RSA Public-Key Encryption and Signature Lab Report

1. Introduction

RSA (RivestShamirAdleman) is one of the first public-key cryptosystems and is widely used for secure communication. The RSA algorithm first generates two large random prime numbers, and then use them to generate public and private key pairs, which can be used to do encryption, decryption, digital signature generation, and digital signature verification. The RSA algorithm is built upon number theories, and it can be quite easily implemented with the support of libraries. Essentially, students will be implementing the RSA algorithm using the C program language.

The lab covers the following security-related topics:

- Public-key cryptography
- The RSA algorithm and key generation
- Big number calculation
- Encryption and Decryption using RSA
- Digital signature
- X.509 certificate

Lab environment: This lab requires the openssl library. I am using Ubuntu 16.04, which is already installed on.

2. Background

The RSA algorithm involves computations on large numbers. These computations cannot be directly conducted using simple arithmetic operators in programs, because those operators can only operate on primitive SEED Labs data types. In this lab, we will use the Big Number library provided by openssl. To use this library, we will define each big number as a BIGNUM type, and then use the APIs provided by the library for various operations, such as addition, multiplication, exponentiation, modular operations, etc.

First, I create a new folder named cs458lab2. Then I write all of the lab codes in this floder.

1. \$ mkdir cs458Lab2

3. Task

3.1 Task 1: Deriving the Private Key

Let p, q, and e be three prime numbers. Let n = p*q. We will use (e, n) as the public key. Please calculate the private key d.

First, I create a Task1.c and use the code showing in the lab insturctions.

```
1. $ vi task1.c
2. #include <stdio.h>
3. #include <openssl/bn.h>
4. #define NBITS 256
5.
6. void printBN(char *msg, BIGNUM *a){
7. // Convert the BIGNUM to number string
8. char * number_str = BN_bn2hex(a);
9. // Print out the number string
10. printf("%s %s\n", msg, number_str);
11. // Free the dynamically allocated memory
12. OPENSSL_free(number_str);
13.}
14.
15. int main(){
16. BN CTX *ctx = BN_CTX_new();
17. BIGNUM *p = BN_new();
18. BIGNUM *q = BN_new();
19. BIGNUM *e = BN_new();
20. BIGNUM *d = BN_new();
21. BIGNUM *res1 = BN new();
22. BIGNUM *res2 = BN new();
23. BIGNUM *res3 = BN_new();
24. BIGNUM *one = BN new();
25. // initalize p q e
26. // Assign the first large prime
27. BN_hex2bn(&p, "F7E75FDC469067FFDC4E847C51F452DF");
29. // Assign the second large prime
30. BN_hex2bn(&q, "E85CED54AF57E53E092113E62F436F4F");
32. // Assign the Modulus
33. BN hex2bn(&e, "0D88C3");
34. BN dec2bn(&one,"1");
35. //res1 = p-1
36. BN_sub(res1, p, one);
37. //res2 = q-1
38. BN_sub(res2, q, one);
39. //res3=res1*res2
40. BN_mul(res3, res1, res2, ctx);
41. //res=a*b mod n
42. BN_mod_inverse(d, e, res3, ctx);
43.//print BN
44. printBN("d= ",d);
45. return 0;
46.}
47.
```

First print out a big number:

```
void printBN(char *msg, BIGNUM *a){
// Convert the BIGNUM to number string
char * number_str = BN_bn2dec(a);
// Print out the number string
printf("%s %s\n", msg, number_str);
// Free the dynamically allocated memory
OPENSSL_free(number_str);
}
```

Then in the main method, create a BN CTX structure to holds BIGNUM temporary variables used by library functions. We need to create such a structure and pass it to the functions that require it. Then we initialize BIGNUM variables: p,q,e,d,res1.res2.res3.one.

There are a number of ways to assign a value to a BIGNUM variable(p,q,e.one)

```
int main(){
BN CTX *ctx = BN CTX new();
BIGNUM *p = BN new();
BIGNUM *q = BN new();
BIGNUM *e = BN new();
BIGNUM *d = BN new();
BIGNUM *res1 = BN new();
BIGNUM * res2 = BN new();
BIGNUM * res3 = BN new();
BIGNUM *one = BN new();
// initalize p q e
// Assign the first large prime
BN hex2bn(&p, "F7E75FDC469067FFDC4E847C51F452DF");
// Assign the second large prime
BN hex2bn(&q, "E85CED54AF57E53E092113E62F436F4F");
// Assign the Modulus
BN_hex2bn(&e, "0D88C3");
BN dec2bn(&one,"1");
```

Compute functions: Compute res1 = p-1, res2 = q-1, res3 = res1 * res2, d*e mod res3 = 1

```
//res1 = p-1
BN_sub(res1, p, one);
//res2 = q-1
BN_sub(res2, q, one);
//res3=res1*res2
BN_mul(res3, res1, res2, ctx);
//res=a*b mod n
BN_mod_inverse(d, e, res3, ctx);
//print BN
printBN("d= ",d);
return 0;
}
-- INSERT -- 45,1
```

Finally, we can get d by following commands:

```
1. seed@VM:~/cs458Lab2$ vi task1.c[10/18/20]
2. seed@VM:~/cs458Lab2$ gcc -o task1 task1.c -lcrypto
3. seed@VM:~/cs458Lab2$ ./task1
4.
```

```
[10/18/20]seed@VM:~/cs458Lab2$ vi task1.c
[10/18/20]seed@VM:~/cs458Lab2$ gcc -o task1 task1.c -lc
rypto
[10/18/20]seed@VM:~/cs458Lab2$ ./task1
d= 3587A24598E5F2A21DB007D89D18CC50ABA5075BA19A33890FE
7C28A9B496AEB
```

Therefore, we get the private key

d=3587A24598E5F2A21DB007D89D18CC50ABA5075BA19A33890FE7C28A9B496AEB

3.2 Task 2: Encrypting a Message

Let (e, n) be the public key, We need to convert this ASCII string to a hex string, and then convert the hex string to a BIGNUM using the hex-to-bn API BN hex2bn(). In this task, I create a task2.c using command

1. vi task2.c

Import libary

```
<mark>#</mark>include <stdio.h>
#include <openssl/bn.h>
#define NBITS 256
```

Print method to make the result

```
//print a big number
void printBN(char *msg, BIGNUM *a){
// Convert the BIGNUM to number string
char * number_str = BN_bn2dec(a);
// Print out the number string
printf("%s %s\n", msg, number_str);
// Free the dynamically allocated memory
OPENSSL_free(number_str);
}
```

According to the lab, we know

```
1. $ python -c 'print("A top secret!".encode("hex"))'
2. 4120746f702073656372657421
```

Therefore, we can use the hexadecimal of M

```
int main(){
    BN CTX *ctx = BN CTX new();
    BIGNUM *m = BN new();
    BIGNUM *e = BN new();
    BIGNUM *n = BN new();
    BIGNUM *d = BN new();
    BIGNUM *enc = BN new();
    BIGNUM *dec = BN new();
    //Initialize
    BN_hex2bn(&e, "010001");
    BN hex2bn(&n, "DCBFFE3E51F62E09CE7032E2677A78946A849
DC4CDDE3A4D0CB81629242FB1A5");
    BN hex2bn(&m, "4120746f702073656372657421");//A top
secret!
    BN hex2bn(&d, " 74D806F9F3A62BAE331FFE3F0A68AFE35B3D
2E4794148AACBC26AA381CD7D30D");
    //encry = m^e \mod n
    BN mod exp(enc,m,e,n,ctx);
    printBN("encrypt message = ", enc);
```

```
//decry = enc^d mod n
BN_mod_exp(dec,enc,d,n,ctx);
printBN("decrypt message = ",dec);
return 0;
}
```

Then, we run the code in the terminal, the result as shown

```
[10/18/20]seed@VM:~/cs458Lab2$ vi task2.c

[10/18/20]seed@VM:~/cs458Lab2$ gcc -o task2 task2.c -lc

rypto

[10/18/20]seed@VM:~/cs458Lab2$ ./task2

encrypt message = 6FB078DA550B2650832661E14F4F8D2CFAEF

475A0DF3A75CACDC5DE5CFC5FADC

decrypt message = 4120746F702073656372657421
```

We can see that the decrypted message and the original message are the same.

