

Q1 A shared variable  $x$ , initialized to zero, is operated on by four concurrent processes  $W, X, Y, Z$  as follows. Each processes  $W$  and  $X$  reads  $x$  from memory, increments by one, store it to memory, and then terminate. Each of the processes  $Y$  and  $Z$  reads  $x$  from memory, decrements by two, store it to memory, and then terminates.

Each process before reading  $x$  invokes the  $P$  operation (i.e. wait) on a counting semaphore  $S$  and invokes the  $V$  operation (i.e. signal) on the semaphore  $S$  after storing  $x$  to memory. Semaphore  $S$  is initialized to two. what is the maximum possible value of  $x$  after all processes complete execution?

Process $\rightarrow$	W	X	Y	Z
	$R(x)$	$R(x)$	$R(x)$	$R(x)$
Operation	$x++$	$x++$	$x = x - 2$	$x = x - 2$
	$W(x)$	$W(x)$	$W(x)$	$W(x)$

~~Ans~~

$R(x)$  is to read  $x$  from memory,  $W(x)$  is to store  $x$  in memory.

- (i)  $W_1(x=0)$  [ $W$  is preempted]
- (ii)  $X_1, X_2, X_3(x=2)$  [ $X$  is completed]
- (iii)  $Z_1, Z_2, Z_3(x=-4)$  [ $Z$  is completed]
- (iv)  $W_2, W_3(x=1)$  [ $W$  increments local copy of  $x$  and stores  $x$  and  $W$  is completed]
- (v)  $X_1, X_2, X_3(x=2)$  [ $X$  is completed]

After all processes completed maximum value of  $x$  is 2.

Q2 The following two function P1 and P2 that share a variable B with an initial value of 2 execute concurrently. What is the number of distinct value that B can possibly takes after the execution?

P1() {

C = B - 1;

B = 2 \* C;

}

P2() {

D = 2 \* B

B = D - 1;

}

There are following ways that concurrent processes can follow:

C = B - 1; // C = 1

B = 2 \* C; // B = 2

D = 2 \* B; // ~~D = 4~~

B = D - 1; // B = 3

C = B - 1; // C = 1

D = 2 \* B; // D = 4

B = D - 1; // B = 3

B = 2 \* C; // B = 2

C = B - 1; // C = 1

D = 2 \* B; // D = 4

B = 2 \* C; // B = 2

B = D - 1; // B = 3

D = 2 \* B; // D = 4

C = B - 1; // C = 1

B = 2 \* C; // B = 2

B = D - 1; // B = 3

D = 2 \* B; // D = 4

B = D - 1; // B = 3

C = B - 1; // C = 2

B = 2 \* C; // B = 4

There are 3 different value of B 2, 3 and 4.

Q3 Enabling and disabling interrupts to prevent timer interrupts - - - - - accuracy of the system clock.

Solution Disabling the interrupts before entering the critical section and enabling them while exiting the critical section as a result, multiple threads cannot be there in critical section. The issue with the above procedure is if the interrupts are disabled for a long time. It affects the performance of the I/O system. Moreover, if there is an infinite loop, the interrupts are disabled permanently.

while (true)

```
    disable Interrupts();  
    /* Enter critical section */  
    /* Infinite loop in critical section */  
    enable Interrupts();
```

consequently the procedures will also affect the system clock. It means that a clock could go off by one or two clocks while waiting for an interrupt to be disabled. This could lead to a lot of lost data.



Q4

Consider the following snapshot of a system in which four resource A, B, C and D are available. The system contains a total of 6 instance of A, 4 of resource B, 4 of resource C, and 2 of resource D.

	Allocation				Max				Min				Available			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	2	0	1	1	3	2	1	1					6	4	4	2
P <sub>1</sub>	1	1	0	0	1	2	0	2								
P <sub>2</sub>	1	0	1	0	3	2	1	0								
P <sub>3</sub>	0	1	0	1	2	1	0	1								

Do the following problem  
(i) Compute what each might - - - column Need

(ii) Is the system is a safe state? why or why not?

