



rekt_n00b's blog

Mo's Algorithm on Trees [Tutorial]

 By [rekt_n00b](#), [history](#), 12 months ago,  

Introduction

Mo's Algorithm has become pretty popular in the past few years and is now considered as a pretty standard technique in the world of Competitive Programming. This blog will describe a method to generalize Mo's algorithm to maintain information about paths between nodes in a tree.

Prerequisites

Mo's Algorithm — If you do not know this yet, read this amazing [article](#) before continuing with this blog.

Preorder Traversal or DFS Order of the Tree.

Problem 1 — Handling Subtree Queries

Consider the following problem. You will be given a rooted Tree T of N nodes where each node is associated with a value $A[node]$. You need to handle Q queries, each comprising one integer u . In each query you must report the number of distinct values in the subtree rooted at u . In other words, if you store all the values in the subtree rooted at u in a set, what would be the size of this set?

Constraints

$$1 \leq N, Q \leq 10^5$$

$$1 \leq A[node] \leq 10^9$$

Solution(s)

Seems pretty simple, doesn't it? One easy way to solve this is to flatten the tree into an array by doing a Preorder traversal and then implement Mo's Algorithm. Maintain a lookup table which maintains the frequency of each value in the current window. By maintaining this, the answer can be updated easily. The complexity of this algorithm would be $O(Q\sqrt{N})$

Note that you can also solve this in $O(N \log^2 N)$ by maintaining a set in each node and merging the smaller set into the larger ones.

Problem 2 — Handling Path Queries

Now let's modify Problem 1 a little. Instead of computing the number of distinct values in a subtree, compute the number of distinct values in the unique path from u to v . I recommend you to pause here and try solving the problem for a while. The constraints of this problem are the same as Problem 1.

→ Pay attention

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→ shivamgarg210

Rating: **1440**
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shivamgarg210

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THE ISSUE

An important reason why Problem (1) worked beautifully was because the dfs-order traversal made it possible to represent any subtree as a contiguous range in an array. Thus the problem was reduced to "finding number of distinct values in a subarray $[L, R]$ of $A[]$ ". Note that it is not possible to do so for path queries, as nodes which are $O(N)$ distance apart in the tree might be $O(1)$ distance apart in the flattened tree (represented by Array $A[]$). So doing a normal dfs-order would not work out.

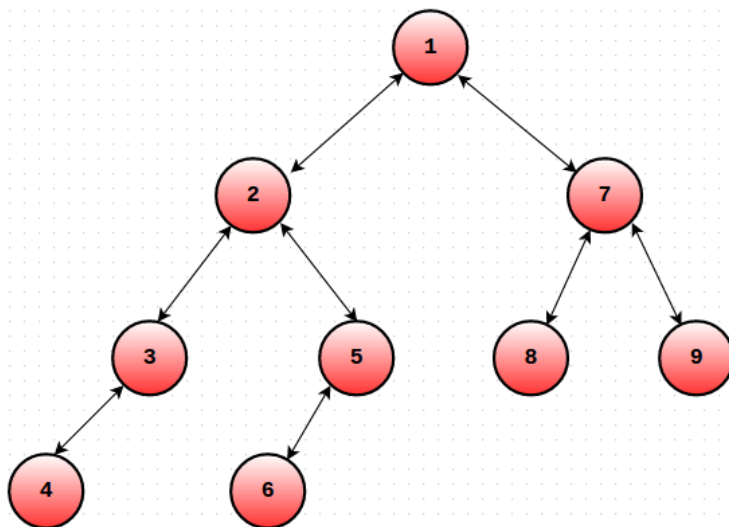
Observation(s)

Let a node u have k children. Let us number them as $v_1, v_2 \dots v_k$. Let $S(u)$ denote the subtree rooted at u .

Let us assume that $dfs()$ will visit u 's children in the order $v_1, v_2 \dots v_k$. Let x be any node in $S(v_i)$ and y be any node in $S(v_j)$ and let $i < j$. Notice that $dfs(y)$ will be called only after $dfs(x)$ has been completed and $S(x)$ has been explored. Thus, before we call $dfs(y)$, we would have entered and exited $S(x)$. We will exploit this seemingly obvious property of $dfs()$ to modify our existing algorithm and try to represent each query as a contiguous range in a flattened array.

