### CHAPTER 2

### **ARRAYS AND STRUCTURES**

All the programs in this file are selected from

Ellis Horowitz, Sartaj Sahni, and Susan Anderson-Freed "Fundamentals of Data Structures in C",

CHAPTER 2

# Arrays

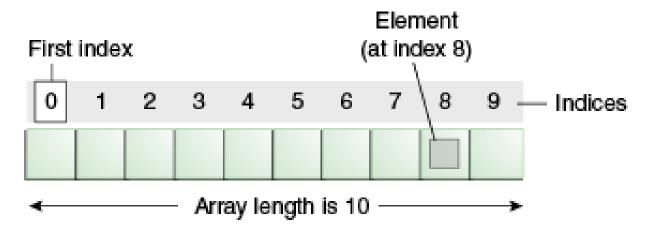
Array: a set of index and value

#### data structure:

For each index, there is a value associated with that index.

### representation (possible):

implemented by using consecutive memory.





#### **Structure** *Array* is

**objects:** A set of pairs *<index, value>* where for each value of *index* there is a value from the set *item*. *Index* is a finite ordered set of one or more dimensions, for example,  $\{0, ..., n-1\}$  for one dimension,  $\{(0,0),(0,1),(0,2),(1,0),(1,1),(1,2),(2,0),(2,1),(2,2)\}$  for two dimensions, etc.

#### **Functions:**

for all  $A \in Array$ ,  $i \in index$ ,  $x \in item$ , j,  $size \in integer$ 

Array Create(j, list) ::= **return** an array of *j* dimensions where list is a j-tuple whose *i*th element is the size of the *i*th dimension. *Items* are undefined.

Item Retrieve(A, i) ::= if  $(i \in index)$  return the item associated with index value i in array A

else return error

Array Store(A, i, x) ::= **if** (i in index) **return** an array that is identical to array

A except the new pair  $\langle i, x \rangle$  has been inserted **else return** error

#### end array

\*Structure 2.1: Abstract Data Type *Array* 

## Arrays in C

int list[5], \*plist[5];

### implementation of 1-D array

list[0]	base address = $\alpha$
list[1]	$\alpha + sizeof(int)$
list[2]	$\alpha + 2*sizeof(int)$
list[3]	$\alpha + 3*sizeof(int)$
list[4]	$\alpha + 4*sizeof(int)$

CHAPTER 2

## Arrays in C (Continued)

Compare int \*list1 and int list2[5] in C.

Same: list1 and list2 are **pointers**.

Difference: list2 reserves **five locations**.

#### **Notations:**

```
list2 → a pointer to list2[0]

(list2 + i) → a pointer to list2[i] (&list2[i])

*(list2 + i) → list2[i] (value)
```

CHAPTER 2

```
目的: 顯示一個陣列的address和value
   int main(void) {
                                      宣告一個陣列並給予值
     int one[] = \{0, 1, 2, 3, 4\};
     print1(&one[0], 5);
   void print1(int *ptr, int rows){
     int i;
     printf("Address Contents\n");
     for(i = 0; i < rows; i++)
        printf("%08u %5d\n", ptr+i, *(ptr+i));
```

目的: 顯示一個陣列的address和value

```
int main(void) {
  int one[] = \{0, 1, 2, 3, 4\};
  print1(&one[0], 5);
                                             陣列one的長度
____陣列one的索引值
                                                    取address
void print1(int *ptr, int rows){
  int i;
  printf("Address Contents\n");
  for(i = 0; i < rows; i++)
     printf("%08u %5d\n", ptr+i, *(ptr+i));
```

目的: 顯示一個陣列的address和value

```
int main(void) {
  int one [] = \{0, 1, 2, 3, 4\};
  print1(&one[0], 5);
void print1(int *ptr, int rows){
  int i;
  printf("Address Contents\n");
  for(i = 0; i < rows; i++){
    printf("\%08u\%5d\n", ptr+i, *(ptr+i));
                八位數的無符號十進位整數,不足以0填滿
```

目的: 顯示一個陣列的address和value

```
int main(void) {
  int one [] = \{0, 1, 2, 3, 4\};
  print1(&one[0], 5);
void print1(int *ptr, int rows){
  int i;
  printf("Address Contents\n");
  for(i = 0; i < rows; i++){
    printf("%08u %5d\n", ptr+i, *(ptr+i));
             五位數的有符號十進位整數,不足以空白填滿
```

目的: 顯示一個陣列的address和value

```
int main(void) {
    int one[] = \{0, 1, 2, 3, 4\};
    print1(&one[0], 5);
}

索引值 0 1 2 3 4
    address 06422284 06422288 06422292 06422296 06422300
    one 0 1 2 3 4
```

\*每個int是4 bytes,所以address之間的間隔差4

```
目的: 顯示一個陣列的address和value
 void print1(int *ptr, int rows){
   int i;
    printf("Address Contents\n");
   for(i = 0; i < rows; i++)
      printf("%08u %5d\n", ptr+i, *(ptr+i));
                                                     Output:
         索引值
                                                     Address
                                                               Contents
         address 06422284
                        06422288
                               06422292
                                     06422296
                                            06422300
                                                     06422284
                                                                ()
                 ptr+0
 i = 0
          one
                *(ptr+0)
```

```
目的: 顯示一個陣列的address和value
void print1(int *ptr, int rows){
   int i;
   printf("Address Contents\n");
   for(i = 0; i < rows; i++)
      printf("%08u %5d\n", ptr+i, *(ptr+i));
                                                     Output:
         索引值
                                                     Address
                                                                Contents
         address 06422284
                        06422288
                                             06422300
                               06422292
                                      06422296
                                                     06422284
                                                                 ()
                        ptr+1
 i = 1
                                                     06422288
                                               4
          one
                       *(ptr+1)
```

```
目的: 顯示一個陣列的address和value
 void print1(int *ptr, int rows){
   int i;
   printf("Address Contents\n");
   for(i = 0; i < rows; i++)
      printf("%08u %5d\n", ptr+i, *(ptr+i));
                                                       Output:
         索引值
                                                       Address
                                                                 Contents
         address 06422284
                                       06422296
                        06422288
                                              06422300
                                06422292
                                                       06422284
                                                                  \mathbf{0}
                                ptr+2
 i = 2
                                                       06422288
                                                       06422292
          one
                               *(ptr+2)
```

```
目的: 顯示一個陣列的address和value
void print1(int *ptr, int rows){
   int i;
   printf("Address Contents\n");
   for(i = 0; i < rows; i++)
      printf("%08u %5d\n", ptr+i, *(ptr+i));
                                                     Output:
         索引值
                                                     Address
                                                               Contents
         address 06422284
                               06422292
                                     06422296
                        06422288
                                            06422300
                                                     06422284
                                      ptr+3
                                                                ()
 i = 3
                                                     06422288
                                                     06422292
          one
                                                     06422296
                                     *(ptr+3)
```

```
目的: 顯示一個陣列的address和value
 void print1(int *ptr, int rows){
   int i;
   printf("Address Contents\n");
   for(i = 0; i < rows; i++)
      printf("%08u %5d\n", ptr+i, *(ptr+i));
                                                      Output:
         索引值
                                                      Address
                                                                 Contents
         address 06422284
                                      06422296
                                              06422300
                        06422288
                               06422292
                                                      06422284
                                                                  \mathbf{0}
                                              ptr+4
  i = 4
                                                      06422288
                                                      06422292
          one
                                                      06422296
                                             *(ptr+4) 06422300
```

## Multiple Dimension Array

- ☐ Two dimension
  - int arr[2][3];

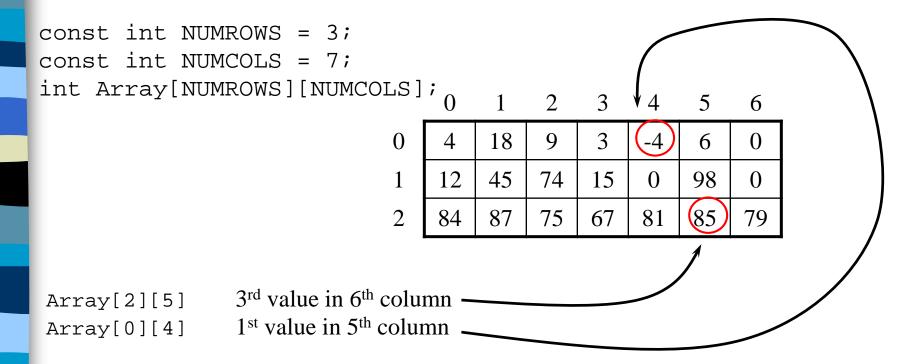
- ☐ Three dimension
  - int arr[2][3][4];

- N dimension
  - int arr[2][3][4][...];

# Multidimensional Arrays

C also allows an array to have more than one dimension.

For example, a two-dimensional array consists of a certain <u>number of rows</u> and columns:



The declaration must specify the number of rows and the number of columns, and both must be constants.

## Processing a 2-D Array

A one-dimensional array is usually processed via a for loop.

Similarly, a two-dimensional array may be processed with a nested for loop:

```
for (int Row = 0; Row < NUMROWS; Row++) {
    for (int Col = 0; Col < NUMCOLS; Col++) {
        Array[Row][Col] = 0;
    }
}</pre>
```

Each pass through the inner for loop will initialize all the elements of the current row to 0.

The outer for loop drives the inner loop to process each of the array's rows.

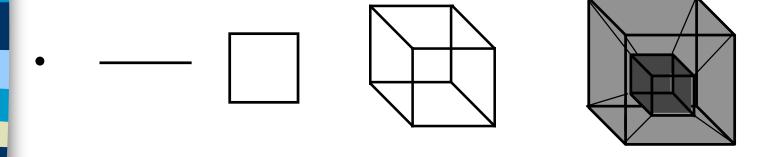
## Higher-Dimensional Arrays

An array can be declared with multiple dimensions.

2 Dimensional

double Coord[100][100];

Multiple dimensions get difficult to visualize graphically.



## Structures (records)

```
struct {
          char name[10];
          int age;
          float salary;
          } person;

strcpy(person.name, "james");
person.age=10;
person.salary=35000;
```

# Create structure data type

```
typedef struct human_being {
       char name[10];
       int age;
       float salary;
       };
or
typedef struct {
       char name[10];
       int age;
       float salary
       } human_being;
human_being person1, person2;
```

23

### Unions

```
Example: Add fields for male and female.
typedef struct sex_type {
       enum tag_field {female, male} sex;
       union {
               int children;
               int beard;
                       Similar to struct, but only one field is
               } u;
                       active.
        };
typedef struct human_being {
       char name[10];
                          human_being person1, person2;
       int age;
                          person1.sex_info.sex=male;
       float salary;
                          person1.sex_info.u.beard=0 (False);
       date dob;
       sex_type sex_info;
                                                           24
                         CHAPTER 2
```

目的:實作structure和 unions

```
typedef struct {
  enum {female, male} sex;
  union
     int children;
     int beard;
   } u;
} sex_type;
typedef struct {
  char name[10];
  int age;
  float salary;
  sex_type sex_info;
} human_being;
```

列舉(Enumeration)是以關鍵字enum開始加上一個列舉名稱,並以大括號括住要群組管理的常數。



#### 說明階層關係

```
typedef struct {
  enum {female, male} sex;
  union {
    int children;
    int beard;
  } u;
} sex_type;
typedef struct {
    char name[10];
    int age;
    float salary;
    sex_type sex_info;
} human_being;
```

sex

### 說明階層關係

```
typedef struct {
  enum {female, male} sex;
  union {
    int children;
    int beard;
  } u;
} sex_type;

typedef struct {
    char name[10];
    int age;
    float salary;
    sex_type sex_info;
} human_being;
```

```
sex
u -> children
-> beard
```

### 說明階層關係

```
typedef struct {
  enum {female, male} sex;
  union {
    int children;
    int beard;
  } u;
} sex_type;
typedef struct {
    char name[10];
    int age;
    float salary;
    sex_type sex_info;
} human_being;
```

```
sex_info -> sex
-> u -> children
-> beard
```

