

Unit-III

Relational Database Design

Functional Dependencies

Functional dependencies are the result of interrelationship b/w attributes or in b/w tuples in any relation.

Definition: In relation R, X & Y are the two subsets of the set of attributes, Y is said to be functionally dependent on X if a given value of X (all attributes in X) uniquely determines the value of Y (all attribute in Y).

It is denoted by $X \rightarrow Y$ (Y depends upon X)

Determinant: Here X is known as determinant of functional dependency.

Eg:

(Employee)

Eid	Name	Salary
1	A	10,000
2	B	20,000
3	C	30,000
4	D	40,000

Here,

$$X(Eid) \rightarrow Y(\text{Name}, \text{Salary})$$

With the help of Eid, we can easily access info name, salary of employee. Name & salary depends on Eid.

Functional Dependency Chart

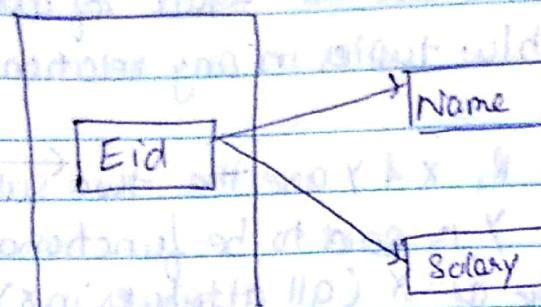
It is the graphical representation of functional dependencies among attributes in any relation.

The full steps to follow to draw FD chart:

- Find out the primary key attribute.

2. Make a rectangle & write all the primary key attributes inside it.
3. Write all non prime key attributes outside the rectangle.
4. Use arrow to show FD among attributes.

Employee



→ Types of Functional Dependencies:

These are 4 major types of FD's.

(i) Partial Dependency & Fully Functional Dependency

- Partial Dependency:

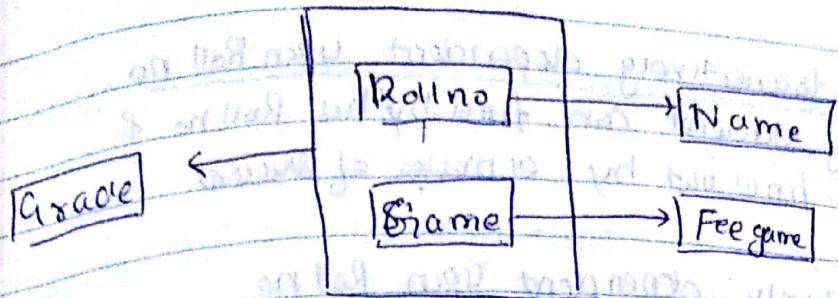
* Suppose we have more than one attribute in primary key * Let A be the non-prime key attribute * If A is not dependent upon all prime key attributes then partially dependent.

- Fully Functional Dependency:

* Suppose have more than 1 attribute in primary key * Let A be the non prime key attribute * If A is dependent upon all prime key attributes

* Then A is said to be fully functional dependent.

Student



here

Prime Key = Roll no & Name
attribute = Name

Non-Prime, Name,
attribute = Fee game,
Grade.

Here, Name & Fee are partially dependent b/c. we can find name by Roll no & Fee game by Grade.

& Grade is Fully Functional Dependent b/c. we can find the grade of any student in a particular game if we know Roll no & game of that student.

② Transitive Dependency & Non-Transitive Dependency:

• Transitive Dependency:

* It is due to dependency b/w non-prime key attributes.

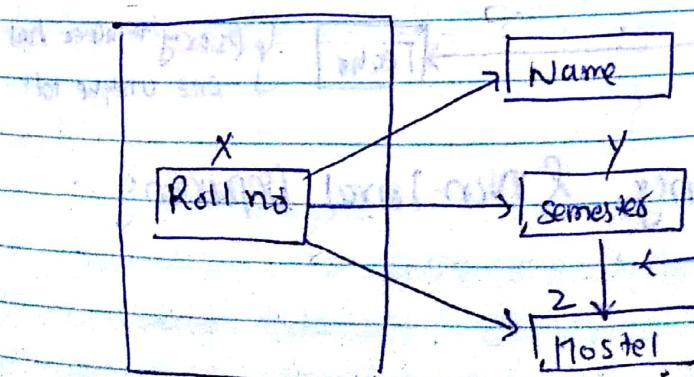
* Suppose in a relation R , $X \rightarrow Y$ (Y depends upon X),
 $Y \rightarrow Z$ (Z depends upon Y) then $X \rightarrow Z$ (Z depends upon X).

