

TWO - Sum

$$\text{arr} = \{ 2, 6, 5, 8, 11 \} \quad \text{target} = 14$$

Are there any 2 ele from the array which sums to 14.

From this 2 type of problem can be made

\Rightarrow Are there any 2 ele which sums to target

\Rightarrow Tell me the location of those 2 items.

① Brute, pick 1st ele and check it with other rem. elements
then pick 2nd ele with " " elements.

for ($i=0; i < n; +i$) $TC = O(n^2)$

 ↑ for ($j=0; j < n; +j$)

 ↓ if ($i=j$) continue;

 if ($\text{arr}[i] + \text{arr}[j] == \text{target}$)

 ↓ return i, j ; }

}

}

② Better (Hashing is used)

eg $\rightarrow x + y = \text{target}$

$$8 + \underline{y} = 14$$

We can find whether y exists in array or not using HashTable.

[2, 6, 5, 8, 11]

for $2 + \underline{12} = 14$

but in left of 2 there is no 12

for $6 + \underline{8} = 14$

for $5 + \underline{9} = 14$

for $8 + \underline{6} = 14$

in left of 8 there is 6
so we can easily return whatever is asked

(5, 2)
(6, 8)
(2, 0)

Hash map
ele index

Two-Sum

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then pick 2nd ele and check it with other rem. elements.

for ($i=0; i < n; +i$) $\quad TC = O(n^2)$

 | for ($j=0; j < n; +j$)

 | if ($i == j$) continue;

 | if ($\text{arr}[i] + \text{arr}[j] == \text{target}$)

 | return i, j ;

}

}

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$\underline{\text{eg}} \rightarrow x + y = \text{target}$

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Hash table.

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for $5 + \underline{9} = 14$

for $8 + \underline{6} = 14$

in left of 8 there is 6

so we can easily
return whatever
is asked

(5, 2)
(6, 1)
(2, 0)

Hash map
ele index

Code

```

{ map<int,int>mpp;
  for (int i=0; i<n; ++i)
  {
    int a = book[i];
    int mpx = target - a;
    if (mpp.find(mpx) != mpp.end())
      { return "Yes"; } → or return {mpp[mpx], i};
    mpp[a] = i;
  }
  return "No"; → or return {-1, -1}
}
  
```

③ Optimal

(does not use map instead use 2 pointer).

Step 1 → Sort the array and take 2 pointer left & right.

Step 2 → sum both values

if sum < target → increment left

if sum > target → decrement right

Code

```

{ int left = 0, right = n-1;
  sort(book.begin(), book.end());
  while (left < right) {
    int sum = book[left] + book[right];
    if (sum == target) { return "Yes"; }

    else if (sum < target) left++;
    else right--;
  }
  return "No";
}
  
```

$$TC = O(N) + \underbrace{O(N \log N)}_{\text{Sorting}}$$

$$SC = O(1)$$

points ★ for solving Q-2 the optimal is ② Better
 we can't solve Q-2 with the 3rd approach beac sc will be T
 if we solve that it is equal to 2nd approach.

map

(Hashmap)
unordered map

$$TC \rightarrow O(N \times \log N)$$

$$\begin{array}{l|l} O(N) & \rightarrow \text{by} \\ O(N^2) & \rightarrow \text{by} \end{array}$$

$$SC \rightarrow O(N)$$

because we are using map.

3-Sum

Ques → Find out the triplets which sum to target.
triplets should be unique

① Brute

arr = [-1, 0, 1, 2, -1, -4]

↑ ↑ ↑
1st 2nd 3rd sum -

(or) ↑ ↑ ↑
1st 2nd 3rd sum +

set<vector<int>> st;

for (i = 0 to n)

{ for (j = i+1 to n)

{ for (k = j+1 to n)

{ if (arr[i] + arr[j] + arr[k] == 0)

{ vector<int> temp = {num[i], num[j], num[k]}

sort (temp.begin(), temp.end());

st.insert (temp);

Triplet
should
be unique
so for checking
uniqueness.

}

}

}

vector<vector<int>> ans (st.begin(), st.end());
return ans;

TC = $O(n^3 \times \log(\text{no. of unique})) \cong O(n^3)$

SC = $2 \times O(\text{no. of triplets})$

extra space \rightarrow set.