#### 說明階層關係

```
typedef struct {
  enum {female, male} sex;
  union {
    int children;
    int beard;
  } u;
} sex_type;

typedef struct {
  char name[10];
  int age;
  float salary;
  sex_type sex_info;
} human_being;
```

name

### 說明階層關係

```
typedef struct {
  enum {female, male} sex;
  union {
    int children;
    int beard;
  } u;
} sex_type;

typedef struct {
    char name[10];
    int age;
    float salary;
    sex_type sex_info;
} human_being;
```

name age

#### 說明階層關係

```
typedef struct {
  enum {female, male} sex;
  union {
    int children;
    int beard;
  } u;
} sex_type;

typedef struct {
    char name[10];
    int age;
    float salary;
    sex_type sex_info;
} human_being;
```

name age salary

### 說明階層關係

```
typedef struct {
  enum {female, male} sex;
  union {
    int children;
    int beard;
  } u;
} sex_type;

typedef struct {
    char name[10];
    int age;
    float salary;
    sex_type sex_info;
} human_being;
```

```
name
age
salary
型別為結構sex_type的sex_info -> sex
-> u -> children
-> beard
```

#### 說明階層關係

```
typedef struct {
  enum {female, male} sex;
  union {
    int children;
    int beard;
  } u;
} sex_type;

typedef struct {
    char name[10];
    int age;
    float salary;
    sex_type sex_info;
} human_being;
```

```
human_being -> name
    -> age
    -> salary
    ->型別為結構sex_type的sex_info -> sex
    -> u -> children
    -> beard
```

階層關係轉換成程式碼

```
human_being person1;
human_being -> name
-> age
-> salary
->型別為結構sex_type的sex_info -> sex
-> u -> children
-> beard
```



### Self-Referential Structures

One or more of its components is a pointer to itself.

```
typedef struct list {
    char data;
    list *link;
    }
```

```
Construct a list with three nodes item1.link=&item2; item2.link=&item3; malloc: obtain a node
```

```
list item1, item2, item3;
item1.data='a';
item2.data='b';
item3.data='c';
item1.link=item2.link=item3.link=NULL;
```

# Ordered List Examples

ordered (linear) list: (item1, item2, item3, ..., itemn)

- ☐ (MONDAY, TUEDSAY, WEDNESDAY, THURSDAY, FRIDAY, SATURDAYY, SUNDAY)
- (2, 3, 4, 5, 6, 7, 8, 9, 10, Jack, Queen, King, Ace)
- $\square$  (1941, 1942, 1943, 1944, 1945)
- $\Box$  (a<sub>1</sub>, a<sub>2</sub>, a<sub>3</sub>, ..., a<sub>n-1</sub>, a<sub>n</sub>)

## Operations on Ordered List

- 1. Find the length, n, of the list.
- 2. Read the items from left to right (or right to left).
- 3. Retrieve the i'th element.
- 4. Store a new value into the i'th position.
- Insert a new element at the position i, causing elements numbered i, i+1, ..., n to become numbered i+1, i+2, ..., n+1
- Delete the element at position i, causing elements numbered i+1, ..., n to become numbered i, i+1, ..., n-1

array (sequential mapping)? (1)~(4) O (5)~(6) X



### Polynomials $A(X)=3X^{20}+2X^5+4$ , $B(X)=X^4+10X^3+3X^2+1$

### **Structure** *Polynomial* is

**objects**:  $p(x) = a_1 x^{e_1} + ... + a_n x^{e_n}$ ; a set of ordered pairs of  $\langle e_i, a_i \rangle$  where  $\underline{a_i}$  in *Coefficients* and  $\underline{e_i}$  in *Exponents*,  $e_i$  are integers  $\geq 0$  functions:

for all  $poly, poly1, poly2 \in Polynomial, coef \in Coefficients, expon \in Exponents$ 

Polynomial Zero() ::= **return** the polynomial, p(x) = 0

Boolean IsZero(poly) ::= if (poly) return FALSEelse return TRUE

Coefficient Coef(poly, expon) ::= if (expon ∈ poly) return its coefficient else return Zero

Exponent Lead\_Exp(poly) ::= return the largest exponent in poly

Polynomial Attach(poly, coef, expon) ::= if (expon  $\in$  poly) return error else return the polynomial poly with the term < coef, expon> inserted



::= if  $(expon \in poly)$  return the polynomial poly with the term whose exponent is  $expon \ deleted$ 

else return error

Polynomial SingleMult(poly, coef, expon) ::= return the polynomial

 $poly \bullet coef \bullet x^{expon}$ 

Polynomial Add(poly1, poly2) ::

::= **return** the polynomial poly1 + poly2

*Polynomial* Mult(*poly1*, *poly2*)

::= **return** the polynomial poly1 • poly2

#### **End** Polynomial

\*Structure 2.2: Abstract data type *Polynomial* 

## **Polynomial Addition**

```
data structure 1:
                    #define MAX_DEGREE 101
                    typedef struct {
                            int degree;
                            float coef[MAX_DEGREE];
                             } polynomial;
/* d = a + b, where a, b, and d are polynomials */
d = Zero()
while (! IsZero(a) &&! IsZero(b)) do {
  switch COMPARE (Lead_Exp(a), Lead_Exp(b)) {
     case -1: d =
                        /* a < b */
       Attach(d, Coef (b, Lead_Exp(b)), Lead_Exp(b));
       b = Remove(b, Lead\_Exp(b));
       break;
    case 0: sum = Coef (a, Lead_Exp(a)) + Coef (b, Lead_Exp(b));
      if (sum) {
         Attach (d, sum, Lead_Exp(a));
         a = Remove(a, Lead\_Exp(a));
         b = Remove(b, Lead\_Exp(b));
                              CHAPTER 2
```

break;

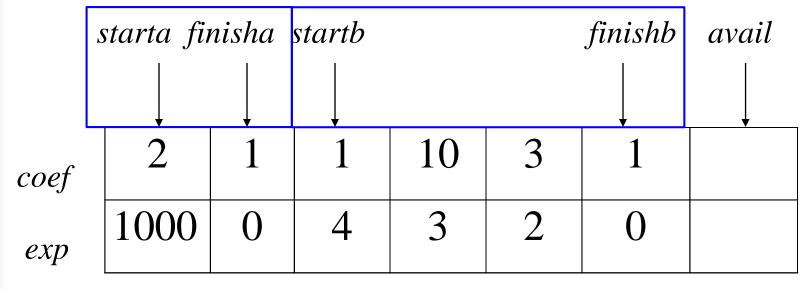
```
case 1: d =
     Attach(d, Coef (a, Lead_Exp(a)), Lead_Exp(a));
     a = Remove(a, Lead_Exp(a));
    }
    insert any remaining terms of a or b into d

advantage: easy implementation
disadvantage: waste space when sparse
```

