

**Hospital Readmission Prediction Of ICU Patients Using
Deep Learning Algorithms**

by

Shivam Sinha

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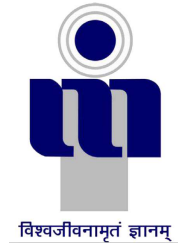
*A thesis submitted in partial fulfilment of the requirements for the
award of the degree of*

Master of Technology

in

Information Technology

2018-19



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I hereby certify that the work, which is being presented in the report/thesis, entitled Hospital Readmission Prediction Of ICU Patients Using Deep Learning Algorithms, in fulfillment of the requirement for the award of the degree of **Master of Technology** in **Information Technology** and submitted to the institution is an authentic record of my own work carried out during the period *May-2018* to *July-2019* under the supervision of Dr. Ritu Tiwari. I also cited the reference about the text(s)/figure(s)/table(s) from where they have been taken.

Dr. Ritu Tiwari

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Abstract

Deep learning healthcare applications have evolved over the last few years. This advancement leads to new applications and possibilities in the field of health care. Due to different variants of deep learning algorithms like convolutional and recurrent neural network these advancements in healthcare application made possible. Healthcare has shown promises, as there is a huge share of the budget in intensive care medicine. This has expanded the interests of healthcare researchers, and they are focusing on providing the best medication to critically-ill patients. DNN models are advanced machine learning models, which have been widely applied for clinical applications in recent times. Due to the lack of ability to capture time dependency in the data which is a major shortcoming, basic machine learning algorithms like Logistic Regression, SVM, Decision Tree, etc. are not very useful. There are several types of deep learning algorithm like Deep belief networks, Deep convolutional neural network, Recurrent neural network, etc. The LSTM variant of the Recurrent neural network have shown promises to work better on data involving time series prediction, and it can transfer the results of previous cell state onto the next cell state so that dependency on time is maintained throughout. In this thesis, the proposed methodology is to use LSTM, and its different variants like Gated Recurrent Unit (GRU), LSTM attention on healthcare applications like hospital readmission prediction using ICU data. The different architectures of LSTM will produce different results based on the data on which architecture is being trained. Then the comparison of performances can be done between LSTM, and its variants on various healthcare applications and provide the best model suitable for each of the different healthcare data being tested. The comparison of time independent machine learning models like Logistic Regression, SVM, Naive Bayes can be done with the results of Deep learning models.

Keywords: Deep learning, LSTM, Healthcare, Recurrent Neural Network, GRU.

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Chapter 1

Introduction

This chapter presents an overview of the context as a part of Hospital Readmission project and how machine learning used in health care applications in section 1.1 and 1.2, respectively. In section 1.3, 1.4, and 1.5, we discuss the algorithms used in this project. In section 1.6, the problems and motivations are presented. Next, in section 1.7, we discuss the objectives of this project.

1.1 Hospital Readmission

Hospital Readmissions are identified as a signal of the poor quality of care, such as insufficient discharge planning and care coordination. Hospital readmission[32] happens when a patient discharge from a hospital is readmitted within a specified interval. Readmission can occur for any planned or unplanned reason. These factors pushed Hospital organizations to think about controlling readmission rates; an increase in readmission rates leads to an increase in penalties. There has been an increased usage of Readmission rates as an outcome criterion in health services analysis and as a quality benchmark for health systems. For Medicare patients, hospitalizations are very stressful, and it is even more when they result in subsequent readmissions. A lot of research studies proved that hospitals could engage in several activities like clarifying patient discharge instructions, coordinating with post-acute care providers, vibrant cleaning mechanism to reduce the rate of readmissions of patients. But these individual follow-ups can be costly.

1.2 Machine Learning For Health Care

Machine learning leads to provide intelligence by providing new knowledge. Since the onset of machine learning, it has been widely used in achieving paramount goals as the healthcare sector is evolving. The healthcare sector is producing an enormous mass of data, and it is beyond human capability to manually analyze this vast data and produce inferences based on that. Machine learning has proven to be a benefit at this level. The machine learning algorithms automatically find patterns in the data, which enable to get inferences from the data easily. Machine learning can assist healthcare providers in a variety of tasks like hospital readmission of patients suffering from chronic illness. This can not only lower the lifetime risk of the patient but also can save millions of dollars if the algorithm can predict efficiently and correctly. Other applications of machine learning in the healthcare domain includes drugs combination which should be avoided taking together, classifying images for different diseases like skin cancer. Keeping this in the picture, it can be said that machine learning can revolutionize the healthcare sector.

1.3 Deep Learning

Deep learning is one of the extended branches of Machine learning, which works on a specific machine learning algorithm, that is the artificial neural network. It's leveraging the recent advancements in computing power and thus using specific purpose neural network to learn from a plethora of data and make predictions based on the patterns detected. The structure consists of several hidden layers which are meant to extract the information by exploiting the structures present in the data. Deep neural networks are specialized in solving problems, including data, which is greatly structured. It also promises to replace hand-engineered features with feature extraction techniques that are hierarchical, unsupervised, or semi-supervised. Multiple hidden units are being used between input and output in case of Deep Neural Network (DNN). Similar to the artificial neural network, the complex non-linear relationships can be modeled using DNN[2]. Similar to the artificial neural network, the complex non-linear relationships can be modeled using DNN.

1.4 Recurrent Neural Network

An artificial neural network has a particular type called recurrent neural network (RNN), and it has directed cycles between connection. The internal state of the network exhibits dynamic temporal behavior. Unlike ANN, arbitrary sequences can be processed by using the internal state of RNN. This is the fundamental architecture developed in the 1980s: neuron-like units in a network, a directed connection between every neuron. There is a time-varying real-valued activation in every unit. There is modifiable real-valued weight in each connection. There are input, output, and hidden nodes. One input vector is supplied at every time steps. At every time step, the non-linear function of the weighted sum of all the activations of connected units is calculated by each non-input unit[25].

1.5 Long Short Term Memory

The Long short-term memory (LSTM) network, a deep learning RNN, is used by numerous researchers, published by Schmidhuber & Hochreiter in 1997[19]. This deep learning system overcomes the vanishing gradient problem of traditional RNN. The recurrent gates called forget gates are augmented in LSTM. The vanishing or exploding of backpropagated error is prevented in LSTM RNNs. There are an unlimited number of virtual layers in LSTM RNNs, through which the error can flow backward. LSTM can learn from events that occurred thousands of time steps ago so it can be used for very deep learning tasks. LSTM has a unique architecture that consists of a memory cell, which can maintain the state which it is currently in, over time. Non-Linear gating units are used in LSTM to regulate the information flow in and out of the memory cell. Over time, many improvements have been suggested and made in the standard architecture of LSTM to make it more efficient. Today, LSTMs are being used in a variety of learning problems which differ in scale and nature significantly when compared to the problems which were initially solved by LSTM.

1.6 Motivation

- For Medicare patients, hospitalizations can be distressing, even more so when they occur in subsequent readmissions. A number of researches show that hospitals can involve in several activities to lower their degree of readmissions, such as clarifying patient discharge instructions, coordinating with post-acute care providers etc.
- The purpose of this thesis is to use deep neural networks which can work effectively to predict the result that can be utilized to avoid unnecessary hospital readmissions.

1.7 Objectives

The primary objective of this thesis is:

- To develop a Deep Neural Network(DNN) models for Healthcare application, i.e., Hospital Readmission.
- To predict hospital readmission of patients using trained deep neural network models.
- To compare results between Deep Learning Models and with existing algorithms.

1.8 Research work flow

This section focuses on how the research is being carried out, how the different algorithms, models and data preprocessing are implemented.