② Better. Because we will be using set and hashing.

$$\Rightarrow \text{arr} = [-1, 0, 1, 2, -1, -4]$$

$\text{target} = 0$, we have to find triplets (unique) which sums to 0.

$$(a) [-1, 0, 1, 2, -1, -4]$$

$i \uparrow$
 $j=1$

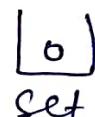
$$\text{arr}[k] = \text{target} - (\text{arr}[i] + \text{arr}[j])$$

(i) $-1 + 0 = -1 \rightarrow$ we need +1 but
 $j=1$ right now set is empty



Set

so before incrementing j, add arr[j] to the set

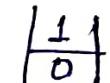


Set

(ii) $-1 + 1 = 0$, which is present in the set.

$j=2$ so triplet is $\{-1, 1, 0\}$

before moving j forward add arr[j] into set



Set

(iii) $-1 + 2 = 1$, we need -1, which is

$j=3$ not in set

add arr[j] into set

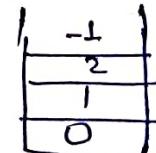


Set

(iv) $j=4$ $-1 + (-1) = -2$, so we need +2 which is present in set.

so other triplet is $\{-1, -1, 2\}$

now add arr[j] into set



Set

(v) $-1 - 4 = -5$, we need +5 which is

not present in set

so add arr[j] into set.

\therefore iteration of j is over now empty the set and make new set for next iteration of $i = 2$.

There is one more set in which we are adding our triplets but before adding we sort those triplets and then add into a outer set.

Code

```
vector<vector<int>> triplet (int n, vector<int> &num)
{
    set<vector<int>> st;
    for (i=0 to n)
    {
        set<int> hashset;
        for (j=i+1 to n)
        {
            int third = -(num[i] + num[j]);
            if (hashset . find (third) != hashset.end ())
            {
                vector<int> temp = {num[i], num[j], third};
                sort (temp.begin (), temp.end ());
                st.insert (temp);
            }
            hashset.insert (num[j]);
        }
    }
    vector<vector<int>> ans (st.begin (), st.end ());
    return ans;
}
```

$$\underline{TC} \Rightarrow N^2 \times \log (\text{size of inner set})$$

$$\underline{SC} \Rightarrow O(N) + O(\underbrace{\text{No. of unique triplets}}_{\text{outer set}})$$

③ Optimal 2 pointer approach.

Step 1 \Rightarrow Firstly sort the given array

$arr[] = [-2 -2 -2 -1 -1 -1 0 0 0 2 2 2]$

$i \quad j$
 \downarrow
 Constant, move j or k

(i) $arr[i] arr[j] arr[k]$
 $-2 -2 + 2 = -2$

$\therefore -2 < \text{target}$ so we will move the left pointer i

$\overset{i}{\cancel{0}} \quad \underline{1}$.

so $j = 2$

{ if $\text{sum} < \text{target}$
 $j++$ }

(ii) $-2 -2 + 2 = -2$

same as above

so $\cancel{j=1}$

if $\text{sum} > \text{target}$
 $k--$ }

(iii) $j=3$

$-2 -1 + 2 = -1$

$-1 < \text{target}$ so $j++$

(iv) $j=4$

$-2 -1 + 2 = -1$

same as above

(v) $j=5$

same as above

(vi) $j=6$

$-2 + 0 + 2 = 0$ $\xrightarrow{\text{target}}$

so we get our 1st triplet in already sorted manner

$[-2, 0, 2]$.

So now increase i but the $i=1$ is -2 which is same as previous so we will move i upto a different value of previous so now $i=3$.

Code

```

vector<vector<int>> triplet (int n , vector<int> &num)
{
    vector<vector<int>> ans;
    sort (num.begin() , num.end());
    for (i=0 to n)
    {
        if (i>0 & num[i] == num[i-1]) continue;
        int j = i+1;
        int k = n-1;
        while (j < k)
        {
            int sum = num[i] + num[j] + num[k];
            if (sum < 0) j++;
            else if (sum > 0) k--;
            else
            {
                vector<int> temp = {num[i], num[j], num[k]};
                ans.push_back (temp);
                j++; k--;
                while (num[j] == num[j-1]) j++;
                while (num[k] == num[k+1]) k--;
            }
        }
    }
}

```

4-Sum

Problem →

$$\text{arr}[] = [1, 0, -1, 0, -2, 2]$$

target = 0

$$[i \neq j \neq k \neq l]$$

find the index of those 4 nos. whose sum goes to equal to target.

