2. **Convexity:**

Hessian Matrix:

Eigen values of the Hessian matrix can be computed by:

Here the numerator of has two components: that is equal to , and that is slightly larger than . Therefore, the numerator is either positive or negative.

Therefore, the Hessian matrix has one positive eigen value and one negative eigen value. This means the is not Positive semi definite or PSD.

Therefore function  **is not convex**. This can also be verified by plotting this function. This plot is given by the following figure.

Chart, surface chart

Description automatically generated



For , the Hessian matrix is given by:

**Proof:**

Let , , and .

, can be simplified to the following:

(

Gradient of is :

Jacobian of is Hessian:

For any matrix , it is defined as positive semi definite, only if, for any real valued nonzero vector ,

Here, is the Euclidian norm of the vector . Euclidian norm is always greater than zero for any vector. Hence

is positive semi definite, which means the is convex.

4**. Logistic Sigmoid Identities:**