\*Program 2.5 :Initial version of padd function

## Data structure 2: use one global array to store all polynomials

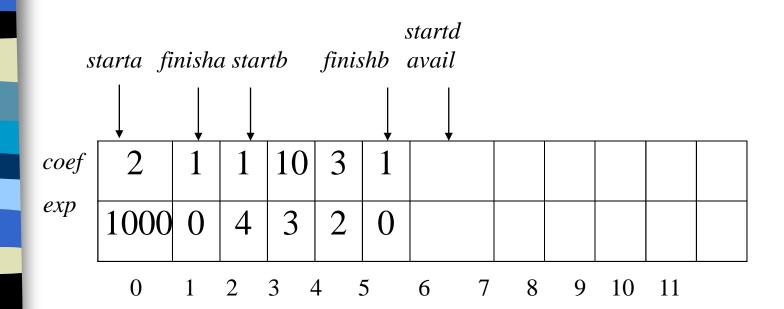
$$A(X)=2X^{1000}+1$$
  
 $B(X)=X^4+10X^3+3X^2+1$ 

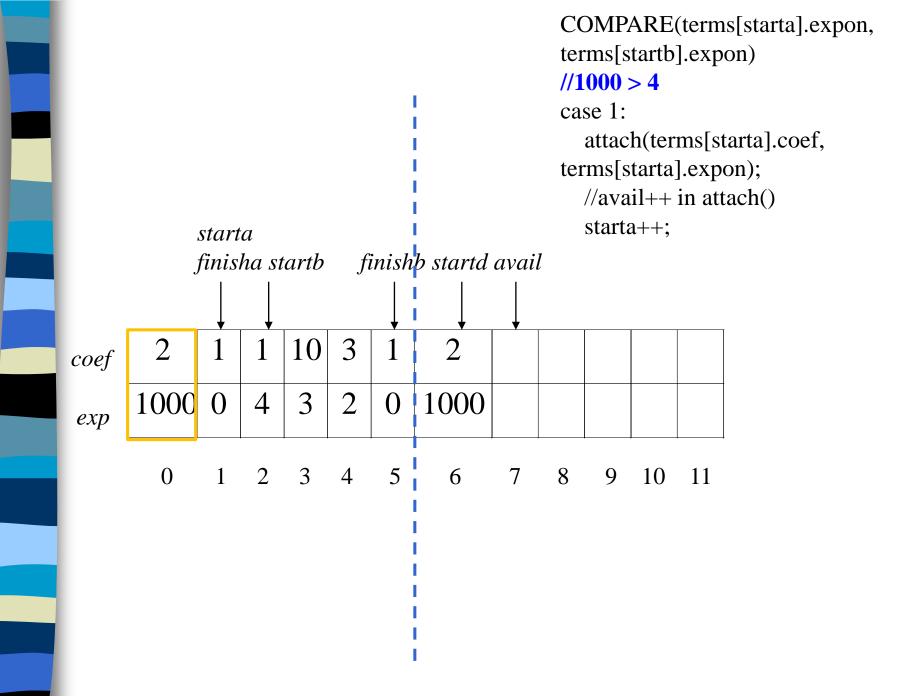


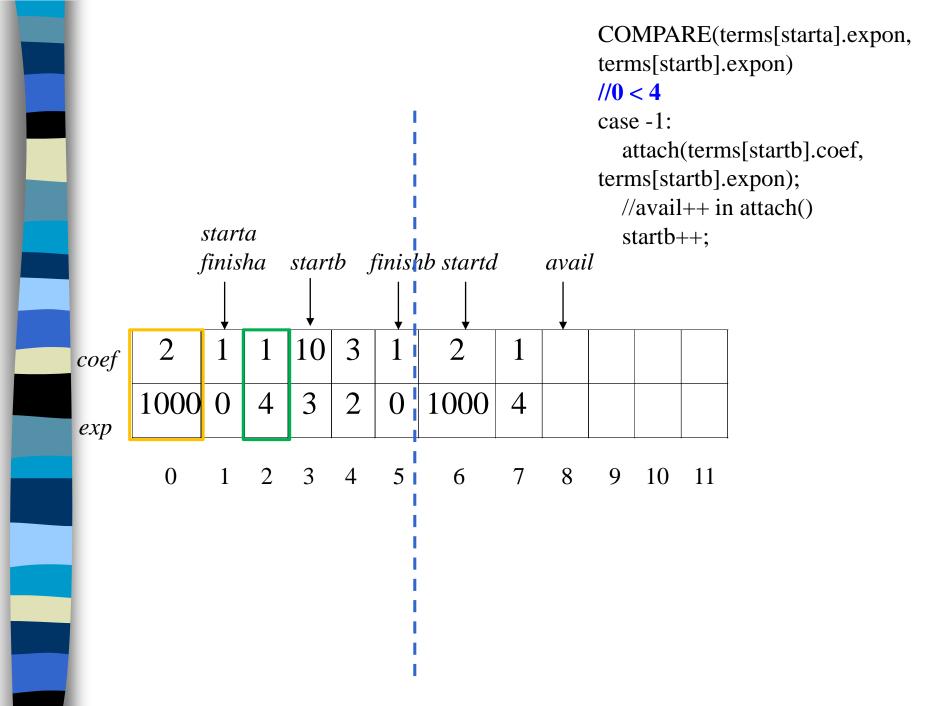
specification poly

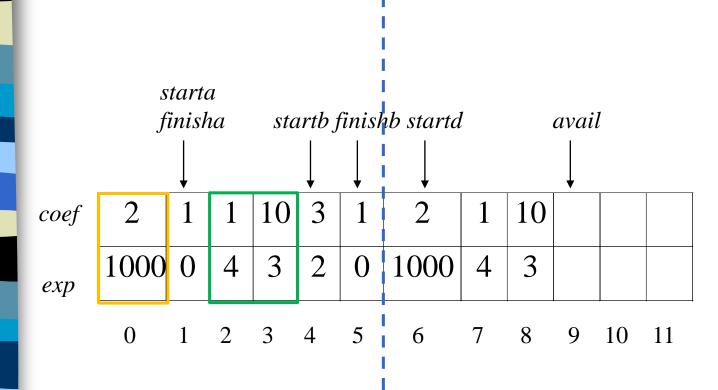
representation <start, finish>

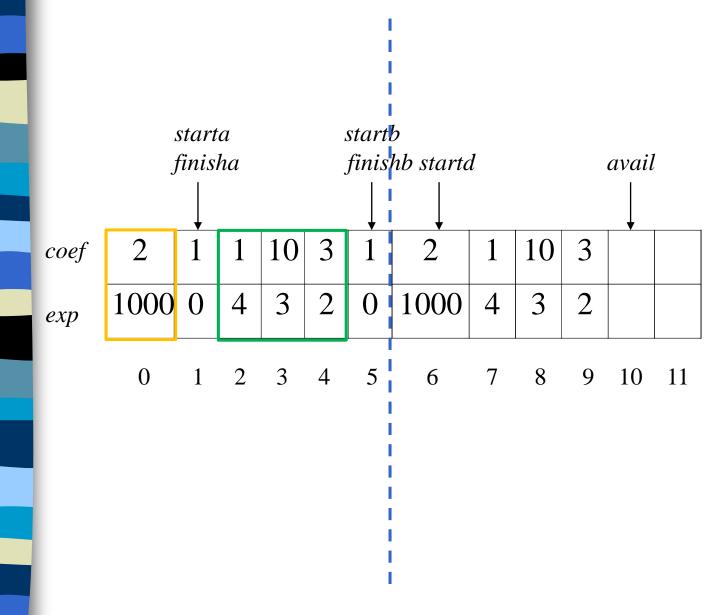
<0,1>

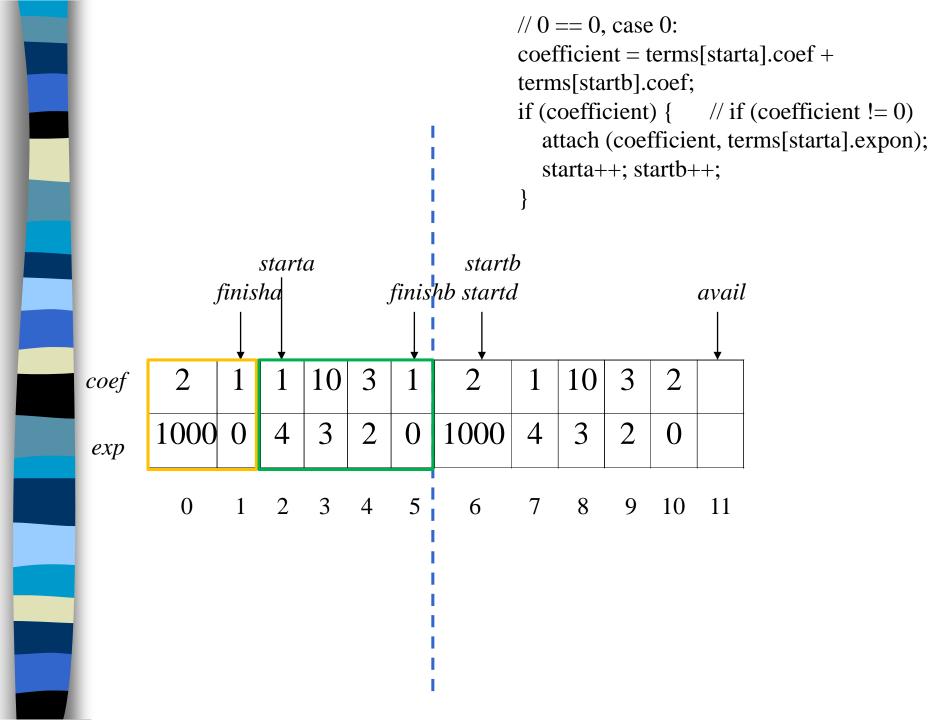


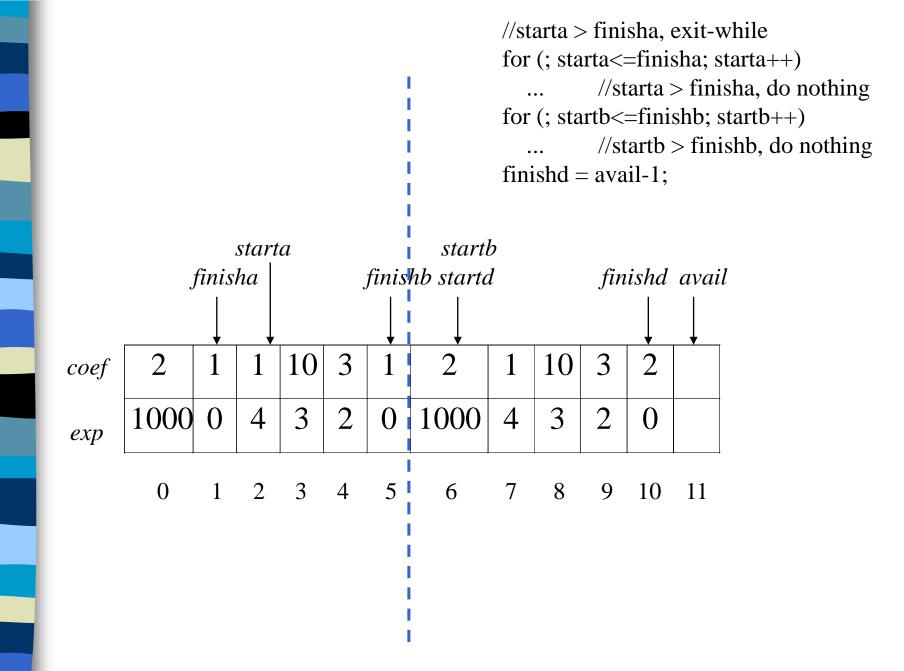












```
MAX_TERMS 100 /* size of terms array */
typedef struct {
     float coef;
     int expon;
     } polynomial;
polynomial terms[MAX_TERMS];
int avail = 0;
```

## Add two polynomials: D = A + B

```
void padd (int starta, int finisha, int startb, int finishb,
                                  int * startd, int *finishd)
/* add A(x) and B(x) to obtain D(x) */
  float coefficient;
  *startd = avail;
  while (starta <= finisha && startb <= finishb)
   switch (COMPARE(terms[starta].expon,
                         terms[startb].expon)) {
    case -1: /* a expon < b expon */
          attach(terms[startb].coef, terms[startb].expon);
          startb++
          break;
```

# Polynomial Addition - data structure 2

目的: 將方程式A(X)和方程式B(X)相加

padd()程式碼說明:

```
void padd (int starta, int finisha, int startb, int finishb,int startd, int finishd){
    float coefficient;
    startd = avail;
    while (starta <= finisha && startb <= finishb){
        switch (COMPARE(terms[starta].expon,terms[startb].expon)) {
            case -1:
                attach(terms[startb].coef, terms[startb].expon);
                startb++;
                break;
                avail是D(X)的開始位置</pre>
```

```
#define COMPARE(x, y) ((x < y) ? -1: (x == y)? 0: 1) a 的 expon < b 的 expon: case -1 如果方程式A的次方<方程式B的次方成立,則放入D(X)
```

```
case 0: /* equal exponents */
           coefficient = terms[starta].coef +
                         terms[startb].coef;
           if (coefficient)
             attach (coefficient, terms[starta].expon);
           starta++;
           startb++;
           break;
case 1: /* a expon > b expon */
       attach(terms[starta].coef, terms[starta].expon);
       starta++;
```

# Polynomial Addition - data structure 2

目的: 將方程式A(X)和方程式B(X)相加

```
case 0:
    coefficient = terms[starta].coef + terms[startb].coef;
    if (coefficient){
        attach (coefficient, terms[starta].expon);
        starta++;
        startb++;
    }
    break;
case 1:
    attach(terms[starta].coef, terms[starta].expon);
    starta++;
```

```
#define COMPARE(x, y) ((x < y)? -1: (x == y)? 0: 1) a 的 expon = b 的 expon: case 0 把兩方程式項目的係數相加且相加後係數不為0則放入D(X) a 的 expon > b 的 expon: case 1 如果方程式A的次方>方程式B的次方成立,則放入D(X)
```

```
/* add in remaining terms of A(x) */
 for( ; starta <= finisha; starta++)</pre>
    attach(terms[starta].coef, terms[starta].expon);
 /* add in remaining terms of B(x) */
 for(; startb <= finishb; startb++)
    attach(terms[startb].coef, terms[startb].expon);
 *finishd =avail -1;
Analysis: O(n+m)
               where n (m) is the number of nonzeros in A(B).
```

**CHAPTER 2** 

\*Program 2.6: Function to add two polynomial

# Polynomial Addition - data structure 2

目的: 將方程式A(X)和方程式B(X)相加

```
for(; starta <= finisha; starta++){
   attach(terms[starta].coef, terms[starta].expon);
}
for(; startb <= finishb; startb++){
   attach(terms[startb].coef, terms[startb].expon);
}
finishd = avail - 1;</pre>
```

第一個for loop 如果方程式B已經結束時,將方程式A剩下的項目放進D(X) 第二個for loop 如果方程式A已經結束時,將方程式B剩下的項目放進D(X)

```
void attach(float coefficient, int exponent)
/* add a new term to the polynomial */
  if (avail >= MAX_TERMS) {
    fprintf(stderr, "Too many terms in the polynomial\n");
    exit(1);
   terms[avail].coef = coefficient;
   terms[avail++].expon = exponent;
```

Problem: Compaction is required when polynomials that are no longer needed. (data movement takes time.)

CHAPTER 2

58

# Polynomial Addition - data structure 2

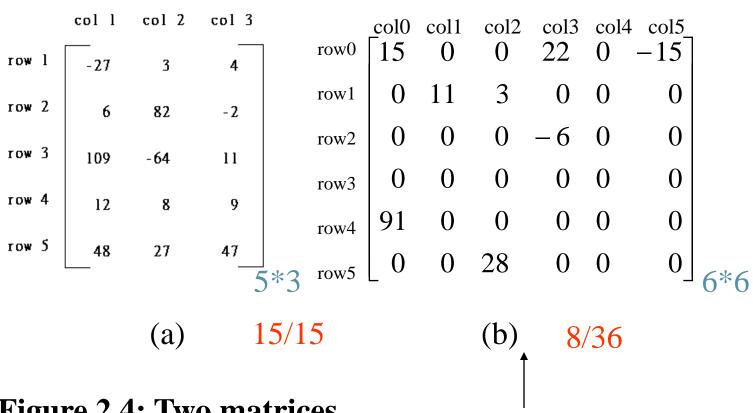
目的: 將方程式A(X)和方程式B(X)相加

## attach()程式碼說明:

```
void attach(float coefficient, int exponent){
    if (avail >= MAX_TERMS) {
        fprintf(stderr, "Too many terms in the polynomial\n");
        exit(1);
    }
    terms[avail].coef = coefficient;
    terms[avail++].expon = exponent;
}
```

如果沒有超過陣列最達長度,則將項目的指數及係數放到D(X)中

# Sparse Matrix



#### Figure 2.4: Two matrices

sparse matrix data structure?

**CHAPTER 2** 60

#### SPARSE MATRIX ABSTRACT DATA TYPE

**Structure** *Sparse\_Matrix* is

**objects:** a set of triples, <*row*, *column*, *value*>, where *row* and *column* are integers and form a unique combination, and *value* comes from the set *item*.

#### functions:

```
for all a, b \in Sparse\_Matrix, x \in item, i, j, max\_col, max\_row \in index
```

Sparse\_Marix Create(max\_row, max\_col) ::=

**return** a *Sparse\_matrix* that can hold up to  $max\_items = max\_row * max\_col$  and whose maximum row size is  $max\_row$  and whose maximum column size is  $max\_col$ .

