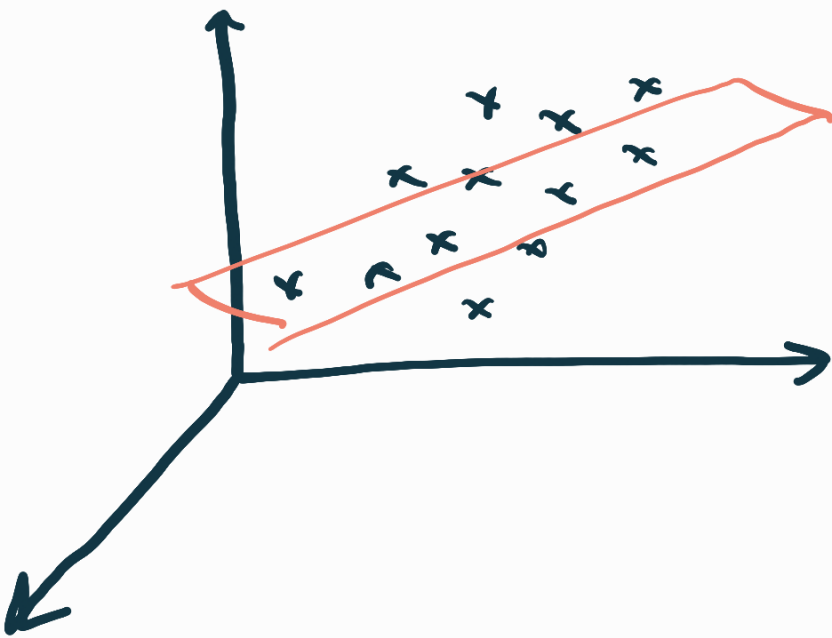


cgpa | iq | lpa



$$y = mx + b$$

$$Y = \beta_0 + \beta_1 x_1 + \beta_2 x_2$$

$$x_1 \Rightarrow 1 \text{ ft. (cgpa)}$$

$$x_2 = 2 \text{ ft. (iq)}$$

$$Y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots \beta_n x_n$$

hyperplane in
 n -dimⁿ co-ordinates

$$\beta_0, \beta_1, \beta_2, \beta_3, \dots \beta_n$$

calculating coefficients

Mathematical Formulation

cgpa | iq | lpa

x_1	x_2	y
8	80	8
7	70	7
5	120	15

$$\hat{y}_1 = \beta_0 + \beta_1 8 + \beta_2 80$$

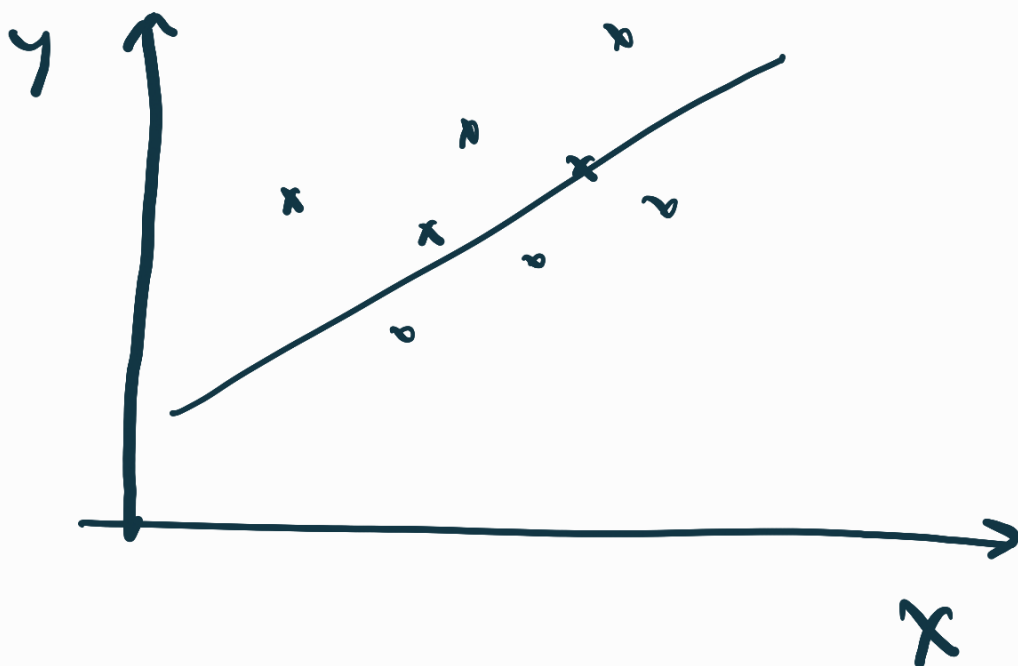
$$\hat{y}_2 = \beta_0 + \beta_1 7 + \beta_2 70$$

