

# i) Confidence Interval and Sample Size Calculation

a) 95 % Confidence Interval for the percentage of voters for Candidate A

1) Calculate Sample Size proportion  $\hat{p}$

- No. of voters for candidate A = 380

- Sample Size = 800

$$\hat{p} = \frac{380}{800} = 0.475$$

2) Z score for 95% Confidence level

$$\text{for } 95\% = 1.96$$

3) Standard error =

$$SE = \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$$

$$= \sqrt{\frac{0.475(1-0.475)}{800}}$$

$$= 0.0176$$

4) Margin of error -

$$ME = Z \times SE$$

$$= 1.96 \times 0.0176$$

$$= 0.0345$$

$$\therefore \text{Confidence Interval} = 0.475 \pm 0.0345$$

$$\therefore CI = (0.4405, 0.5095)$$



b) Sample Size Calculation for Desired margin error

Z-score for 95% confidence level = 1.96

Margin of error  $(E) = 0.02$

$$\therefore \text{Sample size } (n) = \left( \frac{(1.96)^2 \times 0.5(1-0.5)}{(0.02)^2} \right)$$

req. Sample size = 2401

② Hypothesis Testing for Average Arm Span

③ Hypothesis test.

$H_0 : \mu = 160 \text{ cm}$

Alternate  $H_a : \mu > 160 \text{ cm}$

mean = 200 cm

$$Z = \frac{\bar{x} - \mu_0}{\frac{s}{\sqrt{n}}}$$

$$= \frac{200 - 160}{\frac{15}{\sqrt{30}}}$$

$$= 14.6$$

~~P-value~~ = ~~14.6~~

For Z value 14.6 P-value extremely small  
we reject null hypothesis



② 95% Confidence Interval for average Arm Span

$$\begin{aligned}\text{Standard error} &= \frac{15}{\sqrt{30}} \\ &= 2.7386\end{aligned}$$

$$\begin{aligned}\text{Margin of error} &= Z \cdot SE \\ &= 1.96 \times 2.7386 \\ &= 5.37\end{aligned}$$

Confidence interval :

$$CI = 200 \pm 5.37$$

$$\text{Lower limit} = 194.63$$

$$\text{Upper limit} = 205.37$$