

***In The Name of Allah***  
***Pattern Recognition (Spring 2023)***

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***Practical Exercise#4: Feature Extraction***

Due Date: 1402.03.22

Consider MNIST dataset consist of two sets digits images: train and test.

**Principle Component Analysis(PCA)**

Use only the training set to perform this part.

- a) Develop PCA takes  $X(D \times N)$  return  $Y(d \times N)$  ( $d$  is the number of features selected by the PCA algorithm).
- b) Propose a suitable  $d$  using proportion of variance (POV) =95%.
- c) Develop PCA reconstruction takes  $Y_{PCA}(d \times N)$  and return  $\hat{X}(D \times N)$ .  
For different values of  $d = \{1, 2, 3, 4, \dots, 784\}$  reconstruct all samples and calculate the average mean square error (MSE). Plot  $d$  (x-axis) versus MSE (y-axis). Discuss about the results.
- d) Reconstruct 10<sup>th</sup> sample and show it as a 'png' image for  $d = \{1, 10, 50, 250, 784\}$ . Discuss about the results.
- e) For different values of  $d = \{1, 2, 3, \dots, 784\}$  plot  $d$  (x-axis) versus eigenvalues (y-axis). Discuss about the result.

**Note:**

- You are not allowed to employ any available codes from **others** or **on the internet**.
- Prepare a report in PDF format including the figures, answer to the questions and discussions mentioned in the homework.
- Make a folder including your report and your codes (Note that your code is needed to be self-comment)
- Submit all things in a zipped folder named as "YourNameYourFamily - Practical"+ "Exercise Number"+"Student Number".rar

**Good Luck**