	L
19	23	31	37	41

Step 4:

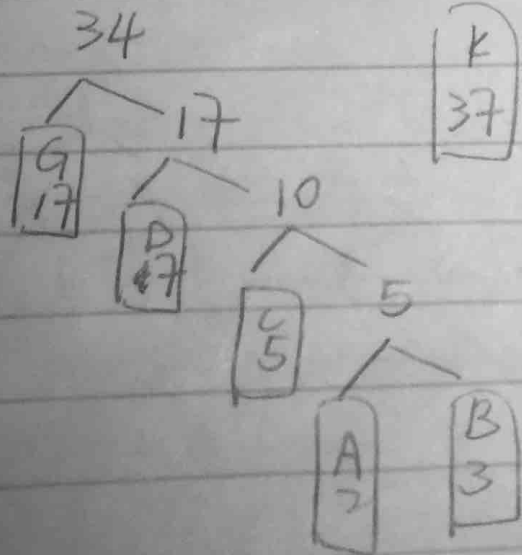


J	K	L
31	37	41

Step 5:

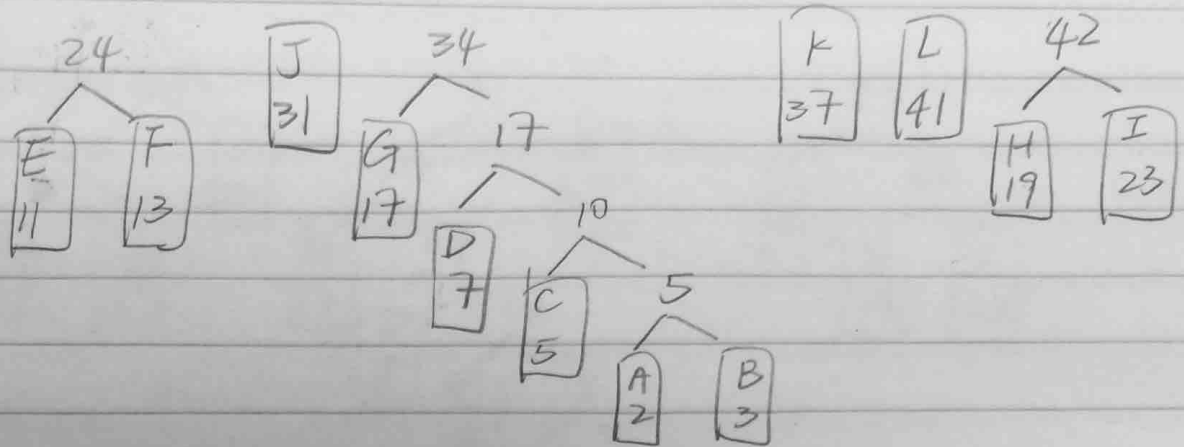


J
31

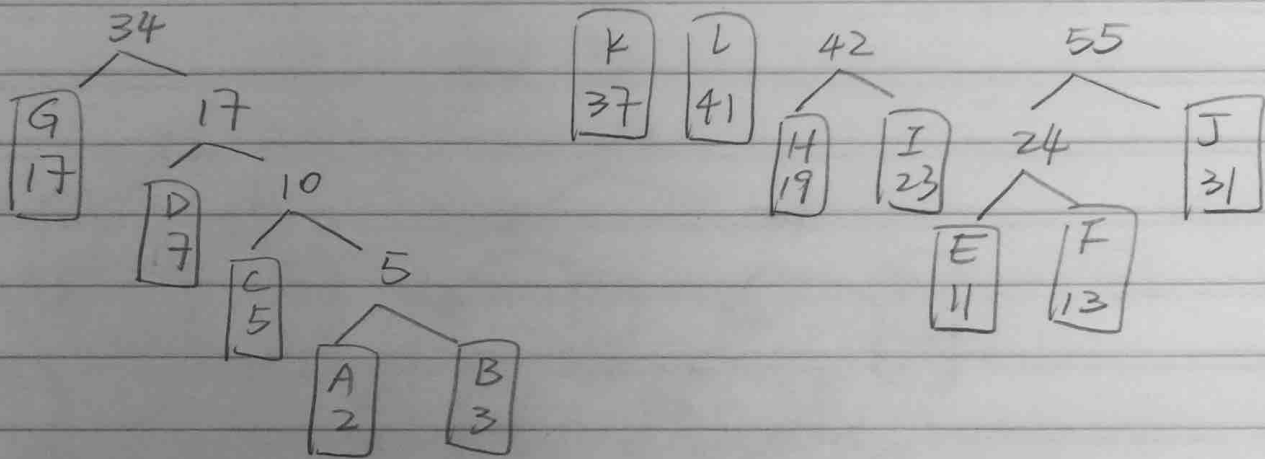


