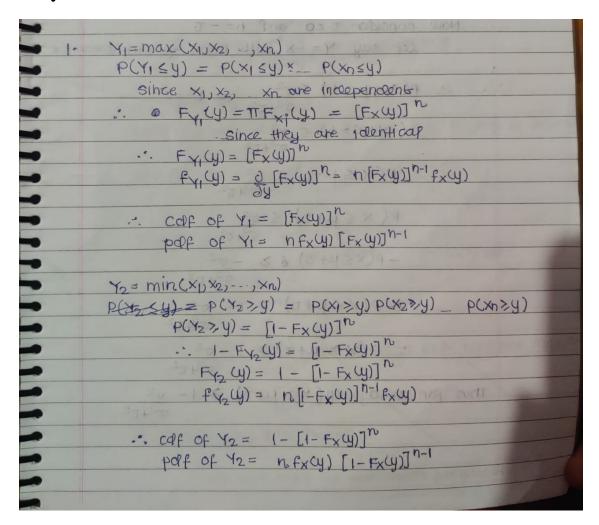
Assignment 1: CS 215

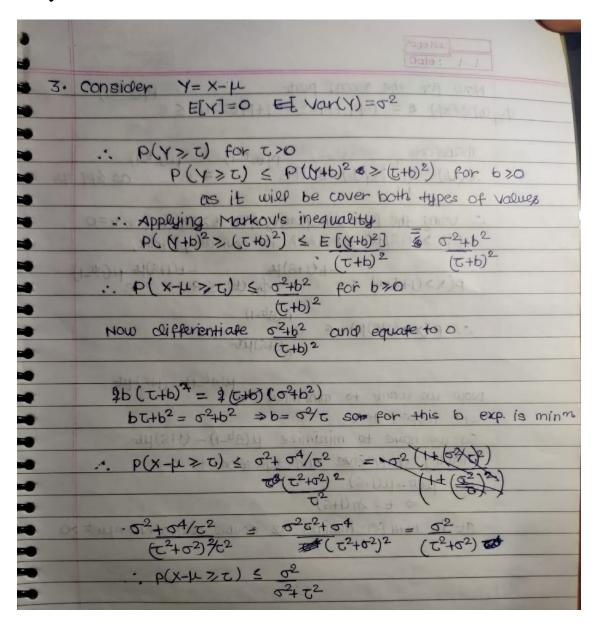
$\begin{array}{ccc} {\bf 190050113} \ {\rm Shivam} \ {\rm Raj} & {\bf 190050080} \ {\rm Pawan} \ {\rm Kumar} \\ {\bf 190020010} \ {\rm Aman} \ {\rm Singh} \end{array}$

September 14, 2020

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(((((((((((((((((((
. for any random variable and 5701	
P(X-4 > t) \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	
54 bb 52	
Now consider to and b=-t	
let say Y = -x with mean - \mu and raniance \si	
(h30x)d = 6(x3x)d = (h31x)d	
$P(Y+\mu > b) \leq \sigma^{2}$ $\sigma^{2}+\tau^{2}$ $P(-X+\mu > b) \leq \sigma^{2}+\tau^{2}$	
1 (() 52+ 52 = () 52 + 52 = () 3 = ()	
P (+x+42b) 5 52	
$\frac{1}{2} \left(b \left(x \leq h - p \right) \leq \frac{a_3 + c_5}{2}$	-
10-+C2	6
P(x < 4+0) < 52	
$P(x \leq \mu + \tau) \leq \sigma^2$	-
$-P(X \leq \mu + \tau) \neq \gamma - \sigma^2$	
52+52	
1-p(x<\u+c) > 1+ 02 (1)	(
1 [(h) × 4 - 1 = (h \(\sigma_2 + \sigma_2 + \sigma_2 \)	
: P(X > µ+z) > 1-52	
1 (D) A - 11 - 1 - (D) 07+c2	
Thus for to <0, P(X > 1+t) > 1- 52	0
72+72	0
HID -1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1	-
+0 1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -	-
1 10 104	