① Brute force $\left\{ \begin{matrix} i \\ j \\ k \\ l \end{matrix} \right\}$ 4 loops

$$TC = O(n^4)$$

$$SC = O(\text{no. of quads}) \times 2$$

② Better

$$\text{num}[l] = \text{target} - (\text{num}[i] + \text{num}[j] + \text{num}[k])$$

Now in this we will use 3 loops & a hashmap.

$$[1 \ 2 \ -1 \ -2 \ 2 \ 0 \ -1]$$

$i \uparrow \uparrow \uparrow \uparrow \uparrow \uparrow$

\sqcup 3 values b/w j & k .
hashmap

$$TC = n^3 \times \log(m)$$

$$SC = O(N) + O(\text{quads}) \times 2$$

set

Code

```

set<vector<int>> st;
for (i=0 to n)
{ for (j = i+2 to n)
    { set<long long> hashset;
        { for (k = j+1 to n)
            { long long sum = nums[i] + nums[j];
                sum = sum + nums[k];
                long long fourth = target - (sum);
                if (hashset.find(fourth) != hashset.end())
                {
                    vector<int> temp = {nums[i], nums[j], nums[k],
                                        nums[l]};
                    sort(temp.begin(), temp.end());
                    st.insert(temp);
                    hashset.insert(nums[k]);
                }
            }
        }
    }
}
vector<vector<int>> ans(st.begin(), st.end());
return ans;

```

- ③ optimized does not use hashset instead uses 2 pointer method.

Step 1 → Sort the array.

arr = [1 1 1 2 2 2 3 3 3 4 4 4 5 5]
i ↑ *j* ↑ *k* ↑ *l* ↑

$$TC \rightarrow O(n^2 \times n) \approx O(n^3)$$

$$SC \rightarrow O(\text{no. of quads})$$

Code

```

int n = nums.size();
vector<vector<int>> ans;
sort(nums.begin(), nums.end());
for (i = 0 to n)
{
    if (i > 0 && nums[i] == nums[i-1]) continue;
    for (j = i+1 to n)
    {
        if (j != (i+1) && nums[i] == nums[j-1]) continue;
        int k = j+1;
        int l = n-1;
        while (k < l)
        {
            long long sum = nums[i];
            if (sum < target)
                sum += nums[j];
            sum += nums[k];
            sum += nums[l];
            if (sum == target)
            {
                vector<int> temp = {nums[i], nums[j], nums[k], nums[l]};
                ans.push_back(temp);
                k++;
                while (k < l && nums[k] == nums[k-1]) k++;
                while (k < l && nums[l] == nums[l+1]) l--;
            }
            else if (sum < target) k++;
            else l--;
        }
    }
}
return ans;

```

Longest Common Sequence

Q arr [] = [102, 4, 100, 1, 101, 3, 2, 1, 1]

eg $\left[\begin{array}{l} 101, 102, \\ 1 \ 2 \ 3 \ 4 \end{array} \right] \Rightarrow \text{len} = 4$ } longest length = 4.

$\left[\begin{array}{l} 100, 101, 102 \\ \rightarrow \text{len} = 3 \end{array} \right]$

① Brute

longst = 1

TC = $O(n^2)$

for (i = 0 to n)

{ $x = \text{arr}[i]$

count = 1;

while (linearsearch (arr, $x+1$) == true)

{ $x = x+1$;

count = count + 1;

}

}

② Better \rightarrow In this 1stly sort the array and take lastsmaller for comparing current ele.

counter = 0; longst = 1, lastsmaller = INT-MIN;

for (i = 0 to n)

{ if (arr[i] - 1 == lastsmaller)

{ counter + 1;

lastsmaller = arr[i];

}

else if (arr[i] != lastsmaller)

{ counter = 1;

lastsmaller = arr[i];

}

longst = max (longst, counter);

TC = $O(n)$

③ Optimal → using set for storing all ele uniquely.
(unordered)

We will do ele by ele approach.

Eg → arr = [102, 4, 100, 1, 101, 3, 2, 1, 1]

Sol → set = {102, 4, 100, 1, 101, 3, 2}.

(i) take 102 (in optimal we will work back of that no.)
search for 101 → It is present so we will not start from this

(ii) take 4
search for 3 → "

(iii) take 100
search for 99 → not present so probably this is starting point
so now look for 101 → Yes
102 → Yes
103 → No } Counter = 3 (as of now).

(iv) take 1
Search for 0 → not present
so now look for 2 → Yes } Counter = 4 (as of now)

(v) take 101
Search for 100 → Yes, so move forward.