 $Sparse\_Matrix Transpose(a) ::=$ **return** the matrix produced by interchanging the row and column value of every triple.  $Sparse\_Matrix Add(a, b) ::=$ if the dimensions of a and b are the same **return** the matrix produced by adding corresponding items, namely those with identical row and column values. else return error *Sparse\_Matrix* Multiply(*a*, *b*) ::= if number of columns in a equals number of rows in **b return** the matrix d produced by multiplying a by b according to the formula: d[i][j] = $\square$ (a[i][k]•b[k][j]) where d(i, j) is the (i, j)th element **else return** error. CHAPTER 2

<sup>\*</sup> **Structure 2.3:** Abstract data type Sparse-Matrix

- (1) Represented by a two-dimensional array. Sparse matrix wastes space.
- (2) Each element is characterized by <row, col, value>.

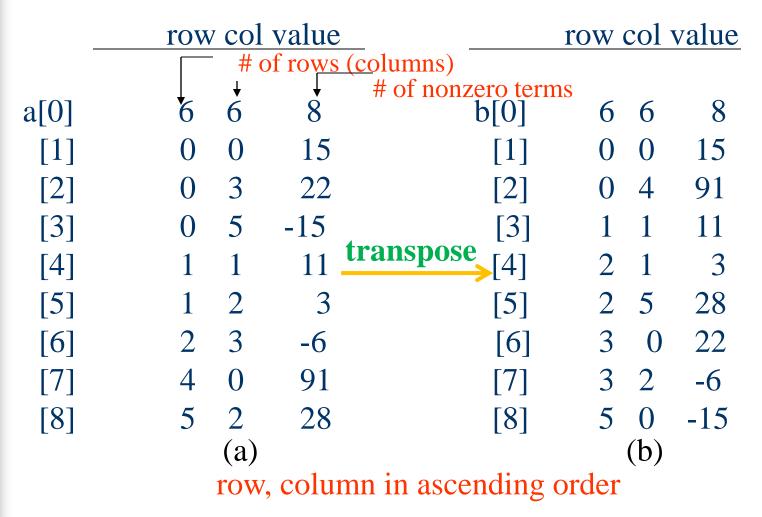


Figure 2.5: Sparse matrix and its transpose stored as triples

```
Sparse_matrix Create(max_row, max_col) ::=

#define MAX_TERMS 101 /* maximum number of terms +1*/
    typedef struct {
        int col;
        int row;
        int value;
        } term;
    term a [MAX_TERMS]
# of rows
# of columns
# of nonzero terms
```

## Transpose a Matrix

(1) for each row i take element <i, j, value> and store it in element <j, i, value> of the transpose.

```
difficulty: where to put \langle j, i, value \rangle

(0, 0, 15) ====> (0, 0, 15)

(0, 3, 22) ===> (3, 0, 22)

(0, 5, -15) ===> (5, 0, -15)

(1, 1, 11) ===> (1, 1, 11)

Move elements down very often.
```

(2) For all elements in column j, place element <i, j, value> in element <j, i, value>

```
void transpose (term a[], term b[])
/* b is set to the transpose of a */
  int n, i, j, currentb;
  n = a[0].value; /* total number of elements */
  b[0].row = a[0].col; /* rows in b = columns in a */
  b[0].col = a[0].row; /*columns in b = rows in a */
  b[0].value = n;
  if (n > 0) {
                   /*non zero matrix */
     currentb = 1;
     for (i = 0; i < a[0].col; i++)
     /* transpose by columns in a */
         for(j = 1; j \le n; j++)
         /* find elements from the current column */
        if (a[i].col == i) {
        /* element is in current column, add it to b */
                           CHAPTER 2
```

66

# columns elements b[currentb].row = a[j].col;b[currentb].col = a[j].row; b[currentb].value = a[j].value; currentb++

\* **Program 2.8:** Transpose of a sparse matrix

Scan the array "columns" times.
The array has "elements" elements. ==> O(columns\*elements)

目的:實作轉置矩陣

transpose()程式碼說明:

```
void transpose (term a[], term b[]){
   int n, i, j, currentb;
   n = a[0].value;
   b[0].row = a[0].col;
   b[0].col = a[0].row;
   b[0].value = n;
   if (n > 0) {
      currentb = 1;
   }
}
```

透過a[0]的基本資料,知道轉置後的資本資料。 row, col: a的col轉置後是b的row

a的row轉置後是b的col

value: 轉置後的非0項目數量不變

矩陣中非0項目 紀錄轉置後的矩 陣,從位置1開始 ,位置0紀錄矩陣 的基本資料

目的:實作轉置矩陣

transpose()程式碼說明:

```
for (i = 0; i < a[0].col; i++){
    for( j = 1; j <= n; j++){
        if (a[j].col == i) {
            b[currentb].row = a[j].col;
            b[currentb].col = a[j].row;
            b[currentb].value = a[j].value;
            currentb++;
        }
    }
}</pre>
```

```
i = 0
         row col value
                              row col value
a[0]
                   8
                        b[0]
          0 0 15
[1]j = 1
                         [1]
                                      15
                  22
 [2]
                         [2]
 [3]
          0 5 -15
                         [3]
 [4]
                         [4]
                11
 [5]
                         [5]
                         [6]
 [6]
                  -6
                         [7]
                  91
 [7]
                         [8]
 [8]
                  28
```

```
for (i = 0; i < a[0].col; i++){
    for( j = 1; j <= n; j++){
        if (a[j].col == i) {
            b[currentb].row = a[j].col;
            b[currentb].col = a[j].row;
            b[currentb].value = a[j].value;
            currentb++;
        }
    }
}</pre>
```

i = 0							
	row	col	value		row	col	value
a[0]	6	6	8	b[0]	6	6	8
[1]	0	0	15	[1]	0	0	15
[2] $j = 2$	0	3	22	[2]			
[3]	0	5	-15	[3]			
[4]	1	1	11	[4]			
[5]	1	2	3	[5]			
[6]	2	3	-6	[6]			
[7]	4	0	91	[7]			
[8]	5	2	28	[8]			

```
for (i = 0; i < a[0].col; i++){
    for( j = 1; j <= n; j++){
        if (a[j].col == i) {
            b[currentb].row = a[j].col;
            b[currentb].col = a[j].row;
            b[currentb].value = a[j].value;
            currentb++;
        }
    }
}</pre>
```

i = 0							
	row	col	value		row	col y	value
a[0]	6	6	8	b[0]	6	6	8
[1]	0	0	15	[1]	0	0	15
[2]	0	3	22	[2]			
[3] $j = 3$	0	5	-15	[3]			
[4]	1	1	11	[4]			
[5]	1	2	3	[5]			
[6]	2	3	-6	[6]			
[7]	4	0	91	[7]			
[8]	5	2	28	[8]			

```
for (i = 0; i < a[0].col; i++){
    for( j = 1; j <= n; j++){
        if (a[j].col == i) {
            b[currentb].row = a[j].row;
            b[currentb].value = a[j].value;
            currentb++;
        }
    }
}</pre>
```

1 = 0							
	row col value				row	col y	value
a[0]	6	6	8	b[0]	6	6	8
[1]	0	0	15	[1]	0	0	15
[2]	0	3	22	[2]			
[3]	0	5	-15	[3]			
[4] $j = 4$	1	1	11	[4]			
[5]	1	2	3	[5]			
[6]	2	3	-6	[6]			
[7]	4	0	91	[7]			
[8]	5	2	28	[8]			

```
for (i = 0; i < a[0].col; i++){
    for( j = 1; j <= n; j++){
        if (a[j].col == i) {
            b[currentb].row = a[j].col;
            b[currentb].col = a[j].row;
            b[currentb].value = a[j].value;
            currentb++;
        }
    }
}</pre>
```

i = 0							
	row col value				row	col y	value
a[0]	6	6	8	b[0]	6	6	8
[1]	0	0	15	[1]	0	0	15
[2]	0	3	22	[2]			
[3]	0	5	-15	[3]			
[4]	1	1	11	[4]			
[5] $j = 5$	1	2	3	[5]			
[6]	2	3	-6	[6]			
[7]	4	0	91	[7]			
[8]	5	2	28	[8]			

```
for (i = 0; i < a[0].col; i++){
    for( j = 1; j <= n; j++){
        if (a[j].col == i) {
            b[currentb].row = a[j].col;
            b[currentb].col = a[j].row;
            b[currentb].value = a[j].value;
            currentb++;
        }
    }
}</pre>
```

i = 0							
	row col value				row	col	value
a[0]	6	6	8	b[0]	6	6	8
[1]	0	0	15	[1]	0	0	15
[2]	0	3	22	[2]			
[3]	0	5	-15	[3]			
[4]	1	1	11	[4]			
[5]	1	2	3	[5]			
[6] $j = 6$	2	3	-6	[6]			
[7]	4	0	91	[7]			
[8]	5	2	28	[8]			
[7]							

```
for (i = 0; i < a[0].col; i++){
    for( j = 1; j <= n; j++){
        if (a[j].col == i) {
            b[currentb].row = a[j].col;
            b[currentb].col = a[j].row;
            b[currentb].value = a[j].value;
            currentb++;
        }
    }
}</pre>
```

i = 0							
_	row	col	value		row	col	value
a[0]	6	6	8	b[0]	6	6	8
[1]	0	0	15	[1]	0	0	15
[2]	0	3	22	[2]	0	4	91
[3]	0	5	-15	[3]			
[4]	1	1	11	[4]			
[5]	1	2	3	[5]			
[6]	2	3	-6	[6]			
[7] j =	7 4	0	91	[7]			
[8]	5	2	28	[8]			

目的:實作轉置矩陣

```
for (i = 0; i < a[0].col; i++){
    for( j = 1; j <= n; j++){
        if (a[j].col == i) {
            b[currentb].row = a[j].col;
            b[currentb].col = a[j].row;
            b[currentb].value = a[j].value;
            currentb++;
        }
    }
}</pre>
```

```
i = 0
         row col value
                             row col value
a[0]
                       b[0]
                        [1]
          0 0 15
                                     15
 [1]
          0 3 22
                        [2]
                                     91
 [2]
          0 5 -15
                        [3]
 [3]
                        [4]
 [4]
                11
 [5]
                        [5]
                        [6]
 [6]
                  -6
                        [7]
 [7]
                  91
                        [8]
 [8] i = 8
                  28
```

目的:實作轉置矩陣

```
for (i = 0; i < a[0].col; i++){
    for( j = 1; j <= n; j++){
        if (a[j].col == i) {
            b[currentb].row = a[j].col;
            b[currentb].col = a[j].row;
            b[currentb].value = a[j].value;
            currentb++;
        }
    }
}</pre>
```

```
i = 1
          row col value
                                row col value
a[0]
                          b[0]
 [1] j = 1
                   15
                           [1]
                                          15
                    22
                           [2]
                                          91
 [2]
           0 5 -15
                           [3]
 [3]
                           [4]
 [4]
                    11
 [5]
                           [5]
                           [6]
                    -6
 [6]
                           [7]
                    91
 [7]
                           [8]
                    28
 [8]
```

目的:實作轉置矩陣

```
for (i = 0; i < a[0].col; i++){
    for( j = 1; j <= n; j++){
        if (a[j].col == i) {
            b[currentb].row = a[j].col;
            b[currentb].col = a[j].row;
            b[currentb].value = a[j].value;
            currentb++;
        }
    }
}</pre>
```

```
i = 1
          row col value
                               row col value
a[0]
                         b[0]
              0 15
                          [1]
 [1]
                                        15
           0 3 22
 [2] i = 2
                          [2]
                                        91
                          [3]
                  -15
 [3]
 [4]
                          [4]
                   11
 [5]
                          [5]
                          [6]
 [6]
                   -6
                          [7]
                   91
 [7]
                          [8]
                   28
 [8]
```

目的:實作轉置矩陣

```
for (i = 0; i < a[0].col; i++){
    for( j = 1; j <= n; j++){
        if (a[j].col == i) {
            b[currentb].row = a[j].col;
            b[currentb].col = a[j].row;
            b[currentb].value = a[j].value;
            currentb++;
        }
    }
}</pre>
```

```
i = 1
           row col value
                                   row col value
a[0]
                            b[0]
                0 15
                              [1]
 [1]
                                              15
 [2]
                      22
                              [2]
                                             91
      i = 3 \ 0
                    -15
                              [3]
                              [4]
 [4]
                      11
 [5]
                              [5]
                              [6]
 [6]
                      -6
                              [7]
                      91
 [7]
                              [8]
                      28
 [8]
```