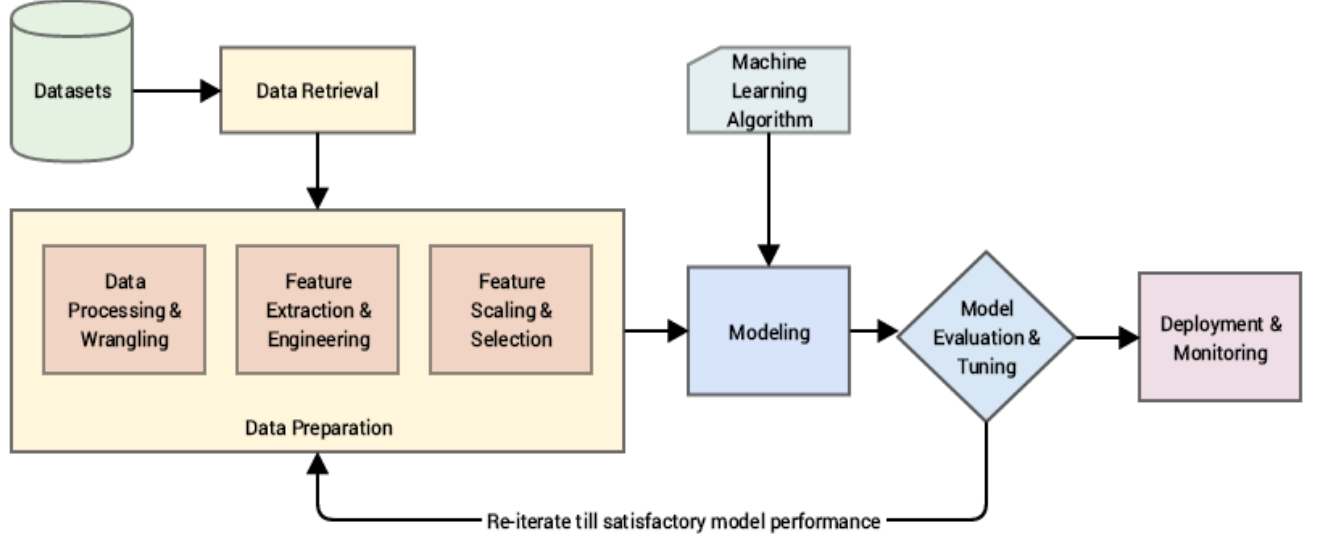


Figure 1.1: Flowchart of proposed methodology

According to the research objectives, the report will describe the work flow as below:

Step 1: Collect a vast readmission dataset with several features.

Step 2: Do data-preprocessing to deal with missing values.

Step 3: Convolution layers can be used for feature extraction, i.e., to retrieve the meaningful data out of the dataset.

Step 4: Do Feature scaling to normalize the dataset to reduce biases.

Step 5: Feature selection can also be done using nature-inspired algorithms to fetch important features from the dataset.

Step 6: Feeding the retrieved dataset into the model.

Step 7: Calculate the Accuracy, FScore, AUC, etc. based on the actual and predicted output.

Step 8: If the results are satisfied, then stop otherwise go to step 2 and repeat the process with different hyperparameters, algorithms, etc.

Chapter 2

Literature review

2.1 Background

A procedure of the current work was performed with a specific end goal to study the most significant healthcare applications literature for the survey and also to study an expansive piece of the most profound learning approaches for healthcare applications.

2.2 Related Research and Analysis

Author (Year)	Meta-heuristic	Paper Name	Comments
Ghassemi et. al (2014) [14]	Multivariate Logistic Regression	A data-driven method to optimized medication dosing: a focus on heparin	An approach is developed that help clinicians determine the optimal initial dose of a drug to safely and quickly reach a therapeutic aPTT window.

Author (Year)	Meta-heuristic	Paper Name	Comments
Pirrachio et al. (2015) [28]	Super ICU Learner Algorithm	Mortality prediction in intensive care units with the Super ICU Learner Algorithm (SIC-ULA): a population-based study.	A super learner algorithm is used for predicting hospital mortality in patients.
Che et al. (2015) [7]	Stacked Denoising Autoencoder & Long Short-Term Memory	Distilling knowledge from deep networks with applications to healthcare domain	A novel called Interpretable Mimic Learning is used, to study interpretable phenotype characteristics for making robust prediction while impersonating the performance of deep learning models meta-heuristics.
Lian and Hu (2015) [24]	Convolution & Recurrent Neural Network	Recurrent convolutional neural network for object recognition	Combination of convolution and recurrent neural network model is used for object detection.
Ioffe and Szegedy (2015) [20]	Batch Normalization	Batch normalization: Accelerating deep network training by reducing internal covariate shift	Reduction in overfitting using batch normalization.

Author (Year)	Meta-heuristic	Paper Name	Comments
Che et. al (2016) [6]	Knowledge Distillation Approach	Interpretable deep models for icu outcome prediction	Interpretable mimic learning is introduced that uses gradient boosting trees to determine interpretable models and at the same time achieves robust prediction performance as deep learning models.
Choi, Bahadori, Schuetz, Stewart and Sun (2016) [9]	Recurrent Neural Networks	Doctor ai: Predicting clinical events via recurrent neural networks	The proportional split of data is found useful for deep learning applications when dealing with the large volume of data.
Choi, Bahadori, Schuetz, Stewart and Sun (2016) [10]	Gated Recurrent Units	Using recurrent neural network models for early detection of heart failure onset	Leveraging longitudinal EHR records for early detection of heart failure using Recurrent Neural Network.
Hanson et al. (2016) [18]	Bidirectional LSTM	Improving protein disorder prediction by deep bidirectional long short-term memory recurrent neural networks	Long short term memory RNN is used to predict disordered proteins, such as SPOT-disorder.

Author (Year)	Meta-heuristic	Paper Name	Comments
Jhonson et al. (2016) [23]	Dataset Extraction	MIMIC-III, a freely accessible critical care database	Medical Information Mart for Intensive Care (MIMIC-III) consists of data about patients admitted to various critical care units in a large hospital.
Che et al. (2017) [8]	Recurrent Neural Networks	Deep Learning Solutions for Classifying Patients on Opioid Use	State-of-the-art deep and recurrent neural network models were applied to achieve robust results on classifying opioid users.
Dey and Salemt (2017) [11]	Gated Recurrent Unit	Gate-variants of Gated Recurrent Unit (GRU) neural networks	Unlock the vanishing gradient problem of a standard RNN.
Greff et al. [17]	LSTM	LSTM: A search space odyssey	Overcomes the vanishing gradient problem of conventional RNN
Rubin et al. (2017) [30]	Convolution Recurrent neural Network	Recognizing abnormal heart sounds using deep learning	Merges the use of time-frequency heat map representations with a deep convolutional neural network (CNN) to classify heart sounds.

Author (Year)	Meta- heuristic	Paper Name	Comments
Franco et al. (2017) [13]	Statistical Algorithms	Impact of prealbumin on mortality and hospital readmission in patients with acute heart failure	Statistical Analysis is used to find the mortality and readmission rates.
Esteva et al. (2017) [12]	Convolution Neural Network	Dermatologist-level classification of skin cancer with deep neural networks	Training of Skin lesions using a single CNN is done on an end-to-end basis from images directly, using only two inputs- pixels and diseases.
Biswal et al. (2017) [3]	SLEEPNET	SLEEPNET: automated sleep staging system via deep learning	Offer SLEEPNET (Sleep EEG neural network), a deployed annotation tool for sleep staging.
Che et al. (2018) [5]	Gated Recurrent Unit	Recurrent neural networks for multivariate time series with missing values	Uses GRU-D to capture long-term temporal dependencies in time series and utilizes the missing patterns to achieve better prediction results.
Reddy and Delen (2018) [29]	LSTM	Predicting hospital readmission for lupus patients: An RNN-LSTM-based deep-learning methodology	Uses deep learning methods to predict rehospitalization within 30 days by extracting the temporal relationships in the longitudinal EHR clinical data.

Author (Year)	Meta-heuristic	Paper Name	Comments
Xiong et al. (2018) [33]	Convolution Recurrent Neural Network	ECG signal classification for the detection of cardiac arrhythmias using a convolutional recurrent neural network	Developed RhythmNet, a 21-layer 1D convolutional recurrent neural network to classify ECGs of different rhythms including AF automatically.
Biswas et al. (2018) [4]	Convolution based encoder & decoder	Deep learning strategy for accurate carotid intima-media thickness measurement: An ultrasound study on Japanese diabetic cohort	The Deep Learning system can be used for stroke risk assessment during routine or clinical trial modes.
Acharya et al. (2018) [1]	Convolution Neural Network	Deep convolutional neural network for the automated detection and diagnosis of seizure using EEG signals	A Novel method for UCAV path planning in a 2D environment. A 13-layer deep learning CNN algorithm is implemented for the automated EEG analysis.

2.3 Research gaps

In the literature survey, we find the following research gaps. These are points that we will be focused on in this thesis.

- The results obtained in these techniques can be improved using novel classification algorithms. Most of the researchers have used existing machine learning algorithms, and it is expected that deep learning techniques will surpass conventional methods.

