

Mid-Semester Test (25% CA)

Name : _____

Adm No : _____

Class : _____

Class S/N : _____

Date : _____

Time allowed : 1.0 hour

Maximum mark : 100

Instructions

Answer all 4 questions. Take $g = 9.80 \text{ m/s}^2$.

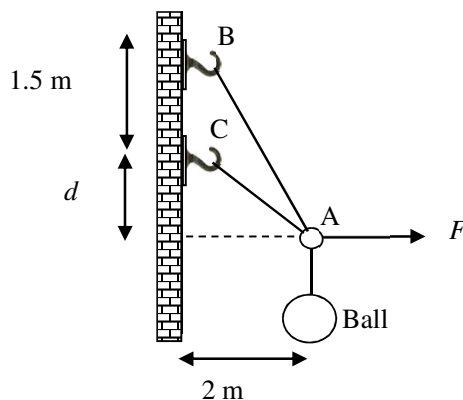
This question paper consists of 4 printed pages including 1 page of formulae.

You are reminded that cheating during test is a serious offence.

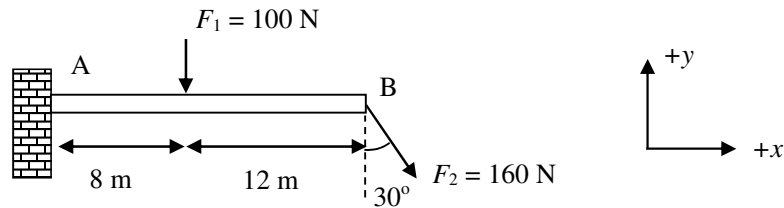
All working in support of your answer must be shown. Answers must be to appropriate significant figures.

1. (a) Determine the dimensions of the following quantities and state their SI units.
- i) Density
 - ii) Rate of change of velocity
 - iii) Work
- (b) In the below figure, a ball of mass 20 kg is connected to a massless ring. A force, $F = 100 \text{ N}$ is applied horizontally to the ring at A. There are two cables that also connect the ring to the wall via the hooks at B and C.
- i) Draw the free body diagram for the ring. Label the tension in cable AB as T_1 and that in cable AC as T_2 .
 - ii) Determine d so that the tension in cable AC is zero.
 - iii) Determine the tension in AB when the tension in cable AC is zero.

(25 marks)

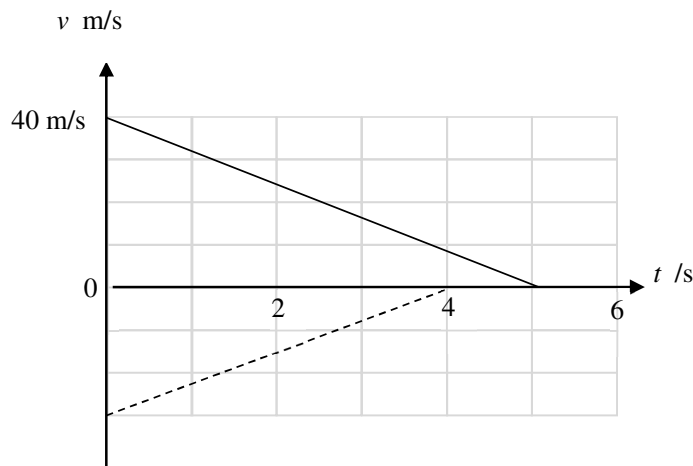


2. (a) Express each of the two forces \vec{F}_1 and \vec{F}_2 in the below diagram in terms of unit vectors \hat{i} and \hat{j} .
- (b) Determine the torque $\vec{\tau}$ about the point A of each of the two forces acting on the beam, where $\vec{\tau} = \vec{r} \times \vec{F}$ and \vec{r} is the position vector. Take right as $+x$ (unit vector \hat{i}), up as $+y$ (unit vector \hat{j}) and out of the paper as $+z$ (unit vector \hat{k}).



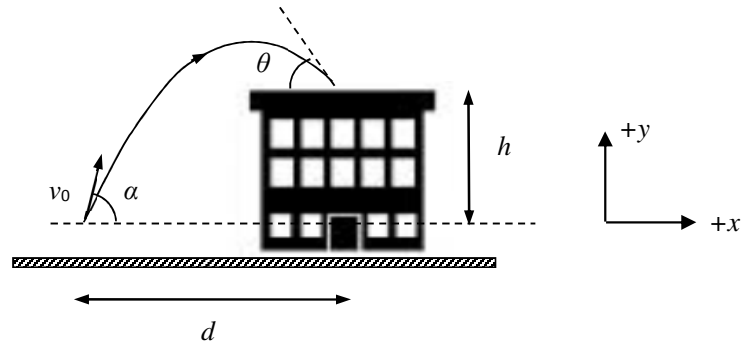
(25 marks)

3. (a) A particle moves so that its position as a function of time is $\vec{r} = \hat{i} + 4t^2\hat{j} + t\hat{k}$.
- Write expressions for its instantaneous velocity and acceleration as functions of time.
 - What is the average velocity and average acceleration between $t = 0 \text{ s}$ and $t = 2 \text{ s}$?
- (b) As two trains move along a straight track, their conductors suddenly notice that they are headed towards each other. The figure below gives their velocities vs time graphs as the conductors slow the trains. The slowing processes begins when the trains are 200 m apart. What is their separation when both trains have stopped?



