## **Recitation 12**

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## **Brief Overview**

We discussed:

- inner product spaces (defined by integrals and weight function)
- Function approximation in the 2-norm (sec. 9.3)
- Function approximation in infinity-norm or "minimax" problem (ch. 8)
- o Eg. 9.4 best approximation in 2-norm and minimax polynomial
- Ill-conditionedness of the linear system which is the solution of function approximation in the 2-norm (last paragraph, sec. 9.3). Also see ex. 4.12 in [3].
- Orthogonal polynomials and how they avoid ill-conditionedness.
- Finding orthogonal polynomials using Gram-Schmidt process

## References

Besides the textbook (ch. 8 and 9), the following references may be useful. Ref. [3, 4] are especially good overviews of the topics, and [5] is extensive in terms of including earlier topics like interpolation/splines.

- 1. <a href="https://wiki.math.ntnu.no/\_media/tma4215/2012h/approx2norm.pdf">https://wiki.math.ntnu.no/\_media/tma4215/2012h/approx2norm.pdf</a>
- 2. http://www.math.usm.edu/lambers/mat772/fall10/lecture12.pdf
- 3. <a href="http://www2.math.umd.edu/~dlevy/classes/amsc466/lecture-notes/approximation-chap.p">http://www2.math.umd.edu/~dlevy/classes/amsc466/lecture-notes/approximation-chap.p</a> df
- 4. <a href="http://home.iitk.ac.in/~sqhorai/TEACHING/MTH308/minimax.pdf">http://home.iitk.ac.in/~sqhorai/TEACHING/MTH308/minimax.pdf</a>
- 5. <a href="http://people.ucsc.edu/~ealdrich/Teaching/ComputationGroup/Slides/lec4.pdf">http://people.ucsc.edu/~ealdrich/Teaching/ComputationGroup/Slides/lec4.pdf</a>