- These earlier works were not able to model high dimensional nonlinear relations as good as RNN.
- Descriptive statistics were being used in earlier methods. However, these statistics like mean, median & mode are always under the risk of losing some vital information.
- Deep learning algorithms are still under a shadow for a variety of healthcare applications.

2.4 Novelty

- With this thesis, the aim is to use deep learning algorithms to overcome the drawbacks of conventional machine learning algorithms.
- The thesis aims to use nature-inspired algorithms for feature extraction.
- The thesis also aims to use the hybrid model (Convolution Recurrent Neural Network), which can further increase the accuracy of the proposed model.

2.5 Conclusion

Hospital Readmissions is a very stressful thing for both patients and hospitals. In our research, we built a powerful model to predict the number of patients readmitted to a hospital. We compared different deep learning models with and without Nature-inspired algorithms to predict readmission probability and concluded that Long Short Term Memory with grey wolf optimizer outperformed the rest of the machine learning models in the prediction quality. We also found that the performance of the combination of LSTM and Convolution layer was remarkable on this data. This framework can be implemented in today's health system to target high risks patients, reduce the rate of readmission, and deliver better health care.

Chapter 3

Methodology

This section introduces the dataset description and the analytical validation of the proposed solution.

3.1 Data description: MIMIC-III

Medical Information Mart for Intensive Care (MIMIC-III)[23] consists of data about patients admitted to various critical care units in a large hospital. MIMIC-III is generally viewed as a large and single-center database. A large number of different parameters are present in MIMIC III database. These parameters include information such as vital signs, medications, laboratory measurements, observations, fluid balance, procedure codes, diagnostic codes, imaging reports, hospital length of stay, survival data, and others. The database consists of information of around 58,576 distinct patients who were admitted to various critical care units of the hospital between 2001 and 2012. The data comprises of patients aged 16 years or above only. Descriptive statistics were performed on this dataset, and it was found that the median age is 65.8 years for adult patients(Q1-Q3: 52:877:8). Out of total patients, there were 55.9% male patients, and only 11.5% of the cases had in-hospital mortality. It was calculated from the data that on an average a patient stayed for 2.1 days in ICU and had an average of 6.9 Days of hospital stay. MIMIC-III database have several idiosyncratic properties about it, and these are mentioned below:

- The dataset is a vast database accumulated throughout more than a decade and consists of very detailed information of each patient under care.

- MIMIC-III database requires a user to oblige by a user data agreement and once it is accepted the analysis is boundless.
- It contains discharge summaries as well as reports of ECG, imaging studies and information about various codes like International Classification of Disease, 9th Edition (ICD-9) codes, Diagnosis Related Group (DRG) codes, and Current Procedural Terminology (CPT) codes.
- It is a time series of data. Clinical variables are recorded concerning time for each patient.

Figure 1 shows the chart of timing clinical variables recorded in the dataset.

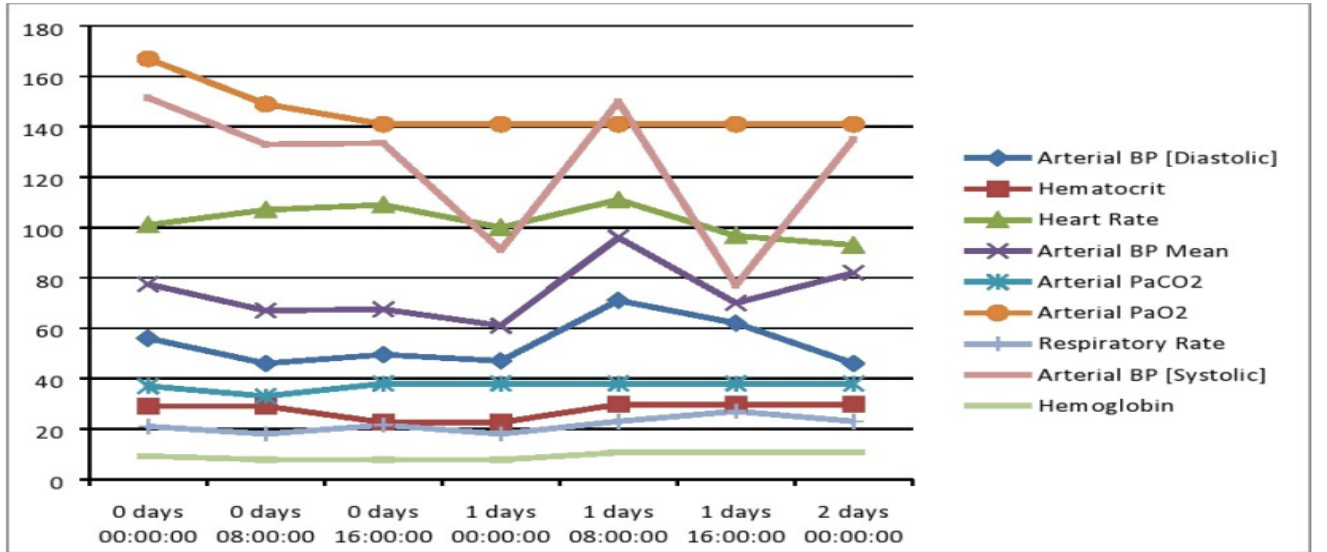


Figure 3.1: Some of the Clinical recordings associated with each patient[23]

3.2 Mechanism/Algorithm

3.2.1 Dataset Preprocessing

3.2.1.1 Data Extraction

MIMIC-III dataset consisted of around 58,576 patients who were diagnosed as suffering from different types of disease and hence mortality due to those diseases. These diseases include Pulmonary disease, Circulatory disease, Trauma, a disease of the digestive system, and many more.

Since the dataset is very large, we only consider data of those patients who were readmitted again, which gives the details of 7,534 patients. The data set is divided into two classes:-

- Patients readmitted in 30 days.
- Patients readmitted after 30 days.

3.2.1.2 Missing Values

MIMIC-III dataset contains missing values in some of the features. The feature will be removed if it contains more missing value otherwise mean will be used to fill the missing values.

3.2.1.3 Normalization

Normalization is used to remove the biases among the features. It brings the data on a standard scale. It standardizes the range of independent features or variables of data, called feature scaling. We use min-max[21] normalization here.

- Min-Max Normalization Let a matrix "A":-

$$A = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix} \quad (3.1)$$

So for L2 normalization we calculate

$$a = \min(a_{11}, a_{21}), \quad (3.2)$$

$$b = \max(a_{11}, a_{12}) \quad (3.3)$$

$$c = \min(a_{12}, a_{22}), \quad (3.4)$$

$$d = \max(a_{21}, a_{22}) \quad (3.5)$$

And "A" becomes:-

$$A = \begin{bmatrix} (a_{11} - a)/(b - a) & (a_{12} - c)/(d - c) \\ (a_{21} - a)/(b - a) & (a_{22} - c)/(d - c) \end{bmatrix} \quad (3.6)$$

3.2.2 Feature Selection

Features are selected through Nature Inspired Algorithms:

3.2.2.1 Bat Algorithm

Bat Algorithm is an optimization algorithm inspired by the echolocation behavior of microbats[34]. Bats uses echolocation to sense distance, and they also distinguish between food/prey and other background barriers. Bats fly randomly with velocity v_i at location x_i with a fixed frequency f_{min} , varying wavelength and loudness A_0 to search for the victim. They can automatically regulate the wavelength (or frequency) of their emitted pulses and adjust the rate of pulse emission r in the scale of $[0, 1]$, depending on the closeness of their target. Although the loudness can diversify in many ways, we assume that the loudness varies from a high (positive) A_0 to a minimum constant value A_{min} . Rules to update position x_i and velocity v_i of bats at time step t is given by:

$$f_i = f_{min} + (f_{max} - f_{min})\beta \quad (3.7)$$

$$v_i^t = v_i^{t-1} + (x_i^{t-1} - x_b)f_i \quad (3.8)$$

$$x_i^t = x_i^{t-1} + v_i^t \quad (3.9)$$

where $\beta \in [0,1]$ is a random vector drawn from a uniform distribution and x_b is the current global best solution which is found after comparing all the solutions among all the n bats. For the local search part once a solution is selected among the current best solutions, a new solution for each bat is generated locally using a local random walk:

$$x_{new} = x_{old} + \epsilon A^t \quad (3.10)$$

where $\epsilon \in [-1,1]$ is a random number. A^t is the average loudness of all the bats at that time step.