Modified DFS-Order

Let us modify the dfs order as follows. For each node u , maintain the Start and End time of $S(u)$. Let's call them $ST(u)$ and $EN(u)$. The only change you need to make is that you must increment the global timekeeping variable even when you finish traversing some subtree ($EN(u) = ++cur$). In short, we will maintain 2 values for each node u . One will denote the time when you entered $S(u)$ and the other would denote the time when you exited $S(u)$. Consider the tree in the picture. Given below are the $ST()$ and $EN()$ values of the nodes.



$$ST(1) = 1 \quad EN(1) = 18$$

$$ST(2) = 2 \quad EN(2) = 11$$

$$ST(3) = 3 \quad EN(3) = 6$$

$$ST(4) = 4 \quad EN(4) = 5$$

$$ST(5) = 7 \quad EN(5) = 10$$

$$ST(6) = 8 \quad EN(6) = 9$$

$$ST(7) = 12 \quad EN(7) = 17$$

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$$ST(8) = 13 \quad EN(8) = 14$$

$$ST(9) = 15 \quad EN(9) = 16$$

$$A[] = \{1, 2, 3, 4, 4, 3, 5, 6, 6, 5, 2, 7, 8, 8, 9, 9, 7, 1\}$$

The Algorithm

Now that we're equipped with the necessary weapons, let's understand how to process the queries.

Let a query be (u, v) . We will try to map each query to a range in the flattened array. Let $ST(u) \leq ST(v)$ where $ST(u)$ denotes visit time of node u in T . Let $P = LCA(u, v)$ denote the lowest common ancestor of nodes u and v . There are 2 possible cases:

Case 1: $P = u$

In this case, our query range would be $[ST(u), ST(v)]$. Why will this work?

Consider any node x that does not lie in the (u, v) path.

Notice that x occurs twice or zero times in our specified query range.

Therefore, the nodes which occur exactly once in this range are precisely those that are on the (u, v) path! (Try to convince yourself of why this is true : It's all because of *dfs()* properties.)

This forms the crux of our algorithm. While implementing Mo's, our add/remove function needs to check the number of times a particular node appears in a range. If it occurs twice (or zero times), then we don't take its value into account! This can be easily implemented while moving the left and right pointers.

Case 2: $P \neq u$

In this case, our query range would be $[EN(u), ST(v)] + [ST(P), ST(P)]$.

The same logic as Case 1 applies here as well. The only difference is that we need to consider the value of P i.e the LCA separately, as it would not be counted in the query range.

This same problem is available on [SPOJ](#).

If you aren't sure about some elements of this algorithm, take a look at this neat [code](#).

Conclusion

We have effectively managed to reduce problem (2) to number of distinct values in a subarray by doing some careful bookkeeping. Now we can solve the problem in $O(Q\sqrt{N})$. This modified DFS order works brilliantly to handle any type path queries and works well with Mo's algo. We can use a similar approach to solve many types of path query problems.

For example, consider the question of finding number of inversions in a (u, v) path in a Tree T , where each node has a value associated with it. This can now be solved in $O(Q\sqrt{N} \log N)$ by using the above technique and maintaining a BIT or Segment Tree.

This is my first blog and I apologize for any mistakes that I may have made. I would like to thank [sidhant](#) for helping me understand this technique.

Sample Problems

1) [Count on a Tree II](#)

- 2) Frank Sinatra — Problem F
 3) Vasya and Little Bear

Thanks a lot for reading!

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▲ +406 ▼



[rekt_n00b](#)



12 months ago



[98](#)



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meintoo

12 months ago, # | ☆

← Rev. 2

▲ +8 ▼

In this case, our query range would be $[EN(u), ST(v)] + [ST(P), ST(P)]$.
 Shouldn't it be $[EN(u), ST(v)] + [ST(P), ST(U)]$ or am I missing something ?

→ [Reply](#)

12 months ago, # ^ | ☆

← Rev. 2

▲ +8 ▼

Nope, it will be $[ST(P), ST(P)]$.

Consider the path from 3 to 5. In this case, $P = 2$



rekt_n00b

$EN(3) = 6$ and $ST(5) = 7$, so we consider the range $[6, 7]$ in $A[]$ corresponding to the nodes $[3, 5]$ giving us the values of nodes 3 and 5.

Our query range does not consider the value of the lca as $ST(P) < EN(u) < ST(v) < EN(P)$. Hence we must account for the value of P separately.

