## 1. Run https://www.tensorflow.org/tutorials/keras/classification . This classifier works on fashion items.

# 1.1. Result

I compiled the code and made it run.

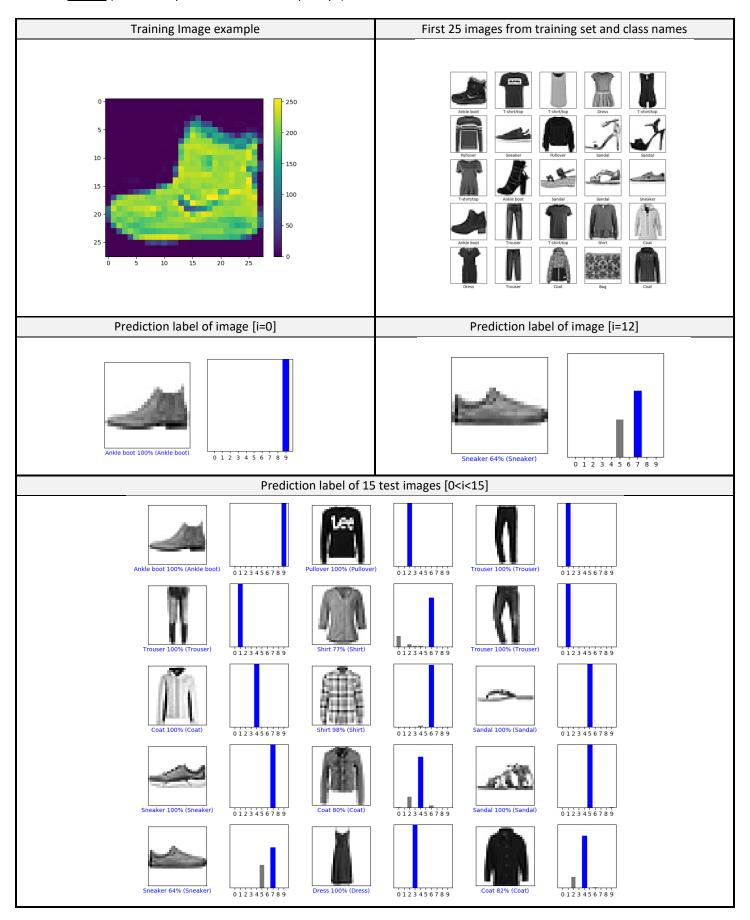
The model was trained using 10 epochs and reached an accuracy of 91.08% on the training data. The accuracy of the test dataset reached 88%.

## 1.2. Output (The full output is available in "Output.zip"):

```
Epoch 1/10
 32/60000 [.....] - ETA: 3:29 - loss: 2.3689 - acc: 0.1562
 832/60000 [.....] - ETA: 11s - loss: 1.3873 - acc: 0.5373
60000/60000 [============] - 4s 58us/sample - loss: 0.4938 - acc: 0.8256
Epoch 2/10
 32/60000 [.....] - ETA: 9s - loss: 0.1532 - acc: 0.9375
 960/60000 [.....] - ETA: 3s - loss: 0.4037 - acc: 0.8635
60000/60000 [============] - 3s 57us/sample - loss: 0.3697 - acc: 0.8671
Epoch 3/10
 32/60000 [.....] - ETA: 9s - loss: 0.3800 - acc: 0.8750
 960/60000 [.....] - ETA: 3s - loss: 0.3207 - acc: 0.8917
60000/60000 [============] - 4s 59us/sample - loss: 0.3338 - acc: 0.8788
Epoch 4/10
 32/60000 [.....] - ETA: 9s - loss: 0.2278 - acc: 0.9375
 960/60000 [.....] - ETA: 3s - loss: 0.2901 - acc: 0.8979
60000/60000 [============] - 3s 57us/sample - loss: 0.3102 - acc: 0.8873
Epoch 5/10
 32/60000 [.....] - ETA: 9s - loss: 0.1193 - acc: 0.9375
 992/60000 [.....] - ETA: 3s - loss: 0.3120 - acc: 0.8831
60000/60000 [============] - 3s 57us/sample - loss: 0.2947 - acc: 0.8918
Epoch 6/10
 32/60000 [.....] - ETA: 9s - loss: 0.2225 - acc: 0.9375
 960/60000 [.....] - ETA: 3s - loss: 0.3150 - acc: 0.8823
Epoch 7/10
 32/60000 [.....] - ETA: 29s - loss: 0.1169 - acc: 0.9688
1152/60000 [.....] - ETA: 3s - loss: 0.2344 - acc: 0.9115
60000/60000 [============] - 3s 57us/sample - loss: 0.2681 - acc: 0.9009
Epoch 8/10
 32/60000 [.....] - ETA: 9s - loss: 0.1449 - acc: 0.9375
 960/60000 [.....] - ETA: 3s - loss: 0.2596 - acc: 0.9042
```

```
60000/60000 [============] - 3s 58us/sample - loss: 0.2579 - acc: 0.9032
Epoch 9/10
 32/60000 [.....] - ETA: 7s - loss: 0.1876 - acc: 0.9688
 928/60000 [.....] - ETA: 3s - loss: 0.2276 - acc: 0.9159
60000/60000 [============ ] - 3s 57us/sample - loss: 0.2472 - acc: 0.9082
Epoch 10/10
 32/60000 [.....] - ETA: 9s - loss: 0.3489 - acc: 0.8438
928/60000 [.....] - ETA: 3s - loss: 0.2369 - acc: 0.9084
60000/60000 [============] - 3s 58us/sample - loss: 0.2410 - acc: 0.9108
10000/10000 - 0s - loss: 0.3494 - acc: 0.8800
Test accuracy: 0.88
(28, 28)
(1, 28, 28)
[[5.5457942e-05 1.6383477e-14 9.9598467e-01 3.2473368e-10 1.3082309e-03
 2.7307448e-16 2.6517855e-03 2.6463840e-17 1.4227564e-10 4.2015943e-15]]
```

# 1.3. Graphs (The full output is available in "Output.zip"):



## 2. Convert it to recognize digits. There is also an minst dataset for digits.

## 2.1. Result

I changed the training dataset into dataset of digit images, and the class names accordingly. The model was trained using 10 epochs and reached an accuracy of 99.56% on the training data. The accuracy of the test dataset reached 97.87%.