Variation of Loudness and Pulse Emission:

$$A_i^{t+1} = \alpha A_i^t \quad (3.11)$$

$$r_i^{t+1} = r_i^0 [1 - \exp(-\gamma t)] \quad (3.12)$$

where α & γ are constant.

3.2.2.2 Grey Wolf Optimizer

Grey Wolf Optimizer (GWO) Algorithm inspired by grey wolves[27]. The GWO algorithm mimics the leadership hierarchy and hunting mechanism of grey wolves in nature. Four types of grey wolves are employed for simulating the leadership hierarchy such as alpha, beta, delta, and omega. Also, the three main steps of hunting, searching for prey, encircling prey, and attacking victim, are implemented.

Alpha wolf is a leader male or female. They make decisions like the sleeping place, hunting, etc. Other wolves acknowledge alpha wolf by their tail down. Beta wolf help alpha wolf in making decisions. They are an advisor for alpha and discipliner for the pack. They also ensure all subordinate obey the order of alpha and give feedback to alpha. Delta wolves also called subordinate. They dominate omega wolves.

Categories of Delta wolves:-

- Scouts - Watch boundaries.
- Sentinels - Protect pack.
- Elders - Alpha or beta wolf sometimes.
- Hunters - Help alpha and beta wolf in hunting.
- Care Taker - Care ill weak and wounded wolves.

Omega wolves are like the scapegoat in the pack. They are last allowed wolves to eat having weak fitness.

Search Process in GWO Algorithm:-

- Searching
- Encircling
- Attacking the prey

Searching

- Search according to alpha, beta and delta wolves. They diverge to search for prey and converge to attack prey.
- Modeled by utilizing A random variable greater than 1 or less than -1.
- When $|A| > 1$ wolves are forced to diverge from prey to find better solution.

Encircling Prey It is the process in which wolves encircle the prey for attack. It is modeled as:

$$\vec{D} = |\vec{C} \vec{X}_p(t) - \vec{X}(t)| \quad (3.13)$$

$$\vec{X}(t+1) = \vec{X}_p(t) - \vec{A} \vec{D} \quad (3.14)$$

Where t is the current iteration, \vec{A} , \vec{C} are coefficient vectors and \vec{X}_p is position of prey and \vec{X} is the position of grey wolf.

Updation of Coefficients

$$\vec{A} = 2 \vec{a} \vec{r1} - \vec{a} \quad (3.15)$$

$$\vec{C} = 2 \vec{r2} \quad (3.16)$$

Where \vec{a} linearly decrease from 2 to 0 over the course of iteration. $\vec{r1}$ and $\vec{r2}$ are random vectors $\in [0,1]$. **Attacking** The hunt is usually guided by alpha. The beta and delta might also participate in hunting. We first save three best solutions i.e. alpha beta and delta which are the best solutions and update positions of other agents based on these three. It is modeled as:

$$\vec{D}_\alpha = |\vec{C}_1 \vec{X}_\alpha - \vec{X}| \quad (3.17)$$

$$\vec{D}_\beta = |\vec{C}_2 \vec{X}_\beta - \vec{X}| \quad (3.18)$$

$$\vec{D}_\delta = |\vec{C}_3 \vec{X}_\delta - \vec{X}| \quad (3.19)$$

$$\vec{X}_1 = \vec{X}_\alpha - \vec{A}_1 \vec{D}_\alpha \quad (3.20)$$

$$\vec{X}_2 = \vec{X}_\beta - \vec{A}_2 \vec{D}_\beta \quad (3.21)$$

$$\vec{X}_3 = \vec{X}_\delta - \vec{A}_3 \vec{D}_\delta \quad (3.22)$$

$$\vec{X}(t+1) = (\vec{X}_1 + \vec{X}_2 + \vec{X}_3)/3 \quad (3.23)$$

Grey wolf attack prey when it stops moving. In GWO vector A is a random value within an interval $[-2a, 2a]$ a decrease from 2 to 0 throughout the iteration. When $|A| < 1$ wolves attack prey.

3.2.3 Feature Extraction

For feature extraction Convolution Neural Network(CNN) is used.

3.2.3.1 Convolutional Neural Network

A convolutional neural network is an effective machine learning technique from deep learning, and it is similar to ordinary Neural Networks. A convolutional neural network is a network with convolutional layers. A convolutional neural network is consists of three steps of neural layers to build its architectures: Convolutional, Pooling, and Fully-Connected.

Convolutional layers: The convolutional layer is the main part of the convolutional neural network. In the convolutional layer the output result is derived from the input by filtering in certain conditions. Convolutional layers consist of a rectangular grid or cubic block of neurons. It means input, output layers with filters can be a rectangular grid or cubic block of neurons.

The filter is supplied from uppermost left to downside right. In every location of the filter, the weighted volume of the pixels is determined by the equation

$$WT^X + b \quad (3.24)$$

and a new neuron is acquired. In the convolutional layer three kind of hyper parameters determine the volume of the output neurons: depth, stride, and zero-padding. A number of the filters with certain strides determines the depth For original RGB image depth equal to three.

Here, whereas the stride equal to 1, the filters runs a single pixel. In this case output neuron is 5x5xd. Whereas the stride equal to 2, the filters are skipped two pixels and output neuron size is 3x3xd. In the last case, when stride is 3 the filters are skipped 3 pixels. Output neuron size is 2x2xd.

Zero padding is the filling process in the input neuron where it zeros are around the edge. Zero-padding is mostly consumed for adjustment the size of the input neuron for research purposes. It is normally applied for when the input neuron size needs to maintain in the output neuron. The output neuron size is calculated by equation

$$Output = (W - K + 2P)/S + 1 \quad (3.25)$$

where W is the input neurons size, K is the filter (kernel) size, P is size of the padding, and S is the stride. In the convolutional neural network linear algebraic operations are also used. Suppose that matrix dimensions are m and n (m rows, n columns). 2D convolution cube calculates the two-dimensional convolution with two input matrices. (MA, NA) is dimensions of the matrix A, and (MB, NB) is dimensions for the matrix B. In case, the cube determines the complete output size, convolution equation is as below

$$C(i, j) = \sum_{m=0}^{M_A-1} \sum_{n=0}^{N_A-1} A(m, n) * B(i - m, j - n) \quad (3.26)$$

Max-pooling layer: After each convolutional layer, a pooling layer executes the next operation. The pooling layers are utilized to decrease the size of the input neuron. This layer acquires small rectangular blocks from the convolutional layer and samples it to provide a single output from that block. The max pooling method is commonly used. A formulation for a single type of the pooling layer, max-pooling is presented in equation

$$h_l^j(x, y) = \max_{x \in \mathcal{N}(x), y \in \mathcal{N}(y)} h_j^{l-1}(\bar{x}, \bar{y}) \quad (3.27)$$

Fully Connected layers: A fully connected layer is the last layer, which is constructed from the connection of all previous neurons. The fully connected layer normally promotes the reduction of spatial information because it fully connected: from all input neurons until all output neurons.

