

- 1. Consider an asset which follows a geometric Brownian motion (GBM) with drift $\mu=10\%$ and volatility $\sigma=20\%$. Assume that the risk free rate is r=5%. The initial asset price at time t=0 is S(0)=100.
 - Simulate 10 different paths of the asset price making use of the GBM, in both the real and the risk-neutral worlds.
 - Now compute the price of a six month fixed-strike Asian option with a strike price of 105 (using arithmetic average). Do the pricing for both call and put options, using Monte Carlo simulation.
 - Repeat the above exercise with strike price K=110 and K=90. How do your results compare ?
 - Now do a sensitivity analysis of the option prices.
- Compute the prices of the Asian options given above by employing variance reduction techniques also and compare your results.