(vi) take 3

Search for 2 → Yes "

(vii) take 2
Search for 1 → Yes "

so longest = 4.

Issue ham aage ke ele search aur check previous search don't open previous make set ki Nahi & iska matlab ye starting point ho skta hai ek consecutive sequence aur isliye ab iske aage ke ele aur dekhenge.

Code

```

int n = a.size();
if (n == 0) return 0;
longst = 1;
unordered_set<int> st;
for (int i = 0 to n)
    { st.insert(a[i]); }  $\Theta(n) \rightarrow \text{worst case}$ 
for (auto it : st)
    if (st.find(it - 1) == st.end())
        {
            int cut = 1;
            int x = it;
            while (st.find(x + 1) != st.end())
                {
                    x = x + 1;
                    cut = cut + 1;
                }
            longst = max(longst, cut);
        }
return longst;
}

```

TC → If we use unordered set then $O(1)$ $\xrightarrow{\text{avg}}$ $\xrightarrow{\text{worst}}$
 $\Delta O(n) \rightarrow \text{worst case when collision happens (rare case)}$

$$O(n) + O(2n) = O(3n)$$

SC $\rightarrow O(N)$

Longest Subarray with sum K

Subarray means → contiguous part of the array.

arr = [1 2 3 1 1 1 1 4 2 3]

$$K = 3$$

ans → subarrays of sum = 3 → $\begin{cases} [1 2] \rightarrow \text{len} = 2 \\ [1 1 1] \rightarrow \text{len} = 3 \\ [3] \rightarrow \text{len} = 1 \end{cases}$ } longest = 3.

① Brute

Generate all subarray.

like → ① → [1 2]

[1 2]
[1 2 3]

[1 2 3] → 3

② [2]

[2 3]
[2 3 1]

[2 3 1] → -3

etc.

Code

for (i=0 to n)

{ for (j=i to n)

{ sum = 0;

 for (k=i to j)

 { sum += arr[k]; }

 if (sum == K) len = max(len, j-i+1)

TC = O(n³)

SC = O(1)

int len;

② Better Brute (2nd)

In brute force we move on summary elem in subarray sum for. Here we can do one thing that is stop iteration when sum is greater than target (K).

```

for (i=0 to n)
{
    sum = 0
    for (j=i to n)
    {
        sum + = arr[j];
        if (sum == k) len = max(len, j-i+1)
    }
}

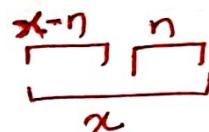
```

$$T = O(n^2)$$

②

Better use hashing. [Prefix Sum]

arr = [1 2 3 1 1 1 4 2 3]
 $\star = 3$



initially prefix sum = 0 len = 0
 \downarrow \downarrow

$$\text{el} \rightarrow \underline{1+2} = 3$$

$$\text{el} \rightarrow \underline{1+2+3} = 6$$

$$\begin{matrix} 3 \\ \dots \\ 6 \end{matrix}$$

we need sum = 3

Hashmap

9	5
8	4
7	3
6	2
3	1
1	0

does there someone with sum = 3 \rightarrow no more

$\text{el} \rightarrow \underline{1+2+3+1} = 7$ so one more subarray but of length = 1

$$\begin{matrix} 4 \\ \dots \\ 7 \end{matrix}$$

does there someone with sum = 4 \rightarrow no

so more

$$\text{el} \rightarrow 1+2+3+1+1 = 8$$

$$\text{el} \rightarrow 1+2+3+1+1+1 = 9$$

$$\begin{matrix} 6 \\ \dots \\ 9 \end{matrix}$$

" $\stackrel{3 \rightarrow \text{sum}}{\dots}$

" sum = 6 \Rightarrow yes

so new subarray of length = 3

[1 1 1]

etc

Code

```

int longestSubarrayWithSumK(vector<int> &a, long long k)
{
    map<long long, int> preSumMap;
    long long sum = 0;
    int maxlen = 0;
    for (int i = 0 to a.size())
    {
        sum += a[i];
        if (sum == k)
            maxlen = max(maxlen, i + 1);
        long long rem = sum - k;
        if (preSumMap.find(rem) != preSumMap.end())
        {
            int len = i - preSumMap[rem];
            maxlen = max(maxlen, len);
        }
        if (preSumMap.find(sum) == preSumMap.end())
            preSumMap[sum] = i;
    }
    return maxlen;
}