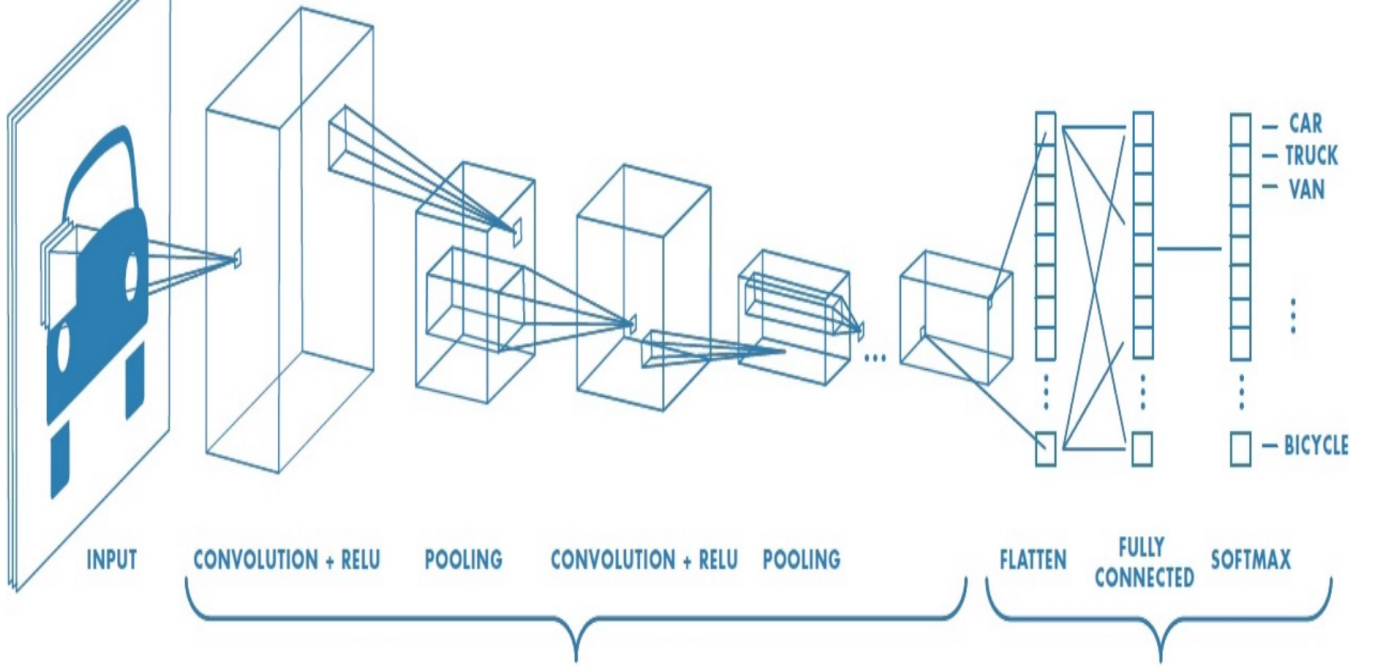


Figure 3.2: Convolution Neural Network Architecture

3.2.4 Algorithms

3.2.4.1 Recurrent Neural Network

Recurrent neural networks (RNN) are used to capture the temporal dependency in the time series data[5]. As most of the healthcare data is a series of temporal recordings, hence RNNs have been widely adopted in the healthcare domain. We are usually provided with a series of observations $x_1 \dots x_T$ and we train a classifier to generate hypotheses \hat{y} . The recurrent connections are added in feed-forward neural networks to make it RNN. The output of a neuron in a typical NN is as follows:

$$y_i^t = \sigma(W_i x^t + b_i) \quad (3.28)$$

Where W_i is the weight matrix, b_i is the bias and represents the sigmoid function. While in the case of RNN, a neuron is fed with the output of the neuron at time $t-1$. The following equation shows the new activation function:

$$y_i^t = (W_i x^t + V_i x^{t-1} + b_i) \quad (3.29)$$

As RNN uses the previous outputs as recurrent connection, their current output depends upon the previous states. This property of RNN makes it very useful in sequence labeling tasks. The backpropagation through time can be used to train RNNs. It was demonstrated by that learning long-term dependencies is difficult using gradient descent. This is mainly because the backpropagating error can vanish which makes the network inefficient in learning long-range dependencies, or frequently explode which makes convergence impossible.

LSTM networks were proposed to tackle the problem of vanishing gradients and were developed to model long-range dependencies efficiently. LSTMs can accomplish this by keeping an internal state that represents the memory cell of the LSTM neuron. This internal state can only be written and read through gates which control the information flowing through the cell state. The following diagram shows the recurrent neural network.

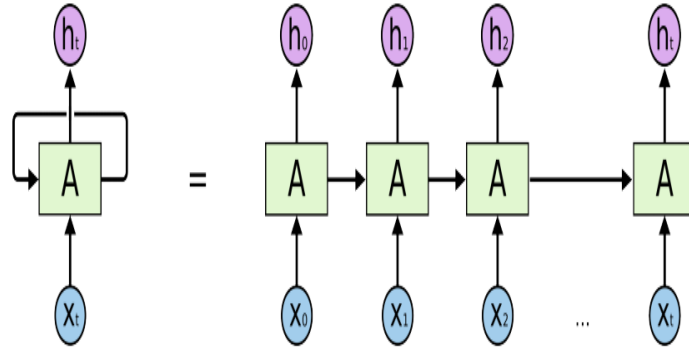


Figure 3.3: An unrolled recurrent neural network[17]

3.2.4.2 Long Short Term Memory (LSTM) Networks

Long Short Term Memory networks usually just called LSTMs are a special kind of RNN, capable of learning long-term dependencies. They were introduced by [19] and were refined and popularized by many people. They work remarkably well on a large variety of problems and are now widely used. To solve long-term dependency problem, LSTMs are explicitly designed. Remembering information for long periods of time is practically their default behavior, not something they struggle to learn! All recurrent neural networks have the form of a chain of repeating modules of the neural network. In traditional RNNs, this repeating module will have a pretty simple structure, such as a single tank layer. LSTMs also have this chain-like structure, but the recurrent module has a different structure. Rather than having a single neural network layer, there are four layers which are interacting extraordinarily. The intermediate information is stored in a single hidden layer h and its state changes over time (h_{t-1}, h_t, h_{t+1}) . On the final hidden state vector h_T , we used a fully connected layer followed by sigmoid function. For loss function, we used log loss. The following equations can be used for calculation of the current hidden layer h_t .

$$f_t = \sigma(W_f X_t + R_f h_{t-1} + b_f) \quad (3.30)$$

$$i_t = \sigma(W_i X_t + R_i h_{t-1} + b_i) \quad (3.31)$$

$$o_t = \sigma(W_o X_t + R_o h_{t-1} + b_o) \quad (3.32)$$

$$\tilde{C}_t = \Phi(W_C X_t + R_C h_{t-1} + b_c) \quad (3.33)$$

$$C_t = f_t C_{t-1} + i_t \tilde{C}_t \quad (3.34)$$

$$h_t = o_t \phi(C_t) \quad (3.35)$$

f_t , i_t and o_t are forget gate, input gate and output gate respectively. To decide which historical information will be discarded from the cell state forget gates are used, the update of cell state is decided by the input gate, and the output gate decides the output of the cell state. Cell states are completely overridden in classical RNN, but LSTM has the potential to add or remove information to the cell state. The input weight of each gate, recurrent weight, and the bias are expressed as W^* , R^* , b^* respectively where $*$ can be f, i, o and c. Here σ , Φ stands for an element-wise application of the sigmoid (logistic) and tanh function respectively. For matrix multiplication. The candidate values are computed in equation (6), and equation(7) old state is multiplied by f_t , and this helps in forgetting the things we decided to forget. Then $i_t * \delta C_t$ is added in it. This is the new candidate values, scaled by how much we decided to update each state value. The final output of an LSTM unit is given by equation 8. Here $*$ represents the Hadamard (element-wise) multiplication operation. Figure 3 shows the LSTM network.

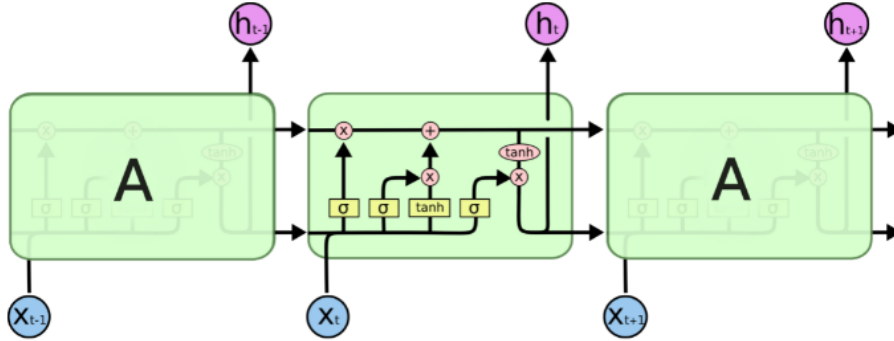


Figure 3.4: The repeating module in an LSTM contains four interacting layers[17]

3.2.4.3 Bidirectional Recurrent Neural Networks (BRNN)

Bidirectional Recurrent Neural Networks also called BRNN is just like RNN but it trains simultaneously on both sides of the time series data[31]. This model gives the better result in both regression and classification problem. BRNN computes both forward (\vec{h}) and backward (\overleftarrow{h}) hidden sequence.

$$\vec{h}_t = \mathcal{H}(W_{x\vec{h}}x_t + W_{\vec{h}\vec{h}}\vec{h}_{t-1} + b_{\vec{h}}) \quad (3.36)$$

$$\overleftarrow{h}_t = \mathcal{H}(W_{x\overleftarrow{h}}x_t + W_{\overleftarrow{h}\overleftarrow{h}}\overleftarrow{h}_{t+1} + b_{\overleftarrow{h}}) \quad (3.37)$$

$$y_t = W_{\overrightarrow{h}y}\overrightarrow{h}_t + W_{\overleftarrow{h}y}\overleftarrow{h}_t + b_o \quad (3.38)$$

The long range context can be accessed in both directions by combining BRNNs with LSTM which gives bidirectional LSTM[16].

