

AEE 5150-E1: Computational Fluid Dynamics

Fall 2021

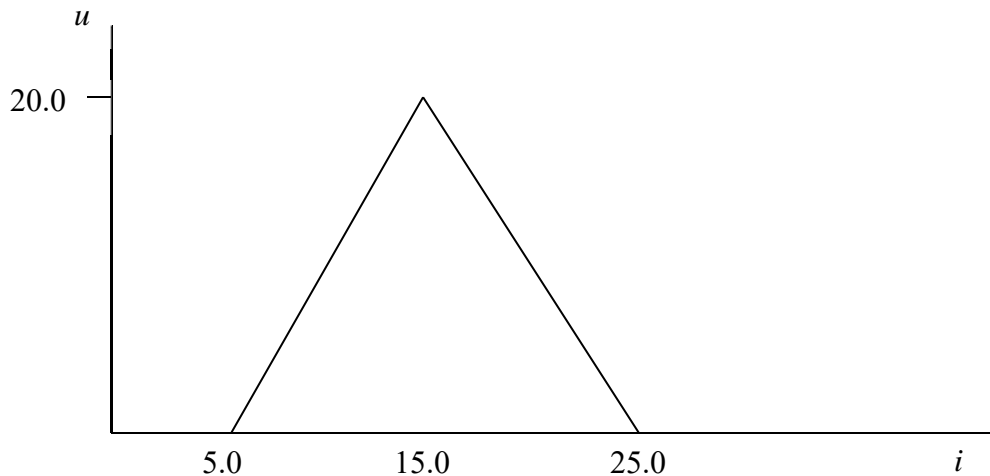
Coding Project 3

Due October 28, 2021

1. A wave is propagating in a closed-end tube. Compute the wave propagation up to $t = 0.15$ sec. by solving the first-order wave equation. Assume the speed of sound to be 200 m/s. The wave has a triangular shape (see figure) which is to be used as the initial condition at $t = 0.0$. You will need to determine the initial u values on the slopes of the triangle and specify them in your code. Solve the problem by the following methods:

FTBS Explicit
Lax-Wendroff
Euler's BTCS Implicit

Use a $\Delta x = 1.0$ and $IM = 71$ ($1 \leq i \leq 71$). For each case, use a $\Delta t = 0.005, 0.0025, 0.00125$ seconds and compare solutions. Run the solution to $t = 0.15$ sec. Print and plot the solution for each method at the initial condition, the end condition, and at the half-way point.



2. Use MacCormack's explicit method to solve the Burgers equation. The initial condition is specified as

$$\begin{aligned}u(x, 0) &= 5.0 & 0.0 \leq x \leq 20.0 \\u(x, 0) &= 0.0 & 20.0 < x \leq 40.0\end{aligned}$$

Print the solution at intervals of 0.4 seconds up to $t = 2.4$ sec. Run the code twice, once for each of the following conditions:

$$\begin{aligned}\Delta x &= 1.0 & \Delta t &= 0.1 \\ \Delta x &= 1.0 & \Delta t &= 0.2\end{aligned}$$

Plot each solution at each print interval.