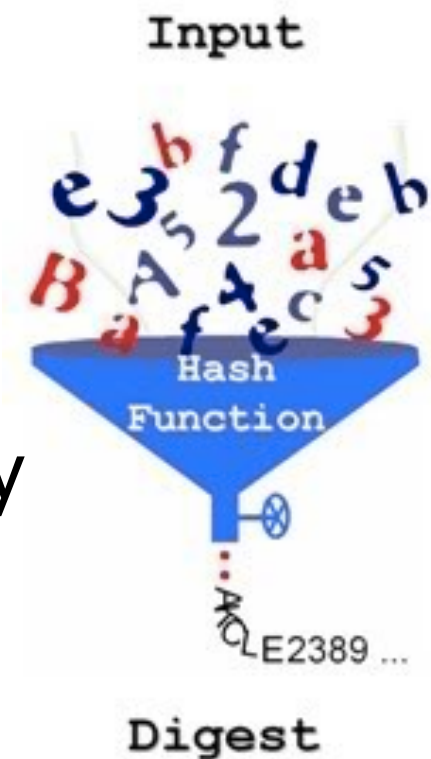


# Cryptographic Hashes

CS 458: Information Security  
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# Reading Material

- Text Chapters 2.2 and 21.1-2
- *Handbook of Applied Cryptography*,  
Menezes, van Oorschot, Vanstone
  - Chapter 9
  - <http://www.cacr.math.uwaterloo.ca/hac/>

# What is Hash or Checksum?

- Mathematical function to generate a set of  $k$  bits from a set of  $n$  bits
  - $k \leq n$  except in unusual circumstances
- Example: ASCII parity bit
  - ASCII has 7 bits; 8th bit is “parity”
  - Even parity: even number of 1 bits
  - Odd parity: odd number of 1 bits

# Example Use

- Bob receives "10111101" as bits.
  - Sender is using even parity;  
six 1 bits, so character was received correctly
    - Note: could be garbled, but 2 bits would need to have been changed to preserve parity
  - Sender is using odd parity; even number of 1 bits, so character was not received correctly

# Another Example

- 8-bit Cyclic Redundancy Check (CRC)
  - XOR all bytes in the file/message
  - Good for detecting accidental errors
  - But easy for malicious user to “fix up” to match altered message
- For example, change the 4<sup>th</sup> bit in one of the bytes. How to “fix up”?
  - Fix up by flipping the 4<sup>th</sup> bit in the CRC
- Easy to find a  $M'$  that has the same CRC

## **Q: Uses of hash functions?**

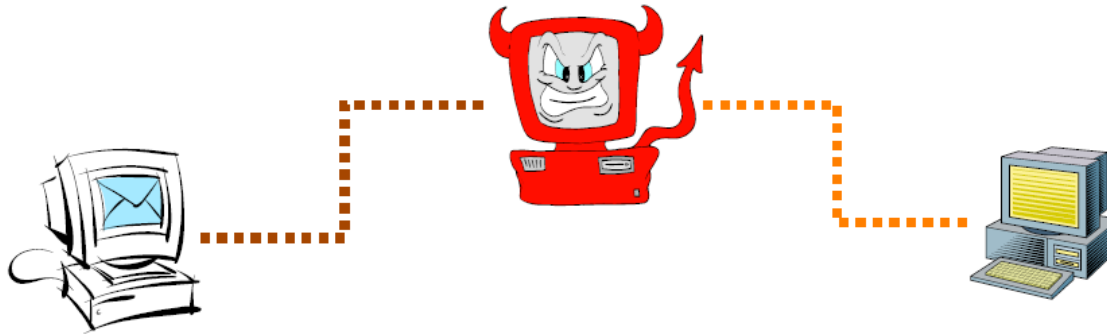
- Software integrity  
E.g., tripwire
- Message authentication
- One-time Passwords
- Digital signature