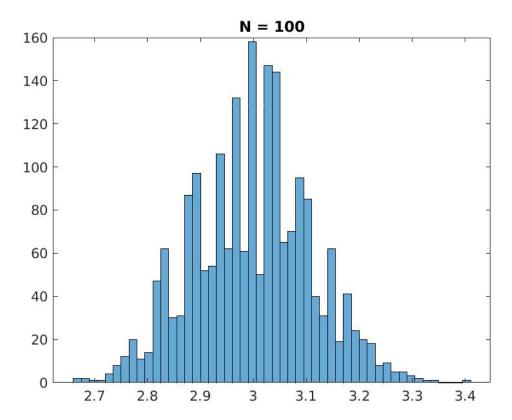
efect
A ROBERTON .
For t <0
For continuous, $\phi_{x}(t) = \int_{-\infty}^{\infty} e^{+tx} f_{x}(x) dx > \int_{-\infty}^{\infty} e^{+tx} f_{x}(x) dx$
φ _x (tt) - 1 - 0 0
if t<0, e+tx1 > e+tx2 ip x1 < x2
12 400)
(1) = 0 xo fx (x) dx = 6 xo fx (x) dx
$\therefore \phi_{x}(t) \geqslant \int_{\infty}^{x_{0}} e^{tx} f_{x}(x) dx \geqslant \int_{\infty}^{x_{0}} e^{x_{0}t} f_{x}(x) dx$
$\frac{1}{100} \frac{1}{100} \frac{1}$
· φ _x (t) / ε - ελοφ _y (t)
THE PORT OF THE PROPERTY OF TH
For discrete, no xit p(x=xi)
For discrete, n part $p(x=xi)$ $ \frac{dy}{dx}(t) = \frac{1}{2} e^{xit} p(x=xi) $
XOTALL VIDEO VICXO
φ _x (t) = 7 ≤ e ^{xot} p(x=x _j) where x _j ≤ x _o because if t < 0, e ^{xot} ≤ e ^{xjt}
the city and an all
φx(th) > e xot p(x ≤ xo)
ψx (8) 2 E P (3 (3 (0))
p(x ≤ x0) ≤ e-tx0 (x (4))
als is and fix=xid tax s (1) x

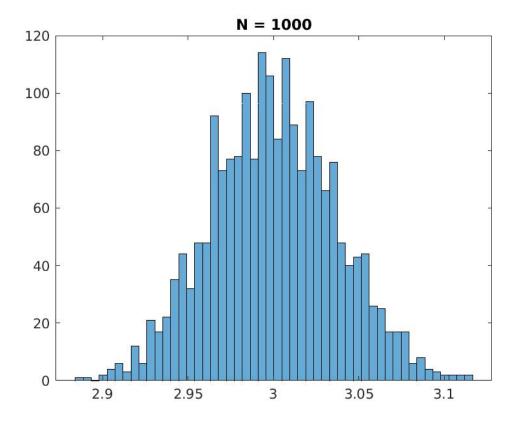
```
Now for the second part

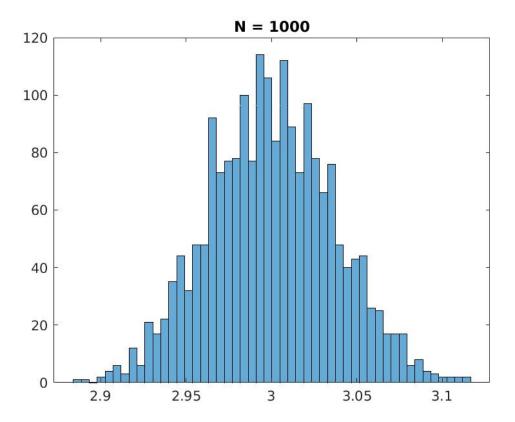
\phi_{x_i}(t)

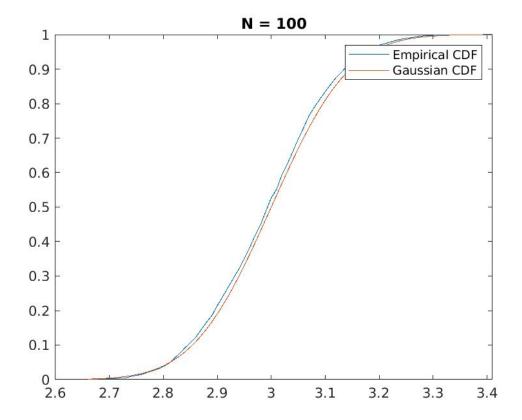
\phi_{
                                         .. using the first inequality for t>0, as for t=0
                                                 p(x>(1+8) \mu) \le 1 which is obviously true,
                                                     -\frac{1}{2}(1+8)\mu -\frac{1
                                                 Now we want to minimize e (1+6) put
                                                        with respect to t
                                                               so we have to minimize \mu(e^{t}-1)-(1+8)\mu t
                                                                Taking derivative and equation to 0
                                                                             met=mu+s)
                                                                                                                         => t=ln(1+s)
                                                                              It is minifor minima as double derivative = met >0
```

