Problem Set #3

Quiz, 5 questions

✓ Congratulations! You passed!

Next Item



1/1 point

1.

Consider an alphabet with five letters, $\{a,b,c,d,e\}$, and suppose we know the frequencies $f_a=0.32$, $f_b=0.25$, $f_c=0.2$, $f_d=0.18$, and $f_e=0.05$. What is the expected number of bits used by Huffman's coding scheme to encode a 1000-letter document?



2230

Correct

For example, a=00, b=01, c=10, d=110, e=111.

- 2400
- 3000
- 3450



1/1 point

2.

Under a Huffman encoding of n symbols, how long (in terms of number of bits) can a codeword possibly be?

- () n
- $\log_2 n$
- n-1

Correct

For the lower bound, take frequencies proportional to powers of 2. For the upper bound, note that the total number of merges is exactly n-1.



Qui **3**.5 questions

Which of the following statements holds for Huffman's coding scheme?

If the most frequent letter has frequency less than 0.33, then all letters will be coded with at least two bits.

Correct

Such a letter will endure a merge in at least two iterations: the last one (which involves all letters), and at least one previous iteration. In the penultimate iteration, if the letter has not yet endured a merge, at least one of the two other remaining subtrees has cumulative frequency at least (1-.33)/2 > .33, so the letter will get merged in this iteration.

A letter with frequency at least 0.5 might get encoded with two or more bits.
If a letter's frequency is at least 0.4 , then the letter will certainly be coded with only one bit.
If the most frequent letter has frequency less than 0.5 , then all letters will be coded with more than one bit.



1/1 point

4.

Which of the following is true for our dynamic programming algorithm for computing a maximum-weight independent set of a path graph? (Assume there are no ties.)

If a vertex is excluded from the optimal solution of two consecutive subproblems, then it is excluded from the optimal solutions of all bigger subproblems.

Correct

By induction, since the optimal solution to a subproblem depends only on the solutions of the previous two subproblems.

If a vertex is excluded from the optimal solution of a subproblem, then it is excluded from the optimal solutions of all bigger subproblems.
The algorithm always selects the maximum-weight vertex.

As long as the input graph has at least two vertices, the algorithm never selects the minimum-weight vertex.



1/1 point

5.

Consider the following $\operatorname{Problem}_{\operatorname{Guign}}$ so $\operatorname{Consider}_{\operatorname{Guign}}$ from G to $\operatorname{Consider}_{\operatorname{Guign}}$	gramming algorithm for computing the maximum-weight independent set of a path graph. proposed extension to more general graphs. Consider an undirected graph with positive ertex v , obtain the graph $G'(v)$ by deleting v and its incident edges from G , and obtain the y deleting v , its neighbors, and all of the corresponding incident edges from G . Let value of a maximum-weight independent set of a graph H . Consider the formula $PT(G'(v)), w_v + OPT(G''(v))$, where v is an arbitrary vertex of G of weight w_v . Which
$OPT(G) = \max\{ORG \}$ of the following statem	

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The formula is always correct in trees, and it leads to an efficient dynamic programming algorithm.

Correct

Indeed. What running time can you get?

The formula is always correct in general graphs, and it leads to an efficient dynamic programming algorithm.
The formula is always correct in trees, but does not lead to an efficient dynamic programming algorithm.

The formula is correct in path graphs but is not always correct in trees.