2.2. <u>Code</u> (The full code is available in "Python.zip"):

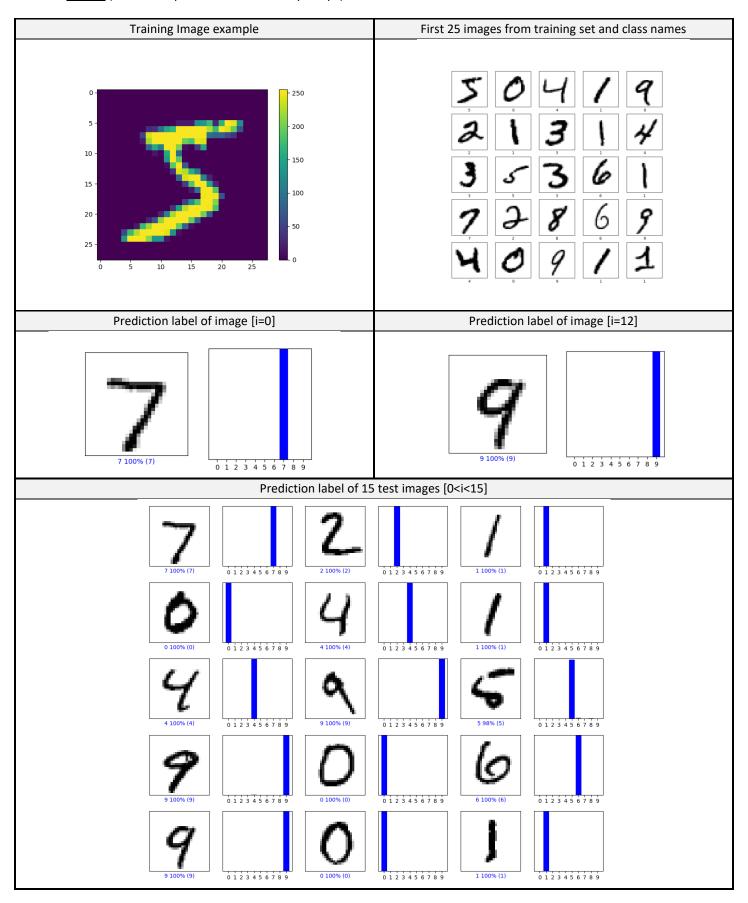
```
digit_minst = keras.datasets.mnist
(train_images, train_labels), (test_images, test_labels) = digit_minst.load_data()
class_names = ['0', '1', '2', '3', '4', '5', '6', '7', '8', '9']
```

2.3. Output (The full output is available in "Output.zip"):

```
Epoch 1/10
 32/60000 [.....] - ETA: 3:12 - loss: 2.5639 - acc: 0.0625
 672/60000 [.....] - ETA: 13s - loss: 1.7868 - acc: 0.4658
60000/60000 [============] - 4s 64us/sample - loss: 0.2554 - acc: 0.9256
Epoch 2/10
 32/60000 [.....] - ETA: 11s - loss: 0.0126 - acc: 1.0000
 768/60000 [.....] - ETA: 4s - loss: 0.1200 - acc: 0.9714
60000/60000 [===========] - 5s 79us/sample - loss: 0.1143 - acc: 0.9668
Epoch 3/10
 32/60000 [.....] - ETA: 11s - loss: 0.0470 - acc: 0.9688
 896/60000 [.....] - ETA: 3s - loss: 0.0740 - acc: 0.9821
60000/60000 [============] - 4s 61us/sample - loss: 0.0786 - acc: 0.9763
Epoch 4/10
 32/60000 [.....] - ETA: 7s - loss: 0.0256 - acc: 1.0000
 832/60000 [.....] - ETA: 3s - loss: 0.0508 - acc: 0.9844
60000/60000 [============] - 4s 59us/sample - loss: 0.0590 - acc: 0.9817
Epoch 5/10
 32/60000 [.....] - ETA: 9s - loss: 0.0391 - acc: 1.0000
 928/60000 [.....] - ETA: 3s - loss: 0.0423 - acc: 0.9860
60000/60000 [============] - 4s 59us/sample - loss: 0.0462 - acc: 0.9855
Epoch 6/10
 32/60000 [.....] - ETA: 9s - loss: 0.0202 - acc: 1.0000
 960/60000 [.....] - ETA: 3s - loss: 0.0510 - acc: 0.9854
60000/60000 [============] - 4s 63us/sample - loss: 0.0355 - acc: 0.9890
Epoch 7/10
 32/60000 [.....] - ETA: 9s - loss: 0.0013 - acc: 1.0000
 800/60000 [.....] - ETA: 4s - loss: 0.0199 - acc: 0.9950
1504/60000 [.....] - ETA: 4s - loss: 0.0249 - acc: 0.9920
60000/60000 [=========================== ] - 4s 66us/sample - loss: 0.0301 - acc: 0.9903
Epoch 8/10
 32/60000 [.....] - ETA: 18s - loss: 0.0074 - acc: 1.0000
 576/60000 [.....] - ETA: 6s - loss: 0.0193 - acc: 0.9965
```

```
60000/60000 [============] - 6s 97us/sample - loss: 0.0229 - acc: 0.9932
Epoch 9/10
 32/60000 [.....] - ETA: 14s - loss: 0.0062 - acc: 1.0000
 608/60000 [.....] - ETA: 5s - loss: 0.0136 - acc: 0.9934
60000/60000 [============] - 4s 65us/sample - loss: 0.0197 - acc: 0.9942
Epoch 10/10
 32/60000 [.....] - ETA: 9s - loss: 0.0058 - acc: 1.0000
 896/60000 [.....] - ETA: 3s - loss: 0.0167 - acc: 0.9978
60000/60000 [=============] - 4s 62us/sample - loss: 0.0152 - acc: 0.9956
10000/10000 - 0s - loss: 0.0812 - acc: 0.9787
Test accuracy: 0.9787
(28, 28)
(1, 28, 28)
[[9.7758135e-11 1.4205011e-07 9.9999821e-01 4.6705611e-07 4.9148202e-18
 2.0141092e-10 4.5865227e-09 1.7331948e-16 1.1550956e-06 4.3926822e-16]]
```

# 2.4. Graphs (The full output is available in "Output.zip"):



- 3. Make modifications to the networks and report the train and test accuracies as you modify the networks. You can also change the activation function.
- 4. Plot a histogram of the accuracies of the test examples for correctly and incorrectly classified objects.

# 4.1. Result

I changed the network by enlarging the training: instead of 10 epochs - I used 200 epochs.

In addition, instead of 128 layers, I used 300 layers.

The model was reached an accuracy of 100% on the training data (In comparison to the accuracy of 99.56% reached in previous model).

The accuracy of the test dataset reached 98.41% (In comparison to the accuracy of 97.87% reached in previous model). In addition, I plotted an histogram that represents the model accuracy. According to the histogram of the accuracies, 98.41% of the test images were correct and 1.59% were incorrect.