目的:實作轉置矩陣

```
for (i = 0; i < a[0].col; i++){
    for( j = 1; j <= n; j++){
        if (a[j].col == i) {
            b[currentb].row = a[j].col;
            b[currentb].col = a[j].row;
            b[currentb].value = a[j].value;
            currentb++;
        }
    }
}</pre>
```

```
i = 1
         row col value
                            row col value
a[0]
         6 6 8
                      b[0]
                       [1]
           0 15
                                    15
 [1]
 [2]
                 22
                       [2]
                                    91
                       [3]
 [3]
           5 -15
                                    11
 [4] j = 4
                       [4]
                11
 [5]
                       [5]
                       [6]
 [6]
                 -6
                       [7]
                 91
 [7]
                       [8]
                 28
 [8]
```

目的:實作轉置矩陣

```
for (i = 0; i < a[0].col; i++){
    for( j = 1; j <= n; j++){
        if (a[j].col == i) {
            b[currentb].row = a[j].col;
            b[currentb].col = a[j].row;
            b[currentb].value = a[j].value;
            currentb++;
        }
    }
}</pre>
```

```
i = 1
          row col value
                                 row col value
a[0]
                     8
                          b[0]
             0 15
                            [1]
                                          15
 [1]
                    22
                            [2]
                                          91
 [2]
           0 5 -15
                            [3]
                                           11
 [3]
 [4]
                            [4]
                    11
 [5] j = 5
                            [5]
                            [6]
 [6]
                    -6
                            [7]
                    91
 [7]
                            [8]
 [8]
                    28
```

目的:實作轉置矩陣

```
for (i = 0; i < a[0].col; i++){
    for( j = 1; j <= n; j++){
        if (a[j].col == i) {
            b[currentb].row = a[j].col;
            b[currentb].col = a[j].row;
            b[currentb].value = a[j].value;
            currentb++;
        }
    }
}</pre>
```

```
i = 1
         row col value
                              row col value
a[0]
          6 6 8
                        b[0]
          0 0 15
                         [1]
                                       15
 [1]
                         [2]
          0 3 22
                                       91
 [2]
          0 5 -15
                         [3]
                                       11
 [3]
 [4]
                         [4]
                   11
 [5]
                         [5]
                         [6]
 [6] j = 6
                  -6
                         [7]
 [7]
                  91
                         [8]
 [8]
                  28
```

目的:實作轉置矩陣

```
for (i = 0; i < a[0].col; i++){
    for( j = 1; j <= n; j++){
        if (a[j].col == i) {
            b[currentb].row = a[j].col;
            b[currentb].col = a[j].row;
            b[currentb].value = a[j].value;
            currentb++;
        }
    }
}</pre>
```

```
i = 1
         row col value
                             row col value
a[0]
          6 6 8
                       b[0]
                         [1]
            0 15
                                      15
 [1]
          0 3 22
                         [2]
                                      91
 [2]
          0 5 -15
                         [3]
                                      11
 [3]
 [4]
                         [4]
                11
 [5]
                         [5]
                         [6]
 [6]
                  -6
                         [7]
                  91
                         [8]
 [8]
                  28
```

目的:實作轉置矩陣

transpose()程式碼說明:

```
for (i = 0; i < a[0].col; i++){
    for( j = 1; j <= n; j++){
        if (a[j].col == i) {
            b[currentb].row = a[j].col;
            b[currentb].col = a[j].row;
            b[currentb].value = a[j].value;
            currentb++;
        }
    }
}</pre>
```

```
i = 1
          row col value
                                row col value
a[0]
                     8
                          b[0]
             0 15
                           [1]
                                          15
 [1]
                    22
                           [2]
                                          91
 [2]
           0 5 -15
                           [3]
                                          11
 [3]
                           [4]
 [4]
                   11
 [5]
                           [5]
                           [6]
 [6]
                    -6
                           [7]
 [7]
                    91
                           [8]
 [8] j = 8
                    28
```

以此類推

Discussion: compared with 2-D array representation

O(columns\*elements) vs. O(columns\*rows)

elements --> columns \* rows when nonsparse O(columns\*columns\*rows)

Problem: Scan the array "columns2\*rows" times.

#### Solution:

Determine the number of elements in each column of the original matrix.

==>

Determine the starting positions of each row in the transpose matrix.

CHAPTER 2 85

```
void fast_transpose(term a[], term b[])
       /* the transpose of a is placed in b */
        int row_terms[MAX_COL], starting_pos[MAX_COL];
        int i, j, num_cols = a[0].col, num_terms = a[0].value;
        b[0].row = num\_cols; b[0].col = a[0].row;
        b[0].value = num_terms;
        if (num_terms > 0){ /*nonzero matrix*/
         \negfor (i = 0; i < num_cols; i++)
columns
          row terms[i] = 0;
___for (i = 1; i <= num_terms; i++) /*計算 row_terms的值*
row_term [a[i].col]++
          starting_pos[0] = 1;
         -for (i =1; i < num_cols; i++)
columns starting_pos[i]=starting_pos[i-1] +row_terms [i-1];
        /*計算 starting_pos的值*/
```

Compared with 2-D array representation

O(columns+elements) vs. O(columns\*rows)

elements --> columns \* rows

O(columns+elements) --> O(columns\*rows)

Cost: Additional row\_terms and starting\_pos arrays are required. Let the two arrays row\_terms and starting\_pos be shared.

目的:實作轉置矩陣

fast\_transpose()程式碼說明:

```
void fast_transpose(term a[], term b[]){
   int row_terms[MAX_COL], starting_pos[MAX_COL];
   int i, j;
   int num_cols = a[0].col;
   int num_terms = a[0].value;
   b[0].row = num_cols;
   b[0].col = a[0].row;
   b[0].value = num_terms;
```

透過a[0]的基本資料,知道轉置後的資本資料。 row, col: a的col轉置後是b的row a的row轉置後是b的col

value:轉置後的非0項目數量不變

目的:實作轉置矩陣

fast\_transpose()程式碼說明:

```
if (num terms > 0){
    for (i = 0; i < num_cols; i++){
        row terms[i] = 0;
    for (i = 1; i \le num terms; i++){}
        row terms[a[i].col]++;
    starting pos[0] = 1;
    for (i = 1; i < num_cols; i++){
        starting_pos[i]=starting_pos[i-1] +row_terms [i-1];
    for (i = 1; i <= num_terms; i++){
        j = starting_pos[a[i].col]++;
        b[j].row = a[i].col;
        b[j].col = a[i].row;
        b[j].value = a[i].value;
```

row\_terms

0 1 2 3 4 5

0 0 0 0 0 0

目的:實作轉置矩陣

```
if (num terms > 0){
    for (i = 0; i < num_cols; i++){
        row terms[i] = 0;
    for (i = 1; i \leftarrow num terms; i++){}
        row terms[a[i].col]++;
    starting pos[0] = 1;
    for (i = 1; i < num_cols; i++){
        starting_pos[i]=starting_pos[i-1] +row_terms [i-1];
    for (i = 1; i <= num_terms; i++){
        j = starting_pos[a[i].col]++;
        b[j].row = a[i].col;
        b[j].col = a[i].row;
        b[j].value = a[i].value;
```

```
i = 1
              row col value
   a[0]
    [1] a[1].col [0]
                         15
                         22
     [2]
     [3]
                       -15
     [4]
                         11
     [5]
     [6]
               2 3
                         -6
     [7]
                         91
    [8]
                         28
row_terms
```

目的:實作轉置矩陣

```
if (num terms > 0){
    for (i = 0; i < num_cols; i++){
        row terms[i] = 0;
    for (i = 1; i \leftarrow num terms; i++){}
        row terms[a[i].col]++;
    starting pos[0] = 1;
    for (i = 1; i < num_cols; i++){
        starting_pos[i]=starting_pos[i-1] +row_terms [i-1];
    for (i = 1; i <= num_terms; i++){
        j = starting_pos[a[i].col]++;
        b[j].row = a[i].col;
        b[j].col = a[i].row;
        b[j].value = a[i].value;
```

```
i = 2
               row col value
   a[0]
                         15
                         22
        a[2].col () | 3
     [3]
                        -15
                         11
     [5]
     [6]
                2 3
                         -6
     [7]
                         91
    [8]
                         28
row_terms
```

目的:實作轉置矩陣

```
if (num terms > 0){
    for (i = 0; i < num_cols; i++){
        row terms[i] = 0;
    for (i = 1; i \leftarrow num terms; i++){}
        row terms[a[i].col]++;
    starting pos[0] = 1;
    for (i = 1; i < num_cols; i++){
        starting_pos[i]=starting_pos[i-1] +row_terms [i-1];
    for (i = 1; i <= num_terms; i++){
        j = starting_pos[a[i].col]++;
        b[j].row = a[i].col;
        b[j].col = a[i].row;
        b[j].value = a[i].value;
```

```
i = 3
               row col value
   a[0]
                          22
     [2]
     [3] a[3].col () 5
                         -15
     [4]
                           11
     [5]
     [6]
                          -6
                          91
     [8]
                          28
row_terms
```

目的:實作轉置矩陣

```
if (num terms > 0){
    for (i = 0; i < num_cols; i++){
        row terms[i] = 0;
    for (i = 1; i \leftarrow num terms; i++){}
        row terms[a[i].col]++;
    starting pos[0] = 1;
    for (i = 1; i < num_cols; i++){
        starting_pos[i]=starting_pos[i-1] +row_terms [i-1];
    for (i = 1; i <= num_terms; i++){
        j = starting_pos[a[i].col]++;
        b[j].row = a[i].col;
        b[j].col = a[i].row;
        b[j].value = a[i].value;
```

```
i = 4
               row col value
   a[0]
                          15
                          22
     [2]
                0 5 -15
     [3]
     [4] a[4].col
                          11
     [5]
     [6]
                          -6
     [7]
                          91
    [8]
                          28
row_terms
```

目的:實作轉置矩陣

```
if (num terms > 0){
    for (i = 0; i < num_cols; i++){
        row terms[i] = 0;
    for (i = 1; i \leftarrow num terms; i++){}
        row terms[a[i].col]++;
    starting pos[0] = 1;
    for (i = 1; i < num_cols; i++){
        starting_pos[i]=starting_pos[i-1] +row_terms [i-1];
    for (i = 1; i <= num_terms; i++){
        j = starting_pos[a[i].col]++;
        b[j].row = a[i].col;
        b[j].col = a[i].row;
        b[j].value = a[i].value;
```

```
i = 5
              row col value
   a[0]
                         15
                         22
    [2]
                0 5 -15
    [3]
    [4]
                         11
    [5] a[5].col 1 2
                         -6
    [6]
    [7]
                         91
    [8]
                         28
row_terms
```

目的:實作轉置矩陣

```
if (num terms > 0){
    for (i = 0; i < num_cols; i++){
        row terms[i] = 0;
    for (i = 1; i \leftarrow num terms; i++){}
        row terms[a[i].col]++;
    starting pos[0] = 1;
    for (i = 1; i < num_cols; i++){
        starting_pos[i]=starting_pos[i-1] +row_terms [i-1];
    for (i = 1; i <= num_terms; i++){
        j = starting_pos[a[i].col]++;
        b[j].row = a[i].col;
        b[j].col = a[i].row;
        b[j].value = a[i].value;
```

	i = 6	)				
	_	r	ov	col	value	
a	[0]		6	6	8	
	[1]		0	0	15	
	[2]		0	3	22	
	[3]		0	5	-15	
	[4]		1	1	11	
	[5]		1	2	3	
		].col	2	3	-6	
'	[7]		4	0	91	
	[8]		5	2	28	
row_t	erms					
0	1	2		3	4	5
1	1	1	T	2	0	1

目的:實作轉置矩陣

```
if (num terms > 0){
    for (i = 0; i < num_cols; i++){
        row terms[i] = 0;
    for (i = 1; i \leftarrow num terms; i++){}
        row terms[a[i].col]++;
    starting pos[0] = 1;
    for (i = 1; i < num_cols; i++){
        starting_pos[i]=starting_pos[i-1] +row_terms [i-1];
    for (i = 1; i <= num_terms; i++){
        j = starting_pos[a[i].col]++;
        b[j].row = a[i].col;
        b[j].col = a[i].row;
        b[j].value = a[i].value;
```

	i = 7	7				
	_	ro	OW	col	value	
					_	
a	[0]	(	5	6	8	
	[1]		0	0	15	
	[2]		0	3	22	
	[3]		0	5	-15	
	[4]		1	1	11	
	[5]		1	2	3	
	[6]	,	2	3	-6	
	<b>[7</b> ] a[7	].col 4	4	0	91	
	[8]	:	5	2	28	
row_t	erms					
0	1	2		3	4	5
2	1	1	Г	2	0	1

