

Solutions

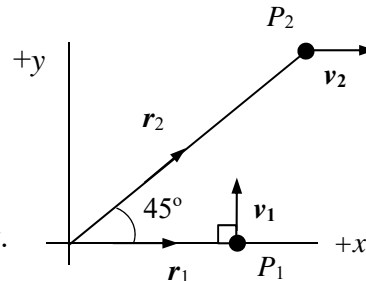
All questions carry 25 marks each.

1. a) State the following:
 - i) SI unit of force in terms of base units.
 - ii) dimension of force.
 - b) The turning effect of a force, M , is defined by $M = Fd$, where F is force and d is perpendicular distance between the direction of F and the pivot. Find the dimension of M and state its SI unit.
 - c) The work done by a constant force, W , is defined by $W = Fs$, where F is force and s is displacement in the direction of F . Show that the dimensions of W is the same as that of M .
 - d) Can the SI unit of M also be written as joule (J)? Give reason for your answer.
 - e) Explain why the equation $v^2 = v_{0x}^2 + a(x - x_0)$ is dimensionally correct but physically incorrect. The variables in the equation have their usual meaning.
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- a) i) $F = ma = \text{kg m/s}^2$ (SI base unit)
 ii) $[M][L][T]^{-2}$ (Dimension)
 - b) Dimension of work M is $[M][L][T]^{-2} \times [L] = [M][L]^2[T]^{-2}$
 SI unit of M is N m.
 - c) Dimension of moment W is $[M][L][T]^{-2} \times [L] = [M][L]^2[T]^{-2}$
 SI unit of W is N m.
 Special name is joule (J)
 - d) The SI unit of M cannot be written as joule (J) because M and W are different physical quantities.
 - e) The missing number 2 in the equation has no dimension.

2. A particle moves with a constant speed 2.0 m/s from P_1 to P_2 along a path (which is not shown in the diagram below). In the diagram, r_1 is 1.0 m and r_2 is 2.0 m. The journey took 2.0 s.

- a) Sketch one possible path traversed by the particle, taking note that \mathbf{v}_1 and \mathbf{v}_2 are instantaneous velocities at P_1 and P_2 respectively and are perpendicular to each other.

- b) Express the following in terms of \mathbf{i} and \mathbf{j} :
- \mathbf{r}_1 , \mathbf{r}_2 and $\Delta\mathbf{r}$.
 - average velocity, \mathbf{v}_{av} , for the journey.
 - \mathbf{v}_1 and \mathbf{v}_2 .
 - average acceleration, \mathbf{a}_{av} , for the journey.



- c) Using the dot product, find the angle between \mathbf{v}_{av} and \mathbf{v}_1 .

- a) Any path such that \mathbf{v}_1 and \mathbf{v}_2 are tangent to the path.

- b) i) $\mathbf{r}_1 = 1.0 \mathbf{i} \text{ m}$
 $\mathbf{r}_2 = 1.4 \mathbf{i} + 1.4 \mathbf{j} \text{ m}$
 $\Delta\mathbf{r} = 1.4 \mathbf{i} + 1.4 \mathbf{j} - 1.0 \mathbf{i} = 0.4 \mathbf{i} + 1.4 \mathbf{j} \text{ m}$

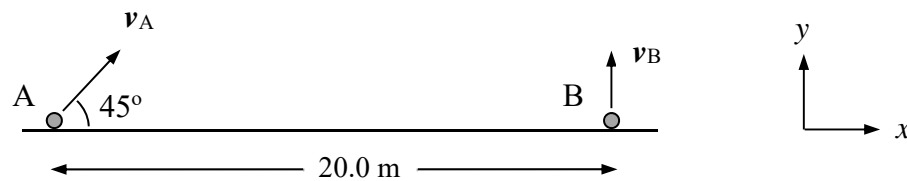
ii) $\mathbf{v}_{av} = (0.4 \mathbf{i} + 1.4 \mathbf{j})/2.0 = 0.2 \mathbf{i} + 0.7 \mathbf{j} \text{ m/s}$

iii) $\mathbf{v}_1 = 2.0 \mathbf{j} \text{ m/s}$
 $\mathbf{v}_2 = 2.0 \mathbf{i} \text{ m/s}$

iv) $\mathbf{a}_{av} = (2.0 \mathbf{i} - 2.0 \mathbf{j})/2.0 = 1.0 \mathbf{i} - 1.0 \mathbf{j} \text{ m/s}^2$