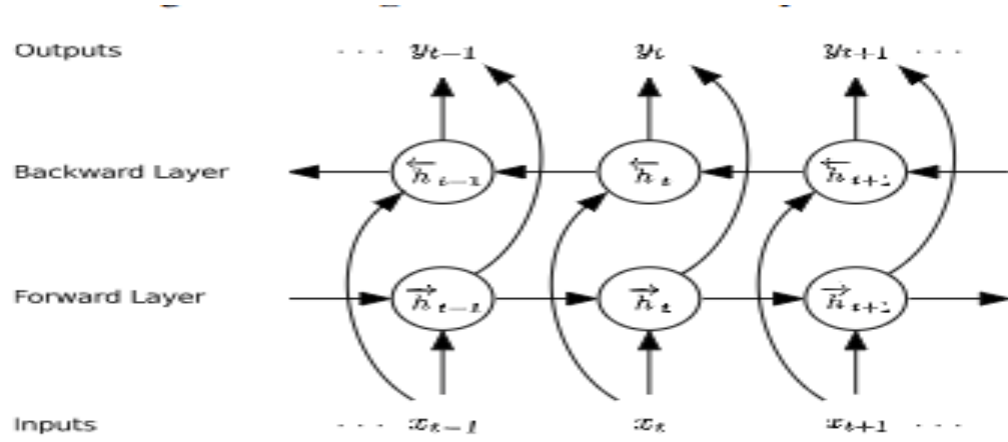


Figure 3.5: Bidirectional Recurrent Neural Networks[15]

3.2.4.4 Auto Encoders

An auto-encoder[26] is a neural network model that seeks to learn a compressed representation of the input. They are an unsupervised learning algorithm, although technically, they are trained using supervised learning algorithms, mentioned as self-supervised. They are commonly trained as part of a deeper model that attempts to recreate the input. The design of the auto-encoder model purposefully makes this challenging by limiting the architecture to a bottleneck at the center of the model, from which the reconstruction of the input data is performed. In this case, once the algorithm is fit, the regeneration aspect of the model can be dropped, and the model up to the point of the bottleneck can be adopted. The result of the model at the congestion is a fixed length vector that produces a compressed representation of the input data. Input data from the region can then be supplied to the model, and the result of the model at the congestion can be used as a feature vector in a supervised learning model, for visualization, or more generally for dimensionality reduction.

3.3 Conclusion

The methodology and the algorithms used to compute, generate, test, and verify the process produces good results.

Chapter 4

Experiments and results

This section discusses the implementation details and the results obtained using various algorithms.

4.1 Implementation Details

The entire dataset was split using stratified sampling and 10% of the dataset was used as a validation set and random search was used for hyperparameter optimization. The rest 80% of the dataset was used for training purpose and was tested on 10% of the dataset. The LSTM model was trained with 30 epochs using Adam optimizer. LSTM layer uses 100 memory cell with no dropout and 25 memory cell with 20% dropout and these architectures are found after validation performance. Also train this model with Bat Algorithm.

Another model train on this dataset was convolution long short term memory (CLSTM). It is a hybrid model in which convolution layers are used for feature extraction. The CLSTM model was trained with 30 epochs and the batch size of 1000. First, the convolution layer was used with 45 filters of size 5×5 . Then the LSTM layer that uses 100 memory cell with 20% dropout. Also train this model with Grey Wolf Optimizer Algorithm.

In the training phase, the model was saved and also compute these performance metrics (AUC, F1, precision, and recall).

Several built-in modules of python will be utilized, namely:

- Numpy

- Pandas
- Scikit-Learn
- Keras
- Matplotlib
- NiaPy

The computations were performed on Ubuntu 16.04 LTS with following hardware specifications:

- **Processor** Intel i7 6th Gen. broadwalle processor.
- **RAM** 24 GB DDR4
- **Secondary Memory** 250 GB SSD
- **Graphics Card** Nvidia 1080Ti 11GB

4.2 Results Obtained

This section presents the readmission prediction results obtained from different predictive models. The prediction accuracy will be compared in terms of two factors AUC under ROC (Receiver Operating Characteristic) Curve[22], and overall accuracy. Both area under ROC curve and overall accuracy depends on the classifiers ability to rank patterns for positive class, but in the case of overall accuracy, it also depends on the ability to calculate the threshold in the ranking to classify the positive class. Applying different algorithms on the dataset, with default parameters, we obtained results we obtained results as mentioned in Table 1.

Algorithm type	Algorithm	AUC	Accuracy	F1 Score Micro	F1 Score Macro
Deep Learning without Nature Inspired Algorithms	Long Short Term Memory	0.88	81.71%	0.80	0.76
	Long Short Term Memory Auto-Encoders	0.73	75.00%	0.70	0.62
	Convolution Long Short Term Memory	0.89	85.63%	0.71	0.66
	Convolution Long Short Term Memory Auto-Encoders	0.87	82.41%	0.80	0.78
	Bi-Directional Long Short Term Memory Auto-Encoders	0.85	83.42%	0.78	0.75
Deep Learning with Nature Inspired Algorithms	Long Short Term Memory with Bat Algorithm	0.75	77.58%	0.70	0.63
	Long Short Term Memory with Grey Wolf optimizer Algorithm	0.85	87.48%	0.79	0.76

Table 4.1: Comparison among different Models implemented so far

Methods	Area Under ROC Curve	Accuracy
Logistic Regression	0.54	58.09%
Support Vector Machines	0.54	59.37%
Decision Tree	0.52	55.68%
Random Forest	0.53	60.49%

Table 4.2: Comparison with Baseline Models

4.2.1 Curves showing Receiver Operating Curve (ROC) and Loss Curve of different models

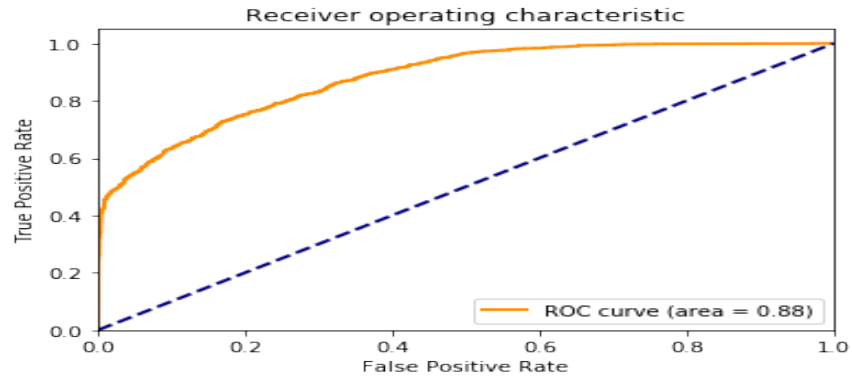


Figure 4.1: Receiver Operating Characteristic Curve: Long Short Term Memory.

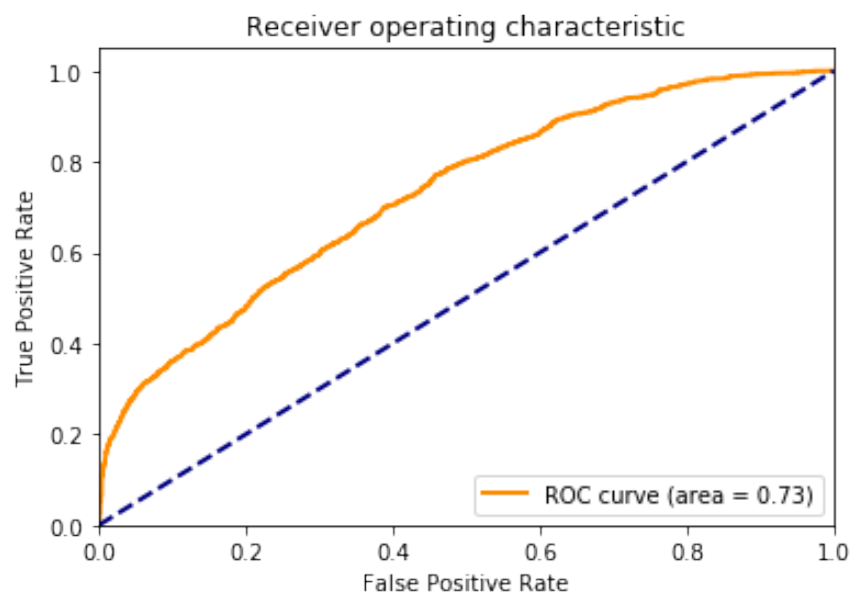


Figure 4.2: Receiver Operating Characteristic Curve: Long Short Term Memory Auto-Encoders.