→ [Reply](#)

12 months ago, # ^ | ☆

▲ +8 ▼



meintoo

Ok !!!
 Thanks
 Nice article anyways

→ [Reply](#)



rekt_n00b

12 months ago, # ^ | ☆

▲ +13 ▼

Thank You :D

→ [Reply](#)



sampri

12 months ago, # | ☆

▲ +23 ▼

Thanks! That was a really nice tutorial!

→ [Reply](#)



rekt_n00b

12 months ago, # ^ | ☆

▲ +13 ▼

Thanks a lot :)

→ [Reply](#)

12 months ago, # | ☆

▲ 0 ▼

Nice tutorial :)

can you give links to some more problems on which similar approach can be





applied ?
→ [Reply](#)



sbansalcs

8 months ago, # [^](#) | [☆](#)

<http://codeforces.com/problemset/problem/375/D>

→ [Reply](#)



rekt_n00b

8 months ago, # [^](#) | [☆](#)

This can be done with standard Mo's Algorithm, because the queries are on subtrees and not paths.

→ [Reply](#)



sbansalcs

8 months ago, # [^](#) | [☆](#)

Oh sorry, I thought this guy was asking for any problems related to the algorithms described above.

→ [Reply](#)

12 months ago, # [^](#) | [☆](#)

← Rev. 2 [+5](#) ▼

BTW, we can find number of distinct values in a subarray $[l, r]$ of a offline in $O((q+n)\log n)$.

Let's sort all queries by l_i .

$d_i = 1$ if i is the first occurrence of a_i in $a[l \dots n]$ otherwise $d_i = 0$.

So, query (l_i, r_i) is finding sum of $d[l_i \dots r_i]$.

When we move from query with l_i to query with $l_i + 1$ we must update only one or zero elements of d_i . It can be done in $O(\log n)$ if we precalculated for each i next occurrence of a_i in array.

→ [Reply](#)



komendart



gongy

7 months ago, # [^](#) | [☆](#)

[+10](#) ▼

If you maintain the tree persistently, you can have an online solution as well.

→ [Reply](#)



joker_in

10 days ago, # [^](#) | [☆](#)

[-6](#) ▼

can you elaborate it . how to handle it online ? thanks in advance.

→ [Reply](#)



bhishma

10 days ago, # [^](#) | [☆](#)

[0](#) ▼

I think this is related to a current running contest.

→ [Reply](#)



joker_in

10 days ago, # [^](#) | [☆](#)

[-6](#) ▼

yes

→ [Reply](#)

10 days ago, # [^](#) | [☆](#)

[0](#) ▼

which contest ?

→ [Reply](#)





SarvagyaAgarwal



joker_in

10 days ago, # ^ | ☆▲0▼

codechef february long challenge

→ [Reply](#)

joker_in

10 days ago, # ^ | ☆▲0▼

In curiosity i asked this question too early .
sorry for that . you can answer it after
contest is over

→ [Reply](#)

SarvagyaAgarwal

10 days ago, # ^ | ☆▲+1▼

Yeah , 3 days early :P

→ [Reply](#)

bluemmb

12 months ago, # | ☆▲0▼

Thanks, Is known who used this idea on trees first time ?

→ [Reply](#)

belltolls

12 months ago, # ^ | ☆▲+5▼

It must have been known from before. But I guess this is the first proper
tutorial/blog for it.

→ [Reply](#)

xrisk

12 months ago, # | ☆▲+1▼

Totally went over my head! Excellent blog!

→ [Reply](#)

as_couple

7 months ago, # ^ | ☆▲+3▼

If it goes over your head, How do you realize it's an excellent ?

→ [Reply](#)

12 months ago, # | ☆▲0▼

Thanks a lot you made my day !!



svg_af

I've been obsessing about COT2 for almost two months without anything that
comes to mind

if only i could upvote more than once

→ [Reply](#)

rekt_n00b

12 months ago, # ^ | ☆▲+1▼

Thanks! I'm glad that you found it useful :)

→ [Reply](#)

12 months ago, # | ☆▲0▼



I implemented this algorithm on the COT2 problem on
SPOJ(<http://www.spoj.com/problems/COT2/>). I am getting WA. Can someone
help me identify the bug in my code? <http://ideone.com/aLS5Yx>



rachitjain

→ [Reply](#)

rachitjain

12 months ago, # ^ | ☆

▲ +8 ▼

I found the mistake. Thanks for the nice tutorial.