```

TC \rightarrow using ordered map $\rightarrow O(N \times \log N)$] \rightarrow don't have any collision
 using unordered map $\rightarrow O(N \times 1)$

SC $\rightarrow O(N)$

Optimal (2 pointers approach).

$$arr = [1 \ 2 \ 3 \ 1 \ 1 \ 1 \ 3 \ 3]$$

$\uparrow \uparrow$

Code

```
int longestSubarraySumK (vector<int> a, long long k)
{
    int left = 0, right = 0;
    long long sum = a[0];
    int maxlen = 0;
    int n = a.size();
    while (right < n)
    {
        while (left <= right && sum > k)
        {
            sum -= a[left];
            left++;
        }
        if (sum == k)
        {
            maxlen = max(maxlen, right - left + 1);
        }
        right++;
        if (right < n) sum += a[right];
    }
    return maxlen;
}
```

Sort an array of 0's 1's & 2's

[Optimal \rightarrow Dutch National Flag Algorithm]

$arr[] = [0, 1, 2, 0, 1, 2, 1, 2, 0, 0, 0, 1]$

① Brute \rightarrow Sort an array

TC $\rightarrow O(N \log N)$ } Merge sort.
SC $\rightarrow O(N)$

② Better

In one loop count the no. of zeros, 1 and 2.
and then from starting we fill 0, 1, 2 based on the
Count:

Code

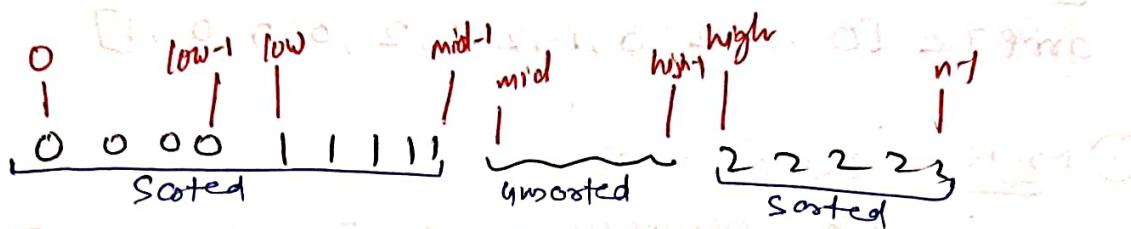
```
cut0 = 0, cut1 = 1, cut2 = 2
for (i = 0 to n) {
    if (a[i] == 0) cut0++;
    else if (a[i] == 1) cut1++;
    else if (a[i] == 2) cut2++;
}
for (i = 0 ; i < cut0 ; ++i) a[i] = 0;
for (i = cut0 ; i < cut0 + cut1 ; ++i) a[i] = 1;
for (i = cut0 + cut1 ; i < n ; ++i) a[i] = 2;
```

$O(N)$ $O(N)$

TC = $O(2N)$

SC = $O(1)$

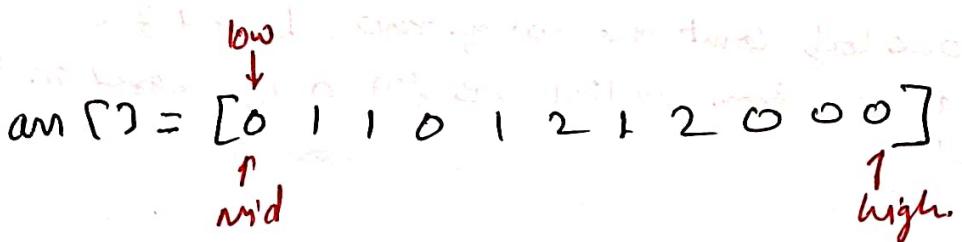
③ Optimal (Dutch National flag Algorithm)



$[0 - \text{low}-1] \rightarrow 0$ extreme left

$[\text{low} - \text{mid}-1] \rightarrow 1$

$[\text{high}+1, n-1] \rightarrow 2$ extreme right



if $a[\text{mid}] = 0 \rightarrow \text{swap}(a[\text{low}], a[\text{mid}])$

$\text{low}++, \text{mid}++;$

if $a[\text{mid}] = 1 \rightarrow \text{swap}(a[\text{mid}], a[\text{high}]);$

$\text{mid}++; \text{high}--;$

if $a[\text{mid}] = 2 \rightarrow \text{swap}(a[\text{high}], a[\text{mid}]);$

$\text{high}--;$

Code

$\text{low} = 0, \text{mid} = 0, \text{high} = n-1;$

while ($\text{mid} \leq \text{high}$)

