Lab Assignment 1

TEAM MEMBERS: Shiva Ghose, @gshiva John Peterson, @jrpeters Wenjian Bai, @baiwenji

Question 1

Question 2

 \mathbf{a}

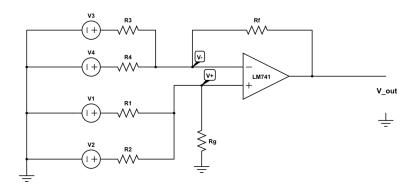


Figure 1: The required circuit diagram for question 2.

b

Circuit analysis:

At the non-inverting terminal, we effectively have a circuit represented by figure 2. We can use Kirchoff's voltage law along with the superposition theorem, we see:

Voltage at V^+ due to V_1 , V_1^+ , is given by:

$$V_1^+ = \frac{\frac{R_2 R_g}{R_2 + R_g}}{R_1 + \frac{R_2 R_g}{R_2 + R_g}} V_1$$

$$\therefore V_1^+ = \left(\frac{1}{\frac{R_1}{R_g} + \frac{R_1}{R_2} + 1}\right) V_1$$

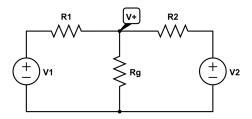


Figure 2: Equivalent circuit at the non-inverting terminal

Similarly, voltage at V^+ due to V_2 , V_2^+ , is given by:

$$V_2^+ = \frac{\frac{R_1 R_g}{R_1 + R_g}}{R_2 + \frac{R_1 R_g}{R_1 + R_g}} V_2$$

$$\therefore V_2^+ = \frac{1}{\frac{R_2}{R_n} + \frac{R_2}{R_1} + 1} V_2$$

Using the superposition theorem to recombine the values, we find that V+ is given by:

$$V^{+} = V_{1}^{+} + V_{2}^{+}$$

$$V^{+} = \frac{1}{\frac{R_{1}}{R_{g}} + \frac{R_{1}}{R_{2}} + 1} V_{1} + \frac{1}{\frac{R_{2}}{R_{g}} + \frac{R_{2}}{R_{1}} + 1} V_{2}$$

We can now move on to the inverting terminal of the op-amp. The corresponding equivalent circuit is shown in figure 3. Analyzing this circuit, we see that:

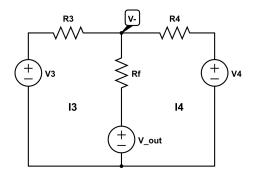


Figure 3: Equivalent circuit at the non-inverting terminal

$$I_3R_3 = V_3 - V^-$$

 $I_4R_4 = V_4 - V^-$
 $V^- - V_{out} = (I_3 + I_4)R_f$

Substituting from the above equations, we get:

$$V^{-} - V_{out} = \left(\frac{V_3 - V^{-}}{R_3} + \frac{V_4 - V^{-}}{R_4}\right) R_f$$

Reordering the terms, we get:

$$\begin{split} V_{out} &= V^{-} - \left(\frac{V_{3} - V^{-}}{R_{3}} + \frac{V_{4} - V^{-}}{R_{4}}\right) \, R_{f} \\ \Longrightarrow \, V_{out} &= V^{-} \left(\frac{R_{f}}{R_{3}} + \frac{R_{f}}{R_{4}} + 1\right) - \left(\frac{R_{f}}{R_{3}}\right) V_{3} - \left(\frac{R_{f}}{R_{4}}\right) V_{4} \end{split}$$

We also know that for an ideal op-amp, $V^+ = V^-$, hence we get:

$$V_{out} = \left(\frac{R_f}{R_3} + \frac{R_f}{R_4} + 1\right) \left(\frac{1}{\frac{R_1}{R_2} + \frac{R_1}{R_2} + 1}\right) V_1 + \left(\frac{R_f}{R_3} + \frac{R_f}{R_4} + 1\right) \left(\frac{1}{\frac{R_2}{R_2} + \frac{R_2}{R_1} + 1}\right) V_2 - \left(\frac{R_f}{R_3}\right) V_3 - \left(\frac{R_f}{R_4}\right) V_4$$

This is equation is the mathematical representation of the problem statement which which required $V_{out} = a_1V_1 + a_2V_2 - a_3V_3 - a_4V_4$, i.e. :

$$a_{1} = \left(\frac{R_{f}}{R_{3}} + \frac{R_{f}}{R_{4}} + 1\right) \left(\frac{1}{\frac{R_{1}}{R_{g}} + \frac{R_{1}}{R_{2}} + 1}\right)$$

$$a_{2} = \left(\frac{R_{f}}{R_{3}} + \frac{R_{f}}{R_{4}} + 1\right) \left(\frac{1}{\frac{R_{2}}{R_{g}} + \frac{R_{2}}{R_{1}} + 1}\right)$$

$$a_{3} = \left(\frac{R_{f}}{R_{3}}\right)$$

$$a_{4} = \left(\frac{R_{f}}{R_{4}}\right)$$

 \mathbf{c}

[DO WE HAVE ANY MORE??]

While building this circuit, we made the following assumptions:

- We are using an ideal op-amp, i.e. the input impedance is infinite and the output impedance is negligible. This implies that the op-amp does not load it's input circuit and loading effects are not seen on the op-amps output terminal.
- The voltage at the non-inverting terminal is equal to the voltage at the non-inverting terminal.
- The open loop op-amp gain is infinite.
- The op-amp will operate in an ideal manner when the output is not saturated above or below its supply limits.

\mathbf{d}

We used the following components in our circuits:

Component Name	Component Type	Component Specification
R_f	Resistor	$9.880~K\Omega$
R_g	Resistor	$9.860~K\Omega$
R_1	Resistor	$49.3~K\Omega$
R_2	Resistor	$24.65~K\Omega$
R_3	Resistor	$3.293~K\Omega$
R_4	Resistor	$2.470~K\Omega$

 \mathbf{e}

Physical implementation.