→ [Reply](#)

SarvagyaAgarwal

5 months ago, # ^ | ☆

▲ 0 ▼

What was the bug ?

→ [Reply](#)

rachitjain

5 months ago, # ^ | ☆

▲ 0 ▼

Lol. Bro that was 7 months ago.

→ [Reply](#)

SarvagyaAgarwal

5 months ago, # ^ | ☆

▲ 0 ▼

Can you share your corrected code ?
Because I'm getting a WA too .→ [Reply](#)

rachitjain

5 months ago, Rev. 2 | ☆ 0 ▼

Sure. Link

→ [Reply](#)

vasandani68

4 months ago, # ^ | ☆

▲ 0 ▼

Can u please explain ur add and del functions. How are u maintaining the result after ignoring all those indexes which have occurred 2 times?

→ [Reply](#)

rachitjain

4 months ago, # ^ | ☆

▲ 0 ▼

Recently I solved one question using Mo's algorithm, and I remembered about this comment here. I overwrote the solution on the same link. Here is the [solution](#) for COT2. I think its self-explanatory how it is working.→ [Reply](#)

12 months ago, # | ☆

← Rev. 2 ▲ 0 ▼



NIKS001

Can someone please provide the $O(N \log^2 N)$ algorithm for Problem 1?The best I could get is $(N^2) \cdot \log N$ [as the sum of sizes of sets of each node is $O(N^2)$ — Worst case linear graph with all values distinct]→ [Reply](#)

rekt_n00b

12 months ago, # ^ | ☆

← Rev. 4 ▲ +3 ▼

Maintain a set of values for each node in the tree. Let $set(u)$ be the set of all values in the subtree rooted at u . We want $size(set(u))$ for all u .Let a node u have k children, $v_1, v_2 \dots v_k$. Every time you want to merge $set(u)$ with $set(v_i)$, pop out the elements from the smaller set and insert them into the larger one. You can think of it like implementing union find based on size

union into, based on size.

Consider any arbitrary node value. Every time you remove it from a certain set and insert it into some other, the size of the merged set is atleast twice the size of the original.

Say you merge sets x and y . Assume $size(x) \leq size(y)$. Therefore, by the algorithm, you will push all the elements of x into y . Let xy be the merged set. $size(xy) = size(x) + size(y)$. But $size(y) \geq size(x)$.

So $size(xy) \geq 2 * size(x)$.

Thus, each value will not move more than $\log n$ times. Since each move is done in $O(\log n)$, the total complexity for n values amounts to $O(n \log^2 n)$

Code

→ [Reply](#)



NIKS001

12 months ago, # [^](#) | [☆](#)

[▲](#) +5 [▼](#)

Awesome! Thanks for the great explanation and code!

→ [Reply](#)



safayet007

5 months ago, # [^](#) | [☆](#)

← Rev. 2 [▲](#) 0 [▼](#)

What if set x and set y isn't completely disjoint? In that case $size(xy) = size(x) + size(y)$ statement isn't valid. Since the value on two nodes might be same.

→ [Reply](#)

5 weeks ago, # [^](#) | [☆](#)

← Rev. 3 [▲](#) 0 [▼](#)

I don't get the proof. Can you explain it a little more?

$$1. size(xy) \geq 2 * size(x)$$

I think, $size(xy) \geq size(y)$, and $size(xy) \leq size(x) + size(y)$

1. Thus, each value will not move more than $\log n$ times.



BlackVsKnight

How?

EDIT I think I understood. For a particular value to be included the maximum number of times in a move operation from set (x) to set (xy) where $size(x) \leq size(y)$, this value must be moved for each of its ancestor upto root. That is only possible if the height of the tree is at most $\log n$.

But the $size(xy) \geq 2 * size(x)$ seems incorrect. I think you meant that the size of subtree of parent of $x \geq 2 * size(x)$.

→ [Reply](#)



iit2015023

3 weeks ago, # [^](#) | [☆](#)

[▲](#) 0 [▼](#)

We cannot use the size function of the set to compare the sizes of the set as it would otherwise lead to N^2 complexity. Am i right?

→ [Reply](#)



3 weeks ago, # [^](#) | [☆](#)

[▲](#) +6 [▼](#)

$set.size()$ is $O(1)$.