K	L
37	41

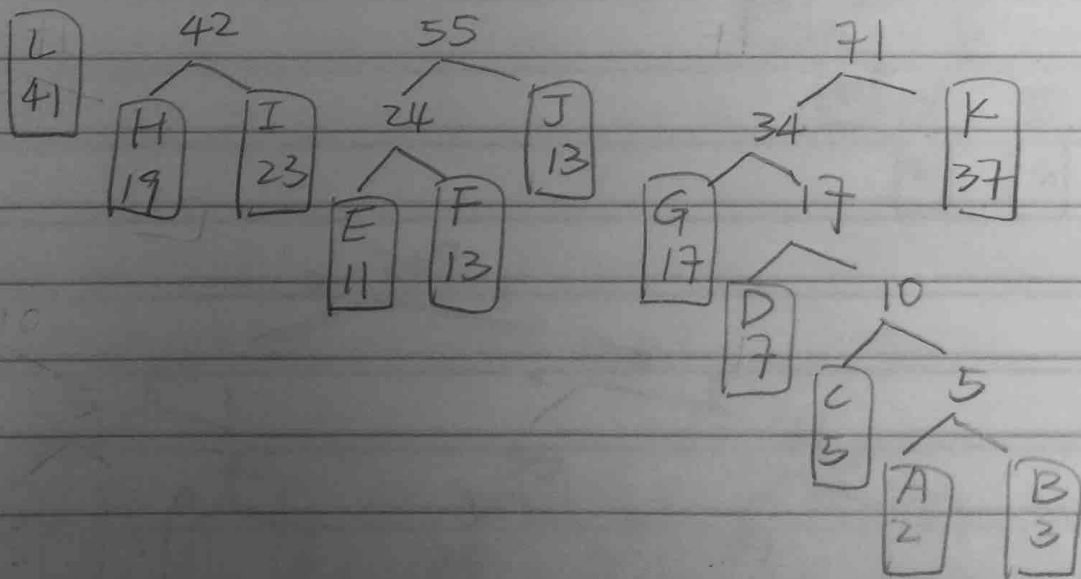
Step 6:



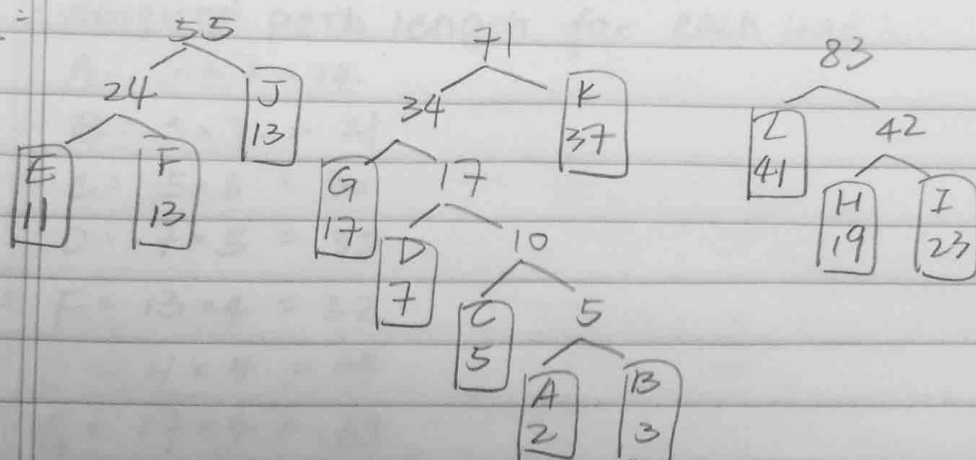
Step 7:



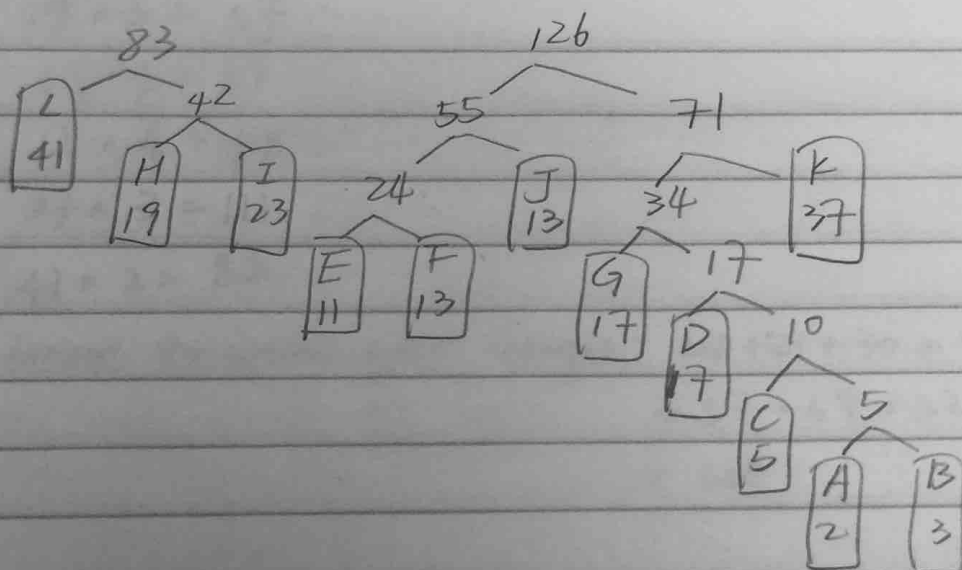
Step 8:



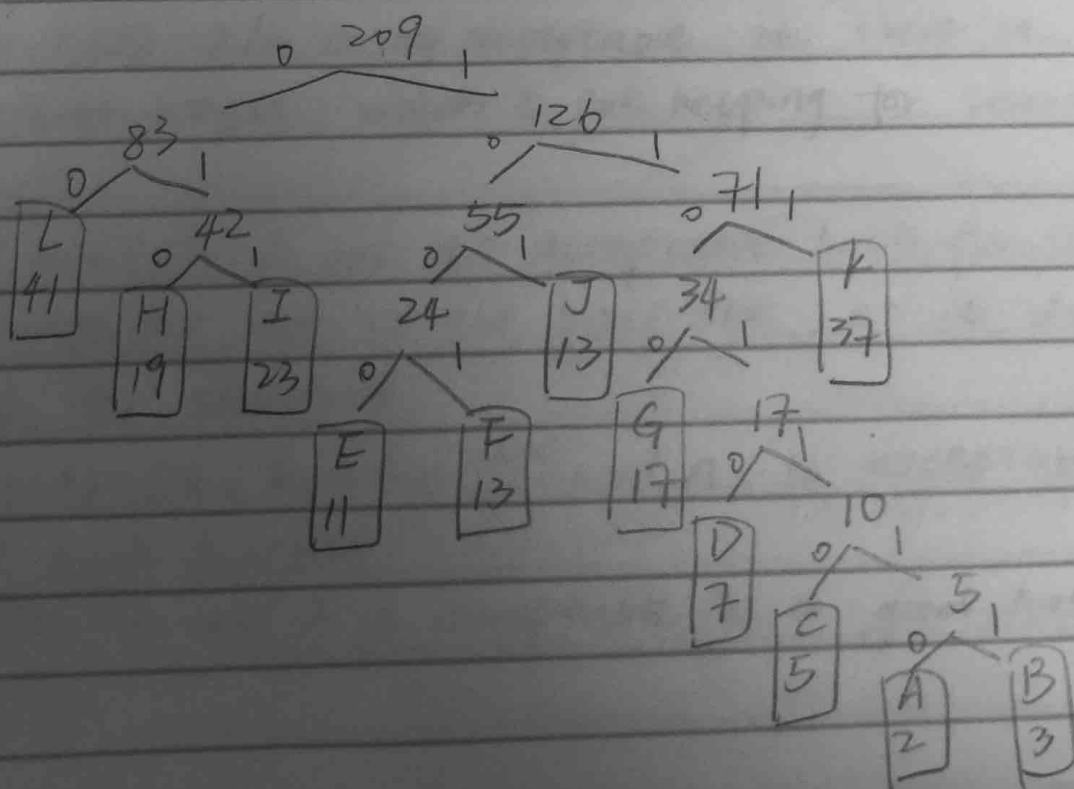
Step 9:



Step 10:



Step 11:



• Weighted path length for each leaf =

$$A = 2 \times 7 = 14$$

$$B = 3 \times 7 = 21$$

$$C = 5 \times 6 = 30$$

$$D = 7 \times 5 = 35$$

$$\nearrow F = 13 \times 4 = 52$$

$$\nearrow E = 11 \times 4 = 44$$

$$G = 17 \times 4 = 68$$

$$H = 19 \times 3 = 57$$

$$I = 23 \times 3 = 69$$

$$J = 13 \times 4 = 52$$

$$K = 37 \times 3 = 111$$

$$L = 41 \times 2 = 82$$

$$\begin{aligned} \text{minimum external path weight} &= 14 + 21 + 30 + 35 + 52 + 44 + 68 \\ &\quad + 57 + 69 + 52 + 111 + 82 \\ &= 608. \end{aligned}$$

9.13.

(a).  $h(k) = k/n$  is not acceptable, b/c there're too many collision exists, which is not helping for searching.

(b)  $h(k) = 1$  is not an acceptable hash function b/c it maps all keys to the same slot, so it does not help for searching.

(c).  $h(k) = (k + \text{Random}(n)) \bmod n$ . is acceptable & is a good hash function.

(d)  $h(k) = k \bmod n$  is acceptable & a good hash function.

9.16

$m=10$

$ks = 3, 12, 9, 2, 79, 44$

	0		
5	1	2	
9	2	12	2
2	3	3	
1	4	44	
4	5		
8	6	79	
6	7		
3	8		
7	9	9	79

probability for each empty slot =

$$0 = 0$$

$$5 = \frac{2}{3}$$

$$7 = \frac{1}{3}$$

$$8 = 0$$

Exercise 13.1

42 12 100 10 50 31 7 11 99

$2^7 = 128 > 100$ , so each key is represented as a 7-bit value.

decimal      binary

42      0101010 X

12      0001100 X

100      1100100 X

10      0001010 X

50      0110010 X

31      0011111 X

7      0000111

11      0001011 X

99      1100011 X

binary tree :