# Uses of hash functions

- [Apache HTTP Server](#) in .md5 file from web.
- [Cisco](#) MD5 for versions of IOS from Software Center on Cisco website.
- [Darwin](#) MD5 on web.
- [Fedora Project](#) SHA-1 on web and SHA1SUM file on ftp.
- [FreeBSD](#) on web and in CHECKSUM.MD5 and CHECKSUM.SHA256 files.
- [GCC](#) on ftp as md5.sum file.
- [Gentoo](#) as .md5 file on ftp.
- [GNOME](#) as MD5SUMS-for-gz and MD5SUMS-for-bz2 files on ftp.
- [GnuPG](#) SHA-1 on web.
- [KDE](#) on web and on ftp as MD5SUMS file.
- [Knoppix](#) in .md5 and .sha1 file.
- [MySQL](#) MD5 on web.
- [OpenOffice.org](#) MD5 on web.
- [OpenSSH](#) SHA-1 in release announcement.
- [OpenSSL](#) .md5 and .sha1 files linked to from web.
- [Perl](#) link to .md5 on web.
- [PostgreSQL](#) in a .md5 file.
- [Python](#) MD5 on web
- [Ubuntu](#) as MD5SUMS on ftp.
- [X.org](#) md5sums file on ftp.

Source: <http://microformats.org/wiki/hash-examples>

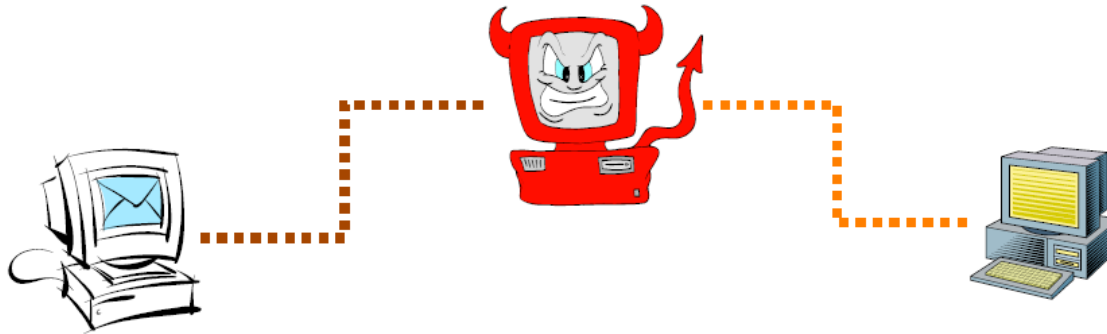
# Data Integrity and Source Authentication



- Integrity: detect unauthorized writing (i.e., modification of data)
- Encryption provides confidentiality (i.e., prevents unauthorized disclosure)
- Encryption alone does not provide integrity
  - One-time pad, ECB cut-and-paste, etc.



# Data Integrity



When data integrity is more important than confidentiality?

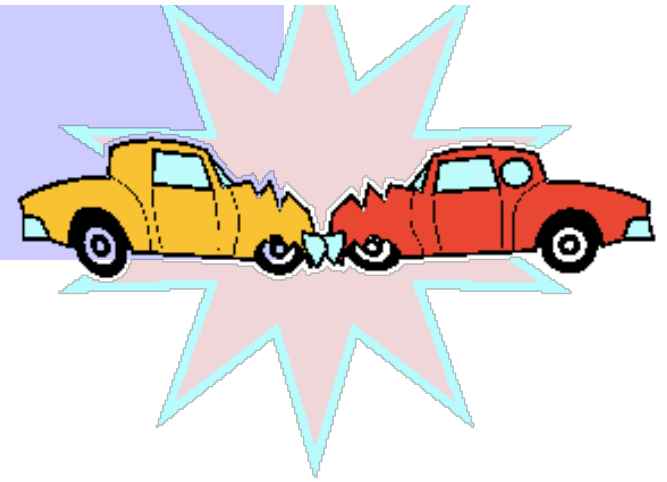
Example: Inter-bank fund transfers

Confidentiality may be nice, integrity is critical

# Secure Hash functions

- Crypto Hash or Checksum
  - Unencrypted **one-way** hash functions
  - Easy to compute hash
  - Hard to find message with a particular hash value
  - Use to verify integrity of publically available information
    - E.g., packets posted on mirror sites
- Message Authentication Code (MAC)
  - Hash to pass along with message
  - Such a hash must be accessed with **key**
    - Otherwise attacker could change MAC in transit

# Collisions



- If  $x \neq x'$  and  $h(x) = h(x')$ ,  
 $x$  and  $x'$  are a ***collision***

Why **collision** could happen?