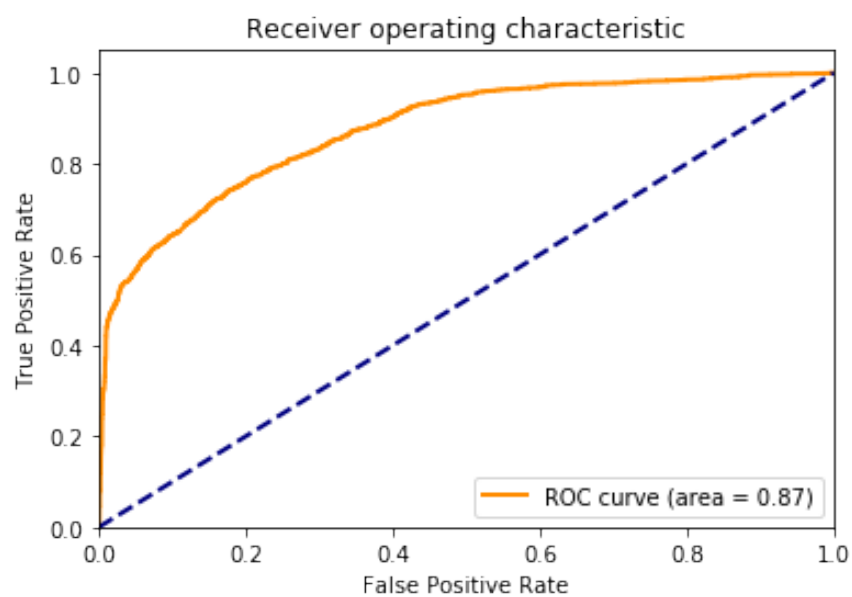


Figure 4.3: Receiver Operating Characteristic Curve: Convolution Long Short Term Memory.

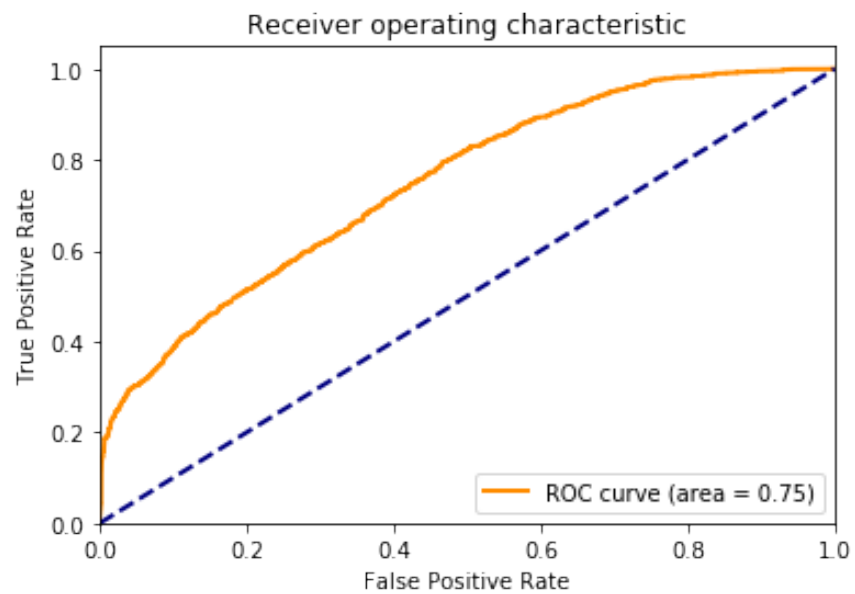


Figure 4.4: Receiver Operating Characteristic Curve: Long Short Term Memory with Bat Algorithm.

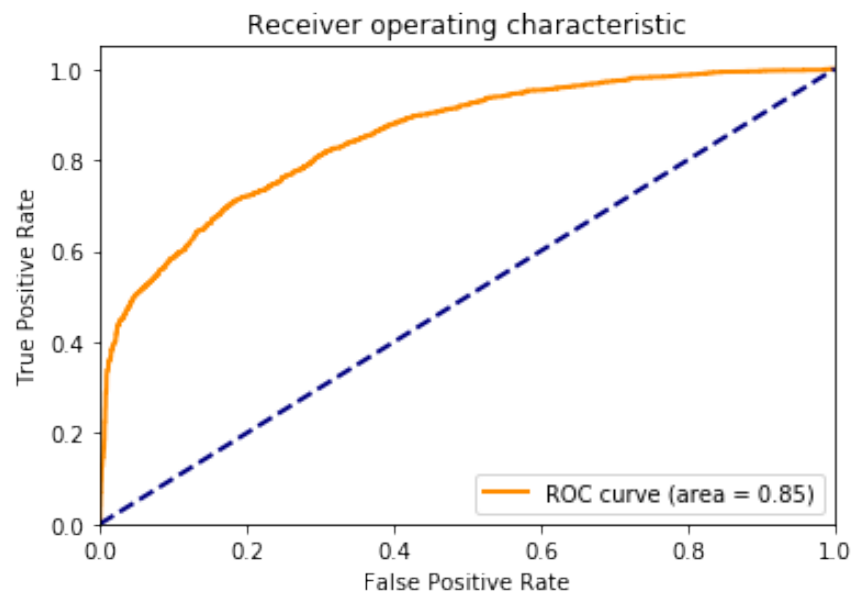


Figure 4.5: Receiver Operating Characteristic Curve: Long Short Term Memory with Grey Wolf Optimizer Algorithm.

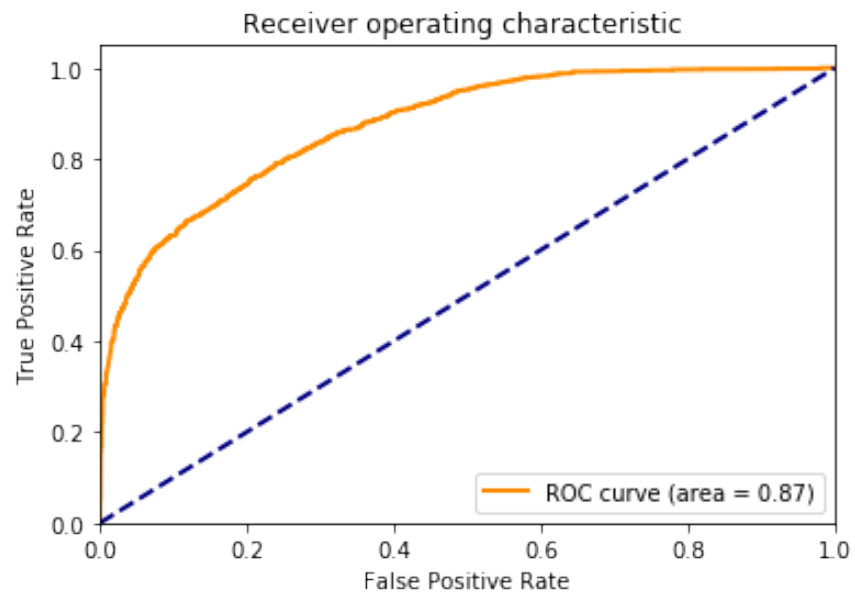


Figure 4.6: Receiver Operating Characteristic Curve Convolution Long Short Term Memory Auto Encoders.