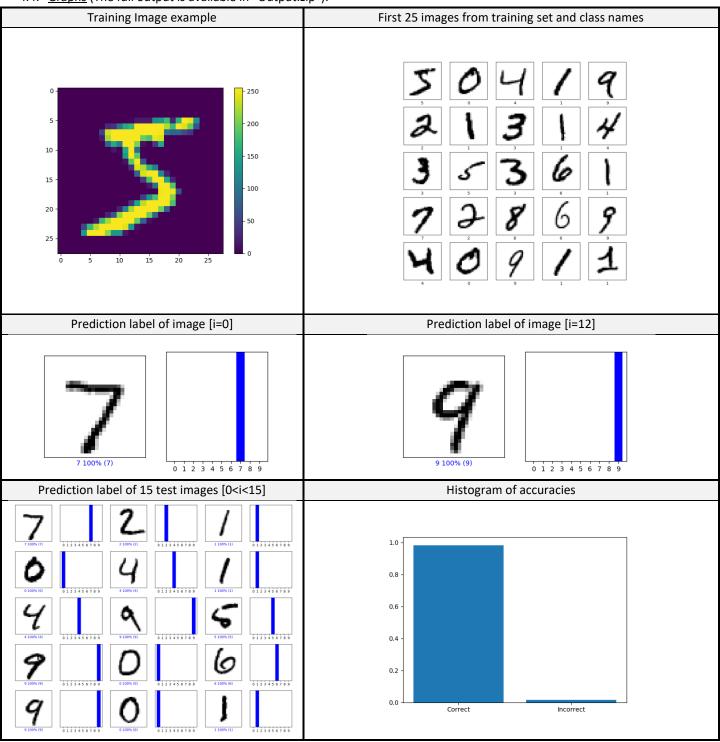
4.2. Code (The full code is available in "Python.zip"):

```
# Build the model
model = keras.Sequential([
    keras.layers.Flatten(input_shape=(28, 28)),
    keras.layers.Dense(300, activation='relu'),
    keras.layers.Dense(10, activation='softmax')
])
model.fit(train_images, train_labels, epochs=200)
# Plot accuracy
x = np.arange(2)
plt.bar(x, height= [test_acc , 1-test_acc])
plt.xticks(x, ['Correct', 'Incorrect'])
```

4.3. Output (The full output is available in "Output.zip"):

```
Epoch 1/200
 32/60000 [.....] - ETA: 2:18 - loss: 2.4784 - acc: 0.0625
 832/60000 [.....] - ETA: 8s - loss: 1.5719 - acc: 0.5541
1600/60000 [.....] - ETA: 6s - loss: 1.1595 - acc: 0.6888
2464/60000 [>.....] - ETA: 5s - loss: 0.9609 - acc: 0.7317
Epoch 200/200
 32/60000 [.....] - ETA: 9s - loss: 0.0000e+00 - acc: 1.0000
 640/60000 [.....] - ETA: 5s - loss: 0.0000e+00 - acc: 1.0000
1216/60000 [.....] - ETA: 5s - loss: 0.0000e+00 - acc: 1.0000
10000/10000 - 1s - loss: 0.2675 - acc: 0.9841
Test accuracy: 0.9841
(28, 28)
(1, 28, 28)
[[0.0000000e+00 1.9053744e-33 1.0000000e+00 0.0000000e+00 0.0000000e+00
 0.0000000e+00 0.0000000e+00 0.0000000e+00 0.0000000e+00 0.0000000e+00]]
```

# 4.4. Graphs (The full output is available in "Output.zip"):



5. Change the test images and use the other test set (for fashion network test on the digits test dataset and vice versa). Here again plot histograms. How sure are the classifiers when run on the wrong type of data?

#### 5.1. Part A:

## 5.1.1. Result

I trained the model on the dataset of images of digits. Then, I tested the model over dataset of images of fashion. As the previous model, I used 200 epochs and 300 layers.

The model was reached an accuracy of 99.97% on the training data.

However, the accuracy of the test dataset reached 7.75%

According to the histogram of the accuracies, 7.75% of the test images were correct and 92.25% were incorrect.

Because the model was trained on one dataset and tested on another dataset - the model does not really know how to distinguish the different classifications of each image in the test dataset. The accuracy obtained seems to be random. Which means, the results the model was "correct" were random. In another run of the model, we may get different accuracy.

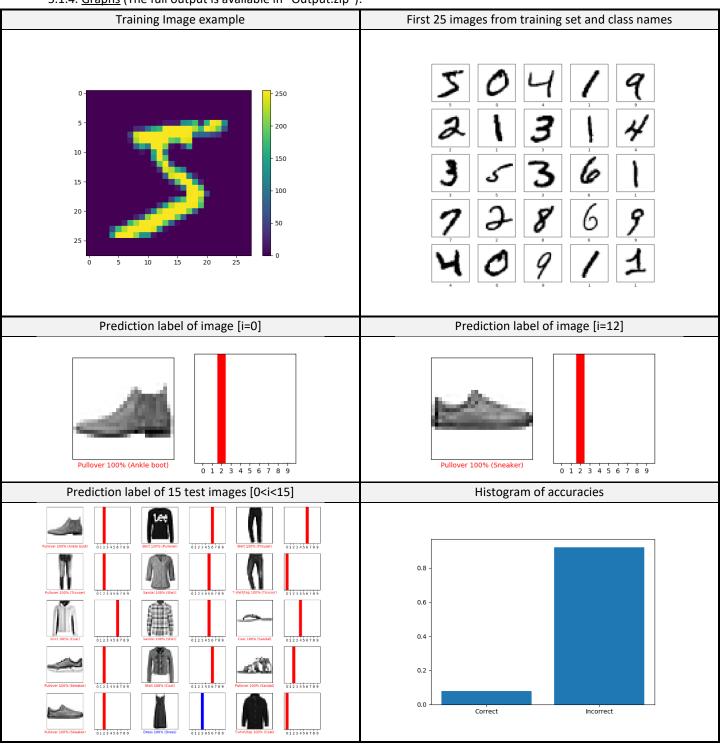
5.1.2. Code (The full code is available in "Python.zip"):

```
# Train the modelg
model.fit(digit_train_images, digit_train_labels, epochs=200)
# Test the model
test_loss, test_acc = model.evaluate(fashion_test_images, fashion_test_labels, verbose=2)
```