* Z is said to be transitively dependent upon X .

• Non-Transitive Dependency:

* Any Functional dependency which is not transitive is known as non-transitive dependency.

* It exists if there is no dependency b/w non prime key attribute.



Dependency b/w
non-prime key
attribute

Now, hostel is transitively dependent upon Roll no.

Semester of any student can find by his Roll no. & hostel can be found by semester of student

& Name is transitively dependent upon Roll no

(3) Single valued Dependency & Multivalued Dependency.

• Single valued dependency: In any relation R, if

for particular value of x, y has single value

then it is known as single valued dependency.

$$x \rightarrow y$$

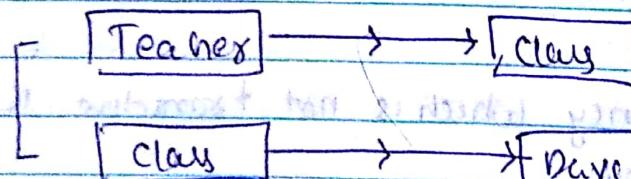
• Multivalued Dependency: In any relation R, if for a

particular value of x, y has more than one value

then it is known as MVD.

ID	Teacher	Class	Days
1	A	IT	6
2	B	CSE	10
1	A	ECE	15

MVD



, teacher can take

more than one class



Class can be more

than one day

SD.



Every teacher has

one unique id.

(4)

Total Dependency & Non-Total Dependency.

Emp-Id	E-name	E-Salary
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Torial FD: In any relation R, $X \rightarrow y$ is torial if $y \subseteq X$ (y is the subset of X)

Non-Torial FD: In any relation R, $X \rightarrow y$ is non-torial if $y \not\subseteq X$ (y is not the subset of X).

Note:

$\text{Emp-Id} \rightarrow \text{Ename}$ (non-torial).

$\{\text{Emp-Id}, \text{Ename}\} \rightarrow \{\text{Ename}\}$. (Torial)

Anomalies in Relational Database.

Anomalies: It refers to the undesirable results b/w. of modification of data.

Eg: Employ

Emp-Id	Ename	Salary	Dept-No.	Dept-name
1	A	5000	2	Accounts
2	B	6000	2	Accounts
3	C	7000	1	Sales
4	D	8000	5	Marketing
5	E	9000	5	Marketing
6	F	10000	2	(Accounts)
7	G	11000	5	Marketing
8	H	12000	2	Accounts

Can not be inserted.

→ Insertion Anomalies

Suppose you want to add new info in any relation but can not enter data b/c. of some constraints. This is known as Insertion anomalies.

- * In any relation employ, u can't add new department finance bcs there is no employ in finance department.
- * Addition of this info violates entity-integrity rules that is primary key can not be NULL.

→ Deletion Anomalies

- * Deletion Anomaly occurs when you try to delete any existing info from any relation & this causes deletion of any undesirable information.

Ex: Deletion of C leads to delete Sales dept. completely.

→ Update Anomalies:

Upd. anomalies occurs

- * When you try to update any existing info in any relation & this causes inconsistency of data.

Attribute closure $[X^+]$ (not in syllabus)

Set of attributes that is defined by X.

$R(A B C D)$ FD. $(A \rightarrow B, B \rightarrow C, C \rightarrow D)$

$A \rightarrow B \rightarrow A B C D$

$B \rightarrow C$

$C \rightarrow D$

i.e. (A^+) Attribute closure.

$R(A B C D E)$ FD's $\{AB \rightarrow C, C \rightarrow D, B \rightarrow E\}$

$(AB)^+ \therefore AB \rightarrow C \rightarrow ABCDE$

$\downarrow C \rightarrow D$

Super Key
& candidate key

$B \rightarrow E$

$(BF) \rightarrow BE$

↳ Attribute closure not having super or candidate key having

$(ABC)^+ \rightarrow ABCDE$

↳ Best having min attributes to key more instead have less

NORMALIZATION

no data loss

no data redundancy

- Normalization is a process by which we can decompose or divide any relation into more than one relation to remove anomalies in relational database.
- It is a step by step process & each step is known as Normal Form
- Normalization is a reversible process.

* Properties of Normalization

- Remove different anomalies.
- Decomposition must be lossless.
- Preserve necessary dependency.
- Reduce redundancy.