Task2 code:

```
1. #include <stdio.h>
2. #include <openss1/bn.h>
3. #define NBITS 256
4.
5. //print a big number
6. void printBN(char *msg, BIGNUM *a){
7. // Convert the BIGNUM to number string
8. char * number_str = BN_bn2hex(a);
9. // Print out the number string
10. printf("%s %s\n", msg, number_str);
11. // Free the dynamically allocated memory
12. OPENSSL_free(number_str);
13. }
14.
```

```
15. int main(){
       BN_CTX *ctx = BN_CTX_new();
16.
       BIGNUM *m = BN_new();
17.
18.
       BIGNUM *e = BN_new();
19.
       BIGNUM *n = BN_new();
       BIGNUM *d = BN_new();
20.
       BIGNUM *enc = BN new();
21.
       BIGNUM *dec = BN new();
22.
        //Initialize
23.
24.
       BN hex2bn(&e,"010001");
        BN hex2bn(&n, "DCBFFE3E51F62E09CE7032E2677A78946A849DC4CDDE3A4D0CB81629242FB1A5");
25.
       BN_hex2bn(&m,"4120746f702073656372657421");//A top secret!
26.
        BN_hex2bn(&d,"74D806F9F3A62BAE331FFE3F0A68AFE35B3D2E4794148AACBC26AA381CD7D30D");
27.
28.
       //encry = m^e \mod n
29.
        BN_mod_exp(enc,m,e,n,ctx);
30.
       printBN("encrypt message = ", enc);
31.
       //decry = enc^d mod n
32.
33.
        BN_mod_exp(dec,enc,d,n,ctx);
       printBN("decrypt message = ",dec);
34.
35.
        return 0:
36.}
```

3.3 Task3 Decrypting a Message

The public/private keys used in this task are the same as the ones used in Task 2. Please decrypt the following ciphertext C, and convert it back to a plain ASCII string

Code is similar to task2:

```
1. #include <stdio.h>
2. #include <openssl/bn.h>
3. #define NBITS 256
4.
5. //print a big number
6. void printBN(char *msg, BIGNUM *a){
7. // Convert the BIGNUM to number string
8. char * number_str = BN_bn2hex(a);
9. // Print out the number string
10. printf("%s %s\n", msg, number_str);
11. // Free the dynamically allocated memory
12. OPENSSL free(number str);
13. }
14.
15. int main(){
       BN_CTX *ctx = BN_CTX_new();
17.
       BIGNUM *n = BN_new();
18.
       BIGNUM *d = BN_new();
19.
       BIGNUM *c = BN_new();
20.
       BIGNUM *dec = BN new();
       //Initialize
21.
       BN_hex2bn(&n, "DCBFFE3E51F62E09CE7032E2677A78946A849DC4CDDE3A4D0CB81629242FB1A5");
22.
23.
       BN_hex2bn(&c, "8C0F971DF2F3672B28811407E2DABBE1DA0FEBBBDFC7DCB67396567EA1E2493F");
       BN_hex2bn(&d,"74D806F9F3A62BAE331FFE3F0A68AFE35B3D2E4794148AACBC26AA381CD7D30D");
24.
25.
        //encry = m^e \mod n
       BN_mod_exp(dec,c,d,n,ctx);
26.
27.
       printBN("encrypt message = ", dec);
28.
29.
       return 0;
```

We decrypt the given cipher text, c using the formula: $c^d \mod n$.

By decrypting, we get the hex value of the message.

We then use the python to decode the hex value:

```
[10/18/20]seed@VM:~/cs458Lab2$ gcc -o task3 task3.c -lcrypto
[10/18/20]seed@VM:~/cs458Lab2$ ./task3
encrypt message = 50617373776F72642069732064656573
[10/18/20]seed@VM:~/cs458Lab2$ python -c 'print("A topsecret!".encode("hex"))'
4120746f702073656372657421
[10/18/20]seed@VM:~/cs458Lab2$
```

3.4 Task4 Signing a Message

First, we get the hex value of "I owe you \$2000."

```
[10/18/20]seed@VM:~/cs458Lab2$ python -c 'print("I owe you $2000.".encode("hex"))'
49206f776520796f752024323030302e
```

Value is 49206f776520796f752024323030302e

We run our code to produce the signature for the message

```
[10/18/20]seed@VM:~/cs458Lab2$ vi task4.c
[10/18/20]seed@VM:~/cs458Lab2$ gcc -o task4 task4.c -lc
rypto
[10/18/20]seed@VM:~/cs458Lab2$ ./task4
encrypt message = 55A4E7F17F04CCFE2766E1EB32ADDBA890BB
E92A6FBE2D785ED6E73CCB35E4CB
Then.
                  the
                              value
                                      of
                                           "T
                                                            $3000."
       we
             get
                        hex
                                               owe
                                                      you
[10/18/20]seed@VM:~/cs458Lab2$ python -c 'print("I owe
you $3000.".encode("hex"))'
49206f776520796f752024333030302e
```

Value is 49206f776520796f752024333030302e

We run our code to produce the signature for the message:

```
[10/18/20]seed@VM:~/cs458Lab2$ vi task4.c
[10/18/20]seed@VM:~/cs458Lab2$ gcc -o task4 task4.c -lc
rypto
[10/18/20]seed@VM:~/cs458Lab2$ ./task4
encrypt message = BCC20FB7568E5D48E434C387C06A6025E90D
29D848AF9C3EBAC0135D99305822
```

We can observe that, though there is only one byte of difference in the message, their signatures differ completely.

Code is similar to task3

```
1. #include <stdio.h>
2. #include <openssl/bn.h>
3. #define NBITS 256
4.
5. //print a big number
6. void printBN(char *msg, BIGNUM *a){
7. // Convert the BIGNUM to number string
8. char * number_str = BN_bn2hex(a);
9. // Print out the number string
10. printf("%s %s\n", msg, number_str);
11. // Free the dynamically allocated memory
12. OPENSSL_free(number_str);
13. }
14.
15. int main(){
       BN_CTX *ctx = BN_CTX_new();
16.
       BIGNUM *n = BN new();
17.
18.
       BIGNUM *d = BN new();
19.
       BIGNUM *c = BN new();
20.
       BIGNUM *dec = BN new();
21.
        //Initialize
22.
       BN hex2bn(&n, "DCBFFE3E51F62E09CE7032E2677A78946A849DC4CDDE3A4D0CB81629242FB1A5");
23.
       BN_hex2bn(&c,"49206f776520796f752024323030302e");// HEX value of "I owe you $2000."
24.
       //BN_hex2bn(&c,"49206f776520796f752024333030302e");// HEX value of "I owe you $3000
25.
       BN_hex2bn(&d,"74D806F9F3A62BAE331FFE3F0A68AFE35B3D2E4794148AACBC26AA381CD7D30D");
26.
       //encry = m^e mod n
27.
       BN mod exp(dec,c,d,n,ctx);
       printBN("encrypt message = ", dec);
28.
29.
30.
       return 0;
31. }
```

3.5 Task5: Verifying a Signature

First, We get the hex value of the message M, "Launch a missile." using python

```
[10/18/20]seed@VM:~/cs458Lab2$ python -c 'print("Launch
a missle.".encode("hex"))'
4c61756e63682061206d6973736c652e
```

We use the signature to compute the value of the message C.