5.1.3. Output (The full output is available in "Output.zip"):

```
Epoch 1/200
 32/60000 [.....] - ETA: 4:08 - loss: 2.5637 - acc: 0.0000e+00
 608/60000 [.....] - ETA: 17s - loss: 1.6100 - acc: 0.5477
1216/60000 [.....] - ETA: 11s - loss: 1.1905 - acc: 0.6743
1792/60000 [.....] - ETA: 9s - loss: 0.9850 - acc: 0.7305
Epoch 200/200
 32/60000 [.....] - ETA: 16s - loss: 0.0000e+00 - acc: 1.0000
 928/60000 [.....] - ETA: 7s - loss: 3.6016e-04 - acc: 1.0000
1408/60000 [.....] - ETA: 6s - loss: 2.3738e-04 - acc: 1.0000
60000/60000 [============= ] - 6s 106us/sample - loss: 0.0018 - acc: 0.9997
Test size: 10000
10000/10000 - 0s - loss: 23955.7466 - acc: 0.0775
Test accuracy (original): 0.0775
Test accuracy (manual): 0.0775000000000001
(28, 28)
(1, 28, 28)
[[0. 0. 0. 0. 0. 0. 1. 0. 0. 0.]]
```

# 5.1.4. Graphs (The full output is available in "Output.zip"):



## 5.2. Part B:

# 5.2.1. Result

I trained the model on the dataset of images of fashion. Then, I tested the model over dataset of images of digits. As the previous model, I used 200 epochs and 300 layers.

The model was reached an accuracy of 99.25% on the training data.

However, the accuracy of the test dataset reached 19.73%.

According to the histogram of the accuracies, 19.73% of the test images were correct and 80.27% were incorrect.

Because the model was trained on one dataset and tested on another dataset - the model does not really know how to distinguish the different classifications of each image in the test dataset. The accuracy obtained seems to be random. Which means, the results the model was "correct" were random. In another run of the model, we may get different accuracy.

# 5.2.2. Code (The full code is available in "Python.zip"):

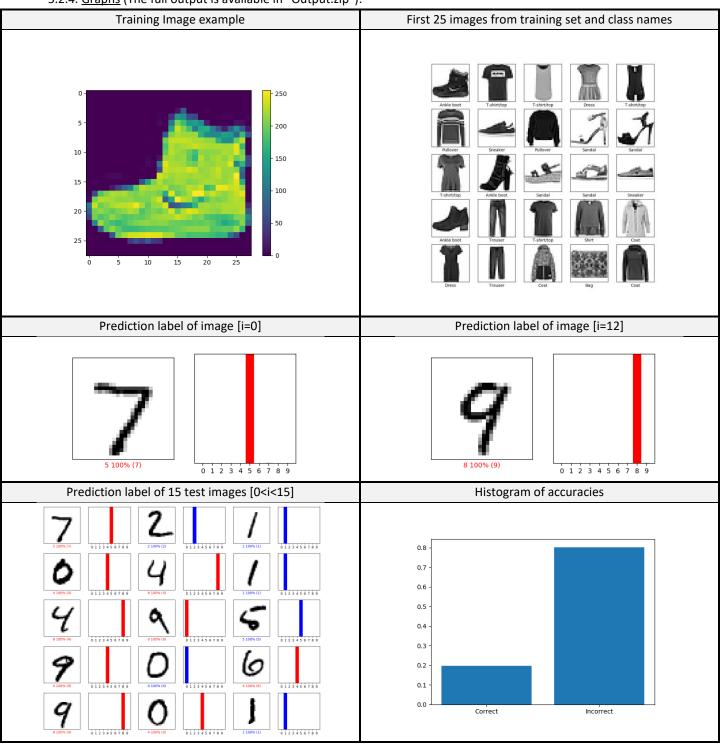
```
# Train the model 1
model.fit(fashion_train_images, fashion_train_labels, epochs=200)

# Test the model
test_loss, test_acc = model.evaluate(digit_test_images, digit_test_labels, verbose=2)
```

# 5.2.3. Output (The full output is available in "Output.zip"):

```
Epoch 1/200
 32/60000 [.....] - ETA: 3:25 - loss: 2.3026 - acc: 0.1875
 544/60000 [.....] - ETA: 17s - loss: 1.5222 - acc: 0.4908
1056/60000 [.....] - ETA: 12s - loss: 1.2227 - acc: 0.5900
1600/60000 [.....] - ETA: 9s - loss: 1.0494 - acc: 0.6494
Epoch 200/200
 32/60000 [.....] - ETA: 11s - loss: 4.4882e-04 - acc: 1.0000
 704/60000 [.....] - ETA: 4s - loss: 0.0422 - acc: 0.9830
1312/60000 [.....] - ETA: 4s - loss: 0.0436 - acc: 0.9840
1952/60000 [.....] - ETA: 4s - loss: 0.0410 - acc: 0.9867
60000/60000 [============] - 5s 82us/sample - loss: 0.0223 - acc: 0.9925
Test size: 10000
10000/10000 - 0s - loss: 10212.9262 - acc: 0.1973
Test accuracy (original): 0.1973
Test accuracy (manual): 0.19730000000000003
(28, 28)
(1, 28, 28)
[[0. 0. 1. 0. 0. 0. 0. 0. 0. 0.]]
```

# 5.2.4. Graphs (The full output is available in "Output.zip"):



6. Given a test image for one digit and a test image for another digit generate a set of images
I(alpha) = alpha \* I1 + (1-alpha) \* I2 for 100 alphas between 0 and 1. Run the digit classifier on these images and plot the results both the classification and the probability of the class. What are your conclusions from that?

# 6.1. Result

I trained the model on the dataset of images of digits.

Then, I generated a new test dataset of 100 images, where each image was generated from a weighted average of 2 images in the training dataset:  $I(\alpha) = \alpha \cdot I_1 + (1-\alpha) \cdot I_2$ ,  $\alpha \in [0,1)$ 

The labels of the generated test images were set according to the following rule: for each generated average-weighted image:  $I(\alpha)$  – if alpha is less than 0.5, then the label of  $I(\alpha)$  will be the label of  $I_2$ . Otherwise, it will be the label of  $I_1$ . Both of the images chosen randomly –  $I_1$  chosen as an image of the digit '2' and  $I_2$  chosen as an image of the digit '1'.  $I(\alpha)$  was an image of the combination of the images of digit '1' and '2'.

The model was reached an accuracy of 99.56% on the training data.

However, the accuracy of the test dataset reached 71%.

According to the histogram of the accuracies, 71% of the test images were correct and 29% were incorrect.

It is possible that in images with approximately alpha = 50%, it was difficult to categorize which class the image belongs to.