{ if ($a[\text{mid}] == 0$)

{ swap($a[\text{low}], a[\text{mid}]$);
 $\text{low}++; \text{mid}++;$ }

else if ($a[\text{mid}] == 1$) {
 $\text{mid}++;$ }

else {
 $\text{swap}(a[\text{mid}], a[\text{high}]);$
 $\text{high}--;$ }

}

$T C = O(N)$

Maximum Subarray Sum

[Kadane's Algo]

Subarray means → contiguous part of the array.

① Brute. Try out all subarrays.



```
maxi = INT-MIN;
for (i=0 to n)
{   for (j=i to n)
    { sum = 0;
      for (k=i to j)
        { sum += arr[k]; }
      maxi = max(sum, maxi);
    }
}
```

TC = O(N³)

SC = O(1)

② Better

```
maxi = INT-MIN;
for (i=0 to n)
{   sum = 0;
    for (j=i to n)
    { sum += arr[j];
      maxi = max(sum, maxi);
    }
}
```

TC = O(N²)

SC = O(1)

③ Optimal (Kadane's Algo)

arr = [-2, -3, 4, -1, -2, 1, 5, -3]

maxi = 4

$$\begin{matrix} \text{sum} = & 0 & -2 & 0 & 4 & -1 & -2 & 1 & 5 & -3 \\ & 0 & -2 & -2 & 2 & 1 & -1 & 0 & 5 & -3 \end{matrix} \quad \left\{ \text{so } \max = 4 \right. \quad \boxed{\text{when sum} < 0 \\ \text{then do sum} = 0}$$

(22)

Code

```

long long subarraysum (int arr[], int n)
{
    long long sum=0, maxi=LONGINT;
    for (i=0 to n)
    {
        sum+=arr[i];
        if (sum > maxi)
            maxi = sum;
        if (sum < 0)
            sum=0;
        if (maxi < 0) maxi=0;
    }
    return maxi;
}

```

 $T.C = O(N)$ $S.C = O(1)$ Few test case

(1) [-4 -2 -3 +1]

max subarray sum = -1

so if sum < 0 then return empty subarray which means sum=0

Ques → Print any subarray of max. sum.

```

for (i=0 to n)
{
    if (sum==0) start=i;
    sum = sum + arr[i];
    if (sum > maxi)
    {
        maxi = sum;
        ansStart = start, ansEnd = i;
    }
    if (sum < 0)
    {
        sum=0;
    }
}

```

 $T.C = O(N)$ $S.C = O(1)$

(right function) having ()
 (left function) having ()

Number of Subarrays with Sum K

arr = [1 2 3 -3 1 1 1 4 2 -3] K = 3.

Ques → Find the no. of subarrays whose sum is K.

Sol

① Brute Generate all subarrays.

$\begin{array}{c} \boxed{1} \\ \boxed{1} \boxed{2} \\ \boxed{1} \boxed{2} \boxed{3} \\ \vdots \\ \boxed{1} \boxed{2} \boxed{3} \end{array}$
 $\begin{array}{c} \boxed{2} \\ \boxed{2} \boxed{3} \\ \boxed{2} \boxed{3} \boxed{-3} \\ \vdots \\ \boxed{2} \boxed{3} \boxed{-3} \end{array}$ etc.

counter = 0

for (i = 0 to n)

 { for (j = i to n)

 { sum = 0

 for (k = i to j)

 sum = sum + arr[k];

 if (sum == K)

 counter++;

}

}

TC = $O(n^3)$

② Better

cnt = 0

for (i = 0 to n)

 { sum = 0;

 for (j = i to n)

 sum += arr[j];

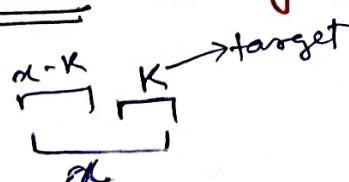
 if (sum == K)

 cnt++;

}

TC = $O(n^2)$

③ Optimal (using prefix sum) + (hashmap)