We then use the BN_cmp API in order to compare the two messages and conclude whether the signature is Alice's or not:

```
[10/18/20]seed@VM:~/cs458Lab2$ vi task5.c
[10/18/20]seed@VM:~/cs458Lab2$ gcc -o task5 task5.c -lc
rypto
[10/18/20]seed@VM:~/cs458Lab2$ ./task5
Driginal Message : 4C61756E63682061206D697373696C652E
Value of computed : 4C61756E63682061206D697373696C652E
Valid Signature!
```

From the result, we know the same message value, therefore, it's Alice's signature.

Code:

```
1. // task5.c
2. //
3. //
4. // Created by SHIQI LIU on 10/18/20.
5. //
6. #include <stdio.h>
7. #include <openssl/bn.h>
8. void printBN(char *msg, BIGNUM *a)
9. {
10.
       char *number_str_a = BN_bn2hex(a);
11.
       printf("%s %s\n", msg, number_str_a);
12.
       OPENSSL_free(number_str_a);
13. }
14. int main()
15. {
16. // init
       BN CTX *ctx = BN CTX new();
17.
18.
       BIGNUM *n = BN_new();
19.
       BIGNUM *e = BN_new();
20.
       BIGNUM *M = BN_new();
21.
       // BIGNUM *d = BN_new();
22.
    BIGNUM *C = BN_new();
23.
       BIGNUM *S = BN_new();
24.
25.
       // assign values
       BN_hex2bn(&n, "AE1CD4DC432798D933779FBD46C6E1247F0CF1233595113AA51B450F18116115");
26.
27.
       BN_dec2bn(&e, "65537");
       BN hex2bn(&M, "4c61756e63682061206d697373696c652e"); //hex encode for " Launch a mi
28.
  ssile."
29.
       BN_hex2bn(&S, "643D6F34902D9C7EC90CB0B2BCA36C47FA37165C0005CAB026C0542CBDB6802F");
30.
       // Get S^e mod: if S=M^d mod n, C=M
31.
       BN_mod_exp(C, S, e, n, ctx);
32. printBN("Original Message : ", M );
33. printBN("Value of computed : ", C);
34. // verify the signature
35.
       if (BN_cmp(C, M) == 0)
36.
37.
           printf("Valid Signature! \n");
38.
39.
       else
40.
       {
41.
           printf("Verification fails! \n");
42.
43.
44.
       return 0;
45.}
```

Suppose that the signature in is corrupted, such that the last byte of the signature changes from 2F to 3F,

S = 643D6F34902D9C7EC90CB0B2BCA36C47FA37165C0005CAB026C0542CBDB6803F We use the signature to compute the value of the message C.

We then use the BN_cmp API in order to compare the two messages and conclude whether the signature is Alice's or not:

```
[10/18/20]seed@VM:~/cs458Lab2$ vi task5.c
[10/18/20]seed@VM:~/cs458Lab2$ gcc -o task5 task5.c -lc
rypto
[10/18/20]seed@VM:~/cs458Lab2$ ./task5
Original Message : 4C61756E63682061206D697373696C652E
Value of computed : 91471927C80DF1E42C154FB4638CE8BC72
6D3D66C83A4EB6B7BE0203B41AC294
Verification fails!
```

Therefore, we get the value of computed message is entirely different form original message, though only 1 byte of the signature is changed. It causes the verification fails.