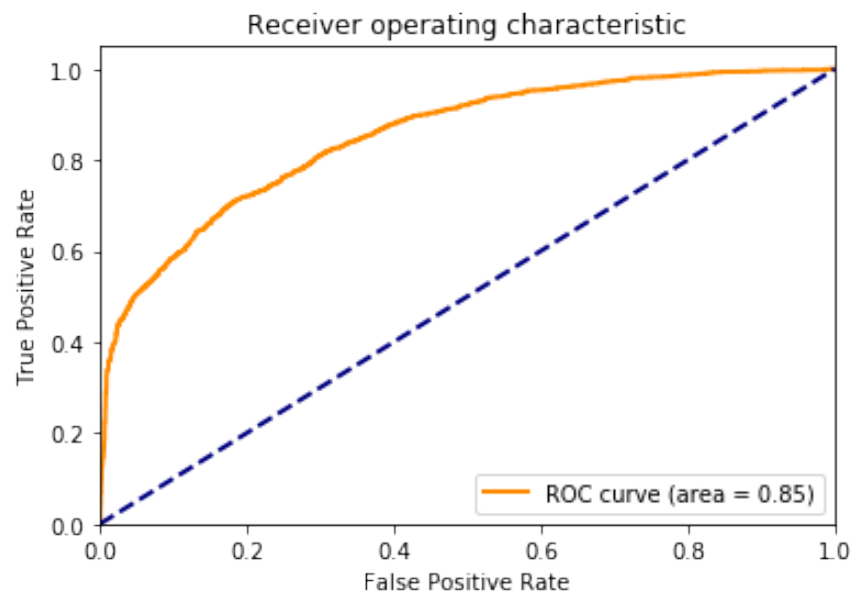


Figure 4.7: Receiver Operating Characteristic Curve Bi-Directional Long Short Term Memory.

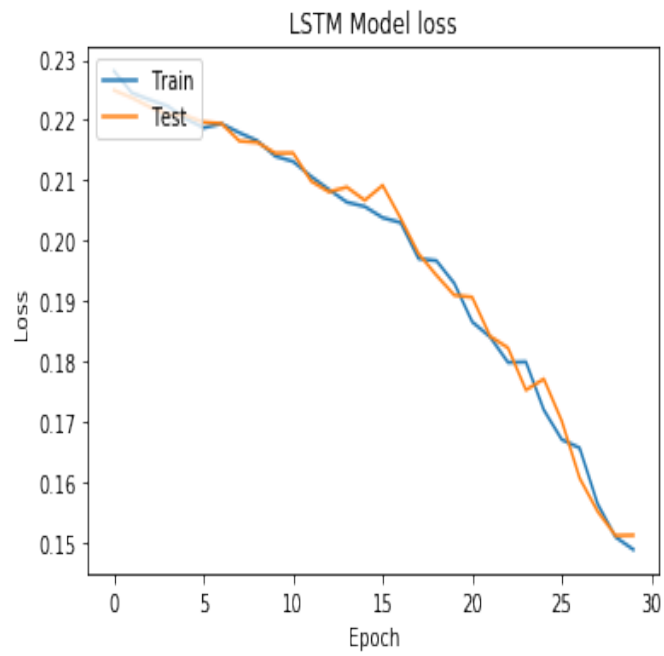


Figure 4.8: Loss Curve: Long Short Term Memory.

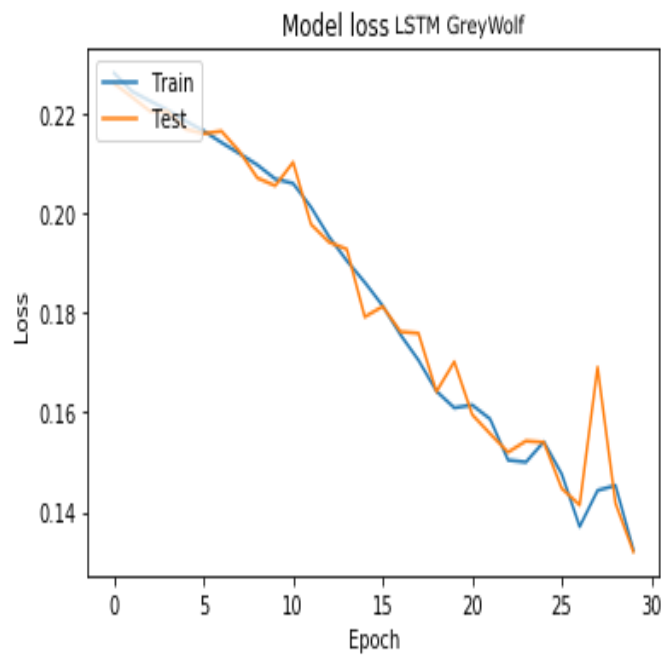


Figure 4.9: Loss Curve: Long Short Term Memory Grey Wolf.

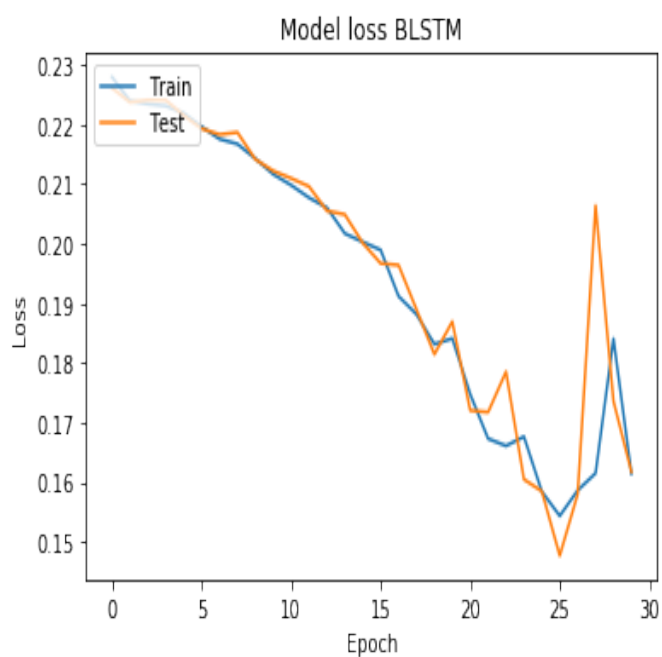


Figure 4.10: Loss Curve: Bidirectional Long Short Term Memory.

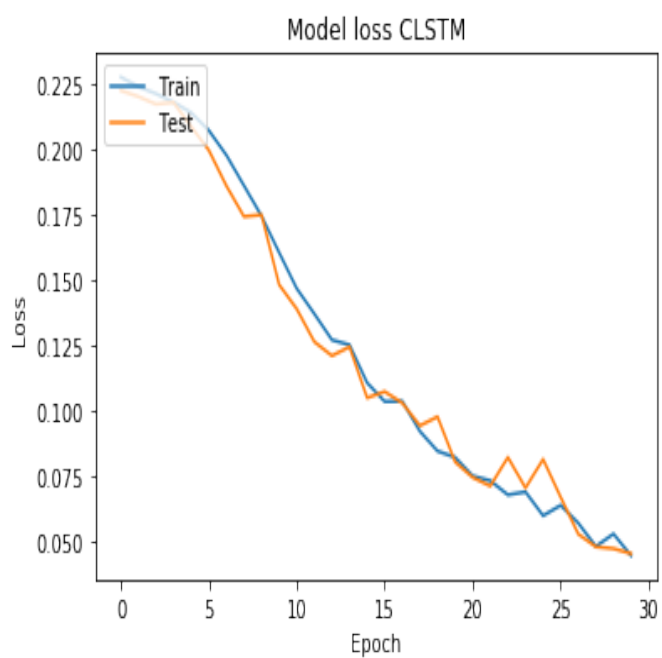


Figure 4.11: Loss Curve: Convolution Long Short Term Memory.

Chapter 5

Discussions and conclusion

In this chapter, the work is concluded and future plan is presented. Next, the research contribution are presented. Finally, limitation of the work and possible future extensions are described respectively.

5.1 Contributions

Following are the contributions made in the research work.

- To compare the performance of various deep learning models on MIMIC-III dataset based on accuracy and area under the roc curve.
- Compare the results of deep learning models with baseline models to point the advantages of deep learning in the field of health-care applications.
- Comparison of deep learning models with or without nature-inspired algorithms.

5.2 Limitations

The computation power and the memory required to process and compute such a big dataset, and the heavy amounts of output becomes one of the major limitations of the model. Since the data is already 35gb and as well as we use the LSTM model and hybrid model, i.e., CLSTM also with nature-inspired algorithms which store a lot of data while computation, therefore memory requirements becomes considerably large.

5.3 Future scope

Presently, this study targets patients who were readmitted to the hospital for sure, whether within 30 days or after 30 days. This study can be extended, and one can classify the data in three categories:

- Patients readmitted in 30 days.
- Patients readmitted after 30 days.
- Patients that were never readmitted.

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