(25 marks)

4. In the below figure a ball is thrown up onto a roof, landing 4.50 s later at height $h = 20.0$ m above the release level. The ball's path just before landing is angled at $\theta = 60.0^\circ$ with the roof.
- Write the horizontal and vertical components of v_0 in terms of unit vectors \hat{i} and \hat{j}
 - Find the horizontal distance d it travels.
 - What is the magnitude of the ball's initial velocity v_0 and angle α (relative to the horizontal)?



(25 marks)

*****End of paper*****

Formula sheet

Name: _____ Admin. No.: _____ Seat No.: _____

<p><u>Kinematics</u></p> $v_x = v_{0x} + a_x t$ $v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$ $x = x_0 + v_{0x}t + \frac{1}{2}a_x t^2$ $\vec{v} = \frac{d\vec{r}}{dt}, \quad \vec{a} = \frac{d\vec{v}}{dt}$ $y = (\tan \theta)x - \left(\frac{g}{2v^2 \cos^2 \theta}\right)x^2$ $R = \frac{v^2 \sin 2\theta}{g}$ <p><u>Dynamics</u></p> $\vec{F} = \frac{d(m\vec{v})}{dt}, \quad F = \mu N$ $a = \frac{v^2}{r}, \quad F = m \frac{v^2}{r}$ $W = \int \vec{F} \cdot d\vec{r}, \quad W_{net} = K_f - K_i$ $KE = \frac{1}{2}mv^2, \quad GPE = mgh$ $P = \frac{dW}{dt}$ <p><u>Linear momentum</u></p> $m_1\vec{u}_1 + m_2\vec{u}_2 = m_1\vec{v}_1 + m_2\vec{v}_2$ $\vec{J} = \int \vec{F} dt = \Delta \vec{p}$ <p><u>Static electricity</u></p> $F = k \frac{q_1 q_2}{r^2}, \quad k = \frac{1}{4\pi \epsilon_o}$ $F = qE$ $V = k \frac{q}{r}, \quad U = qV$ $\Phi_E = \oint \vec{E} \cdot d\vec{A} = \frac{q}{\epsilon_o}$ $V = Ed, \quad W = qV$	<p><u>Current electricity</u></p> $Q = It, \quad V = IR$ $P = VI = I^2 R = \frac{V^2}{R}$ <p><u>Magnetism & electromagnetism</u></p> $\vec{F} = q\vec{v} \times \vec{B} \quad \vec{F} = i\vec{L} \times \vec{B}$ $\epsilon = -N \frac{d\Phi_B}{dt} \quad \Phi_B = \vec{B} \cdot \vec{A}$ <p><u>Thermodynamics</u></p> $\Delta U = Q - W$ $W = \int p dV$ $Q = mc\Delta T, \quad Q = ml$ $Q_V = nC_V \Delta T \quad \text{const vol}$ $Q_p = nC_p \Delta T \quad \text{const pressure}$ <p><u>Ideal Gas</u></p> $pV = nRT$ $pV^\gamma = c \quad (\text{adiabatic})$ $\gamma = \frac{c_p}{c_v}, \quad c_p - c_v = R$ $W = pV \ln \frac{V_2}{V_1} = nRT \ln \frac{V_2}{V_1}$ $W = \frac{1}{\gamma - 1} (p_1 V_1 - p_2 V_2)$ <p><u>Rotational Motion</u></p> $\omega = \frac{d\theta}{dt}, \quad \alpha = \frac{d\omega}{dt}$ $\omega = \omega_0 + \alpha t$ $\omega^2 = \omega_0^2 + 2\alpha(\theta - \theta_0)$ $\theta = \theta_0 + \omega_0 t + \frac{1}{2}\alpha t^2$ $I = \sum_i m_i r_i^2, \quad K = \frac{1}{2}I\omega^2$	<p><u>SHM & waves</u></p> $T = \frac{1}{f} \quad v = f\lambda \quad \omega = 2\pi f$ $\omega = \frac{2\pi}{T} \quad k = \frac{2\pi}{\lambda}$ $\omega = \sqrt{k/m} \quad \omega = \sqrt{g/L}$ $x = A \cos(\omega t + \phi)$ $y(x, t) = A \cos(\omega t \pm kx)$ $\frac{\partial^2 y}{\partial x^2} = \frac{1}{v^2} \frac{\partial^2 y}{\partial t^2}$ <p><u>Circuits</u></p> $R = R_1 + R_2 + R_3 + \dots \quad \text{series}$ $\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots \quad \text{parallel}$ $\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} + \dots \quad \text{series}$ $C = C_1 + C_2 + C_3 + \dots \quad \text{parallel}$ $Q = CV, \quad U = \frac{1}{2}CV^2$ <p><u>Constants</u></p> <p>Charge on electron</p> $e = -1.60 \times 10^{-19} \text{ C}$ <p>Coulomb's constant</p> $k = 9 \times 10^9 \text{ N m}^2 \text{ C}^{-2}$ <p>Ideal gas constant</p> $R = 8.314 \text{ J mol}^{-1} \text{ K}^{-1}$ <p>Mass of proton</p> $m_p = 1.67 \times 10^{-27} \text{ kg}$ <p>Mass of electron</p> $m_e = 9.11 \times 10^{-31} \text{ kg}$ <p>Permeability of free space</p> $\mu_o = 4\pi \times 10^{-7} \text{ N A}^{-2}$ <p>Permittivity of free space</p> $\epsilon_o = 8.85 \times 10^{-12} \text{ C}^2 \text{ N}^{-1} \text{ m}^{-2}$ <p>Speed of light in vacuum</p> $c = 3.00 \times 10^8 \text{ m s}^{-1}$
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