3.6 Task6 Manually Verifying an X.509 Certificate

• Step 1

Download a certificate from a real web server. We use the <u>www.google</u>.com server in this document

```
1. [10/18/20]seed@VM:~/cs458Lab2$ openssl s client -connect www.google.com:443 -
   showcerts
2. CONNECTED(00000003)
3. depth=2 OU = GlobalSign Root CA - R2, O = GlobalSign, CN = GlobalSign
4. verify return:1
5. depth=1 C = US, O = Google Trust Services, CN = GTS CA 101
6. verify return:1
7. depth=0 C = US, ST = California, L = Mountain View, O = Google LLC, CN = www.google.com
8. verify return:1
9. ---
10. Certificate chain
11. 0 s:/C=US/ST=California/L=Mountain View/O=Google LLC/CN=www.google.com
      i:/C=US/O=Google Trust Services/CN=GTS CA 101
13. ----BEGIN CERTIFICATE----
14. MIIFkTCCBHmgAwIBAgIQB5q2sT+2NbIIAAAAAFst1zANBgkqhkiG9w0BAQsFADBC
15. MQswCQYDVQQGEwJVUzEeMBwGA1UEChMVR29vZ2xlIFRydXN0IFNlcnZpY2VzMRMw
16. EQYDVQQDEwpHVFMgQ0EgMU8xMB4XDTIwMDkyMjE1MTYxOVoXDTIwMTIxNTE1MTYx
17. OVowaDELMAkGA1UEBhMCVVMxEzARBgNVBAgTCkNhbGlmb3JuaWExFjAUBgNVBAcT
18. DU1vdW50YWluIFZpZXcxEzARBgNVBAoTCkdvb2dsZSBMTEMxFzAVBgNVBAMTDnd3
19. dy5nb29nbGUuY29tMIIBIjANBgkqhkiG9w0BAQEFAAOCAQ8AMIIBCgKCAQEAnG1D
20. Z2T1815ruTFxLz5PmUKZjYFEihvXKsmiu2d0NTKv8RgWvMItgvP/1IfIz+076jn3
21. meC71lP10LST+wI+vFPE9vEL/Zie5veUijpXE0bUApeud+Rnlsw4UJ1x50PCBdSN
22. r41sNVCAAU98ibSGlc5n2Qr1/YYhs2qnqKKG8i8zNMbjDYyzOWyjfmRVi8W7eU2Z
23. FpJVwc3D6WEACqQrLATPcFNK0Jb3f5j7eohea9eMCslB13e43iIbA2zHb8owE2Mu
24. F7GKhYiTr80EFy4aq7meEeIFHDB/05e0+6nSxV0p3dBsdxXu/BlEVRuwnigCtMAn
25. LVS50EhwBuz1Wl+VWwIDAQABo4ICWzCCAlcwDgYDVR0PAQH/BAQDAgWgMBMGA1Ud
26. JQQMMAoGCCsGAQUFBwMBMAwGA1UdEwEB/wQCMAAwHQYDVR00BBYEFDDRC4ywBM9P
27. OAk0QWnLJlg3HjmJMB8GA1UdIwQYMBaAFJjR+G4Q68+b7GCfGJAboOt9Cf0rMGgG
```

```
28. CCsGAQUFBwEBBFwwWjArBggrBgEFBQcwAYYfaHR0cDovL29jc3AucGtpLmdvb2cv
29. Z3RzMW8xY29yZTArBggrBgEFBQcwAoYfaHR0cDovL3BraS5nb29nL2dzcjIvR1RT
30. MU8xLmNydDAZBgNVHREEEjAQgg53d3cuZ29vZ2xlLmNvbTAhBgNVHSAEGjAYMAgG
31. BmeBDAECAjAMBgorBgEEAdZ5AgUDMDMGA1UdHwQsMCowKKAmoCSGImh0dHA6Ly9j
32. cmwucGtpLmdvb2cvR1RTMU8xY29yZS5jcmwwggEDBgorBgEEAdZ5AgQCBIH0BIHx
33. AO8AdQDwlaRZ8gDRgkAQLS+TiI6tS/4dR+OZ4dA0prCoqo6ycwAAAXS2mgE4AAAE
34. AwBGMEQCIBA000C/IxSaE2sVhS+dJtnXsh7fSYjeybHOnFOtoRFCAiBnTcymqGeb
35. lwBe5U3nJyG3tngeH9YCfBdkeShmHdf6DgB2ALIeBcyLos2KIE6HZvkruYolIGdr
36. 2vpw57JJUy3vi5BeAAABdLaaADoAAAQDAEcwRQIgBFJa178fY3/4Pb95N5hh2JfR
37. 3EJ9AUbb0vff31qx/NsCIQDJTBFLs1QdubTe6S+Xc7EuQC9rh3YVLSYc8+dSRZuV
38. 3zANBgkqhkiG9w0BAQsFAAOCAQEAfznjbmvP1GKbyj7RIT5L/x6dkPBCWp6u6toi
39. lak4chqHN7mkJkazcb+DGoSAkz7DWfvrVt6Kruh7Vq93Z90g9Nnp5ZiMvkHd5+JM
40. VqVq3SEK0x+Bd//cW7364zsqnCP97Dg1kvPZz/Rqkq04i9ajSGNxkiMjkkFG4kl0
41. tBuMXOmjoIPwa81iXT1tpV8TqV3uQj0FJ+WZXrYP33HSFGgEXO4VJq6cAh1o5V4z
42. +3KOF1Si5pVAzIHjEbTB9RP2WK7XQ2VkmyfqcnEJYCEnLDAReQkkGQMmJV014jHh
43. SRcKMTc/HXPKihjE7cPmhE1EehHzWkJLsYwYZcIGOP+shpz1rw==
44. ----END CERTIFICATE----
45. 1 s:/C=US/O=Google Trust Services/CN=GTS CA 101
      i:/OU=GlobalSign Root CA - R2/O=GlobalSign/CN=GlobalSign
47. ----BEGIN CERTIFICATE----
48. MIIESjCCAzKgAwIBAgINAeO@mqGNiqmBJWlQuDANBgkqhkiG9w@BAQsFADBMMSAw
49. HgYDVQQLExdHbG9iYWxTaWduIFJvb3QgQ0EgLSBSMjETMBEGA1UEChMKR2xvYmFs
50. U2lnbjETMBEGA1UEAxMKR2xvYmFsU2lnbjAeFw0xNzA2MTUwMDAwNDJaFw0yMTEy
51. MTUwMDAwNDJaMEIxCzAJBgNVBAYTAlVTMR4wHAYDVQQKExVHb29nbGUgVHJ1c3Qg
52. U2VydmljZXMxEzARBgNVBAMTCkdUUyBDQSAxTzEwggEiMA0GCSqGSIb3DQEBAQUA
53. A4IBDwAwggEKAoIBAQDQGM9F1IvN05zkQO9+tN1pIRvJzzyOTHW5DzEZhD2ePCnv
54. UAOQk28FgICfKqC9EksC4T2fWBYk/jCfC3R3VZMdS/dN4ZKCEPZRrAzDsiKUDzRr
55. mBBJ5wudgzndIMYcLe/RGGFl5yODIKgjEv/SJH/UL+dEaltN11BmsK+eQmMF++Ac
56. xGNhr59qM/9il71I2dN8FGfcddwuaej4bXhp0LcQBbjxMcI7JP0aM3T4I+DsaxmK
57. FsbjzaTNC9uzpFlg0Ig7rR25xoynUxv8vNmkq7zdPGHXkxWY7oG9j+JkRyBABk7X
58. rJfoucBZEqFJJSPk7XA0LKW0Y3z5oz2D0c1tJKwHAgMBAAGjggEzMIIBLzAOBgNV
59. HO8BAf8EBAMCAYYwHQYDVR01BBYwFAYIKwYBBQUHAwEGCCsGAQUFBwMCMBIGA1Ud
60. EWEB/WOIMAYBAf8CAOAWHOYDVR0OBBYEFJiR+G4068+b7GCfGJAboOt9Cf0rMB8G
61. A1UdIwOYMBaAFJviB1dnHB7AagbeWbSaLd/cGYYuMDUGCCsGAOUFBwEBBCkwJzAl
62. BggrBgEFBQcwAYYZaHR0cDovL29jc3AucGtpLmdvb2cvZ3NyMjAyBgNVHR8EKzAp
63. MCegJaAjhiFodHRwOi8vY3JsLnBraS5nb29nL2dzcjIvZ3NyMi5jcmwwPwYDVR0g
64. BDgwNjA0BgZngQwBAgIwKjAoBggrBgEFBQcCARYcaHR0cHM6Ly9wa2kuZ29vZy9y
65. ZXBvc210b3J5LzANBgkqhkiG9w0BAQsFAAOCAQEAGoA+Nnn78y6pRjd9X1QWNa7H
66. TgiZ/r3RNGkmUmYHPQq6Scti9PEajvwRT2iWTHQr02fesqQqBY2ETUwgZQ+lltoN
67. FvhsO9tvBCOIazpswWC9aJ9xju4tWDQH8NVU6YZZ/XteDSGU9YzJqPjY8q3MDxrz
68. mqepBCf5o8mw/wJ4a2G6xzUr6Fb6T8McD022PLRL6u3M4Tzs3A2M1j6bykJYi8wW
69. IRdAvKLWZu/axBVbzYmqmwkm5zLSDW5nIAJbELCQCZwMH56t2Dvqofxs6BBcCFIZ
70. USpxu6x6td0V7SvJCCosirSmIatj/9dSSVD0ibet8q/7UK4v4ZUN80atnZz1yg==
71. ----END CERTIFICATE----
72. ---
73. Server certificate
74. subject=/C=US/ST=California/L=Mountain View/O=Google LLC/CN=www.google.com
75. issuer=/C=US/O=Google Trust Services/CN=GTS CA 101
77. No client certificate CA names sent
78. Peer signing digest: SHA256
79. Server Temp Key: ECDH, P-256, 256 bits
80. ---
81. SSL handshake has read 3247 bytes and written 431 bytes
82. ---
83. New, TLSv1/SSLv3, Cipher is ECDHE-RSA-AES128-GCM-SHA256
84. Server public key is 2048 bit
85. Secure Renegotiation IS supported
86. Compression: NONE
87. Expansion: NONE
88. No ALPN negotiated
```

```
89. SSL-Session:
       Protocol : TLSv1.2
                : ECDHE-RSA-AES128-GCM-SHA256
       Cipher
92.
       Session-ID: BC337A8A0CE22588A9845CD955A25131346F558771B2B435CFB7373C3534E9E7
93.
       Session-ID-ctx:
       Master-
   Key: 42EA2EB90D0B1F59618908405370AAB39B2C8E27CD06BB4C99E71435294027B3DAB36CCA97E370AA4A
   738095F45CDBC0
95.
       Key-Arg
                : None
96.
      PSK identity: None
       PSK identity hint: None
97.
98.
      SRP username: None
99.
       TLS session ticket lifetime hint: 100800 (seconds)
100.
             TLS session ticket:
             0000 - 01 95 05 1c 6a 74 90 8c-f9 0e 6c 5a cc dc cd 1b
                                                                   ....jt....1Z....
101.
102.
             0010 - e0 a3 61 6d 1a 72 be 3c-e5 8a b1 55 2e d7 5a ab
                                                                  ..am.r.<...U..Z.
103.
             0020 - a9 01 59 f0 e8 eb 0e a2-e5 34 a4 b6 be 05 ec 7c
                                                                   ..Y.....4....
104.
             0030 - 08 9e e2 70 94 9c e1 8b-47 8e 10 24 c8 e6 e6 5c
                                                                  ...p....G..$...\
105.
             0040 - cc 83 71 a2 a2 1c c8 c3-db 1f df c9 15 23 3e e0
                                                                   ..q.....#>.
106.
             0050 - dc f9 73 33 46 83 27 d9-ab 92 40 0d 92 41 89 6f
                                                                  ..s3F.'...@..A.o
107.
             0060 - 49 bb 2f 30 8c 8e fc fd-bc 3a 44 c5 67 3d c2 15
                                                                   I./0....:D.g=..
                                                                   ),.9Sf.hpH6.P...
108.
             0070 - 29 2c 86 39 53 66 a0 68-70 48 36 99 50 e7 09 ba
109.
             0080 - 39 ce 7f 5b d1 fb a1 7f-83 b9 6b be 36 b5 c1 a6
                                                                   9..[.....k.6...
110.
             0090 - a7 32 f0 85 d7 04 77 1b-e4 c4 03 77 d3 0b 27 92
                                                                 .2....w...w..'.
             00a0 - 1d 4d a5 06 35 67 69 5e-8b 51 cd 64 2e 91 8f 79
                                                                   .M..5gi^.Q.d...y
111.
112.
             00b0 - fa c8 5b 17 8f 63 f4 c5-89 e0 83 2d 16 2f 9e f7
                                                                  ..[..c...-./..
113.
             00c0 - 33 20 5d 03 00 c6 f4 0d-ec b5 a2 d0 6a 49 a4 49
                                                                   3 ].....jI.I
114.
             00d0 - e5 6a a9 fc f7 05 34 d5-7d 63 af 4d 79
                                                                   .j....4.}c.My
115.
116.
             Start Time: 1603076169
117.
             Timeout
                      : 300 (sec)
118.
             Verify return code: 0 (ok)
119.
120.
          read:errno=0
121.
          [10/18/20]seed@VM:~/cs458Lab2$
    [10/18/20]seed@VM:~/cs458Lab2$ openssl s client -connec
    t www.google.com:443 -showcerts
    CONNECTED (00000003)
    depth=2 OU = GlobalSign Root CA - R2, O = GlobalSign, C
    N = GlobalSign
    verify return:1
    depth=1 C = US, O = Google Trust Services, CN = GTS CA
    101
    verify return:1
    depth=0 C = US, ST = California, L = Mountain View, O =
     Google LLC, CN = www.google.com
    verify return:1
    Certificate chain
     0 s:/C=US/ST=California/L=Mountain View/0=Google LLC/C
    N=www.google.com
        i:/C=US/O=Google Trust Services/CN=GTS CA 101
       ---BEGIN CERTIFICATE----
    MIIFkTCCBHmgAwIBAgIQB5q2sT+2NbIIAAAAAFst1zANBgkqhkiG9w0
    BAQsFADBC
```

```
VqVq3SEK0x+Bd//cW7364zsqnCP97Dq1kvPZz/Rqkq04i9ajSGNxkiN
ikkFG4kl0
tBuMXOmjoIPwa81iXT1tpV8TqV3uQj0FJ+WZXrYP33HSFGgEX04VJq6
cAh1o5V4z
+3K0F1Si5pVAzIHjEbTB9RP2WK7XQ2VkmyfqcnEJYCEnLDAReQkkGQN
mJV014jHh
SRcKMTc/HXPKihjE7cPmhElEehHzWkJLsYwYZcIGOP+shpz1rw==
----END CERTIFICATE----
1 s:/C=US/O=Google Trust Services/CN=GTS CA 101
  i:/OU=GlobalSign Root CA - R2/O=GlobalSign/CN=Global
Sign
----BEGIN CERTIFICATE----
MIIES;CCAzKqAwIBAqINAeO0mqGNiqmBJWlQuDANBqkqhkiG9w0BAQs
FADBMMSAw
dgYDV00LExdHbG9iYWxTaWduIFJvb30g00EgLSBSMjETMBEGA1UEChN
KR2xvYmFs
U2lnbjETMBEGA1UEAxMKR2xvYmFsU2lnbjAeFw0xNzA2MTUwMDAwNDJ
aFw0yMTEy
MTUwMDAwNDJaMEIxCzAJBgNVBAYTAlVTMR4wHAYDVQQKExVHb29nbGU
aVHJ1c30a
U2VydmljZXMxEzARBgNVBAMTCkdUUyBDQSAxTzEwggEiMA0GCSqGSIb
3DQEBAQUA
q1Z/r3KNGkmUmYHPQqb5ct19PEajVwKIZ1WIHQr0ZtesqUqBYZEIUw
ZQ+lltoN
vhs09tvBC0IazpswWC9aJ9xju4tWD0H8NVU6YZZ/XteDSGU9YzJqPi
/8g3MDxrz
ngepBCf5o8mw/wJ4a2G6xzUr6Fb6T8McD022PLRL6u3M4Tzs3A2M1j6
ykJYi8wW
[RdAvKLWZu/axBVbzYmqmwkm5zLSDW5nIAJbELCQCZwMH56t2Dvqofx
6BBcCFIZ
JSpxu6x6td0V7SvJCCosirSmIatj/9dSSVDQibet8g/7UK4v4ZUN80a
nZz1yq==
----END CERTIFICATE----
Server certificate
subject=/C=US/ST=California/L=Mountain View/O=Google LL
C/CN=www.google.com
issuer=/C=US/0=Google Trust Services/CN=GTS CA 101
No client certificate CA names sent
Peer signing digest: SHA256
erver Temp Key: ECDH, P-256, 256 bits
SL handshake has read 3247 bytes and written 431 bytes
```