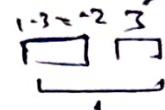
Hashmap < Presum, Counter >

$$arr = [1, 2, 3, -3, 1, 1, 1, 4, 2, -3] \quad k = 3$$

dry run
preffo presum = 0 + 1 + 2 + 3 + -3 + 1 + 1 + 1 + 4 + 2 + -3 = 9

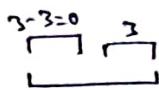
$$cnt = 0 + 1 + 2 + 3 + 4 + 5 + 6 + 7 + 8 = 36$$

for ele $\rightarrow 1$



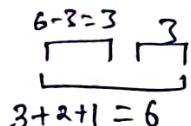
$\because -2$ is not in the hashmap.

for ele $\rightarrow 2$



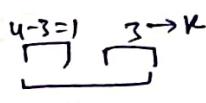
$\because 0$ is present in hashmap

for ele $\rightarrow 3$



$\because 3$ is " "
Hashmap
(presum, cnt)

for ele $\rightarrow 1$



$\because 1$ is a presum so if we exclude '1' then there is a sum of $k(3)$

for ele $\rightarrow 1$



\because presum 3 has 2 occurrences so which on removal gives sum = 3.

etc.

Code

```
{
    unordered_map<int, int> mpp;
    mpp[0] = 1;
    int presum = 0, cnt = 0;
    for (i = 0 to n) {
        presum += arr[i];
        int remove = presum - k;
        cout += mpp[remove];
        mpp[presum] += 1;
    }
    return cout;
}
```

(Handling & (first element given) - longer

Number of Subarrays with XOR as K

XOR → compares 2 bits. And if 2 bits are diff. → set bit 1
2 bits are same → "", 0

A	B	XOR
0	0	0
0	1	1
1	0	1
1	1	0

$$4 \wedge 2 =$$

$$100 \wedge 010 = 110 = 6$$

$$7 \wedge 7 = 0$$

(XOR is used in bit manipulation tricks)

$$\text{arr} = [4 \ 2 \ 2 \ 6 \ 4] \quad k=6$$

→ So no. of subarrays with XOR=6 are. ① $x \wedge x = 0$

$$[4 \ 2] \ [2 \ 2 \ 6] \ [4 \ 2 \ 2 \ 6 \ 4]$$

$$\textcircled{2} \ x \wedge 0 = x$$

Count = 4

① Brute generate all subarrays and count the subarrays with XOR as K.

```

for(i=0 to n)
  {
    for(j=i to n)
      {
        xor=0
        for(k=i to j)
          {
            xor=xor^arr[k];
            if(xor==k) cnt++;
          }
      }
  }

```

② Better

```

for(i=0 to n)
  {
    xor=0
    for(j=i to n)
      {
        xor=xor^arr[j];
        if(xor==k) cnt++;
      }
  }

```

③ optimal, using hashmap and similar approach like prefixsum.

$$\begin{array}{c} \boxed{XR} \\ \downarrow \quad \downarrow \\ x \quad k = _ \end{array}$$

$$\begin{aligned} &\Rightarrow x \wedge k = XR \\ &\Rightarrow x^n k^n k = X R^n k \\ &\Rightarrow \boxed{x = X R^n k} \end{aligned}$$

→ Here from the starting xR is XR and we are looking for k and from starting we are looking for x in the hashmap.

$$\rightarrow arr = [4, 2, 2, 6, 4] \quad k=6$$

$$\text{for ele } 4 \rightarrow xR = 4$$

$$\begin{array}{c} \boxed{4} \\ \downarrow \quad \downarrow \\ x \quad 6 \end{array}$$

so no 2 is present previously. (front xR , cnt)

$$\text{for ele } 2 \rightarrow xR = 4^1 2 = 6$$

$$\begin{array}{c} \boxed{6} \\ \downarrow \quad \downarrow \\ x \quad 6 \end{array}$$

$x = 6^1 6 = 0$ (which is present)

$$\text{for ele } 2 \rightarrow xR = 6^1 2 = 4$$

$$cnt = 1$$

$$\begin{array}{c} \boxed{4} \\ \downarrow \quad \downarrow \\ 2 \quad 6 \end{array}$$

$$\text{for ele } 6 \rightarrow xR = 4^1 6 = 2$$

$$\begin{array}{c} \boxed{2} \\ \downarrow \quad \downarrow \\ 4 \quad 6 \end{array}$$

code

```
int xR = 0;
map<int, int> mpp; ] → N logN or L
```

$mpp[XR]++$

int cnt = 0;

for ($i = 0$ to $a.size()$)

{ $xR = xR^n a[i]$;

int $x = xR^n k$;

$cnt += mpp[x]$;

$mpp[XR]++$;

}

return cnt ;

$TC = O(N)$

$SC = O(N)$

Set Matrix zeroes

Ques → Given an $m \times n$ integer matrix, if an element is 0, set its entire row and column to 0. You must do it in place.

$$\begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 0 & 0 & 1 \\ 1 & 1 & 0 & 1 \\ 1 & 1 & 1 & 1 \end{bmatrix} \longrightarrow \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 1 \end{bmatrix}$$

① Brute

→ First we will use 2 loops (nested loops) to traverse all the cells of the matrix.