目的:實作轉置矩陣

```
if (num terms > 0){
    for (i = 0; i < num_cols; i++){
        row terms[i] = 0;
    for (i = 1; i \leftarrow num terms; i++){}
        row terms[a[i].col]++;
    starting pos[0] = 1;
    for (i = 1; i < num_cols; i++){
        starting_pos[i]=starting_pos[i-1] +row_terms [i-1];
    for (i = 1; i <= num_terms; i++){
        j = starting_pos[a[i].col]++;
        b[j].row = a[i].col;
        b[j].col = a[i].row;
        b[j].value = a[i].value;
```

	i = 8					
	_	ro	W	col	value	
a	[0]	6	)	6	8	
	[1]	(	)	0	15	
	[2]	(	)	3	22	
	[3]	(	)	5	-15	
	[4]	1	l	1	11	
	[5]	1	l	2	3	
	[6]	2	2	3	-6	
	[7]	4	1	0	91	
	[ <mark>8]</mark> a[8	].col 5	5	2	28	
row_t	erms					
0	1	2		3	4	5
2	1	2		2	0	1

目的:實作轉置矩陣

fast\_transpose()程式碼說明:

```
if (num terms > 0){
    for (i = 0; i < num_cols; i++){
        row terms[i] = 0;
    for (i = 1; i \le num terms; i++){
        row terms[a[i].col]++;
    starting pos[0] = 1;
    for (i = 1; i < num_cols; i++){}
        starting pos[i]=starting pos[i-1] +row_terms [i-1];
    for (i = 1; i <= num_terms; i++){
        j = starting_pos[a[i].col]++;
        b[j].row = a[i].col;
        b[j].col = a[i].row;
        b[j].value = a[i].value;
```

starting pos[1]=

row terms [0]

starting\_pos[0] +

目的:實作轉置矩陣

#### fast\_transpose()程式碼說明:

```
if (num terms > 0){
    for (i = 0; i < num_cols; i++){
        row terms[i] = 0;
    for (i = 1; i \le num terms; i++){
        row terms[a[i].col]++;
    starting_pos[0] = 1;
   for (i = 1; i < num cols; i++){
        starting pos[i]=starting pos[i-1] +row_terms [i-1];
    for (i = 1; i <= num_terms; i++){
        j = starting_pos[a[i].col]++;
        b[j].row = a[i].col;
        b[j].col = a[i].row;
        b[j].value = a[i].value;
```

starting\_pos[2]=
starting\_pos[1] +
row\_terms [1]

目的:實作轉置矩陣

```
if (num terms > 0){
    for (i = 0; i < num_cols; i++){
        row terms[i] = 0;
    for (i = 1; i <= num_terms; i++){
        row terms[a[i].col]++;
    starting_pos[0] = 1;
   for (i = 1; i < num cols; i++){
        starting pos[i]=starting pos[i-1] +row_terms [i-1];
    for (i = 1; i <= num_terms; i++){
        j = starting_pos[a[i].col]++;
        b[j].row = a[i].col;
       b[j].col = a[i].row;
        b[j].value = a[i].value;
```

```
starting_pos[3]=
starting_pos[2] +
row_terms [2]
```

目的:實作轉置矩陣

```
if (num terms > 0){
    for (i = 0; i < num_cols; i++){
        row terms[i] = 0;
    for (i = 1; i \le num terms; i++){
        row terms[a[i].col]++;
    starting pos[0] = 1;
   for (i = 1; i < num cols; i++){
        starting pos[i]=starting pos[i-1] +row_terms [i-1];
    for (i = 1; i <= num_terms; i++){
        j = starting_pos[a[i].col]++;
        b[j].row = a[i].col;
        b[j].col = a[i].row;
        b[j].value = a[i].value;
```

```
starting_pos[4]=
starting_pos[3] +
row_terms [3]
```

目的:實作轉置矩陣

#### fast\_transpose()程式碼說明:

```
if (num terms > 0){
    for (i = 0; i < num_cols; i++){
        row terms[i] = 0;
    for (i = 1; i \le num terms; i++){
        row terms[a[i].col]++;
    starting_pos[0] = 1;
   for (i = 1; i < num cols; i++){
        starting pos[i]=starting pos[i-1] +row_terms [i-1];
    for (i = 1; i <= num_terms; i++){
        j = starting_pos[a[i].col]++;
        b[j].row = a[i].col;
        b[j].col = a[i].row;
        b[j].value = a[i].value;
```

starting\_pos[5]=
starting\_pos[4] +
row\_terms [4]

目的:實作轉置矩陣

#### fast\_transpose()程式碼說明:

```
if (num terms > 0){
    for (i = 0; i < num_cols; i++){
        row terms[i] = 0;
    for (i = 1; i \le num terms; i++){
        row terms[a[i].col]++;
    starting pos[0] = 1;
    for (i = 1; i < num_cols; i++){
        starting_pos[i]=starting_pos[i-1] +row_terms [i-1];
    for (i = 1; i <= num_terms; i++){
        j = starting_pos[a[i].col]++;
        b[j].row = a[i].col;
        b[j].col = a[i].row;
        b[j].value = a[i].value;
```

```
a[0]
          a[1].col [1]
                                         15
                                         22
                                        -15
                     [3]
                     [4]
                                         11
                     [5]
                     [6]
                                         -6
i = 1
                                         91
                     [7]
                                         28
                     [8]
starting_pos
```

b[0]	6	6	8
[1]	0	0	15
[2]			
[3]			
[4]			
[5]			
[6]			
[7]			
[8]			

row col value

row col value

目的:實作轉置矩陣

```
if (num terms > 0){
    for (i = 0; i < num_cols; i++){
        row terms[i] = 0;
    for (i = 1; i \le num terms; i++){
        row terms[a[i].col]++;
    starting pos[0] = 1;
    for (i = 1; i < num_cols; i++){
        starting_pos[i]=starting_pos[i-1] +row_terms [i-1];
    for (i = 1; i <= num_terms; i++){
        j = starting_pos[a[i].col]++;
        b[j].row = a[i].col;
        b[j].col = a[i].row;
        b[j].value = a[i].value;
```

```
row col value
                   a[0]
          a[2].col [1]
                                        15
                                        22
                                       -15
                    [3]
                    [4]
                                         11
                    [5]
                    [6]
                                        -6
i = 2
                                        91
                    [7]
                                        28
                    [8]
starting_pos
```

	row	col v	<u>value</u>
b[0]	6	6	8
[1]	0	0	15
[2]			
[3]			
[4]			
[5]			
[6]	3	0	22
[7]			
[8]			

目的:實作轉置矩陣

#### fast\_transpose()程式碼說明:

```
if (num terms > 0){
    for (i = 0; i < num_cols; i++){
        row terms[i] = 0;
    for (i = 1; i \le num terms; i++){
        row terms[a[i].col]++;
    starting pos[0] = 1;
    for (i = 1; i < num_cols; i++){}
        starting_pos[i]=starting_pos[i-1] +row_terms [i-1];
    for (i = 1; i <= num_terms; i++){
        j = starting_pos[a[i].col]++;
        b[j].row = a[i].col;
        b[j].col = a[i].row;
        b[j].value = a[i].value;
```

	row col value			
b[0]	6	6	8	
[1]	0	0	15	
[2]				
[3]				
[4]				
[5]				
[6]	3	0	22	
[7]				
[8]	5	0	-15	

row col value

目的:實作轉置矩陣

```
if (num terms > 0){
    for (i = 0; i < num_cols; i++){
        row terms[i] = 0;
    for (i = 1; i \le num terms; i++){
        row terms[a[i].col]++;
    starting pos[0] = 1;
    for (i = 1; i < num_cols; i++){}
        starting_pos[i]=starting_pos[i-1] +row_terms [i-1];
    for (i = 1; i <= num_terms; i++){
        j = starting_pos[a[i].col]++;
        b[j].row = a[i].col;
        b[j].col = a[i].row;
        b[j].value = a[i].value;
```

	row	col	<u>value</u>
b[0]	6	6	8
[1]	0	0	15
[2]			
[3]	1	1	11
[4]			
[5]			
[6]	3	0	22
[7]			
[8]	5	0	-15

目的:實作轉置矩陣

```
if (num terms > 0){
    for (i = 0; i < num_cols; i++){
        row terms[i] = 0;
    for (i = 1; i \le num terms; i++){
        row terms[a[i].col]++;
    starting pos[0] = 1;
    for (i = 1; i < num_cols; i++){}
        starting_pos[i]=starting_pos[i-1] +row_terms [i-1];
    for (i = 1; i <= num_terms; i++){
        j = starting_pos[a[i].col]++;
        b[j].row = a[i].col;
        b[j].col = a[i].row;
        b[j].value = a[i].value;
```

	row col value		
b[0]	6	6	8
[1]	0	0	15
[2]			
[3]	1	1	11
[4]	2	1	3
[5]			
[6]	3	0	22
[7]			
[8]	5	0	-15

目的:實作轉置矩陣

```
if (num terms > 0){
    for (i = 0; i < num_cols; i++){
        row terms[i] = 0;
    for (i = 1; i \le num terms; i++){
        row terms[a[i].col]++;
    starting pos[0] = 1;
    for (i = 1; i < num_cols; i++){
        starting_pos[i]=starting_pos[i-1] +row_terms [i-1];
    for (i = 1; i <= num_terms; i++){
        j = starting_pos[a[i].col]++;
        b[j].row = a[i].col;
        b[j].col = a[i].row;
        b[j].value = a[i].value;
```

	row	col '	<u>value</u>	
b[0]	6	6	8	
[1]	0	0	15	
[2]				
[3]	1	1	11	
[4]	2	1	3	
[5]				
[6]	3	0	22	
[7]	3	2	-6	
[8]	5	0	-15	

目的:實作轉置矩陣

```
if (num terms > 0){
    for (i = 0; i < num_cols; i++){
        row terms[i] = 0;
    for (i = 1; i \le num terms; i++){
        row terms[a[i].col]++;
    starting pos[0] = 1;
    for (i = 1; i < num_cols; i++){
        starting_pos[i]=starting_pos[i-1] +row_terms [i-1];
    for (i = 1; i <= num_terms; i++){
        j = starting_pos[a[i].col]++;
        b[j].row = a[i].col;
        b[j].col = a[i].row;
        b[j].value = a[i].value;
```

	row col value		
b[0]	6	6	8
[1]	0	0	15
[2]	0	4	91
[3]	1	1	11
[4]	2	1	3
[5]			
[6]	3	0	22
[7]	3	2	-6
[8]	5	0	-15

row col value

# Fast transpose matrix

目的:實作轉置矩陣

```
if (num terms > 0){
    for (i = 0; i < num_cols; i++){
        row terms[i] = 0;
    for (i = 1; i \le num terms; i++){
        row terms[a[i].col]++;
    starting pos[0] = 1;
    for (i = 1; i < num_cols; i++){
        starting_pos[i]=starting_pos[i-1] +row_terms [i-1];
    for (i = 1; i <= num_terms; i++){
        j = starting_pos[a[i].col]++;
        b[j].row = a[i].col;
        b[j].col = a[i].row;
        b[j].value = a[i].value;
```

```
a[0]
         a[8].col [1]
                           0 0 15
                                   22
                           0 5 -15
                  [3]
                  [4]
                                   11
                  [6]
                                    -6
i = 8
                                    91
                  [7]
                                    28
                  [8]
starting_pos
```

	row	col	<u>value</u>
b[0]	6	6	8
[1]	0	0	15
[2]	0	4	91
[3]	1	1	11
[4]	2	1	3
[5]	2	5	28
[6]	3	0	22
[7]	3	2	-6
[8]	5	0	-15

# Compare

	space	time
2D array	O(rows * cols)	O(rows * cols)
T	O(alamanta)	O(2212 * 212 * 2212)
Transpose	O(elements)	O(cols * elements)
Fast Transpose	O(elements+MAX _COL)	O(cols + elements)

CHAPTER 2 113

## Sparse Matrix Multiplication

Definition:  $[D]_{m*p} = [A]_{m*n} * [B]_{n*p}$ 

Procedure: Fix a row of A and find all elements in column j

of B for j=0, 1, ..., p-1.