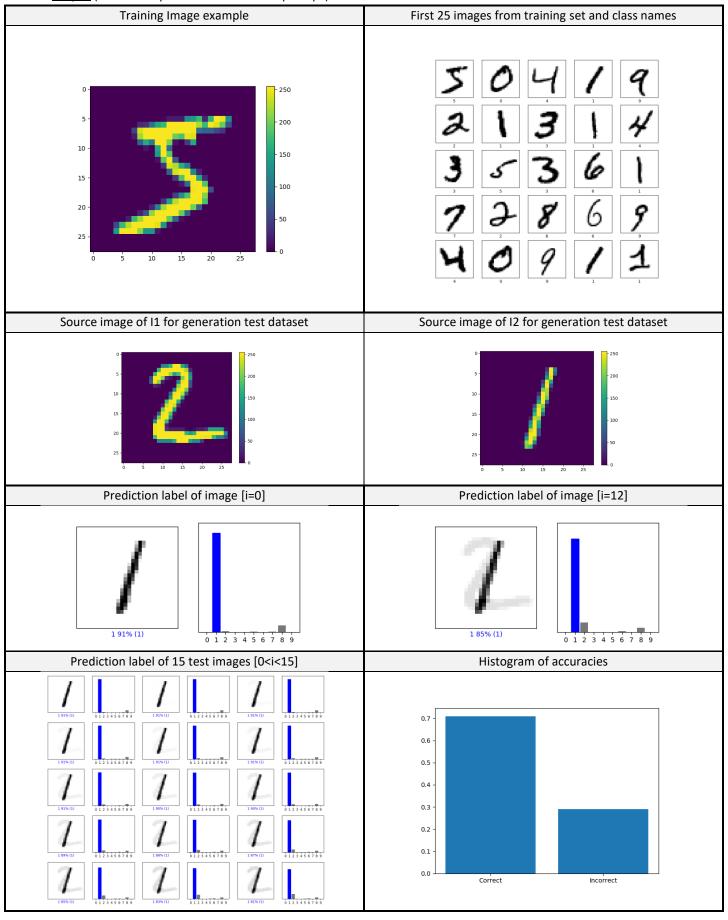
6.2. <u>Code</u> (The full code is available in "Python.zip"):

```
# Create new array
test_images_with_alpha_temp=[]
test_labels_with_alpha_temp=[]
test_images_with_alpha = np.array([])
test_labels_with_alpha = np.array([])
# Alpha is a number between 0 and 1
for number in range(0, 100, 1):
    # Create alpha
   alpha = (number/100)
   # Create new image
   img_new = ((img1 * alpha) + (img2 * (1 - alpha))) / 2
   print(img_new)
    if (number < 50):
        label_new = label2
        label_new = label1
    # Add new image to the list
   test_images_with_alpha_temp.append(img_new)
    # Add new image label to the array
   test_labels_with_alpha_temp.append(label_new)
# Create array of the generated images
test_images_with_alpha = np.stack(test_images_with_alpha_temp, axis=0)
test_labels_with_alpha = np.stack(test_labels_with_alpha_temp, axis=0)
test_loss, test_acc = model.evaluate(test_images_with_alpha, test_labels_with_alpha, verbose=2)
```

## 6.3. Output (The full output is available in "Output.zip"):

```
Epoch 1/10
 32/60000 [.....] - ETA: 2:14 - loss: 2.2323 - acc: 0.0938
 896/60000 [.....] - ETA: 8s - loss: 1.5415 - acc: 0.5614
1728/60000 [.....] - ETA: 5s - loss: 1.1578 - acc: 0.6840
Epoch 10/10
 32/60000 [.....] - ETA: 7s - loss: 0.0039 - acc: 1.0000
 992/60000 [.....] - ETA: 3s - loss: 0.0132 - acc: 0.9940
60000/60000 [============] - 4s 73us/sample - loss: 0.0146 - acc: 0.9956
Test images [[[0. 0. 0. ... 0. 0. 0.]
 [0. 0. 0. ... 0. 0. 0.]
 [0. 0. 0. ... 0. 0. 0.]
 [0. 0. 0. ... 0. 0. 0.]
 [0. 0. 0. ... 0. 0. 0.]
 [0. 0. 0. ... 0. 0. 0.]]
[[0. 0. 0. ... 0. 0. 0.]
 [0. 0. 0. ... 0. 0. 0.]
 [0. 0. 0. ... 0. 0. 0.]
 [0. 0. 0. ... 0. 0. 0.]
 [0. 0. 0. ... 0. 0. 0.]
 [0. 0. 0. ... 0. 0. 0.]]]
100/100 - 0s - loss: 0.9968 - acc: 0.7100
Test accuracy (original): 0.71
Test accuracy (manual): 0.71
(28, 28)
(1, 28, 28)
[[2.1226342e-04 9.0937620e-01 1.3782789e-02 5.6325016e-04 1.8312243e-03
 3.9818413e-03 4.1574440e-03 5.1381667e-03 6.0741700e-02 2.1514372e-04]]
```

# 6.4. Graphs (The full output is available in "Output.zip"):



7. Taking the two test images mentioned above, extract the results of the second layer (128 numbers) V1 and V2. Print them. These are the internal representation of the images.

## 7.1. Result

Using the previous model, I ran the algorithm once again and printed the images via representation in an array.

The first image was taken from the test dataset and was an image of the digit '2'.

The second image was taken from the test dataset and was an image of the digit '1'.

Then, I extracted the results of the second layer for each of them.

7.2. Code (The full code is available in "Python.zip"):

```
img1 = test_images[1]
label1 = test_labels[1]

img2 = test_images[2]
label2 = test_labels[2]

# Extract the second layer of each image from the test dataset

my_input_data = test_images

new_temp_model = K.Model(model.input, model.layers[1].output) #replace 3 with index of desired layer
output_of_2nd_layer = new_temp_model.predict(my_input_data) #this is what you want
output_of_2nd_layer_flatten = output_of_2nd_layer.flatten()

np.set_printoptions(threshold=np.inf) #Print all results
print('output_of_2nd_layer len=', len(output_of_2nd_layer)) # print test size

for i in range (len(output_of_2nd_layer)):
    print('\n','\n','output_of_2nd_layer, i=', i, 'output =' ,output_of_2nd_layer[i]) #print layers
```