We save these two certificates in the files c0.pem and c1.pem respectively

• Step2 Extract the public key (e, n) from the issuer's certificate.

We get the value of n using -modulus:

- [10/18/20]seed@VM:~/cs458Lab2\$ openssl x509 -in c1.pem -noout -modulus
- Modulus=D018CF45D48BCDD39CE440EF7EB4DD69211BC9CF3C8E4C75B90F3119843D9E3C29EF 500D10936F0580809F2AA0BD124B02E13D9F581624FE309F0B747755931D4BF74DE1928210F6 51AC0CC3B222940F346B981049E70B9D8339DD20C61C2DEFD1186165E7238320A82312FFD224 7FD42FE7446A5B4DD75066B0AF9E426305FBE01CC46361AF9F6A33FF6297BD48D9D37C1467DC 75DC2E69E8F86D7869D0B71005B8F131C23B24FD1A3374F823E0EC6B198A16C6E3CDA4CD0BDB B3A4596038883BAD1DB9C68CA7531BFCBCD9A4ABBCDD3C61D7931598EE81BD8FE26447204006 4ED7AC97E8B9C05912A1492523E4ED70342CA5B4637CF9A33D83D1CD6D24AC07

```
[10/18/20]seed@VM:~/cs458Lab2$ vi c0.pem
[10/18/20]seed@VM:~/cs458Lab2$ vi c1.pem
[10/18/20]seed@VM:~/cs458Lab2$ openssl x509 -in c1.pem
-noout -modulus
Modulus=D018CF45D48BCDD39CE440EF7EB4DD69211BC9CF3C8E4C7
5B90F3119843D9E3C29EF500D10936F0580809F2AA0BD124B02E13D
9F581624FE309F0B747755931D4BF74DE1928210F651AC0CC3B2229
40F346B981049E70B9D8339DD20C61C2DEFD1186165E7238320A823
12FFD2247FD42FE7446A5B4DD75066B0AF9E426305FBE01CC46361A
F9F6A33FF6297BD48D9D37C1467DC75DC2E69E8F86D7869D0B71005
B8F131C23B24FD1A3374F823E0EC6B198A16C6E3CDA4CD0BDBB3A45
96038883BAD1DB9C68CA7531BFCBCD9A4ABBCDD3C61D7931598EE81
BD8FE264472040064ED7AC97E8B9C05912A1492523E4ED70342CA5B
4637CF9A33D83D1CD6D24AC07
```