- Pigeonhole principle: if there are  $n$  containers for  $n+1$  objects, then at least one container will have 2 objects in it.
- Application: if there are 32 files and 8 possible cryptographic checksum values, at least one value corresponds to at least 4 files

# Security Requirements for Cryptographic Hash Functions

Given a function  $h:X \rightarrow Y$ , then we say that  $h$  is:

- **preimage resistant (one-way)**  
if given  $y \in Y$  it is computationally infeasible to find a value  $x \in X$  s.t.  $h(x) = y$   
e.g., computing  $x^3$  vs cube root of  $x$  by hand
- **2nd preimage resistant (weak collision resistant)**  
if **given**  $x \in X$  it is computationally infeasible to find a value  $x' \in X$ , s.t.  $x' \neq x$  and  $h(x') = h(x)$
- **collision resistant (strong collision resistant)**  
if it is computationally infeasible to find two distinct values  $x', x \in X$ , s.t.  $h(x') = h(x)$

# Brute Force Attacks on Hash Functions

## Attacking one-wayness

- Goal: given  $h:X \rightarrow Y$ ,  $y \in Y$ , find  $x$  such that  $h(x)=y$
- Algorithm:
  - pick a random value  $x$  in  $X$ , check if  $h(x)=y$ , if  $h(x)=y$ , returns  $x$ ; otherwise iterate
  - after failing  $q$  iterations, return fail
- The average-case success probability (with replacement) is

$$\varepsilon = 1 - \left(1 - \frac{1}{|Y|}\right)^q \approx \frac{q}{|Y|}$$

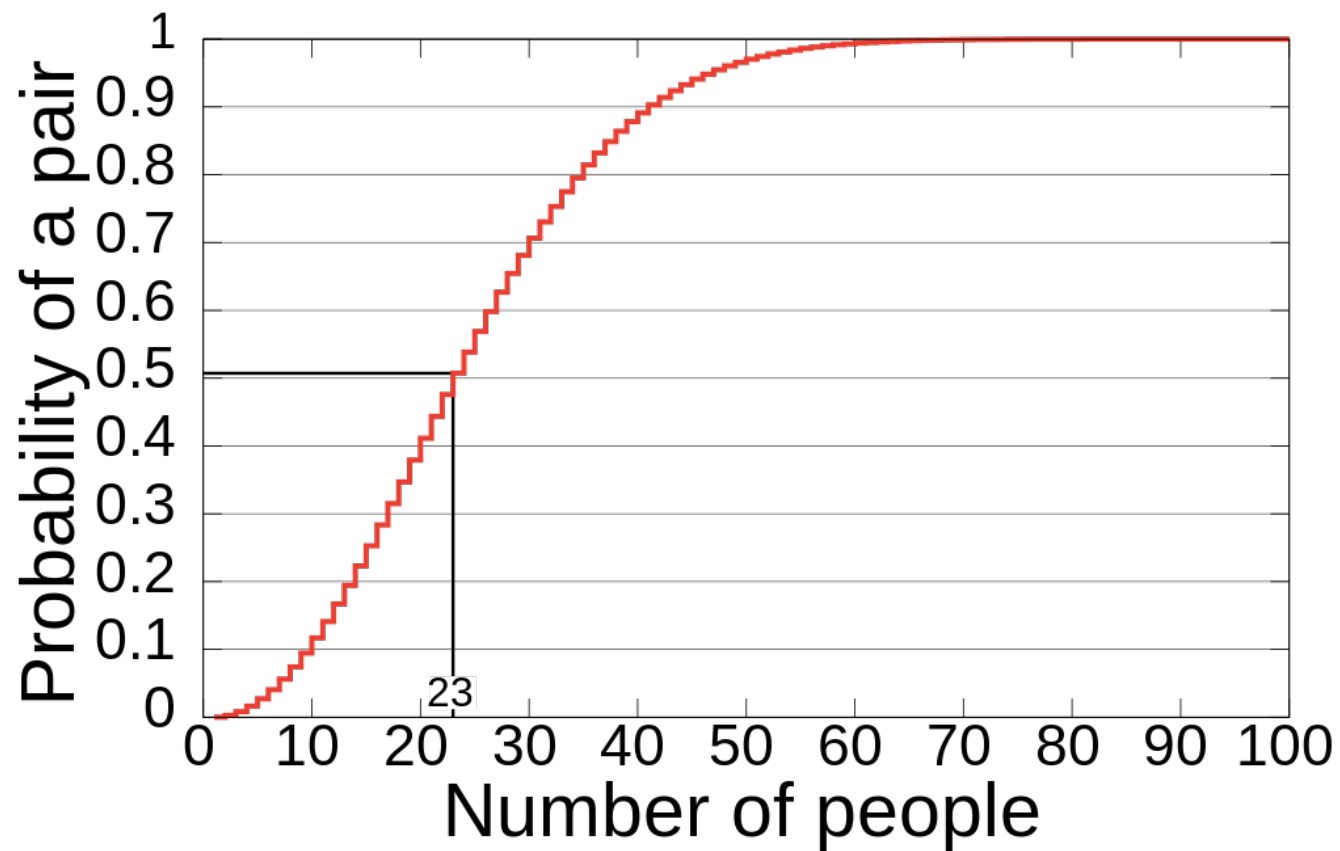
- Let  $|Y|=2^m$ , to get  $\varepsilon$  to be close to 0.5,  $q \approx 2^{m-1}$