→ [Reply](#)



rekt_n00b



iit2015023

3 weeks ago, # ^ | ☆

▲ 0 ▼

I thought it is $O(n)$. Thanks for the info.→ [Reply](#)

himanshujaju

12 months ago, # | ☆

▲ 0 ▼

Very neatly written tutorial. You make it seem amazingly easy!

→ [Reply](#)

rekt_n00b

12 months ago, # ^ | ☆

▲ 0 ▼

Thanks a lot :)

→ [Reply](#)

mbrc

12 months ago, # | ☆

▲ +11 ▼

Superb idea! :D

Thanks! :D

→ [Reply](#)

demon_cross

12 months ago, # | ☆

▲ 0 ▼

Nicely written!

→ [Reply](#)

rekt_n00b

12 months ago, # ^ | ☆

▲ 0 ▼

Thanks a lot :D

→ [Reply](#)

naruto09

10 months ago, # | ☆

▲ 0 ▼

shouldn't it be end time of u to start time of v in case 1. If we start from start time of u then u will be included 2 times one for its start time and once for end time. Correct me if I am wrong..

→ [Reply](#)

rekt_n00b

10 months ago, # ^ | ☆

▲ 0 ▼

Case 1 implies that u is an ancestor of v .

Therefore, we won't visit u twice in the range $[ST(u), ST(v)]$ as $EN(u) > ST(v)$.

→ [Reply](#)

baobab

10 months ago, # | ☆

▲ 0 ▼

Has anyone managed to get accepted on the SPOJ problem with a Java solution? I'm getting NZEC Runtime Error, but it looks like it's actually due to time limit exceeding.

→ [Reply](#)

9 months ago, # | ☆

▲ +3 ▼

Update 1: Added sample problems.→ [Reply](#)



rekt_n00b

8 months ago, # ^ | ☆

▲ 0 ▼

For the "Frank Sinatra" problem. How could you find the less value not present in the path?



Absolut

I realize that any value greather than the size of the tree wouldn't change the answer. So, if i have at most $1E5$ different values I can build a BIT. $pos[i] = 1$ if value i is present in the path. Then I binary search the less value k wich $sum[0...k]$ is less than k . That would be my answer. However the complexity is $O(N * \sqrt{N} * \log(N) * \log(N))$ and I think is excessive.

→ [Reply](#)

8 months ago, # ^ | ☆

▲ 0 ▼



rekt_n00b

The complexity wouldn't be $O(N\sqrt{N}\log^2 N)$, it would be $O(N\sqrt{N}\log N + N\log^2 N)$.

The first term is because you update your bit atmost $N\sqrt{N}$ times and the second term is because you binary search once for each query.

→ [Reply](#)

8 months ago, # ^ | ☆

▲ 0 ▼



Absolut

Thanks, my mistake.

So, it is the best completely? Or there is another approach

→ [Reply](#)

8 months ago, # ^ | ☆

▲ 0 ▼



rekt_n00b

You can solve the problem in $O(N\sqrt{N})$ by doing square root decomposition on the values. Each update would be done in constant time and you will take additional \sqrt{N} time per query to find the *block* which has the smallest value.

[Code](#)→ [Reply](#)

SProf

9 months ago, # | ☆

▲ 0 ▼

can it gives me tle,if i can't use weight compress?

→ [Reply](#)

rekt_n00b

9 months ago, # ^ | ☆

▲ 0 ▼

If you do not compress weights, you'll need a map and that would add an additional $\log(n)$ factor. However, you might be able to squeeze your solution within the TL with an `unordered_map`.

→ [Reply](#)

meshanya

9 months ago, # | ☆

▲ +39 ▼

BTW, there is a standard solution for the first problem ([see this link in Russian](#)). For each of the colors order all the vertices of this color according to the dfs traversal, let the vertices be labelled v_1, v_2, \dots, v_k . Add +1 to each of these vertices, and add -1 to the LCAs of the neighboring vertices $lca(v_1, v_2), lca(v_2, v_3), \dots, lca(v_{k-1}, v_k)$. If you sum up the values inside a subtree, you get the number of distinct elements in it.

Since the ordering can be done in $O(n)$, and in theory you can answer lca

queries for a static tree in $O(1)$ with $\tilde{O}(n)$ pre-processing, you have a linear solution (assuming $0 \leq A[x] < N$).