Alternative 1. Scan all of B to find all elements in j.

Alternative 2. Compute the transpose of B.

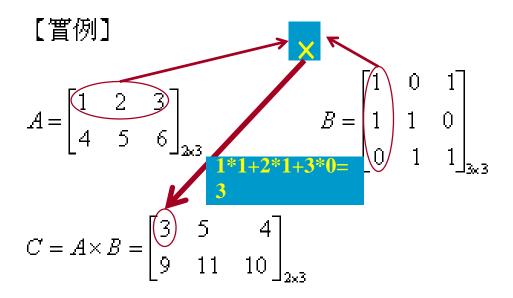
(Put all column elements consecutively)

$$d_{ij} = a_{i0} * b_{0j} + a_{i1} * b_{1j} + ... + a_{i(n-1)*} b_{(n-1)j}$$

## [例如]

$$\mathbf{C}_{11} = \begin{bmatrix} A_{11} & & A_{12} & & \dots & A_{1n} \end{bmatrix} \times \begin{bmatrix} B_{11} \\ B_{21} \\ \vdots \\ B_{n1} \end{bmatrix}$$

$$= A_{11} \times B_{11} + A_{12} \times B_{21} + \dots + A_{1n} \times B_{n1}$$



## Sparse Matrix Multiplication

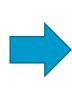
目的:實作稀疏矩陣a\*矩陣b

做法說明:

$$\begin{pmatrix} 5 & 0 & 0 \\ 0 & 11 & 3 \\ 0 & 0 & 2 \end{pmatrix} \times \begin{pmatrix} 5 & 0 & 2 \\ 0 & 11 & 0 \\ 0 & 3 & 0 \end{pmatrix} = \begin{pmatrix} 25 & 0 & 10 \\ 0 & 130 & 0 \\ 0 & 6 & 0 \end{pmatrix}$$

a

$$\begin{bmatrix} 5 & 0 & 0 \\ 0 & 11 & 3 \\ 0 & 0 & 2 \end{bmatrix}$$



_	IOW	COI	value
a[0]	3	3	4
[1]	0	0	5
[2]	1	1	11
[3]	1	2	3
[4]	2	2	2
[5]	3	0	0

set boundary condition

b



	_	row	col	value
	b[0]	3	3	4
	[1]	0	0	5
	[2]	0	2	2
,	[3]	1	1	11
	[4]	2	1	3



ne

transpose

wB[0]	3	3	4
[1]	0	0	5
[2]	1	1	11
[3]	1	2	3
[4]	2	0	2

col value

CHAPTER 2

```
colsA=a[0].col=3
                                       totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                       break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                        CHAPTER 2
    row = a[i].row;
```

colsB=b[0].col=3

initial

rowsA=a[0].row=3

```
col value
                                    col value
    row
                              row
           3
a[0]
                  4 newB[0]
            0
 [1]
                  5
                          [1]
 [2]
                 11
                          [2]
                                          11
                                           3
 [3]
                  3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 1, j = 1, rowBegin = 1, column = 0
 a[i].row=0, row=0
 => False
```

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                    col value
    row
                               row
       3
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                           11
 [3]
                  3
                          [3]
                                            3
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 1, j = 1, rowBegin = 1, column = 0
```

newB[j].row=0, column=0 => False

```
initial
           rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
         else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                      break;
                i++;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                    col value
    row
                              row
a[0]
                  4 newB[0]
           0
                  5
 [1]
                          [1]
                                0
                 11
 [2]
                          [2]
                                           11
 [3]
                                           3
                  3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 1, j = 1, rowBegin = 1, column = 0
```

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                   col value
    row
                             row
           3
                                    3
a[0]
                  4 newB[0]
                                          5
                5
 [1]
            0
                         [1]
                 11
 [2]
                         [2]
 [3]
                  3
                         [3]
 [4]
                         [4]
 [5]
                                          0
                         [5]
 i = 1, j = 1, rowBegin = 1, column = 0
```

```
a[i++].value=5
newB[j++].value=5
sum = 25 i = 2 j = 2
```

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
           colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (i = 1: i <= totalB+1:) {
       if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
               i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
               j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                   col value
    row
                              row
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                          11
                                           3
 [3]
                  3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 2, j = 2, rowBegin = 1, column = 0
 a[i].row=1, row=0
 => True
```

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
               j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                    col value
    row
                              row
       3
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                           11
                                           3
 [3]
                  3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 2, j = 2, rowBegin = 1, column = 0
```

```
row
           col value
d[0]
       3
            3
 [1]
       0
                  25
            0
 [2]
 [3]
 [4]
```

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
               j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                    col value
    row
                              row
      3
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                          11
                                           3
 [3]
                  3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 2, j = 2, rowBegin = 1, column = 0
```

$$i=1$$
  $j=2$  column=1

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
           colsA=a[0].col=3
                                      totalB=b[0].value=4
           totalA=a[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (i = 1: i <= totalB+1:) {
       if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
    row = a[i].row;
```

```
col value
                                    col value
    row
                              row
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                          11
                                           3
 [3]
                  3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 1, j = 2, rowBegin = 1, column = 1
 a[i].row=0, row=0
 => False
```

124

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                    col value
    row
                               row
       3
            3
a[0]
                  4 newB[0]
 [1]
            0
                          [1]
                          [2]
 [2]
                 11
                                           11
 [3]
                  3
                          [3]
                                            3
 [4]
                          [4]
 [5]
                          [5]
                                            0
 i = 1, j = 2, rowBegin = 1, column = 1
```

```
newB[j].row=1, column=1
=> False
```

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                      break;
                i++;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                    col value
    row
                              row
a[0]
                  4 newB[0]
           0
                  5
 [1]
                          [1]
                 11
                                           11
 [2]
                          [2]
 [3]
                                           3
                  3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
 i = 1, j = 2, rowBegin = 1, column = 1
```

```
initial
           rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                    col value
    row
                               row
       3
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                           11
                                            3
 [3]
                  3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                            0
 i = 1, j = 2, rowBegin = 1, column = 1
```

i=2

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
           colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (i = 1: i <= totalB+1:) {
       if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
    row = a[i].row;
```

```
col value
                                   col value
    row
                              row
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                          11
                                           3
 [3]
                  3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 2, j = 2, rowBegin = 1, column = 1
 a[i].row=1, row=0
 => True
```

128

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
            totalA=a[0].value=4
                                      totalB=b[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
               i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
               j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
```

row = a[i].row;

_	row	col	value	_	row	col	value
a[0]	3	3	4	newB[0]	3	3	4
[1]	0	0	5	[1]	0	0	5
[2]	1	1	11	[2]	1	1	11
[3]	1	2	3	[3]	1	2	3
[4]	2	2	2	[4]	2	0	2
[5]	3	0	0	[5]	3	0	0
i =	2, i	=2.	rowI	Begin = 1	, col	umn	1 = 1

```
row
          col value
       3
            3
d[0]
 [1]
       0
                  25
 [2]
 [3]
 [4]
```

storeSum()判斷 沒有新的Sum值需要儲存 故陣列沒有增加資料

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
               j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                    col value
    row
                              row
      3
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                          11
                                           3
 [3]
                  3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 2, j = 2, rowBegin = 1, column = 1
```

$$i=1$$
  $j=4$  column=2

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
           colsA=a[0].col=3
                                      totalB=b[0].value=4
           totalA=a[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (i = 1: i <= totalB+1:) {
       if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
               i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
               j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                   col value
    row
                              row
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                          11
 [3]
                                           3
                  3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 1, j = 4, rowBegin = 1, column = 2
 a[i].row=0, row=0
 => False
```

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
               j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                    col value
    row
                              row
       3
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                           11
 [3]
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 1, j = 4, rowBegin = 1, column = 2
```

newB[i].row=2, column=2 => False

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                      break;
                i++;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                    col value
    row
                              row
a[0]
                  4 newB[0]
          0
                  5
 [1]
                          [1]
                 11
 [2]
                          [2]
                                           11
 [3]
                          [3]
 [4]
                          [4]
 [5]
                          [5]
 i = 1, j = 4, rowBegin = 1, column = 2
```

```
colsA=a[0].col=3
                                       totalB=b[0].value=4
            totalA=a[0].value=4
            row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                       break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                        CHAPTER 2
    row = a[i].row;
```

colsB=b[0].col=3

initial

rowsA=a[0].row=3

```
col value
                                   col value
    row
                             row
           3
a[0]
                 4 newB[0]
                5
 [1]
           0
                         [1]
                 11
 [2]
                         [2]
                                         11
 [3]
                         [3]
                                         2
 [4]
                         [4]
 [5]
                         [5]
 i = 1, j = 4, rowBegin = 1, column = 2
```

a[i++].value=5 newB[j++].value=2 sum=10 i=2 j=5

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
           colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (i = 1: i <= totalB+1:) {
       if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
    row = a[i].row;
```

```
col value
                                   col value
    row
                              row
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                          11
                                           3
 [3]
                  3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 2, j = 5, rowBegin = 1, column = 2
 a[i].row=1, row=0
 => True
```

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
```

j++;

for (; a[i].row == row; i++);

rowBegin = i;

row = a[i].row;

```
col value
                                    col value
    row
                              row
       3
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                           11
                                           3
 [3]
                  3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 2, j = 5, rowBegin = 1, column = 2
```

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
               j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                    col value
    row
                              row
       3
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                           11
                                           3
 [3]
                  3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 2, j = 5, rowBegin = 1, column = 2
```

$$i=1$$
  $j=5$  column=3

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
           colsA=a[0].col=3
                                      totalB=b[0].value=4
           totalA=a[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (i = 1: i <= totalB+1:) {
       if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
               i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
               j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                    col value
    row
                              row
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                          11
 [3]
                                           3
                  3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 1, j = 5, rowBegin = 1, column = 3
 a[i].row=0, row=0
 => False
```

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                    col value
    row
                               row
       3
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                           11
 [3]
                  3
                          [3]
                                            3
 [4]
                          [4]
 [5]
                          [5]
                                            0
 i = 1, j = 5, rowBegin = 1, column = 3
```

newB[j].row=3, column=3 => False

```
initial
           rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                      break;
                i++;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                    col value
    row
                              row
a[0]
                  4 newB[0]
           0
                  5
 [1]
                          [1]
                 11
 [2]
                          [2]
                                          11
 [3]
                                           3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
 i = 1, j = 5, rowBegin = 1, column = 3
```

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[1].row=0
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                   col value
    row
                             row
           3
a[0]
                  4 newB[0]
                5
 [1]
            0
                         [1]
                 11
 [2]
                         [2]
                                          11
 [3]
                         [3]
 [4]
                         [4]
 [5]
                                         0
                         [5]
 i = 1, j = 5, rowBegin = 1, column = 3
```

a[i++].value=5 newB[j++].value=0 sum=0 i=2 j=6

```
col value
           initial
                                                                     row
                                                                                              row
                                                                       3
                                                                            3
                                                                a[0]
                                                                                  4 newB[0]
           rowsA=a[0].row=3
                                     colsB=b[0].col=3
                                                                 [1]
                                                                            0
                                                                                  5
                                                                                          [1]
           colsA=a[0].col=3
                                                                 [2]
                                                                                 11
                                                                                          [2]
                                      totalB=b[0].value=4
           totalA=a[0].value=4
                                                                 [3]
                                                                                  3
                                                                                          [3]
           row=a[1].row=0
                                                                 [4]
                                                                                          [4]
for (i = 1; i \leftarrow totalA;)
                                                                 [5]
                                                                                          [5]
    column = newB[1].row;
                                                                 i = 2, j = 6, rowBegin = 1, column = 3
    for (j = 1; j <= totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
           sum = 0;
                                                                     column = 0
           i = rowBegin;
           for (; newB[j].row == column; j++);
           column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
           sum = 0;
           i = rowBegin;
           column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
               i++;
                      break;
            case 0:
               sum += (a[i++].value * newB[j++].value);break;
           case 1:
               j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                      CHAPTER 2
                                                                            rowBegin=2
                                                                                              row=1
    row = a[i].row;
```

col value

142

11

3

```
colsA=a[0].col=3
                                       totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[2].row=1
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (i = 1: i <= totalB+1:) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                       break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
    row = a[i].row;
```

colsB=b[0].col=3

Round 2

rowsA=a[0].row=3

```
col value
                                   col value
    row
                              row
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                          11
                                           3
 [3]
                  3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 2, j = 1, rowBegin = 2, column = 0
 a[i].row=1, row=1
 => False
```