Print all attributes of the certificate, and then find the exponent, which is public key e(line 35)

```
[10/18/20]seed@VM:~/cs458Lab2$ openssl x509 -in c1.pem -text -noout
1.
   Certificate:
2.
       Data:
3.
4.
            Version: 3 (0x2)
            Serial Number:
5.
                01:e3:b4:9a:a1:8d:8a:a9:81:25:69:50:b8
6.
7.
       Signature Algorithm: sha256WithRSAEncryption
8.
            Issuer: OU=GlobalSign Root CA - R2, O=GlobalSign, CN=GlobalSign
9.
            Validity
                Not Before: Jun 15 00:00:42 2017 GMT
10.
                Not After: Dec 15 00:00:42 2021 GMT
11.
12.
            Subject: C=US, O=Google Trust Services, CN=GTS CA 101
13.
            Subject Public Key Info:
14.
                Public Key Algorithm: rsaEncryption
15.
                    Public-Key: (2048 bit)
16.
                    Modulus:
17.
                        00:d0:18:cf:45:d4:8b:cd:d3:9c:e4:40:ef:7e:b4:
18.
                        dd:69:21:1b:c9:cf:3c:8e:4c:75:b9:0f:31:19:84:
19.
                        3d:9e:3c:29:ef:50:0d:10:93:6f:05:80:80:9f:2a:
20.
                        a0:bd:12:4b:02:e1:3d:9f:58:16:24:fe:30:9f:0b:
21.
                        74:77:55:93:1d:4b:f7:4d:e1:92:82:10:f6:51:ac:
22.
                        0c:c3:b2:22:94:0f:34:6b:98:10:49:e7:0b:9d:83:
23.
                        39:dd:20:c6:1c:2d:ef:d1:18:61:65:e7:23:83:20:
24.
                        a8:23:12:ff:d2:24:7f:d4:2f:e7:44:6a:5b:4d:d7:
                        50:66:b0:af:9e:42:63:05:fb:e0:1c:c4:63:61:af:
25.
                        9f:6a:33:ff:62:97:bd:48:d9:d3:7c:14:67:dc:75:
26.
```

```
27.
                    dc:2e:69:e8:f8:6d:78:69:d0:b7:10:05:b8:f1:31:
28.
                    c2:3b:24:fd:1a:33:74:f8:23:e0:ec:6b:19:8a:16:
29.
                    c6:e3:cd:a4:cd:0b:db:b3:a4:59:60:38:88:3b:ad:
30.
                    1d:b9:c6:8c:a7:53:1b:fc:bc:d9:a4:ab:bc:dd:3c:
31.
                    61:d7:93:15:98:ee:81:bd:8f:e2:64:47:20:40:06:
32.
                    4e:d7:ac:97:e8:b9:c0:59:12:a1:49:25:23:e4:ed:
33.
                    70:34:2c:a5:b4:63:7c:f9:a3:3d:83:d1:cd:6d:24:
34.
                    ac:07
35.
                Exponent: 65537 (0x10001)
            [10/18/20]seed@VM:~/cs458Lab2$ openssl x509 -in c1.pem
             -text -noout
            Certificate:
                 Data:
                     Version: 3 (0x2)
                     Serial Number:
                          01:e3:b4:9a:a1:8d:8a:a9:81:25:69:50:b8
                 Signature Algorithm: sha256WithRSAEncryption
                     Issuer: OU=GlobalSign Root CA - R2, O=GlobalSig
            n, CN=GlobalSign
                     Validity
                          Not Before: Jun 15 00:00:42 2017 GMT
                          Not After: Dec 15 00:00:42 2021 GMT
                     Subject: C=US, O=Google Trust Services, CN=GTS
            CA 101
                     Subject Public Key Info:
                          Public Key Algorithm: rsaEncryption
                              Public-Key: (2048 bit)
                              Modulus:
                                  00:d0:18:cf:45:d4:8b:cd:d3:9c:e4:40
             :ef:7e:b4:
            63:61:af:
                                 9f:6a:33:ff:62:97:bd:48:d9:d3:7c:14
            67:dc:75:
                                 dc:2e:69:e8:f8:6d:78:69:d0:b7:10:05
            b8:f1:31:
                                 c2:3b:24:fd:1a:33:74:f8:23:e0:ec:6b
            19:8a:16:
                                 c6:e3:cd:a4:cd:0b:db:b3:a4:59:60:38
            88:3b:ad:
                                 1d:b9:c6:8c:a7:53:1b:fc:bc:d9:a4:ab
            bc:dd:3c:
                                 61:d7:93:15:98:ee:81:bd:8f:e2:64:47
            20:40:06:
                                 4e:d7:ac:97:e8:b9:c0:59:12:a1:49:25
            23:e4:ed:
                                 70:34:2c:a5:b4:63:7c:f9:a3:3d:83:d1
```

• Step3 Extract the signature from the server's certificate:

ac:07

Exponent: 65537 (0x10001)

cd:6d:24:

We run the command: openssl x509 -in c0.pem -text -noout to extract the signature from the server's certificate, c0.pem. We put this signature into a file.

```
1. [10/18/20]seed@VM:~/cs458Lab2$ openssl x509 -in c0.pem -text -noout
2.
       Signature Algorithm: sha256WithRSAEncryption
             7f:39:e3:6e:6b:cf:d4:62:9b:ca:3e:d1:21:3e:4b:ff:1e:9d:
3.
4.
             90:f0:42:5a:9e:ae:ea:da:22:d5:a9:38:72:1a:87:37:b9:a4:
5.
             26:46:b3:71:bf:83:1a:84:80:93:3e:c3:59:fb:eb:56:de:8a:
             ae:e8:7b:56:af:77:67:dd:20:f4:d9:e9:e5:98:8c:be:41:dd:
6.
7.
             e7:e2:4c:56:a5:6a:dd:21:0a:d3:1f:81:77:ff:dc:5b:bd:fa:
8.
             e3:3b:2a:9c:23:fd:ec:38:35:92:f3:d9:cf:f4:6a:92:ad:38:
9.
             8b:d6:a3:48:63:71:92:23:23:92:41:46:e2:49:4e:b4:1b:8c:
10.
             5c:e9:a3:a0:83:f0:6b:cd:62:5d:3d:6d:a5:5f:13:a9:5d:ee:
11.
             42:3d:05:27:e5:99:5e:b6:0f:df:71:d2:14:68:04:5c:ee:15:
12.
             26:ae:9c:02:1d:68:e5:5e:33:fb:72:8e:17:54:a2:e6:95:40:
13.
             cc:81:e3:11:b4:c1:f5:13:f6:58:ae:d7:43:65:64:9b:27:ea:
14.
             72:71:09:60:21:27:2c:30:11:79:09:24:19:03:26:25:53:b5:
15.
             e2:31:e1:49:17:0a:31:37:3f:1d:73:ca:8a:18:c4:ed:c3:e6:
16.
             84:49:44:7a:11:f3:5a:42:4b:b1:8c:18:65:c2:06:38:ff:ac:
17.
             86:9c:f5:af
18. [10/18/20]seed@VM:~/cs458Lab2$
```

```
Signature Algorithm: sha256WithRSAEncryption
         7f:39:e3:6e:6b:cf:d4:62:9b:ca:3e:d1:21:3e:4b:f
f:1e:9d:
         90:f0:42:5a:9e:ae:ea:da:22:d5:a9:38:72:1a:87:3
7:b9:a4:
         26:46:b3:71:bf:83:1a:84:80:93:3e:c3:59:fb:eb:5
6:de:8a:
         ae:e8:7b:56:af:77:67:dd:20:f4:d9:e9:e5:98:8c:b
e:41:dd:
         e7:e2:4c:56:a5:6a:dd:21:0a:d3:1f:81:77:ff:dc:5
b:bd:fa:
         e3:3b:2a:9c:23:fd:ec:38:35:92:f3:d9:cf:f4:6a:9
2:ad:38:
         8b:d6:a3:48:63:71:92:23:23:92:41:46:e2:49:4e:b
4:1b:8c:
         5c:e9:a3:a0:83:f0:6b:cd:62:5d:3d:6d:a5:5f:13:a
9:5d:ee:
         42:3d:05:27:e5:99:5e:b6:0f:df:71:d2:14:68:04:5
c:ee:15:
         26:ae:9c:02:1d:68:e5:5e:33:fb:72:8e:17:54:a2:e
6:95:40:
         cc:81:e3:11:b4:c1:f5:13:f6:58:ae:d7:43:65:64:9
```

