

```

1 import os, sys
2 sys.path.append(os.path.join(os.path.dirname(__file__), '../ch02'))
3
4 from program2_1 import Dvector
5 from program2_2 import Dmatrix
6 from program2_3 import input_vector
7
8 M = 6 # データのペア数
9 N = 3 # N次式で近似
10
11 def main():
12     global M, N
13
14     x = Dvector(1, M) # x[1...M]
15     y = Dvector(1, M) # y[1...M]
16
17     # ファイルのオープン
18     with open("input_func.dat", "r") as fin:
19         with open("output_func.dat", "w") as fout:
20             input_vector( x, 'x', fin, fout ) # ベクトル x の入出力
21             input_vector( y, 'y', fin, fout ) # ベクトル y の入出力
22
23             least_square( x, y, fout ) # 最小2乗近似
24
25
26 def least_square(x: Dvector, y: Dvector, fout):
27     global M, N
28     p = Dmatrix(1, N+1, 1, N+1) # p[1...N+1][1...N+1]
29     a = Dvector(1, N+1)         # a[1...N+1]
30
31     # 右辺ベクトルの作成
32     for i in range(1, N+2):
33         a[i] = 0.0
34         for j in range(1, M+1):
35             a[i] += y[j] * (x[j] ** (i - 1))
36
37     # 係数行列の作成
38     for i in range(1, N+2):
39         for j in range(1, i+1):
40             p[i][j] = 0.0
41             for k in range(1, M+1):
42                 p[i][j] += x[k] ** (i+j-2)
43             p[j][i] = p[i][j]
44
45     # 連立一次方程式を解く．結果は a に上書き
46     a = gauss2( p, a, N+1 )
47
48     # 結果の出力
49     fout.write("最小2乗近似式は y=\n")
50     for i in range(N+1, 0, -1):
51         fout.write("+ {:.2f} x^{ } ".format(a[i], i-1))
52     fout.write("\n")
53
54
55 # 部分ピボット選択付きガウス消去法
56 def gauss2(a: Dvector, b: Dvector, n: int):
57     eps = 2.0 ** -50.0 # eps = 2^{-50} とする
58
59     for k in range(1, n):
60         # ピボットの選択
61         amax = abs(a[k][k])
62         ip = k
63         for i in range(k+1, n+1):
64             if abs(a[i][k]) > amax:
65                 amax = abs(a[i][k])
66                 ip = i
67
68         # 正則性の判定
69         if amax < eps:
70             print("入力した行列は正則ではない!!!")
71         # 行交換
72         if ip != k:
73             for j in range(k, n+1):
74                 tmp = a[k][j]
75                 a[k][j] = a[ip][j]
76                 a[ip][j] = tmp
77             tmp = b[k]
78             b[k] = b[ip]
79             b[ip] = tmp
80
81         # 前進消去
82         for i in range(k+1, n+1):
83             alpha = -a[i][k] / a[k][k]
84             for j in range(k+1, n+1):
85                 a[i][j] = a[i][j] + alpha * a[k][j]
86             b[i] = b[i] + alpha * b[k]
87
88     # 後退代入
89     b[n] = b[n] / a[n][n]
90     for k in range(n-1, 0, -1):
91         tmp = b[k]
92         for j in range(k+1, n+1):
93             tmp = tmp - a[k][j] * b[j]
94         b[k] = tmp / a[k][k]
95
96     return b
97
98
99 if __name__ == "__main__":
100     main()

```