(iii) Is the system deadlocked? why or why not.

(iv) If a request from P<sub>3</sub> arrives for (2, 1, 0, 0) can request be granted immediately?

Solution

(i) We first calculate the need array as follows:

	Allocation				Max				Need				Available			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	2	0	1	1	3	2	1	1	1	2	0	0	6	4	4	2
P <sub>1</sub>	1	1	0	0	1	2	0	2	0	1	0	2				
P <sub>2</sub>	1	0	1	0	3	2	1	0	2	2	0	0				
P <sub>3</sub>	0	1	0	1	2	1	0	1	2	0	0	0				

Because P<sub>0</sub>'s Need = [1, 2, 0, 1] ≤ Available = [6, 4, 4, 2]

P<sub>0</sub> can run and return its Allocation = [2, 0, 1, 1] to Available. The new Available = [6, 4, 4, 2] + [2, 0, 1, 1] = [8, 4, 5, 3]

	Allocation				Max				Need				Available			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>					3	2	1	1					8	4	5	3
P <sub>1</sub>	1	1	0	0	1	2	0	2	0	1	0	2				
P <sub>2</sub>	1	0	1	0	3	2	1	0	2	2	0	0				
P <sub>3</sub>	0	1	0	1	2	1	0	1	2	0	0	0				

Now we run P<sub>1</sub>. After that P<sub>1</sub> returns its Allocation = [1, 1, 0, 0] to Available, and hence Available = old Available = [8, 4, 5, 3] + P<sub>1</sub>'s Allocation = [1, 1, 0, 0] = [9, 5, 5, 3].

	Allocation				Max				Need				Available			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>					3	2	1	1					9	5	5	3
P <sub>1</sub>					1	2	0	2								
P <sub>2</sub>	1	0	1	0	3	2	1	0	2	2	0	0				
P <sub>3</sub>	0	1	0	1	2	1	0	1	2	0	0	0				

Now we can run P<sub>2</sub> followed by P<sub>3</sub>.  
 consequently, the system is in a safe state.  
 Because the deadlock state is on the unsafe area and because this system is in a safe state, this system is not deadlocked.

Now get back to the original situation:-

	Allocation				Max				Need				Available			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	2	0	1	1	3	2	1	1	1	2	0	0	6	4	4	2
P <sub>1</sub>	1	1	0	0	1	2	0	2	0	1	0	2				
P <sub>2</sub>	1	0	1	0	3	2	1	0	2	2	0	0				
P <sub>3</sub>	0	1	0	1	2	1	0	1	2	0	0	0				

If a new request P<sub>3</sub> arrives for [2, 1, 0, 0], this is a mistake because P<sub>3</sub>'s Request = [2, 1, 0, 0].  
 P<sub>3</sub>'s Need = [2, 0, 0, 0] and this request cannot be granted.  
 see Resource-Request algorithm for the details.

Q5. Clearly justify why deadlocks cannot arise on a bounded buffer producers-consumers system.

Solution mutex = 1, full = 0, empty = n

Producer:- do {

```
// produce item
wait(empty);
wait(mutex);
// place in buffer;
signal(mutex);
signal(full);
} while (true)
wait(s);
while (sx <= 0);
```

Consumer:- do {

```
wait(full);
wait(mutex);
// remove item from buffer
signal(mutex);
signal(empty);
// consume item
} while (true)
signal(s);
s++;
```

S--; // busy  
#waiting

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Necessary condition for deadlock to occur are

- 1) Mutual Exclusion
- 2) Hold & wait
- 3) No Preemption
- 4) Circular wait.

As we can see producer and consumer are operating on different semaphores; hence these won't be hold and wait. All 4 condition aren't satisfied, hence deadlock can't arise.