We put this signature into a file, then remove all the colons and spaces from the signature:

```
    [10/18/20]seed@VM:~/cs458Lab2$ vi signature
    [10/18/20]seed@VM:~/cs458Lab2$ cat signature | tr -d '[:space:]:'
```

^{3.} ee87b56af7767dd20f4d9e9e5988cbe41dde7e24c56a56add210ad31f8177ffdc5bbdfae33b2a9c2 3fdec383592f3d9cff46a92ad388bd6a3486371922323924146e2494eb41b8c5ce9a3a083f06bcd6 25d3d6da55f13a95dee423d0527e5995eb60fdf71d21468045cee1526ae9c021d68e55e33fb728e1 754a2e69540[10/18/20]seed@VM:~/cs458Lab2\$

```
[10/18/20]seed@VM:~/cs458Lab2$ vi signature
[10/18/20]seed@VM:~/cs458Lab2$ cat signature | tr -d '[
:space:]:'
ee87b56af7767dd20f4d9e9e5988cbe41dde7e24c56a56add210ad3
1f8177ffdc5bbdfae33b2a9c23fdec383592f3d9cff46a92ad388bd
6a3486371922323924146e2494eb41b8c5ce9a3a083f06bcd625d3d
6da55f13a95dee423d0527e5995eb60fdf71d21468045cee1526ae9
c021d68e55e33fb728e1754a2e69540[10/18/20]seed@VM:~/cs45
8Lab2$
```

• Step4: Extract the body of the server's certificate

```
[10/18/20]seed@VM:~/cs458Lab2$ openssl asn1parse -i -in c0.pem
    0:d=0 hl=4 l=1425 cons: SEQUENCE
    4:d=1 hl=4 l=1145 cons: SEQUENCE
   8:d=2 hl=2 l= 3 cons:
                              cont [ 0 ]
   10:d=3 hl=2 l=
                    1 prim:
                               INTEGER
  13:d=2 hl=2 l=
                   16 prim:
                              INTEGER
                                                :079AB6B13FB635B20800000000
5B2DD7
   31:d=2 hl=2 l=
                   13 cons:
                              SEQUENCE
  33:d=3 hl=2 l=
                    9 prim:
                               OBJECT
                                                 :sha256WithRSAEncryption
   44:d=3 hl=2 l=
                    0 prim:
                               NULL
  46:d=2 h1=2 1= 66 cons:
                              SEQUENCE
   48:d=3 hl=2 l= 11 cons:
                               SET
  50:d=4 hl=2 l=
                                SEQUENCE
                   9 cons:
                    3 prim:
   52:d=5 hl=2 l=
                                 OBJECT
                                                   :countryName
   57:d=5 h1=2 1=
                   2 prim:
                                 PRINTABLESTRING
   61:d=3 hl=2 l=
                   30 cons:
  63:d=4 hl=2 l= 28 cons:
                              SEQUENCE
   65:d=5 hl=2 l=
                    3 prim:
                                 OBJECT
                                                   :organizationName
  70:d=5 hl=2 l=
                   21 prim:
                                 PRINTABLESTRING
                                                   :Google Trust Services
   93:d=3 hl=2 l=
                   19 cons:
                               SET
  95:d=4 hl=2 l=
                   17 cons:
                                SEQUENCE
  97:d=5 hl=2 l=
                    3 prim:
                                 OBJECT
                                                   :commonName
 102:d=5 hl=2 l=
                   10 prim:
                                 PRINTABLESTRING
                                                   :GTS CA 101
 114:d=2 hl=2 l=
                   30 cons:
                              SEQUENCE
 116:d=3 hl=2 l= 13 prim:
                               UTCTIME
                                                 :200922151619Z
 131:d=3 hl=2 l= 13 prim:
                               UTCTIME
                                                 :201215151619Z
 146:d=2 hl=2 l= 104 cons:
                              SEOUENCE
 148:d=3 hl=2 l= 11 cons:
                               SFT
 150:d=4 hl=2 l=
                                SEQUENCE
                   9 cons:
 152:d=5 hl=2 l=
                    3 prim:
                                 OBJECT
                                                   :countryName
 157:d=5 hl=2 l=
                    2 prim:
                                 PRINTABLESTRING
  161:d=3 hl=2 l=
                   19 cons:
 163:d=4 hl=2 l= 17 cons:
                                SEQUENCE
 165:d=5 hl=2 l=
                    3 prim:
                                                   :stateOrProvinceName
                                 OBJECT
 170:d=5 hl=2 l=
                   10 prim:
                                 PRINTABLESTRING
                                                   :California
  182:d=3 hl=2 l=
                   22 cons:
 184:d=4 hl=2 l=
                   20 cons:
                                SEQUENCE
 186:d=5 hl=2 l=
                                                   :localityName
                    3 prim:
                                 OBJECT
 191:d=5 hl=2 l=
                                 PRINTABLESTRING
                                                   :Mountain View
                   13 prim:
  206:d=3 hl=2 l= 19 cons:
```

```
208:d=4 hl=2 l= 17 cons:
                                SEQUENCE
  210:d=5 hl=2 l=
                    3 prim:
                                 OBJECT
                                                   :organizationName
 215:d=5 hl=2 l=
                                 PRINTABLESTRING
                   10 prim:
                                                   :Google LLC
 227:d=3 hl=2 l=
                   23 cons:
                               SET
                   21 cons:
 229:d=4 hl=2 l=
                                SEQUENCE
 231:d=5 hl=2 l=
                    3 prim:
                                 OBJECT
                                                   :commonName
 236:d=5 hl=2 l= 14 prim:
                                 PRINTABLESTRING
                                                   :www.google.com
  252:d=2 hl=4 l= 290 cons:
                              SEQUENCE
 256:d=3 hl=2 l= 13 cons:
                               SEQUENCE
 258:d=4 hl=2 l=
                    9 prim:
                                OBJECT
                                                  :rsaEncryption
 269:d=4 h1=2 1=
                    0 prim:
                                NULL
  271:d=3 hl=4 l= 271 prim:
                               BIT STRING
 546:d=2 hl=4 l= 603 cons:
                              cont [ 3 ]
 550:d=3 h1=4 l= 599 cons:
                               SEQUENCE
 554:d=4 hl=2 l= 14 cons:
                                SEQUENCE
 556:d=5 hl=2 l=
                    3 prim:
                                 OBJECT
                                                   :X509v3 Key Usage
 561:d=5 hl=2 l=
                                 BOOLEAN
                    1 prim:
                                                   :255
 564:d=5 hl=2 l=
                    4 prim:
                                 OCTET STRING
                                                   [HEX DUMP]:030205A0
 570:d=4 hl=2 l= 19 cons:
                                SEQUENCE
 572:d=5 hl=2 l=
                    3 prim:
                                 OBJECT
                                                   :X509v3 Extended Key Usa
ge
 577:d=5 hl=2 l=
                   12 prim:
                                 OCTET STRING
                                                   [HEX DUMP]:300A06082B060
10505070301
 591:d=4 hl=2 l=
                                SEQUENCE
                   12 cons:
 593:d=5 hl=2 l=
                                                   :X509v3 Basic Constraint
                    3 prim:
                                 OBJECT
 598:d=5 h1=2 1=
                                                   :255
                    1 prim:
                                 BOOLEAN
 601:d=5 hl=2 l=
                                                   [HEX DUMP]:3000
                    2 prim:
                                 OCTET STRING
 605:d=4 hl=2 l=
                   29 cons:
                                SEQUENCE
 607:d=5 hl=2 l=
                                                   :X509v3 Subject Key Iden
                    3 prim:
                                 OBJECT
tifier
 612:d=5 hl=2 l= 22 prim:
                                 OCTET STRING
                                                   [HEX DUMP]:041430D10B8CB
004CF4F3809344169CB2658371E3989
 636:d=4 hl=2 l= 31 cons:
                                SEQUENCE
 638:d=5 h1=2 1=
                                 OBJECT
                                                   :X509v3 Authority Key Id
                    3 prim:
entifier
 643:d=5 hl=2 l= 24 prim:
                                 OCTET STRING
                                                   [HEX DUMP]:3016801498D1F
86E10EBCF9BEC609F18901BA0EB7D09FD2B
 669:d=4 hl=2 l= 104 cons:
                                SEQUENCE
 671:d=5 hl=2 l=
                                                   :Authority Information A
                    8 prim:
                                 OBJECT
ccess
                                 OCTET STRING
                                                   [HEX DUMP]:305A302B06082
 681:d=5 hl=2 l= 92 prim:
F7265302B06082B06010505073002861F687474703A2F2F706B692E676F6F672F677372322F4
75453314F312E637274
 775:d=4 hl=2 l= 25 cons:
                                SEQUENCE
 777:d=5 hl=2 l=
                    3 prim:
                                 OBJECT
                                                   :X509v3 Subject Alternat
ive Name
 782:d=5 hl=2 l= 18 prim:
                                 OCTET STRING
                                                   [HEX DUMP]:3010820E77777
72E676F6F676C652E636F6D
 802:d=4 hl=2 l= 33 cons:
                                SEQUENCE
 804:d=5 hl=2 l=
                    3 prim:
                                 OBJECT
                                                   :X509v3 Certificate Poli
cies
 809:d=5 hl=2 l= 26 prim:
                                 OCTET STRING
                                                   [HEX DUMP]:3018300806066
7810C010202300C060A2B06010401D679020503
 837:d=4 hl=2 l= 51 cons:
                                SEQUENCE
 839:d=5 hl=2 l=
                    3 prim:
                                 OBJECT
                                                   :X509v3 CRL Distribution
 Points
```

```
844:d=5 hl=2 l= 44 prim:
                                                   [HEX DUMP]:302A3028A026A
                                 OCTET STRING
0248622687474703A2F2F63726C2E706B692E676F6F672F475453314F31636F72652E63726C
  890:d=4 hl=4 l= 259 cons:
                                SEQUENCE
 894:d=5 hl=2 l= 10 prim:
                                 OBJECT
                                                   :CT Precertificate SCTs
 906:d=5 hl=3 l= 244 prim:
                                 OCTET STRING
                                                   [HEX DUMP]:0481F100EF007
500F095A459F200D18240102D2F93888EAD4BFE1D47E399E1D034A6B0A8AA8EB27300000174B
69A0138000004030046304402201034D340BF23149A136B15852F9D26D9D7B21EDF4988DEC9B
1CE9C53ADA111420220674DCCA6A8679B97005EE54DE72721B7B6781E1FD6027C17647928661
DD7FA0E007600B21E05CC8BA2CD8A204E8766F92BB98A2520676BDAFA70E7B249532DEF8B905
E00000174B69A003A0000040300473045022004525AD7BF1F637FF83DBF79379861D897D1DC4
27D0146DBD2F7DFDF5AB1FCDB022100C94C114BB3541DB9B4DEE92F9773B12E402F6B8776152
D261CF3E752459B95DF
1153:d=1 hl=2 l= 13 cons:
                             SEQUENCE
 1155:d=2 hl=2 l=
                    9 prim:
                              OBJECT
                                                :sha256WithRSAEncryption
 1166:d=2 hl=2 l=
                    0 prim:
                              NULL
 1168:d=1 hl=4 l= 257 prim: BIT STRING
```

```
25 cons:
                                 SEQUENCE
  775:d=4
           hl=2 l=
  777:d=5
                                   OBJECT
                                                     : X5
           hl=2 l=
                     3 prim:
09v3 Subject Alternative Name
                                                     [HE
  782:d=5
         hl=2 l= 18 prim:
                                  OCTET STRING
X DUMP]:3010820E7777772E676F6F676C652E636F6D
  802:d=4 hl=2 l=
                    33 cons:
                                 SEQUENCE
  804:d=5
          hl=2 l=
                     3 prim:
                                   OBJECT
09v3 Certificate Policies
  809:d=5 hl=2 l=
                    26 prim:
                                  OCTET STRING
                                                     THE
X DUMP]:30183008060667810C010202300C060A2B06010401D6790
20503
  837:d=4
                    51 cons:
           hl=2 l=
                                 SEQUENCE
  839:d=5
          hl=2 l=
                     3 prim:
                                   OBJECT
                                                     :X5
09v3 CRL Distribution Points
  844:d=5 hl=2 l=
                                                     THE
                    44 prim:
                                   OCTET STRING
X DUMP1:302A3028A026A0248622687474703A2F2F63726C2E706B6
92E676F6F672F475453314F31636F72652E63726C
  890:d=4
         hl=4 l= 259 cons:
                                 SEQUENCE
  894:d=5
          hl=2 l= 10 prim:
                                   OBJECT
                                                     :CT
 Precertificate SCTs
  906:d=5 hl=3 l= 244 prim:
                                   OCTET STRING
                                                     [HE
X DUMP]:0481F100EF007500F095A459F200D18240102D2F93888EA
```

