

MATRIX

What Is Matrix?

- Matrix is a rectangular grid with rows and columns.
- It is a two-dimensional grid
- No. of rows are denoted by 'n' and no. of columns are denoted by 'm'

Ex:

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix} \quad \text{order of matrix} \rightarrow 2 \times 3$$

In the above matrix, $A[0][2] = 3$

$$A[2][2] = 9$$

Properties of the Matrix:

$$\begin{bmatrix} 1 & 0 & 5 & 10 \\ 4 & 5 & 6 & 7 \\ 15 & 12 & 10 & 9 \\ 5 & 4 & 3 & 2 \end{bmatrix} \quad \begin{array}{l} \text{row} = [0 \dots n - 1] \\ \text{col} = [0 \dots n - 1] \\ \text{it is a } 4 \times 4 \text{ matrix.} \end{array}$$

All diagonal elements have the same rows and column. In the above example,

the diagonal elements are [1, 5, 10, 2].

Anti-diagonal elements are, [10, 6, 12, 5]

Diagonal Elements		
	rows	col
1	0	0
5	1	1
10	2	2
12	3	3

Anti-Diagonal		
	rows	col
10	0	3
6	1	2
12	2	1
5	3	0

The sum of rows and columns is always equal to n in this case 3.

- In a matrix, if no. of rows is equal to no. of columns, it is called a square matrix.
- If no. of rows is not equal to no. of columns, it is called rectangle matrix.

For a rectangular matrix,

$$\begin{bmatrix} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \\ 9 & 10 & 11 & 12 \end{bmatrix}$$

the diagonal elements are [1, 6, 11] and
the anti-diagonal elements are [4, 7, 10].

In the above matrix, the elements in the first column i.e., column '0' are [1, 4, 7]. In this, the value of row increases but the value of column is constant. In the same way, for the elements in the first row i.e., row '0' are [1, 2, 3] in which, the value of the row is constant, but the value of column increases.

Matrix Representation in Python

In a list, if you have another list,

```
[  
    [1, 2, 3],  
    [4, 5, 6],  
    [7, 8, 9]  
]  
A[0][1] → 2  
A[2][2] → 9  
A[1][2] → 6
```

the simplest form to get a matrix in one line would be,

```
[[0 for _ in range(m)] for _ in range(n)]  
[[0, 0, 0, 0], [0, 0, 0, 0], [0, 0, 0, 0], [0, 0, 0, 0]]
```

We can replace elements in the matrix as following:

```
>>> [[0 for _ in range(m)] for _ in range(n)]  
[[0, 0, 0, 0], [0, 0, 0, 0], [0, 0, 0, 0], [0, 0, 0, 0]]  
>>> A[0][0] = 5  
>>> A  
[[5, 0, 0, 0], [0, 0, 0, 0], [0, 0, 0, 0], [0, 0, 0, 0]]  
>>> A[0][3] = 15  
>>> A  
[[5, 0, 0, 15], [0, 0, 0, 0], [0, 0, 0, 0], [0, 0, 0, 0]]
```

To print elements from the matrix.

No. of rows = 3 = len(A).

No. of columns = 3 = len(A[0])

Q) print all elements of row 2.

INPUT	OUTPUT:
<pre>for i in range(m): print (A[x-1][i])</pre>	4 5 6

Q) print all elements in col 1.

INPUT	OUTPUT:
<pre>for i in range(n): print (A[i] [x-1])</pre>	2 5 8

```
for i in range(n):  
    for j in range(m):  
        print(A[i][j])
```

this prints all elements in the matrix.

INPUT:	OUTPUT:
<pre>for i in range(n): for j in range(m): print (A[i][j], end=" ") print ()</pre>	1 2 3 4 5 6 7 8 9

Q) to print diagonal elements.

INPUT:

```
row = 0
col = 0
while row < n and col < m:
    print(A[row][col])
    row += 1
    col += 1
```

OR

```
for i in range (min(m,n)):
    print(A[i][i])
```

OUTPUT:

1
5
9