

Overlapping Community Detection in Social Networks

1

Overlapping Community Detection: Link Partition

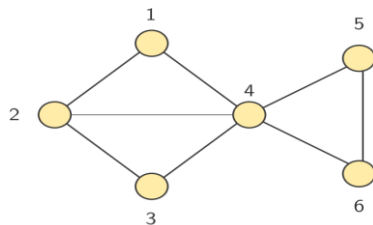
- ❑ Uses **links (edges)** in the networks to detect communities
- ❑ Two major approaches
 - ❑ Create a **link network** and apply a node partitioning algorithm or disjoint community detection algorithm to find the community
 - ❑ Use **similarity measures** on the edges to find the communities directly by creating the dendrogram
- ❑ Jaccard coefficient might be good choice for similarity measure
- ❑ For two edges e_{ik} and e_{jk} connected to node k ,

$$Sim(e_{ik}, e_{jk}) = \frac{|N_i \cap N_j|}{|N_i \cup N_j|}$$

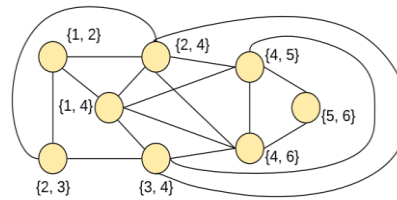
Where N_i and N_j are the neighbours of the nodes i and j

2

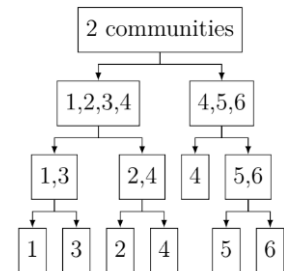
Link Partition Method for Overlapping Community Detection: Illustration



Example Network



Link Network for the example network



Dendrogram for the example network obtained using similarity measures

3

Overlapping Community Detection: BigClam

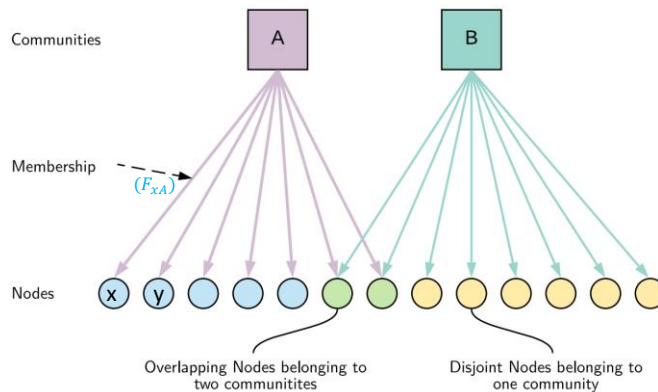
- ❑ Proposed by Yang and Leskovec in 2013
- ❑ Based on a generative modeling approach
 - Define **models** that can generate the required network
 - Find a model that generates a network that **fits best**
- ❑ **Affiliation Graphical Model (AGM)** parameterized as $G(V, C, M, P_c)$ to generate a network
 - V is the set of nodes of the network
 - C is the set of communities
 - M is the association between nodes and communities
 - P_c is the probability of community C
- ❑ Probability of edges between a pair of nodes x and y

$$P(x, y) = 1 - \prod_{c \in M_x \cap M_y} (1 - P_c)$$

where M_x and M_y are communities x and y belongs to

4

Overlapping Community Detection: BigClam



- F_{xA} : Membership strength of node x to community A
- $F_{xA} = 0$: No Membership
- Each community links nodes independently
- Probability of two edges in one community

$$P_A(x, y) = 1 - \exp(-F_{xA} \cdot F_{yA})$$
- Overall probability of an edge between two nodes

$$P(x, y) = 1 - \exp(-F_x \cdot F_y^T)$$

5

Overlapping Community Detection: BigClam

- ❑ Given the above, we need to find values for matrix F
- ❑ Estimate F such that probability of network G can be maximized.
- ❑ Above can be solved just by applying gradient descent method

6