# Birthday Paradox



- What is the probability that someone in the room has the same birthday as me?
- What is the probability that two people in the room have the same birthday?
  - $P(n) = 1 - (365! / (365^n * (365-n)!))$
  - Any 2 persons do not have the same bDay  
 $= 364/365 * 363/365 * 362/365 \dots 365-(n-1)/365$   
 $= [365 * 364 * \dots 365-(n-1)] / 365^n$   
 $= [365! / (365-n)!] / 365^n$
  - $P(n) > 1/2$  for  $n = 23$
  - Section 2.15 – Handbook of Applied Cryptography
  - [http://en.wikipedia.org/wiki/Birthday\\_paradox](http://en.wikipedia.org/wiki/Birthday_paradox)

# Birthday Paradox



# Birthday Paradox

- In general, probability of a collision reaches 50% for  $M$  units when
  - $n = \text{sqrt}(M)$
- If hash has  $m$  bits, this means  $M = 2^m$  possible hash values
  - $n = 2^{m/2}$  for 50% probability collision



# Another View of Collisions

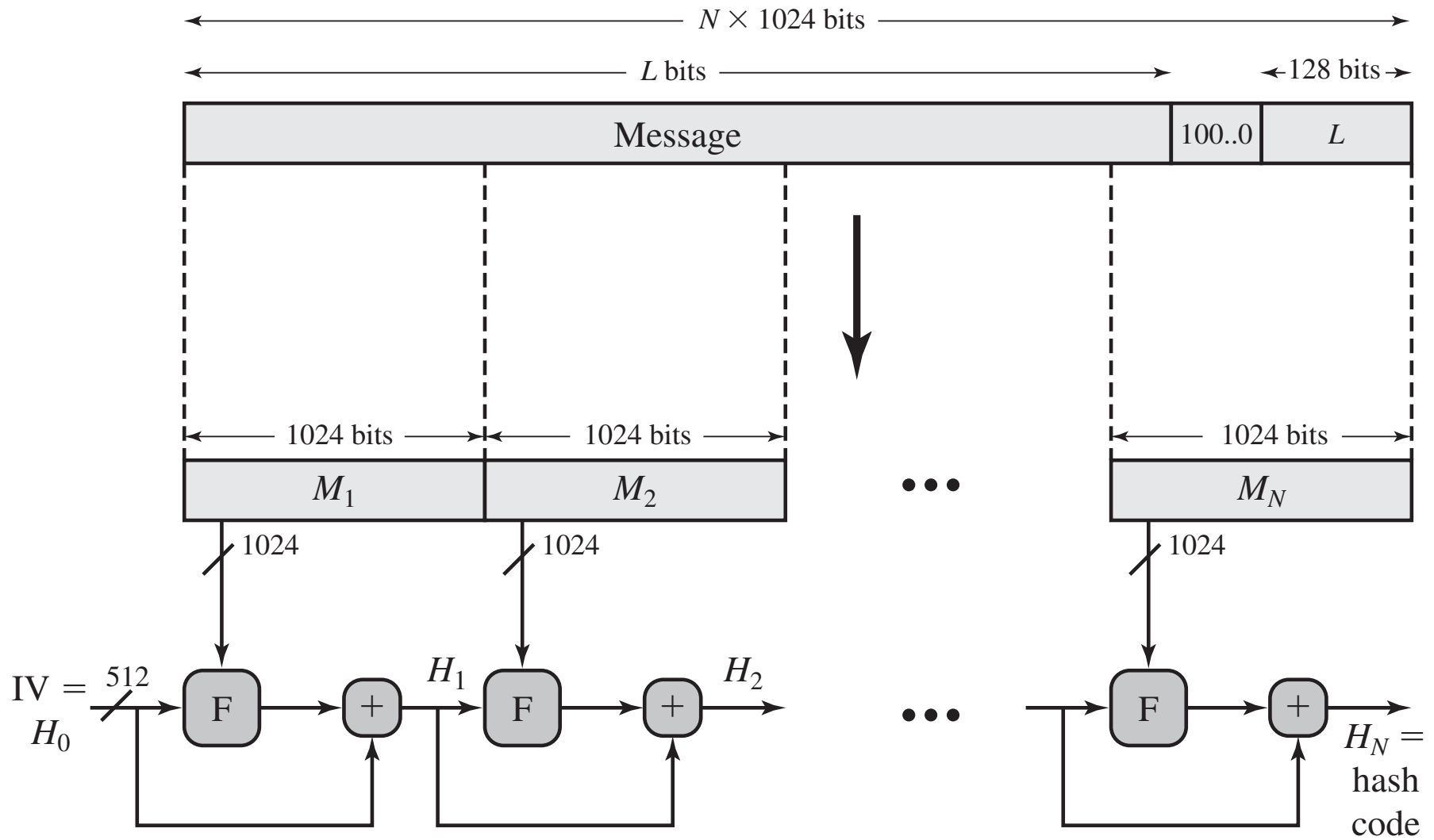
- **Birthday attack** works thus:
  - opponent generates  $2^{m/2}$  variations of a valid message all with essentially the same meaning
  - opponent also generates  $2^{m/2}$  variations of a desired fraudulent message
  - two sets of messages are compared to find pair with same hash (probability  $> 0.5$  by birthday paradox)
  - have user sign the valid message, then substitute the forgery which will have a valid signature
- Need to use larger MACs

# MD5 and SHA

- Most widely used **keyless crypto hashes**