$$\hat{y}_3 = \beta_0 + \beta_1 5 + \beta_2 120$$

$$\hat{y} = \begin{bmatrix} \hat{y}_1 \\ \hat{y}_2 \\ \vdots \\ \hat{y}_n \end{bmatrix} = \begin{bmatrix} \beta_0 + \beta_1 x_{11} + \beta_2 x_{12} + \dots \\ \beta_0 + \beta_1 x_{21} + \beta_2 x_{22} + \dots \\ \vdots \\ \beta_0 + \beta_1 x_{n1} + \beta_2 x_{n2} + \dots \end{bmatrix}$$

$$= \begin{bmatrix} 1 & x_{11} & x_{12} & + & \dots & x_{1m} \\ 1 & x_{21} & x_{22} & + & \dots & x_{2m} \\ \vdots & \vdots & \vdots & & & \vdots \\ 1 & x_{n1} & x_{n2} & + & \dots & x_{nm} \end{bmatrix} \begin{bmatrix} \beta_0 \\ \beta_1 \\ \vdots \\ \beta_m \end{bmatrix}$$

$$\hat{y} = X\beta \quad \text{--- (1)}$$



$$E = \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

→ matrix form

$$y = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{bmatrix} \quad \hat{y} = \begin{bmatrix} \hat{y}_1 \\ \hat{y}_2 \\ \vdots \\ \hat{y}_n \end{bmatrix}$$

$$e = y - \hat{y} = \begin{bmatrix} y_1 - \hat{y}_1 \\ y_2 - \hat{y}_2 \\ \vdots \\ y_n - \hat{y}_n \end{bmatrix}$$

$$\begin{bmatrix} y_2 - \hat{y}_2 \\ \vdots \\ y_n - \hat{y}_n \end{bmatrix}$$

$$e^T e = [y_1 - \hat{y}_1 \quad y_2 - \hat{y}_2 \quad \dots \quad y_n - \hat{y}_n] \cdot e$$

$$= \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

$$\boxed{E = e^T e} \quad \text{--- (11)}$$

Imp.

$$\hat{y} = X \beta \quad \text{--- (1)}$$

$$E = e^T e \quad \text{--- (11)}$$

Minimize the G

↳ minimize

$$E = (Y - \hat{Y})^T (Y - \hat{Y}) = (Y^T - \hat{Y}^T)(Y - \hat{Y})$$

$$= Y^T Y - Y^T \hat{Y} - \hat{Y}^T Y + \hat{Y}^T \hat{Y}$$

$$E = Y^T Y - 2Y^T \hat{Y} + \hat{Y}^T \hat{Y}$$

L (iii)

$$\hat{Y} = X\beta$$

$$2) E = Y^T Y - 2Y^T X\beta + \beta^T X^T X\beta$$

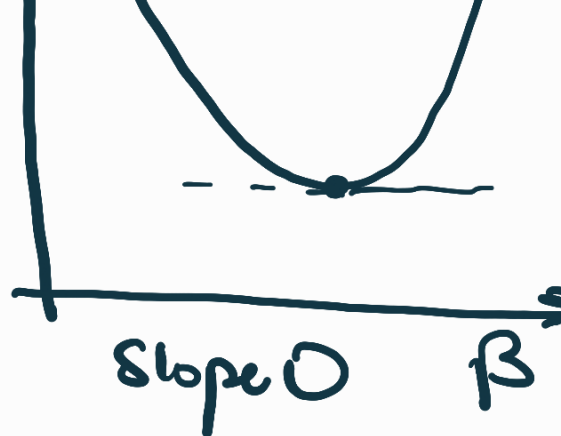
L (iv)

E(β)

* We have to find such value of β such that E is least

E

$$\frac{\partial E}{\partial \beta} = 0$$



$$\frac{\partial E}{\partial \beta} = 0$$

$$0 - \cancel{2} Y^T X + \cancel{2} \beta^T X^T X = 0$$

$$\beta^T X^T X = Y^T X$$

$$\beta^T X^T X (X^T X)^{-1} = Y^T X (X^T X)^{-1}$$

$$\beta^T I = Y^T X (X^T X)^{-1}$$

$$\beta^T = Y^T X (X^T X)^{-1}$$

$$\beta = \left[Y^T X (X^T X)^{-1} \right]^T$$

$$\boxed{\beta = \left[(X^T X)^{-1} \right] X^T Y}$$

L (V)