## 7.3. Output (The full output is available in "Output.zip"):

label1 = 2

label2 = 1

output of 3	2nd layer, :	i= 1 outpui	F =		
[ 939.6247		0.		271.7932	0.
0.	0.			0.	817.9914
0.	669.9198			3.7656143	0.
0.	0.			98.77909	0.
545.8703	1639.1353			0.	0.
0.	869.582			0.	0.
2011.0665	0.			0.	0.
0.	0.	67.6		0.	0.
0.	304.4722			0.	0.
0.	0.			0.	0.
220.194	235.007				649.9116
0.	1392.4863			0.	0.
79.09892	0.			0.	0.
0.	519.595	54 0.		0.	0.
579.05383	1064.267		6:	26.804	0.
0.	972.136			0.	17.06022
0.	0.	0.		0.	0.
751.52686	0.	0.		65.27749	972.2796
184.36916	217.7673	3 0.		0.	0.
1013.7535	0.	0.		0.	181.12967
414.6407	1936.073	7 1989.60	023	0.	0.
85.19098	0.	0.	5	73.9432	0.
1167.6256	252.0218	35 0.		0.	570.8768
1663.2925		0.	6	57.4305	0.
0.	0.	0.	3	78.42084	330.3594
0.	0.	1475.9			
	2nd_layer, :				
	0.				603.65845
0.	557.0574	160.29947			48.41715
	423.2381	0.	0.		619.0772
0.					384.31854
283.62143	0.	0.		783.4692	
759.8518	34.8955	0.	0.	0.	0.
0.	0.	155.04541			73.29929
	635.4768		0.	0.	631.0795
	754.39124		0.	819.6793	
0.	0.	743.5557	0.	81.9681	
	0.			4 0.	
	43.361137	0.		276.6797	
					5 186.16173
				3 560.9479	
	568.3852		0.		
0.				7 811.0693	
54.205692	U.	830.5772	564.8198	25.6098	0. 430.67285
35.071133	U.	93.640594	U.	U.	430.67285
				0.	
	215.61148	0.	U.	7/16.0542	32.31893
0.	0. 396.6044	υ.	184.7853	4 0.	0.
108.8321/	390.6044	I			

8. Predict the results of the network using these vectors. That means run the final level only on them. You should get the same results.

## 8.1. Result

Using the previous model, I ran the algorithm once again and extracted the results of the last layer for each of the test images.

In each image, the last layer contains an array of probabilities - where each index represents the class possibilities of what the image can be, and each value in the array represents the probability that what is shown in the image is that class.

Then, I compared the classified results of the last layer to the true results of the test images.

The calculated accuracy and the accuracy of the model were equal. The accuracy that was obtained was 69%.

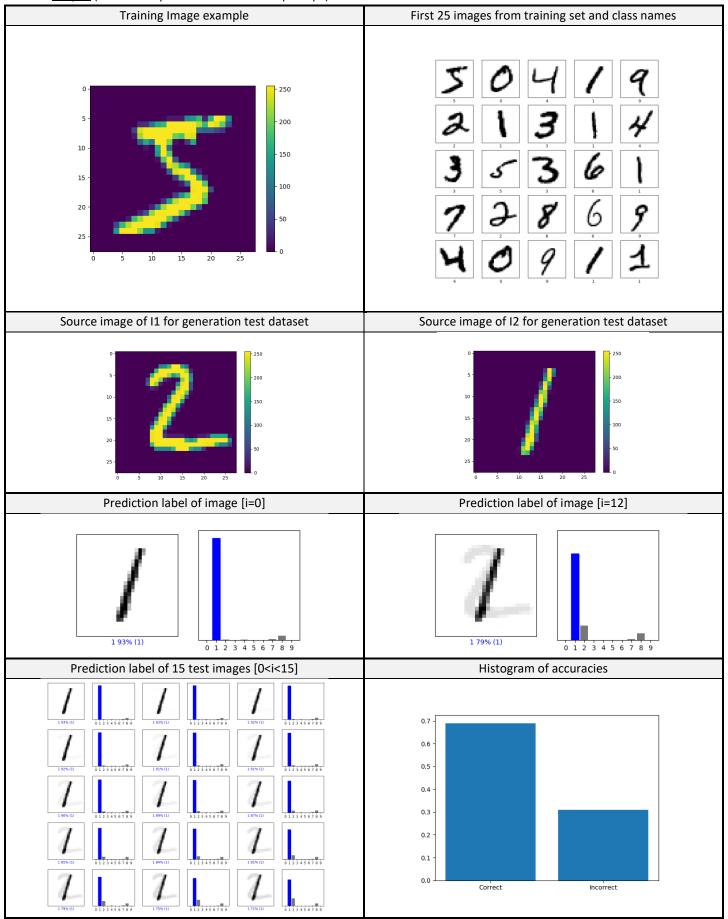
8.2. <u>Code</u> (The full code is available in "Python.zip"):

```
# Extract the second layer of each image from the test dataset
my_input_data = test_images_with_alpha
last_layer = len(model.layers)-1
new_temp_model = K.Model(model.input, model.layers[last_layer].output) #replace 3 with index of desired layer
output_of_last_layer = new_temp_model.predict(my_input_data) #this is what you want
output of last_layer_flatten = output_of_last_layer.flatten()
np.set printoptions(threshold=np.inf) #Print all results
list_of_max_index = []
for i in range (len(output_of_last_layer)):
    output_of_last_layer_of_img = output_of_last_layer[i]
    max_value = np.amax(output_of_last_layer_of_img)
    for j in range (len(output_of_last_layer_of_img)):
        if output_of_last_layer_of_img[j] == max_value:
            max_index = j
            list_of_max_index.append(j)
            break
    print('\n','\n','output_of_last_layer, i=', i, '\n',' output ='
,output_of_last_layer_of_img,'\n','max_value',max_value,'\n','max_index',max_index) #print Layers
# Evaluate accuracy
test_labels_with_alpha_list = np.array(test_labels_with_alpha)
test_loss, test_acc = model.evaluate(test_images_with_alpha, test_labels_with_alpha, verbose=2)
p = model.predict(test_images_with_alpha)
p = np.argmax(p,axis=1)
test_acc1 = 1-np.count_nonzero(p-test_labels_with_alpha)/len(test_labels_with_alpha)
check acc = 0
for k in range (len(test_labels_with_alpha_list)):
   if list_of_max_index[k] == test_labels_with_alpha_list[k]:
       check acc += 1
test_acc_from last_layer = check_acc / len(test_labels_with_alpha_list)
print('\nTest accuracy (original):', test acc, '\nTest accuracy (manual):', test acc1, '\nTest accuracy calculated
from last layer :', test_acc_from_last_layer)
```