- Both are round based bit operations
  - Similar in spirit to AES and DES
  - Looking for avalanche effect to make output appear random
- MD5 is 128 bits and SHA-1 is 160 bit
- Problem with MD5?

MD5 is only strong collision resistant to  $2^{64}$  bits. Too small.

# SHA



$+$  = word-by-word addition mod  $2^{64}$

# Message Authentication Codes

- MAC is a crypto hash that is a proof of a message's integrity
  - Important that adversary cannot fix up MAC if he/she changes message
- MAC's rely on **keys** to ensure integrity
  - Similar to a hash augmented with a key

# Hash vs. MAC

## Hash

1. Alice->Bob: Hash(M)
  - Transmission must be *authentic* (integrity), need not be secret
2. Alice->Bob: M
  - Can use insecure channel
  - Integrity of M assured

## MAC

1. Alice->Bob: K (*key*)
  - Transmission must be authentic *and confidential*
  - Only Alice and Bob know K
2. Alice->Bob: M, MAC<sub>K</sub>(M)
  - Bob can verify integrity of M (Others cannot)
  - M does not have to be known ahead of time

# Use Symmetric Ciphers for Keyed Hash

- Can use DES or AES in CBC mode
  - Last block is the hash
- DES with 64 bit block size is too small to be effective MAC

# HMAC

- Can compute a MAC of the message  $M$  with key  $K$ , using a “hashed MAC” or **HMAC**
- HMAC is a **keyed hash**
  - Why would we need a key?
- How to compute HMAC?
  - Two obvious choices:  $h(K,M)$  and  $h(M,K)$
  - Which is better?