→ [Reply](#)



rekt_n00b

9 months ago, # |

Thanks! This idea is pretty cool :)

→ [Reply](#)



SProf

9 months ago, # |

in problem frank sinatra, can i quickly find minimal number, that is not present in given set.

→ [Reply](#)



howsiwei

9 months ago, # |

Isn't the time complexity of Mo's algorithm $O(N \cdot \sqrt{Q})$ instead of $O(Q \cdot \sqrt{N})$?

→ [Reply](#)



rekt_n00b

9 months ago, # |

The complexity of Mo's depends on the number of times we increment/decrement the `curL`, `curR` variables. This [link](#) explains the time complexity of Mo's algorithm.

→ [Reply](#)



howsiwei

9 months ago, # |

← Rev. 2

+10

If the size of each block is k , then the time complexity of moving the left pointer is $O(Q \cdot k)$ and the time complexity of moving the right pointer is $O(N/k \cdot N)$. The optimal value of k is N/\sqrt{Q} which results in total time complexity $O(N \cdot \sqrt{Q})$.

→ [Reply](#)



rekt_n00b

9 months ago, # |

That is true. However, in most cases upper bounds on Q and N are equal (or pretty close), so it doesn't make a difference.

→ [Reply](#)

9 months ago, # |

I wrote the code for COT2 judge gives runtime error at 10th testcase pls help me i cant find the error thanks in advance



aashishkr

pls see my code

<https://ideone.com/MG3XbK>

→ [Reply](#)



sbansalcs

8 months ago, # |

Awesome Tutorial!

→ [Reply](#)

8 months ago, # |

Thank you!

→ [Reply](#)



rekt_nuud



alphaguy4

7 months ago, # | ☆

▲ 0 ▼

Can anyone explain how to linearize the tree .. (Not binary tree but any tree in general)

As in Problem 1..

→ [Reply](#)



rekt_n00b

7 months ago, # ^ | ☆

▲ 0 ▼

[Click](#)

→ [Reply](#)



alphaguy4

7 months ago, # ^ | ☆

▲ 0 ▼

Thanks alot... !

→ [Reply](#)



uttom

7 months ago, # | ☆

▲ 0 ▼

I got Runtime Error. Here is my code There is any wrong my creating lca label or anything else. Thanks in advance.

→ [Reply](#)



ankeshgupta007

7 months ago, # | ☆

▲ 0 ▼

amazing tutorial!

→ [Reply](#)



stould

7 months ago, # | ☆

← Rev. 3 ▲ 0 ▼

If the tree store the values on the edges, you could store these values on the children (going from the root), and change the *Case 2* to:

```
if(P == u || P == v) check(P);
```

```
.... asnw the query
```

```
if(P == u || P == v) check(P);
```

→ [Reply](#)



RobertBruce

6 months ago, # | ☆

▲ 0 ▼

Why don't you write more tutorials?

→ [Reply](#)

5 months ago, # | ☆

▲ 0 ▼

<http://www.spoj.com/problems/DQUERY/> a practice problem

→ [Reply](#)

EbraM96



SarvagyaAgarwal

5 months ago, # | ☆

▲ +3 ▼

COT2 code link doesnt work .

→ [Reply](#)



rekt_n00b

5 months ago, # ^ | ☆

▲ +7 ▼

Updated.

→ [Reply](#)



SarvagyaAgarwal

5 months ago, # | ☆

▲ 0 ▼

Why does this get WA for COT2 :/ ?

→ Reply



ace_pocket

4 months ago, # | ☆

▲ +5 ▼

Could you explain your idea for the problem of finding number of inversions in a (u, v) path in a Tree T.

→ Reply



SarvagyaAgarwal

10 days ago, # ^ | ☆

▲ 0 ▼

Just maintain a BIT during Mo's

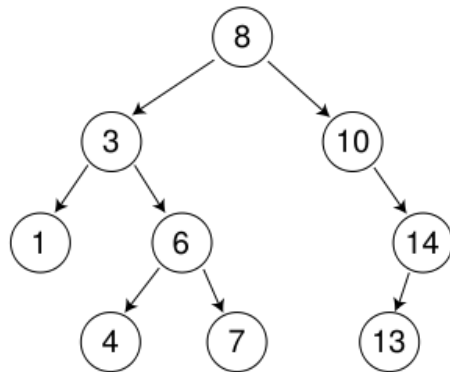
→ Reply

4 months ago, # | ☆

← Rev. 2 ▲ 0 ▼



Vicennial



If I flatten the above tree, my array would be:

8 3 1 6 4 7 10 14 13

Suppose I need to use Mo's algorithm for subtrees (assume I need to find sum of values of each subtree indicated by the query)

For a given query 'Vj' how would I find its end range index in the array?