In this we cannot determine the end of the body. So we use -strparse to get the field from the offset 4, which will give us the body of the certificate, excluding the signature block.

^{1. [10/18/20]}seed@VM:~/cs458Lab2\$ openssl asn1parse -i -in c0.pem -strparse 4 out c0 body.bin -noout

^{2. [10/18/20]}seed@VM:~/cs458Lab2\$ sha256sum c0 body.bin

^{3.} fe5623d9b8e79ffa12b3b6471ae96c3ebc8ee5b6144305320c8c7de06443269a c0_body.bin

```
[10/18/20]seed@VM:~/cs458Lab2$ openssl asn1parse -i -in c0.pem -strparse 4 -out c0_body.bin -noout [10/18/20]seed@VM:~/cs458Lab2$ sha256sum c0_body.bin fe5623d9b8e79ffa12b3b6471ae96c3ebc8ee5b6144305320c8c7de 06443269a c0_body.bin [10/18/20]seed@VM:~/cs458Lab2$
```

• Step5: Verify the signature.

Code is similar to 3.5, We use the values obtained from the previous steps, get the signature and verify the signature obtained with the original signature

```
#include <stdio.h>
#include <openssl/bn.h>
#define NBITS 256
//print a big number
void printBN(char *msg, BIGNUM *a){
char * number str = BN bn2hex(a);
printf("%s %s\n", msg, number_str);
OPENSSL free(number str);
int main(){
    BN CTX *ctx = BN CTX new();
    BIGNUM *S = BN new();//signature from server step3
    BIGNUM *M = BN new();//signature cerificate
    BIGNUM *n = BN new();//modulus
    BIGNUM *e = BN new();//exponent
    BIGNUM *M1 = BN new();
    //Initialize
    BN hex2bn(&e, "01001");
"task6.c" 44L, 1731C
```

```
[10/19/20]seed@VM:~/cs458Lab2$ vi task6.c
[10/19/20]seed@VM:~/cs458Lab2$ gcc -o task6 task6.c -lc
rypto
[10/19/20]seed@VM:~/cs458Lab2$ ./task6
Valid Signature!
[10/19/20]seed@VM:~/cs458Lab2$
```

We can notice that the original message and the hash value of the computed message is the same. Hence we can conclude that the www.google.com certificate is verified to be right.