→ If any cell (i, j) contains the value 0, we will mark all cells in row i and column j with -1 except those which contain 0.

→ We will perform step 2 for every cell containing 0.

→ Finally we will mark all the cells containing -1 with 0.

→ Thus the given matrix will be modified according to the question.

Code

```
for (i=0 to n)
  for (j=0 to m)
    if (a[i][j] == 0)
      { MaskRow(i)
        MaskCol(j)
      }
```

maskRow(i)

```
{ for (j=0 to m)
  if (a[i][j] != 0)
    a[i][j] = -1;
  }
```

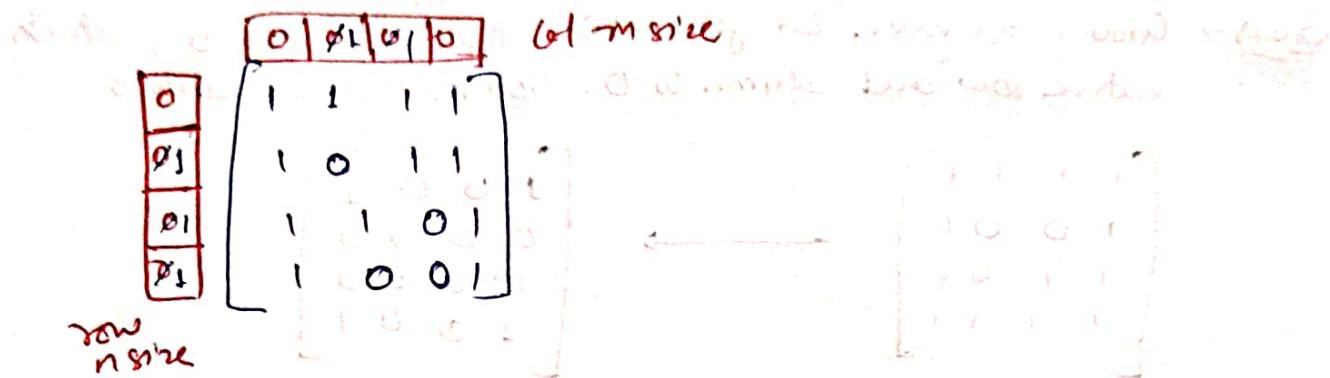
maskCol(j)

```
{ for (i=0; i<n; ++i)
  if (a[i][j] != 0)
    a[i][j] = -1;
  }
```

$$TC = (nm)(n+m) + (nm) \approx O(n^3)$$

```
for (i=0 to n)
  for (j=0 to n)
    if (a[i][j] == -1)
      a[i][j] = 0;
```

② Better, (using 2 extra arrays)



- Declare 2 arrays $\text{row}[n]$ & $\text{col}[m]$ all stored with 0.
- Traverse each cells, if any cell contains 0, we will mark i^{th} index of row array i.e. $\text{row}[i]$ and j^{th} index of col array $\text{col}[j]$ as 1. (It signifies that all the elements in the i^{th} row and j^{th} column will be 0 in the final matrix).
- We again traverse the entire matrix and we will put 0 into all the cells (i, j) for which either $\text{row}[i]$ or $\text{col}[j]$ is marked as 1.

Code

$\text{col}[m] = \{0\}$, $\text{row}[n] = \{0\}$

for ($i = 0$ to n) } $O(nm)$

 | for ($j = 0$ to m)

 | if ($a[i][j] == 0$)

 | $\text{row}[i] = 1$;

 | $\text{col}[j] = 1$;

 | }

}

$$\left\{ \begin{array}{l} TC = O(2 \times n \times m) \\ SC = O(n) + O(m) \end{array} \right\}$$

for ($i = 0$ to n) } $O(nm)$

 | for ($j = 0$ to m)

 | if ($\text{row}[i] \text{ || } \text{col}[j]$)

 | $a[i][j] = 0$.