Eg if given query is node '6', the starting range would be idx 3 and ending would be idx 5.

→ Reply



SarvagyaAgarwal

4 months ago, # ^ | ☆

▲ +1 ▼

Store the starting and ending times for every node during your dfs .

→ Reply



Vicennial

4 months ago, # ^ | ☆

▲ 0 ▼

Thanks, understood it after a bit of googling about discovery/begin/end times.

→ Reply



Toby_And_Friends

4 months ago, # | ☆

▲ 0 ▼

For a problem like this: http://lightoj.com/volume_showproblem.php?problem=1348 where I need to return sum of all the nodes in a given path &

update the value of a node, how should I approach using this technique of linearizing the tree? I mean since I need to ignore nodes which have occurrence of 2 so the range becomes discontinuous for a segment tree structure.

→ Reply



memset0

4 months ago, # | ☆

▲ 0 ▼

Nice Article ... BTW Can we solve the problem with Binary lifting ?

→ Reply



arjun95

2 months ago, # | ☆

How can apply this method if weight is given on edges instead vertices

→ [Reply](#)

▲ 0 ▼



SarvagyaAgarwal

5 weeks ago, # ^ | ☆

Root the tree arbitrarily . Map the weight of edge (parent-child) to the child .

→ [Reply](#)

▲ 0 ▼



arjun95

5 weeks ago, # ^ | ☆

and what about the weight of root?

→ [Reply](#)

▲ 0 ▼



SarvagyaAgarwal

5 weeks ago, # ^ | ☆

Are you saying that both edges and nodes have weights ?

→ [Reply](#)

▲ 0 ▼



arjun95

5 weeks ago, # ^ | ☆

no, i mean as you said map the weight of edge (parent-child) to the child but root has no parent so what value is map to the root of the tree?

→ [Reply](#)

▲ 0 ▼



SarvagyaAgarwal

5 weeks ago, # ^ | ☆▲ 0 ▼

nothing is mapped to the root . A tree has $n - 1$ edges which would be mapped to $n - 1$ vertices of the tree .→ [Reply](#)

5 weeks ago, # ^▲ 0 ▼

☆

thanks now i understand

→ [Reply](#)

arjun95



BlackVsKnight

5 weeks ago, # ^ | ☆▲ 0 ▼

assign it an impossible value like -INFINITY. This means whenever you see this value, you know it's not allowed, and you ignore it.

→ [Reply](#)

▲ 0 ▼



GklolosK

5 weeks ago, # | ☆

how to calculate LCA fast? i only know the $O(n)$ algorithm...→ [Reply](#)

▲ 0 ▼



rekt_n00b

5 weeks ago, # ^ | ☆

[Click](#)→ [Reply](#)

▲ +5 ▼

5 weeks ago, # | ☆

▲ 0 ▼

In this case, our query range would be $[EN(u), ST(v)] + [ST(P), ST(P)]$.



CuSO45H2O

Consider on this case, if we select 3 and 8 on the tree given to explain the DFS-Order, the range $[EN(u), ST(v)]$ contains the whole subtree $S(5)$ which is not on our query path. Are we supposed to judge every node in the range or Am I missing something? Thx!

→ [Reply](#)

GkiolosK

5 weeks ago, # ^ | ☆

▲ 0 ▼

you only consider nodes which appear once in the range, so maintain a frequency count of the current nodes, if a node appears twice, remove it from the list of nodes

→ [Reply](#)

9 days ago, # | ☆

▲ 0 ▼



a88796366

Thanks a lot, but I don't really understand the meaning of **If it occurs twice (or zero times), then we don't take it's value into account! This can be easily implemented while moving the left and right pointers.** and I wrote the code as what you have said in this essay, but it seems wrong and I don't know where I count the answer incorrectly

[my code](#)→ [Reply](#)

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 The only programming contests Web 2.0 platform
 Server time: Feb/26/2017 15:13:53 (c3).
 Desktop version, switch to [mobile version](#).