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                       totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[2].row=1
for (i = 1; i \leftarrow totalA;)
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                       break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                        CHAPTER 2
    row = a[i].row;
```

```
col value
                                    col value
    row
                              row
       3
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                           11
 [3]
                  3
                          [3]
                                            3
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 2, j = 1, rowBegin = 2, column = 0
```

newB[j].row=0, column=0 => False

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[2].row=1
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                    col value
    row
                               row
a[0]
                  4 newB[0]
 [1]
                   5
                          [1]
                                0
                 11
                                           11
 [2]
                          [2]
                  3
                                            3
 [3]
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                            0
 i = 2, j = 1, rowBegin = 2, column = 0
```

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[2].row=1
for (i = 1; i \leftarrow totalA;)
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                       break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
```

row = a[i].row;

```
col value
                                    col value
    row
                              row
       3
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                           11
                                           3
 [3]
                  3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 2, j = 1, rowBegin = 2, column = 0
```

j=2

146

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                       totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[2].row=1
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                       break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
    row = a[i].row;
```

```
col value
                                   col value
    row
                              row
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                          11
                                           3
 [3]
                  3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 2, j = 2, rowBegin = 2, column = 0
 a[i].row=1, row=1
 => False
```

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[2].row=1
for (i = 1; i \leftarrow totalA;)
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                       break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                        CHAPTER 2
    row = a[i].row;
```

```
col value
                                    col value
    row
                              row
       3
            3
a[0]
                  4 newB[0]
 [1]
            0
                          [1]
                          [2]
 [2]
                 11
                                           11
 [3]
                  3
                          [3]
                                            3
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 2, j = 2, rowBegin = 2, column = 0
```

newB[i].row=1, column=0 => True

```
Round 2
         rowsA=a[0].row=3 colsB=b[0].col=3
         colsA=a[0].col=3
         totalA=a[0].value=4
                               totalB=b[0].value=4
         row=a[2].row=1
for (i = 1; i <= totalA; ) {
```

```
column = newB[1].row;
for (j = 1; j \leftarrow totalB+1;) {
    if (a[i].row != row) {
        storeSum(d, &totalD, row, column, &sum);
        sum = 0;
        i = rowBegin;
        for (; newB[j].row == column; j++);
        column =newB[j].row;
    }else if(newB[j].row != column){
        storeSum(d, &totalD, row, column, &sum);
        sum = 0;
        i = rowBegin;
        column = newB[j].row;
    }else switch (COMPARE (a[i].col, newB[j].col)) {
        case -1:
            i++;
                   break;
        case 0:
            sum += (a[i++].value * newB[j++].value);break;
        case 1:
            j++;
for (; a[i].row == row; i++);
rowBegin = i;
row = a[i].row;
```

_	row	col	value	_	row	col	value
a[0]	3	3	4	newB[0]	3	3	4
[1]	0	0	5	[1]	0	0	5
[2]	1	1	11	[2]	1	1	11
[3]	1	2	3	[3]	1	2	3
[4]	2	2	2	[4]	2	0	2
[5]	3	0	0	[5]	3	0	0
i = 2, $j = 2$ , rowBegin = 2, column = 0							

_	row	col	value
d[0]	3	3	4
[1]	0	0	25
[2]	0	2	10
[3]			
[4]			

storeSum()判斷 沒有新的Sum值需要儲存 故陣列沒有增加資料

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[2].row=1
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0:
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                    col value
    row
                              row
       3
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                           11
                                           3
 [3]
                  3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 2, j = 2, rowBegin = 2, column = 0
```

i=2 newB[2].row=1 column=1

```
colsA=a[0].col=3
                                       totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[2].row=1
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (i = 1: i <= totalB+1:) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                       break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
    row = a[i].row;
```

colsB=b[0].col=3

Round 2

rowsA=a[0].row=3

```
col value
                                    col value
    row
                              row
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                          11
                                           3
 [3]
                  3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 2, j = 2, rowBegin = 2, column = 1
 a[i].row=1, row=1
 => False
```

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[2].row=1
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                    col value
    row
                              row
       3
            3
a[0]
                  4 newB[0]
 [1]
            0
                          [1]
                          [2]
 [2]
                 11
                                           11
 [3]
                  3
                          [3]
                                            3
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 2, j = 2, rowBegin = 2, column = 1
```

newB[j].row=1, column=1 => False

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[2].row=1
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                    col value
    row
                               row
a[0]
                  4 newB[0]
 [1]
                          [1]
                 11
                                           11
 [2]
                          [2]
                  3
                                            3
 [3]
                          [3]
 [4]
                          [4]
 [5]
                          [5]
 i = 2, j = 2, rowBegin = 2, column = 1
```

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[2].row=1
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                   col value
    row
                             row
           3
a[0]
                 4 newB[0]
 [1]
                         [1]
                11
                                         11
 [2]
                         [2]
 [3]
                         [3]
 [4]
                         [4]
 [5]
                         [5]
 i = 2, j = 2, rowBegin = 2, column = 1
```

a[i++].value=11 newB[j++].value=11sum = 121 i = 3 j = 3

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                       totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[2].row=1
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                       break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
    row = a[i].row;
```

```
col value
                                   col value
    row
                              row
           3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                          11
 [3]
                  3
                                           3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 3, j = 3, rowBegin = 2, column = 1
 a[i].row=1, row=1
 => False
```

155

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[2].row=1
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                    col value
     row
                               row
       3
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                           11
 [3]
                                            3
                  3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                            0
 i = 3, j = 3, rowBegin = 2, column = 1
```

newB[j].row=1, column=1 => False

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[2].row=1
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
         }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                       break;
                i++;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                     col value
     row
                               row
            3
a[0]
                  4 newB[0]
 [1]
                   5
                           [1]
 [2]
                  11
                           [2]
                                            11
                                            3
                  3
 [3]
                           [3]
 [4]
                           [4]
 [5]
                           [5]
 i = 3, j = 3, rowBegin = 2, column = 1
```

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                       totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[2].row=1
for (i = 1; i \leftarrow totalA;)
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                       break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                        CHAPTER 2
    row = a[i].row;
```

```
col value
                                   col value
    row
                             row
           3
a[0]
                  4 newB[0]
 [1]
           0
                         [1]
 [2]
                         [2]
                 3
 [3]
                         [3] 1
 [4]
 [5]
                         [5]
 i = 3, j = 3, rowBegin = 2, column = 1
```

```
a[i++].value=3
newB[j++].value=3
sum=11*11+3*3=130 i=4 i=4
```

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                       totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[2].row=1
for (i = 1; i \leftarrow totalA;)
    column = newB[1].row;
    for (j = 1; j <= totalB+1;) {
       if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
    row = a[i].row;
```

```
col value
                                   col value
    row
                              row
       3
           3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                          11
                                           3
 [3]
                          [3]
            2
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 4, j = 4, rowBegin = 2, column = 1
 a[i].row=2, row=1
 => True
```

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[2].row=1
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
```

rowBegin = i;

row = a[i].row;

```
col value
                                    col value
    row
                              row
       3
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                           11
                                           3
 [3]
                  3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 4, j = 4, rowBegin = 2, column = 1
```

_	row	col	value
d[0]	3	3	4
[1]	0	0	25
[2]	0	2	10
[3]	1	1	130
[4]			

```
rowsA=a[0].row=3
                                      colsB=b[0].col=3
            colsA=a[0].col=3
                                      totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[2].row=1
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                      break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
                                                       CHAPTER 2
    row = a[i].row;
```

```
col value
                                    col value
    row
                              row
      3
            3
a[0]
                  4 newB[0]
 [1]
            0
                  5
                          [1]
 [2]
                 11
                          [2]
                                          11
                                           3
 [3]
                  3
                          [3]
 [4]
                          [4]
 [5]
                          [5]
                                           0
 i = 4, j = 4, rowBegin = 2, column = 1
```

$$i=2$$
  $j=4$  column=2

```
colsA=a[0].col=3
                                       totalB=b[0].value=4
            totalA=a[0].value=4
           row=a[2].row=1
for (i = 1; i <= totalA; ) {
    column = newB[1].row;
    for (j = 1; j \leftarrow totalB+1;) {
        if (a[i].row != row) {
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            for (; newB[j].row == column; j++);
            column =newB[j].row;
        }else if(newB[j].row != column){
            storeSum(d, &totalD, row, column, &sum);
            sum = 0;
            i = rowBegin;
            column = newB[j].row;
        }else switch (COMPARE (a[i].col, newB[j].col)) {
            case -1:
                i++;
                       break;
            case 0:
                sum += (a[i++].value * newB[j++].value);break;
            case 1:
                j++;
    for (; a[i].row == row; i++);
    rowBegin = i;
    row = a[i].row;
```

colsB=b[0].col=3

Round 2

rowsA=a[0].row=3

```
col value
                                   col value
                             row
      3
           3
a[0]
                  4 newB[0]
 [1]
                  5
                         [1]
 [2]
                 11
                         [2]
                                          11
 [3]
                         [3] 1
 [4]
 [5]
                         [5]
 i = 2, j = 4, rowBegin = 2, column = 2
```

## 以此類推

_	row	col	value
d[0]	3	3	4
[1]	0	0	25
[2]	0	2	10
[3]	1	1	130
[4]	2	1	6

$$\begin{pmatrix} 5 & 0 & 0 \\ 0 & 11 & 3 \\ 0 & 0 & 2 \end{pmatrix} \times \begin{pmatrix} 5 & 0 & 2 \\ 0 & 11 & 0 \\ 0 & 3 & 0 \end{pmatrix} = \begin{pmatrix} 25 & 0 & 10 \\ 0 & 130 & 0 \\ 0 & 6 & 0 \end{pmatrix}$$

```
void mmult (term a[], term b[], term d[])
/* multiply two sparse matrices */
 int i, j, column, totalb = b[].value, totald = 0;
 int rows_a = a[0].row, cols_a = a[0].col,
  totala = a[0].value; int cols_b = b[0].col,
 int row_begin = 1, row = a[1].row, sum =0;
 int new_b[MAX_TERMS][3];
 if (cols_a != b[0].row){
 /*compare the row of a and the col of b*/
     fprintf (stderr, "Incompatible matrices\n");
     exit (1);
```

CHAPTER 2 195

```
fast_transpose(b, new_b); /* the transpose of b is placed in new_b */
/* set boundary condition */ cols_b + totalb
a[totala+1].row = rows_a; /* a[0].row*/
new_b[totalb+1].row = cols b;
new_b[totalb+1].col = 0;
-for (i = 1; i \le totala;) {/* a[0].val* / at most rows_a times
   column = new_b[1].row; /* b[1].col*/
   -for (j = 1; j \le totalb+1;) \{ /*b[0].val*/ at most cols_b times \}
   /* mutiply row of a by column of b */
   if (a[i].row != row) { /* a[1].row */
     storesum(d, &totald, row, column, &sum);
     i = row_begin;
     for (; new_b[j].row == column; j++)
     column =new_b[j].row; /* next col */
```

CHAPTER 2 196

```
else switch (COMPARE (a[i].col, new_b[j].col)) {
     case -1: /* go to next term in a */
           i++; break;
     case 0: /* add terms, go to next term in a and b */
           sum += (a[i++].value * new_b[j++].value);
           break;
     case 1: /* advance to next term in b*/
           j++
 } /* end of for j \le totalb+1 */ at most cols_b times
 for (; a[i].row == row; i++)
 row_begin = i; row = a[i].row;
} /* end of for i <=totala */ at most rows_a times
d[0].row = rows_a; /* a[0].row*/
d[0].col = cols_b; /* b[0].cols*/
d[0].value = totald;
```

```
void storesum(term d[], int *totald, int row, int column,
                                    int *sum)
/* if *sum != 0, then it along with its row and column
  position is stored as the *totald+1 entry in d */
  if (*sum)
    if (*totald < MAX_TERMS) {
      d[++*totald].row = row;
      d[*totald].col = column;
      d[*totald].value = *sum;
   else {
     fprintf(stderr, "Numbers of terms in product
                             exceed %d\n", MAX_TERMS);
 exit(1);
```

CHAPTER 2 198