## 8.3. Output (The full output is available in "Output.zip"):

```
test images with alpha [[[0. 0. 0. ... 0. 0. 0.]
 [0. 0. 0. ... 0. 0. 0.]
 [0. 0. 0. ... 0. 0. 0.]
Epoch 1/10
 32/60000 [.....] - ETA: 2:18 - loss: 2.3738 - acc: 0.0312
 896/60000 [.....] - ETA: 8s - loss: 1.6885 - acc: 0.5033
1664/60000 [.....] - ETA: 6s - loss: 1.2850 - acc: 0.6394
Epoch 10/10
60000/60000 [============] - 4s 71us/sample - loss: 0.0163 - acc: 0.9951
output of last layer, i= 0
 output = [6.9685047e-05 9.2785943e-01 7.5802724e-03 3.6837559e-04 6.9567957e-03
1.4146540e-03 4.8387828e-04 1.1721648e-02 4.3481901e-02 6.3396154e-05]
max value 0.9278594
max index 1
output of last layer, i= 1
 output = [7.8523102e-05 9.2608994e-01 9.4182445e-03 3.9074241e-04 6.7476197e-03
1.3486085e-03 5.3330365e-04 1.1593652e-02 4.3733556e-02 6.5767621e-05]
max value 0.92608994
max index 1
output of last layer, i= 2
output = [8.9377652e-05 9.2298049e-01 1.1829171e-02 4.2266774e-04 6.5958980e-03
1.3053172e-03 5.8274908e-04 1.1664173e-02 4.4460990e-02 6.9110501e-05]
max value 0.9229805
max index 1
2, 21
Test images [[[0.00000000e+00 0.0000000e+00 0.0000000e+00 0.0000000e+00
 0.0000000e+00 0.0000000e+00 0.0000000e+00 0.0000000e+00
 0.0000000e+00 0.0000000e+00 0.0000000e+00 0.0000000e+00
 0.0000000e+00 0.0000000e+00 0.0000000e+00 0.0000000e+00
  0.0000000e+00 0.0000000e+00 0.0000000e+00 0.0000000e+00
  0.0000000e+00 0.0000000e+00 0.0000000e+00 0.0000000e+00
  0.00000000e+00 0.00000000e+00 0.0000000e+00 0.00000000e+00]
...11
100/100 - 0s - loss: 0.9574 - acc: 0.6900
Test accuracy (original): 0.69
Test accuracy (manual): 0.69
Test accuracy calculated from last layer: 0.69
(28, 28)
(1, 28, 28)
[[7.8522884e-05 9.2609006e-01 9.4182501e-03 3.9074247e-04 6.7476141e-03
 1.3486061e-03 5.3330371e-04 1.1593665e-02 4.3733548e-02 6.5767628e-05]]
```

# 8.4. Graphs (The full output is available in "Output.zip"):



9. Take V1 and V2 and generate 50 vectors, where V(alpha) = alpha \* V1 + (1-alpha) \*V2, where alpha is between -1 and 2. Plot the probabilities for these two classes for all these values. See what values you get when alpha is far from 0 (digit 1) and 1 (digit 2).

#### 9.1. Result

I trained the model on the dataset of images of digits.

Then, I generated a new test dataset of 50 images, where each image was generated from a weighted average of 2 images in the training dataset:  $V(\alpha) = \alpha \cdot I_1 + (1 - \alpha) \cdot I_2$ ,  $\alpha \in [-1,2)$ 

The labels of the generated test images were set according to the following rule: for each generated average-weighted image:  $I(\alpha)$  – if alpha is less than 0.5 ((-1+2)/2 = 0.5), then the label of  $I(\alpha)$  will be the label of  $I_2$ . Otherwise, it will be the label of  $I_1$ .

Both of the images chosen randomly –  $I_1$  chosen as an image of the digit '2' and  $I_2$  chosen as an image of the digit '1'.  $I(\alpha)$  was an image of the combination of the images of digit '1' and '2'.

The model was reached an accuracy of 99.49% on the training data.

However, the accuracy of the test dataset reached 66%.

According to the histogram of the accuracies, 66% of the test images were correct and 34% were incorrect.

According to the results, when alpha is far from 0, which means closer to  $I_1$  and the image of the digit '2' is more prominent but white - then the model recognizes most of the test images as an image of the digit '7'.

However, when alpha is closer to from 0, which means closer to  $I_2$  and the image of the digit '1' is more prominent but white - then the model recognizes most of the test images as an image of the digit '2'.

9.2. Code (The full code is available in "Python.zip"):

```
# Create new array
test_images_with_alpha_temp=[]
test_labels_with_alpha_temp=[]
test_images_with_alpha = np.array([])
test_labels_with_alpha = np.array([])
# Alpha is a number between -1 and 2
alpha=-1
while alpha<2:</pre>
    # Create new image
    img_new = ((img1 * alpha) + (img2 * (1 - alpha))) / 2
   print(img_new)
    if (alpha < 0.5):
        label_new = label2
    else:
        label_new = label1
    # Add new image to the list
   test_images_with_alpha_temp.append(img_new)
    # Add new image label to the array
    test_labels_with_alpha_temp.append(label_new)
    #test_labels_with_alpha = np.append(test_labels_with_alpha, label_new)
    alpha += 0.06
# Create array of the generated images
test_images_with_alpha = np.stack(test_images_with_alpha_temp, axis=0)
test_labels_with_alpha = np.stack(test_labels_with_alpha_temp, axis=0)
test_loss, test_acc = model.evaluate(test_images_with_alpha, test_labels_with_alpha, verbose=2)
```