* Various Normal Forms

1. First Normal Form (1NF)

A relation is in 1NF if & only if

- This rule defines that all the attributes in a relation must have atomic domains.
- The values in an atomic domain are individual units.
- It means atomicity must be present in relation.

Consider a relation "Language"

Course	Content
Java	Java
Programming	Java, C++
web	HTML, CSS

We re-arrange the relation (table) as below, to convert it to First Normal Form.

Course	Content
Programming	Java
Programming	C++
web	HTML
web	CSS

Each attribute must contain only a single value from its pre-defined domain.

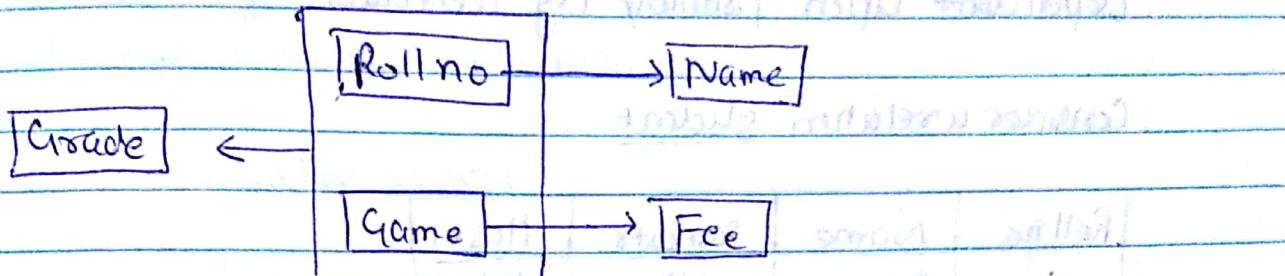
2. Second Normal Form (2NF)

- A relation is in 2NF if it is in 1NF & all non-prime Key attributes must be fully functional dependent upon prime Key attributes.

Consider the relation student:

Rollno	Game	Name	Fee	Grade
1	Cricket	Akash	200	A
2	Badminton	Rohit	300	B
3	Cricket	Shiv	200	A

(a)



Dependency chart (b)
(Student relation with anomalies)

Relation student is in 1-NF but still contains anomalies.

- (i) Deletion anomaly: Suppose u want to delete Rohit but after deleting it you loose all info. of Badminton bcz he is the only player for badminton.
- (ii) Insertion anomaly: Suppose u want to add? basketball but ~~it is~~ u can not add this until there is ^{is no} a player for this.
- (iii) Update anomaly: Suppose u want to change fee of Cricket Then u have to search all the students participated in cricket & update fee individually otherwise it produces inconsistency.

The solution of this problem is to separate Partial dependencies & Fully functional dependencies. So, divide Student relation into 3 parts!

Student Games Performance.

Rollno Name	Game Fee	Rollno Game Grade
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Now, deletion, insertion & update operations can be performed without causing inconsistency.

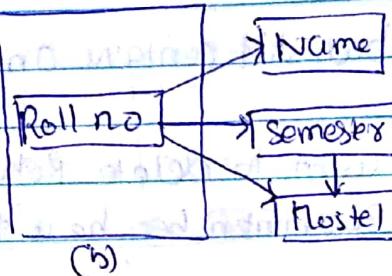
3. Third Normal Form (3NF)

→ A relation is in Third Normal Form if it is in 2NF & non prime key attributes must be non-transitively dependent upon primary key attributes.

Consider a relation student

Roll no	Name	Semester	Hostel
1	Aakash	1st	H1
2	Rohit	2nd	H2

(a)



(b)

Student relation is in 2NF but still contains anomalies

(i) Deletion Anomaly: suppose u want to delete Rohit but after deleting it u loose all info. of hostel H2 bcoz he is the only student in H2.

(ii) Insertion Anomaly: suppose u want to add new hostel H3 but u can not add this until there is a shadow for this.

(iii) Update Anomaly: suppose u want to change the hostel of 1st yr student's then u have to search all the students of 1st sem & update them individually otherwise it creates inconsistency.

The ^{seln} student of this problem is to divide relation student into two relations:

Student:

hostel:

Roll no	Name	Semester	Semester	Hostel
1	Aakash	1st	1st	H1

Now, deletion, insertion & update operations can be performed without causing inconsistency.