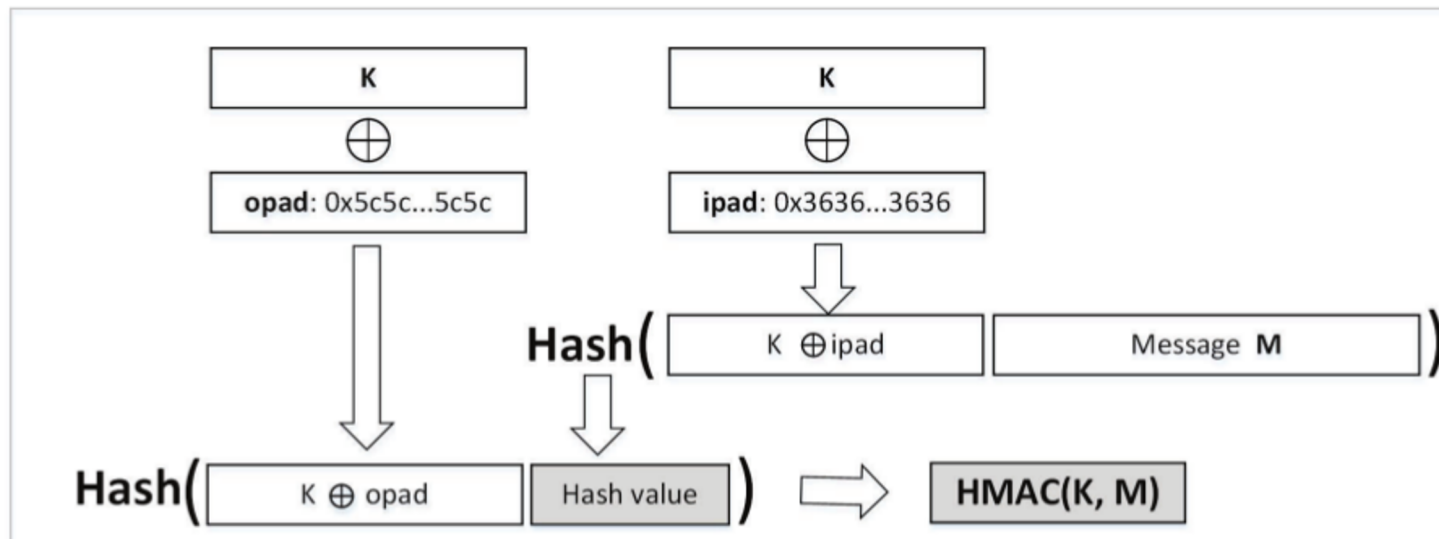
# HMAC

- Should we compute HMAC as  $h(K, M)$  ?
- Hashes computed in blocks
  - $h(B_1, B_2) = F(F(A, B_1), B_2)$  for some  $F$  and constant  $A$
  - Then  $h(B_1, B_2) = F(h(B_1), B_2)$
- Let  $M' = (M, X)$ 
  - Then  $h(K, M') = F(h(K, M), X)$
  - Attacker can compute HMAC of  $M'$  without  $K$
- Is  $h(M, K)$  better?
  - Yes, but... if  $h(M') = h(M)$  then we might have  
 $h(M, K) = F(h(M), K) = F(h(M'), K) = h(M', K)$



# The Right Way to HMAC

- Uses hash function  $H$  (compression function block size  $B$ ) and a secret key  $K$
- $\text{ipad} = 0x36$  ( $B$  times),  $\text{opad} = 0x5c$  ( $B$  times)
- Can be used with any one-way hash function



# Example: HMAC-SHA512

- Apply HMAC to SHA512 to make a keyed MAC
- $\text{HMAC-SHA512}(k, m) =$   
 $\text{SHA512}(k' \oplus [01011100]^8 \parallel$   
 $\text{SHA512}(k' \oplus [00110110]^8 \parallel m))$

$\oplus$  exclusive or,       $\parallel$  concatenation

# HMAC and Strong Collisions

- Birthday attacks don't make sense in HMAC scenario
  - Attacker would need to know  $K$  to generate candidate message/hash pairs
  - Thus HMAC-MD5 is still a reasonable option

# Key Points

- Data integrity is important too
  - Sometimes more important than confidentiality
- Cryptohashes and Message Authentication Codes (MAC) both have their uses