# Interview Questions: Analysis of Algorithms (ungraded)

练习测验, 3个问题



## 恭喜!您诵讨了!



1/1 分数

**3-SUM in quadratic time.** Design an algorithm for the 3-SUM problem that takes time proportional to  $n^2$  in the worst case. You may assume that you can sort the n integers in time proportional to  $n^2$  or better.

Note: these interview questions are ungraded and purely for your own enrichment. To get a hint, submit a solution.

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您的回答不能超过 10000 个字符。

### 感谢您的回答。

*Hint:* given an integer x and a sorted array a[] of n distinct integers, design a linear-time algorithm to determine if there exists two distinct indices i and j such that a[i] + a[j] == x.



1/1 分数

**Search in a bitonic array.** An array is *bitonic* if it is comprised of an increasing sequence of integers followed immediately by a decreasing sequence of integers. Write a program that, given a bitonic array of n distinct integer values, determines whether a given integer is in the array.

- Standard version: Use  $\sim 3\lg n$  compares in the worst case.
- Signing bonus: Use  $\sim 2\lg n$  compares in the worst case (and prove that no algorithm can guarantee to perform fewer than  $\sim 2\lg n$  compares in the worst case).

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练习测验, 3个问题

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#### 感谢您的回答。

*Hints*: Standard version. First, find the maximum integer using  $\sim 1\lg n$  compares—this divides the array into the increasing and decreasing pieces.

Signing bonus. Do it without finding the maximum integer.



1/1 分数

3.

**Egg drop.** Suppose that you have an n-story building (with floors 1 through n) and plenty of eggs. An egg breaks if it is dropped from floor T or higher and does not break otherwise. Your goal is to devise a strategy to determine the value of T given the following limitations on the number of eggs and tosses:

- Version 0: 1 egg,  $\leq T$  tosses.
- Version 1:  $\sim 1 \lg n$  eggs and  $\sim 1 \lg n$  tosses.
- Version 2:  $\sim \lg T$  eggs and  $\sim 2\lg T$  tosses.
- Version 3: 2 eggs and  $\sim 2\sqrt{n}$  tosses.
- Version 4: 2 eggs and  $\leq c\sqrt{T}$  tosses for some fixed constant c.

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#### 感谢您的回答。

Hints:

- Version 0: sequential search.
- Version 1: binary search.
- Version 2: find an interval containing T of size  $\leq 2T$ , then do binary search.

• Version 3: find an interval of size  $\sqrt{n}$ , then do sequential search. Note: can be improved to  $\sim \sqrt{2n}$  Interview Questions: Analysis of Algorithms (ungraded)

练习测验, version 4:  $1+2+3+\ldots+t \sim \frac{1}{2}t^2$  . Aim for  $c=2\sqrt{2}$ 