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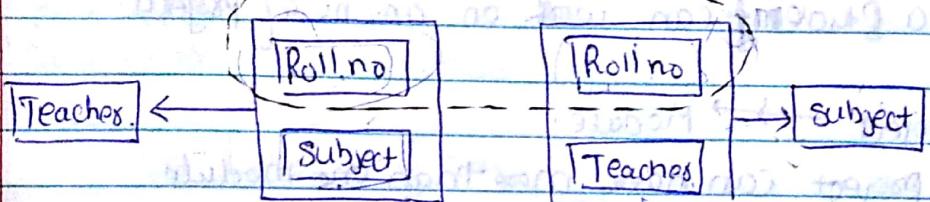
4. Boyce Codd Normal Form (BCNF)

- BCNF is a strict format of 3NF
- A relation is in BCNF if & only if all determinants are candidate keys
- BCNF deals with multiple candidate keys.

Consider a relation Student:

Roll no	Subject	Teacher
1	C	T ₁
2	C++	T ₂
3	C	T ₃
4	JAVA	T ₄

→ Overloaded candidate key.



Student relation is in BCNF but still contains anomalies.

- (i) Deletion Anomaly: Suppose u want to delete all info of Roll no 2 but after deleting it u loose all info of Teacher T₂ that teaches subject C++
- (ii) Insertion anomaly: Suppose u want to add new subject HTML but u can't add this until there is a student for this
- (iii) Update anomaly: Suppose u want to change teacher of subject C then u have to search all the students having subject C & update them individually.

The solution of this problem is to divide relation Student into two relations:
(Student-Teacher) (Subject-Teacher)

Roll NO	Teacher
1	T ₁

Teacher	Subject
T ₁	C

Fourth Normal Form (4NF)

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→ A relation is in 4NF if it is in BCNF & for all multi-valued functional dependencies (MVD) of the form $X \rightarrow\rightarrow Y$ either $X \rightarrow Y$ is a total MVD or X is a superkey of relation.

Consider a relation student - details

Student Name	Project	Module
S1	1	M1
S2	1	M2
S1	2	M1

Dependencies in Relation student are -

$\text{Student Name} \xrightarrow{\text{Student}} \text{Project}$

i.e. A Student can work on any no of projects.

$\text{Project} \rightarrow\rightarrow \text{Module}$.

i.e. a project can have more than one module.

Student-details Relation is in BCNF but still contains anomalies:

- (i) Deletion anomaly: Suppose u want to delete Project 2 but after deleting it u loose all info abt student 2.
- (ii) Insertion anomaly: Suppose u want to add new project 3 but u can not add this until there is a student for this.
- (iii) Updation anomaly: suppose u want to update name of project 2 then u have to search all the students of 2 & update them individually otherwise it causes inconsistency.

The soln of this problem is to divide relation student-details into two relations.

Student - Project

Project - module

Student	Project
S1	1
S2	1
S1	2

Project	Module
1	M1
1	M2
2	M1

Here, Programmes is the Super Key.

Here, Project is the superkey.

6. Project Join Normal Form (PJNF) or (SNF) or Join Dependency

→ Join dependency: Let R be a given relation upto 4NF & if decompose (Project or divided) into $\{R_1, R_2, R_3, \dots, R_n\}$

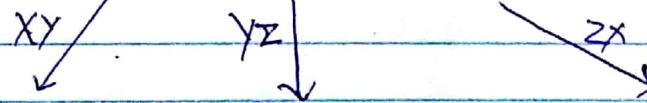
→ The relation R satisfy the join dependency $\{R_1, R_2, R_3, \dots, R_n\}$ if & only if joining of R_1 to $R_n = R$.

Consider a

~~Relation~~ Re XYZ relation

X#	Y#	Z#
X1	-Y1	/ Z2 \
X1	Y2	= Z1
X2	Y1	= Z1

X1	Y1	Z1
X1	Y1	Z2
X1	Y2	Z1
X2	Y1	Z1



X#	Y#	Z#
X1	X1	
X1	Y2	Z2
X2	Y1	Z1

Z#	X#
Z2	X1
Z1	X1
Z1	X2

Joining

X#	Y#	Z#
X1	X1	Z2
X1	Y1	Z1
X1	Y2	Z1
X2	Y1	Z2
X2	Y1	Z1

→ Ans

X#	Y#	Z#
X1	Y1	Z2
X1	Y2	Z1
X2	Y1	Z1
X1	Y1	Z1

Original
XY

not in original
XYZ

→ 5NF is the ultimate Normal Form. A relation in 5NF
is guaranteed to be free of anomalies.