# 9.3. Output (The full output is available in "Output.zip"):

img				0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
[	0	0	0	0	0	0	0	0	0	0]	0	0	0	0	0	0	0	0		
]	0	0	0	0	0	0	0	0	0	0]	0	0	0	0	0	0	0	0		
]	0	0	0	0	0	0	0	0	0		116	125	171	255	255	150	93	0		
]	0	0	0	0	0	0	0	0	0	0] 169	253	253	253	253	253	253	218	30		
[	0	0	0	0	0	0	0	0	0 169	0] 253	253	253	213	142	176	253	253	122		
	0	0	0	0	0	0	0	0	0	0]										
[	0	0	0	0	0	0	0	0	250	253	210	32	12	0	ю	206	253	140		
[	0	0	0	0	0	0	0			210	25	0	0	0	122	248	253	65		
[	0	0	0	0	0	0	0	0	0 31	0] 18	0	0	0	0	209	253	253	65		
г	0	0	0	0	0	0	0	0	0	0]	0	0	0	117	247	253	100	10		
[	0	0	0	0	0	0	0	0	0	0]		U	U	11/	241	233	190	10		
[	0	0	0	0	0	0	0	0	0	0	0	0	76	247	253	231	63	0		
[	0	0	0	0	0	0	0	0	0	0]	0	0	128	253	253	144	0	0		
г	0	0	0	0	0	0	0	0	0	0]		176	216	252	150	1 0	0	0		
[	0	0	0	0	0	0	0	0	0	0 0]		1/0	240	253	159	12	U	U		
[	0	0	0	0	0	0	0	0	0	0		234	253	233	35	0	0	0		
[	0	0	0	0	0	0	0	0	0	0]		253	253	141	0	0	0	0		
	0	0	0	0	0	0	0	0	0	0]										
[	0	0	0	0	0	0	0	0	0	78 0]		253	189	12	0	0	0	0		
[	0	0	0	0	0	0	0	0		200		253	141	0	0	0	0	0		
]	0	0	0	0	0	0	0	0	134	0] 253	253	173	12	0	0	0	0	0		
L	0	0	0	0	0	0	0	0	0	0]	200	175		Ü	Ü	Ü	Ü	Ü		
[	0	0	0	0	0	0	0	0	248	253	253	25	0	0	0	0	0	0		
[	0	0	0	0	0	0	0			253	253	43	20	20	20	20	5	0		
1	5	20	20	37 0	150	150	150 0			0] 253	253	253	253	253	253	253	168	143		
1	66	253	253	253	253	253	253	253	123	0]										
							0 117		174 57	253 0]		253	253	253	253	253	253	253		
[		0	0	0	0	0	0	0		118		123	123	166	253	253	253	155		
		123	41	0	0	0	0	0	0	0]		0	0	0	0	0	0	0		
[	0	0	0	0	0	0	0	0	0	0 0]	0	0	U	U	U	U	0	0		
[	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0		
[	0	0	0	0	0	0	0	0	0	0]	0	0	0	0	0	0	0	0		
	0	0	0	0	0	0	0	0	0	0]			_	_	_	_	_	_		
[	0	0	0	0	0	0	0	0	0	0 0]	0	0	0	0	0	0	0	0		
[	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0		
lab	0 el1	0	0	0	0	0	0	0	0	0]	]									

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img	2 =	] ]	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	0	0	0	0	0	0	0	0	0	0]										
[	0	0	0	0	0	0	0	0	0	0 0]	0	0	0	0	0	0	0	0		
[	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0		
	0	0	0	0	0	0	0	0	0	0]										
[	0	0	0	0	0	0	0	0	0	0 0]	0	0	0	0	0	0	0	0		
[	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	38	254		
1	09	0	0	0	0	0	0	0	0	0]										
[	0 82	0	0	0	0	0	0	0	0	0 0]	0	0	0	0	0	0	87	252		
[	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	135	241		
	0	0	0	0	0	0	0	0	0	0]										
[	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	45	244	150		
[	0	0	0	0	0	0	0	0	0	0]	0	0	0	0	0	84	254	63		
٠	0	0	0	0	0	0	0	0	0	0]										
[	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	202	223	11		
[	0	0	0	0	0	0	0	0	0	0]	0	0	0	0	32	254	216	0		
L	0	0	0	0	0	0	0	0	0	0]	Ü		Ü	Ü	02	201	210	Ü		
[	0	0	0	0	0	0	0	0	0	0	0	0	0	0	95	254	195	0		
[	0	0	0	0	0	0	0	0	0	0]	0	0	0	0	140	254	77	0		
L	0	0	0	0	0	0	0	0	0	0]	U	U	U	U	140	234	, ,	U		
[	0	0	0	0	0	0	0	0	0	0	0	0	0	57	237	205	8	0		
	0	0	0	0	0	0	0	0	0	0]	0	0	0	101	255	1 ( =	0	0		
[	0	0	0	0	0	0	0	0	0	0 0]	0	0	U	124	255	165	0	0		
[	0	0	0	0	0	0	0	0	0	0	0	0	0	171	254	81	0	0		
	0	0	0	0	0	0	0	0	0	0]										
[	0	0	0	0	0	0	0	0	0	0	0	0	24	232	215	0	0	0		
[	0	0	0	0	0	0	0	0	0	0]	0	0	120	254	159	0	0	0		
	0	0	0	0	0	0	0	0	0	0]										
[	0	0	0	0	0	0	0	0	0	0	0	0	151	254	142	0	0	0		
[	0	0	0	0	0	0	0	0	0	0]	0	0	228	25/	66	0	0	0		
L	0	0	0	0	0	0	0	0	0	0]	U	U	220	234	00	U	U	U		
[	0	0	0	0	0	0	0	0	0	0	0	61	251	254	66	0	0	0		
-	0	0	0	0	0	0	0	0	0	0]	0	1 1 1	0.54	205	2	0	0	0		
[	0	0	0	0	0	0	0	0	0	0]	0	141	254	205	3	U	0	0		
[	0	0	0	0	0	0	0	0	0	0	10	215	254	121	0	0	0	0		
	0	0	0	0	0	0	0	0	0	0]										
[	0	0	0	0	0	0	0	0	0	0	5	198	176	10	0	0	0	0		
[	0	0	0	0	0	0	0	0	0	0]	0	0	0	0	0	0	0	0		
٠	0	0	0	0	0	0	0	0	0	0]										
[	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0		
[	0	0	0	0	0	0	0	0	0	0]	0	0	0	0	0	0	0	0		
L	0	0	0	0	0	0	0	0	0	0]	U	U	U	U	U	U	U	U		
[	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0		
	0	0	0	0	0	0	0	0	0	0]	]									
⊥ab	e⊥2	= 1																		

```
2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
Train on 60000 samples
Epoch 1/10
 32/60000 [.....] - ETA: 2:40 - loss: 2.4426 - acc: 0.0625
 832/60000 [.....] - ETA: 9s - loss: 1.7527 - acc: 0.4952
1664/60000 [.....] - ETA: 6s - loss: 1.2789 - acc: 0.6454
Epoch 10/10
60000/60000 [============] - 5s 79us/sample - loss: 0.0160 - acc: 0.9949
Test images [[[0. 0. 0. ... 0. 0. 0.]
 [0. 0. 0. ... 0. 0. 0.]
 [0. 0. 0. ... 0. 0. 0.]
 . . .
 [0. 0. 0. ... 0. 0. 0.]
 [0. 0. 0. ... 0. 0. 0.]
 [0. 0. 0. ... 0. 0. 0.]]]
2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
50/50 - 0s - loss: 3.0280 - acc: 0.6600
Test accuracy (original): 0.66
(28, 28)
(1, 28, 28)
[[1.1649617e-16 2.1574893e-08 6.3789146e-16 1.1028823e-11 2.9255222e-07
1.9048621e-10 1.5124934e-14 9.9999785e-01 5.2894117e-10 1.7355468e-06]]
```

