

SORTING – 2

Given 2 sorted array A and B, we need to merge them and get sorted array C.

A = [1, 4, 6, 7, 8, 9]

B = [3, 5, 14, 18]

C = [1, 3, 4, 5, 6, 7, 8, 9, 14, 18]

CODE:

```
def Merge2SortedArray(A, B):  
    C = list()  
    for x in A:  
        C.append(x)  
  
    for x in B:  
        C.append(x)  
  
    C.sort() # Time Complexity: O(N logn)  
    return C  
  
"""  
Can we do this in O(N) time complexity, this means without using sort  
"""
```

We compare A & B to find the least number in the given two sorted arrays.

The first element from A is compared with the first element in B and the least value between a_1 and b_1 will be appended to the empty array C.

If a_1 is appended to C array, then in the next step, b_1 will be compared to a_2 and the lesser value is appended to the C array.

These steps are repeated again and again until all the values of A and B are added to the empty list C in ascending order.

This gives us a sorted array C. The code would be as follows:

CODE:

```
def Merge2SortedArray2(A, B):
    n = len(A)
    m = len(B)

    p1 = 0 # this is the pointer for A array
    p2 = 0 # this is the pointer for B array

    while p1 < n and p2 < m: # as long as p1 is in n and p2 is in m
        if A[p1] < B[p2]:
            C.append(A[p1])
            p1 += 1
        else:
            C.append(B[p2])
            p2 += 1

    while p1 < n: # one of the pointers might not be complete
        C.append(A[p1])
        p1 += 1

    while p2 < m:
        C.append(B[p2])
        p2 += 1

    return C

A = [1, 4, 6, 7, 8, 9]
B = [3, 5, 14, 18]

C = []
print(Merge2SortedArray2(A, B))
```

OUTPUT:

[1, 3, 4, 5, 6, 7, 8, 9, 14, 18]

Merge Sort

Merge sort is one of the most efficient sorting algorithms. It works on the principle of Divide and Conquer. Merge sort repeatedly breaks down a list into several sub-lists until each sub-list consists of a single element and merging those sub-lists in a manner that results into a sorted list. With worst-case time complexity being $O(n \log n)$, it is one of the most respected algorithms. Merge sort first divides the array into equal halves and then combines them in a sorted manner.

First Step: divide the array into two parts

Second Step: merge the parts.

For list = [2, 12, 3, 7, 5, 4];

[2, 12, 3, 7, 5, 4]

l = 0, r = 5, mid = 2

[2, 12, 3]

[7, 5, 4]

l = 0, r = 2, mid = 1

l = 3, r = 5, mid = 4

[2, 12]

[3]

[7, 5]

[4]

l = 0, r = 1, mid = 0

l = 3, r = 4, mid = 3

[2]

[12]

[3]

[7]

[5]

[4]

NOTE: every time it is divided, the from 0th index to the (mid) index is taken into the left part and (mid + 1) index to the last element into right part.

This is the first step of this algorithm. In the second part, we will merge all the elements into one array.

[2]

[12]

[3]

[7]

[5]

[4]

[2] & [12] are sorted array just as [7] & [5]

[2, 12]

[3]

[5, 7]

[4]

[2, 12] & [3] are sorted array just as [5, 7] & [4] so,

[2, 3, 12]

[4, 5, 7]

[2, 3, 12] & [4, 5, 7] are sorted array

[2, 3, 4, 5, 7, 12]

So, we can write it as,

```
def mergeSort (A, left, right):  
    if left >= right:  
        return  
    mid = (left + right // 2  
    mergeSort (A, left, mid)  
    mergeSort (A, mid + 1, right)  
    merge (A, left, mid, mid + 1, right)
```

CODE:

```
def merge(A, start1, end1, start2, end2):  
    # start1 is the starting index of the left Array  
    # end1 is the ending index of the left Array  
    # start2 is the starting index of the right Array  
    # end2 is the ending index of the right Array  
    p1 = start1  
    p2 = start2  
  
    temp = list()  
  
    while p1 <= end1 and p2 <= end2:  
        if A[p1] < A[p2]:  
            temp.append(A[p1])  
            p1 += 1  
        else:  
            temp.append(A[p2])  
            p2 += 1  
  
    while p1 < end1:  
        temp.append(A[p1])  
        p1 += 1  
  
    while p2 < end2:  
        temp.append(A[p2])  
        p2 += 1  
  
    idx = 0  
    while idx < len(temp):  
        A[start1 + idx] = temp[idx]  
        idx += 1
```

```

def mergeSort(A, left, right):
    if left >= right:
        return

    mid = (left + right) // 2
    mergeSort(A, left, mid)
    mergeSort(A, mid + 1, right)

    merge(A, left, mid, mid + 1, right)

if __name__ == "__main__":
    A = [5, 6, 2, 3, 66, 7, 1, 2, 2, 34, 5]
    print("Unsorted Array is ", A)
    mergeSort(A, 0, len(A) - 1)
    print("Sorted Array is ", A)

```

The time complexity of merge is $O(n)$ and $2 * T(N/2)$ as we have called mergeSort function twice. So, the Time Complexity for this equation would be **$O(n \log n)$**

Quick Sort is also an algorithm, whose time complexity is **$O(n \log n)$** .