

```

1 import os, sys
2 sys.path.append(os.path.join(os.path.dirname(__file__), '../ch02'))
3 sys.path.append(os.path.join(os.path.dirname(__file__), '../ch03/program3_4'))
4
5 from program2_1 import Dvector
6 from program2_2 import Dmatrix
7 from program2_8 import vector_norm_max
8 from program3_4 import cholesky_decomp, cholesky_solve
9
10 def main():
11     print("分割数を入力してください--->", end="")
12     n = int(input())
13
14     u = Dvector(1,n-1)
15     u_bvp = bvp( u, 0.0, 1.0, 0.0, 0.0, n, func )
16     h = 1.0 / n
17
18     print("求める答え u と誤差の最大値 e は次の通りです.")
19     for i in range(1,n):
20         print("u[{}]={:.6f}".format(i, u_bvp[i]))
21     for i in range(1,n):
22         u_bvp[i] -= exact(i*h)
23     print("e={:.6f}".format(vector_norm_max(u_bvp)))
24
25
26 # 境界値問題を解く
27 def bvp(b: Dvector, a1: float, a2: float, u0: float,
28         un: float, n: float, f) -> Dvector:
29     h = (a2 - a1) / n # 刻み幅
30     h2 = h * h
31     a = Dmatrix(1, n-1, 1, n-1) # 係数行列
32
33     # 行列の作成
34     for i in range(2, n-1):
35         a[i][i] = 2.0
36         a[i][i+1] = -1.0
37         a[i][i-1] = -1.0
38
39     for j in range(3, n):
40         a[1][j] = 0.0
41     a[1][1] = 2.0
42     a[1][2] = -1.0
43     for j in range(1, n-2):
44         a[n-1][j] = 0.0
45     a[n-1][n-2] = -1.0
46     a[n-1][n-1] = 2.0
47
48     # 右辺ベクトルの作成
49     for i in range(1, n):
50         b[i] = h2 * func( a1 + h*i )
51     b[1] += u0
52     b[n-1] += un
53
54     # 修正コレスキー分解
55     a_cd = cholesky_decomp(a, n-1)
56     # 修正コレスキー分解を利用して連立一次方程式を解く
57     b_cs = cholesky_solve( a_cd, b, n-1)
58
59     return b_cs
60
61
62 # 関数の定義
63 def func(x: float) -> float:
64     return 20.0*x*x*x
65
66
67 def exact(x: float) -> float:
68     return x - pow(x,5.0)
69
70
71 if __name__ == "__main__":
72     main()

```