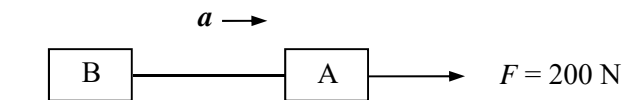
- c) $\mathbf{v}_{av} \cdot \mathbf{v}_1 = v_{av} v_1 \cos \theta$
 $(0.2 \mathbf{i} + 0.7 \mathbf{j}) \cdot (2.0 \mathbf{j}) = 1.4$
 $v_{av} = \sqrt{0.2^2 + 0.7^2} = 0.728$
 $v_1 = \sqrt{2.0^2} = 2.0$
 $\cos \theta = \frac{1.4}{2.0 \times 0.728}$
 $\theta = 16.0^\circ$

3. a) Define “projectile motion”.
- b) Object A is launched with an initial speed $v_A = 20.0$ m/s at 45° with respect to the ground. Object B is launched with an initial speed $v_B = 15.0$ m/s vertically. The launch point of B is 20.0 m from A as shown in the diagram.
- How high is B at $t = 1.0$ s?
 - Write the vertical and horizontal components of initial velocities, v_A and v_B , respectively, in terms of unit vectors \mathbf{i} and \mathbf{j} .
 - How long does it take A to travel 20.0 m horizontally?
 - Show that A and B will not collide.



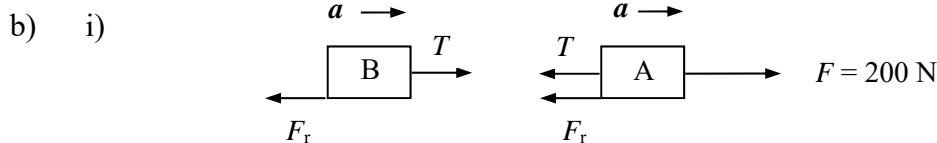
- a) Projectile motion is the motion of an object due to force of gravity only.
- b) i) $y_B = v_B t - \frac{1}{2} g t^2$
 $= 15 \times 1.0 - \frac{1}{2} 9.8 \times 1.0^2$
 $= 10.1$ m
- ii) $v_A = 20.0 \cos 45^\circ \mathbf{i} + 20.0 \sin 45^\circ \mathbf{j}$ m/s
 $= 14.1 \mathbf{i} + 14.1 \mathbf{j}$ m/s
 $v_B = 15 \mathbf{j}$ m/s
- iii) $\text{speed} = \frac{\text{distance}}{\text{time}}$
 $\text{time} = \frac{20}{14.1} = 1.42$ s
- iv) A and B will not collide because at 1.42 s, A and B are at heights given by
- $$y_A = u_A t - \frac{1}{2} g t^2$$
- $$= 20.0 \sin 45^\circ 14.1 \times 1.42 - \frac{1}{2} \times 9.8 \times 1.42^2$$
- $$= 14.1 \times 1.42 - \frac{1}{2} \times 9.8 \times 1.42^2$$
- $$= 10.1$$
- m
- $$y_B = v_B t - \frac{1}{2} g t^2$$
- $$= 15.0 \times 1.42 - \frac{1}{2} \times 9.8 \times 1.42^2$$
- $$= 11.4$$
- m

4. a) Define friction.
- b) The diagram below shows two objects A and B resting on a rough surface and connected by a 2.0 m string. Object A is towed by a 200 N horizontal force to the right. The mass of A is 20 kg while that of B is 10 kg. The coefficient of kinetic friction for both objects is 0.5.
- i) Draw the free body diagrams of A and B.
- ii) Determine the tension in the string and acceleration of the two objects.
- iii) Determine the velocity of A and B when $t = 5.0$ s.



- c) If at $t = 5.0$ s, F is removed, describe the motion of A and B and determine if A and B will collide.

- a) Friction is the force that resists motion.



ii) $F_r = \mu mg$

For A, $200 - T - 20 \times 9.8 \times 0.5 = 20a \dots (1)$

For B, $T - 10 \times 9.8 \times 0.5 = 10a \dots (2)$

$(1) + (2) \quad 53 = 30a$

$a = 1.8 \text{ m/s}^2$

$T = 67 \text{ N}$

iii) $v = at = 1.8 \times 5.0$

$= 9.0 \text{ m/s}$

- c) If F is removed, both A and B will decelerate at the same rate to a stop.
given by $F_r = \mu mg = ma$ or $a = \mu g$.

$a_A = -0.5 \times 9.8 = -4.9 \text{ m/s}^2$

$a_B = -0.5 \times 9.8 = -4.9 \text{ m/s}^2$

Hence A and B will not collide.

*****End*****