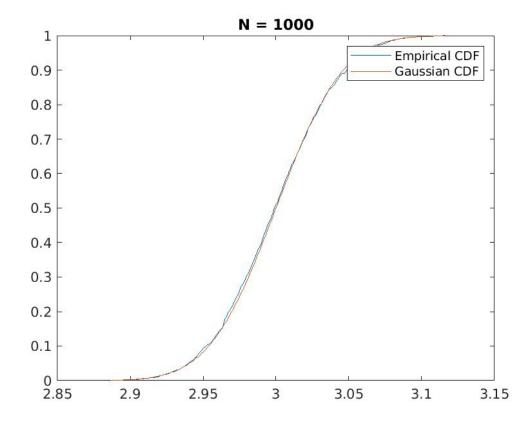
Code for this qsn is in file named 'q5.m'

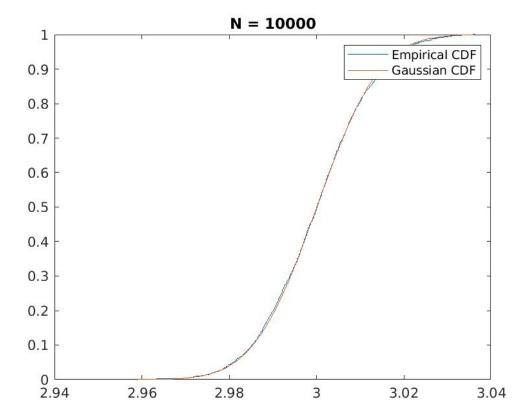


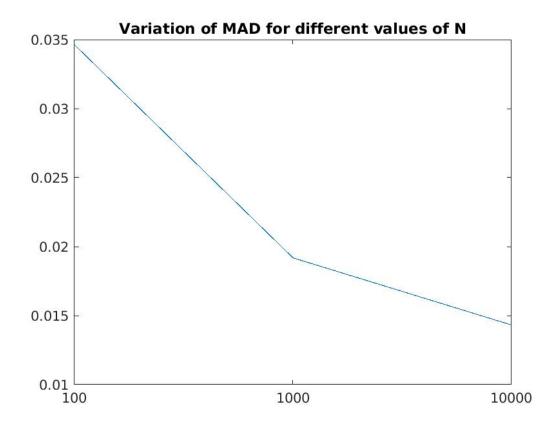












Code of this question is in the file 'q6.m'

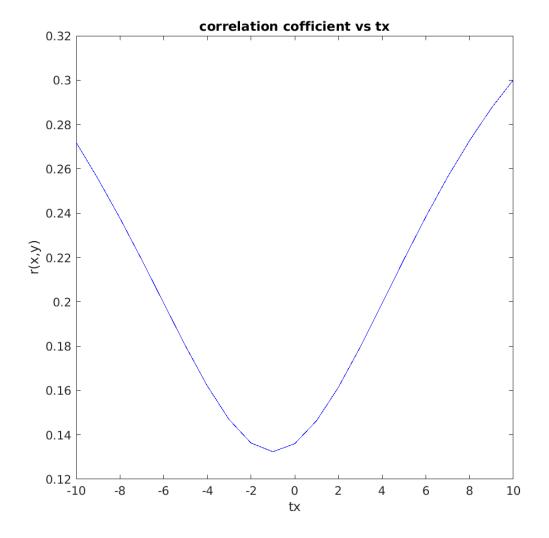


Figure 1: This plot correspond to T1.jpg and T2.jpg

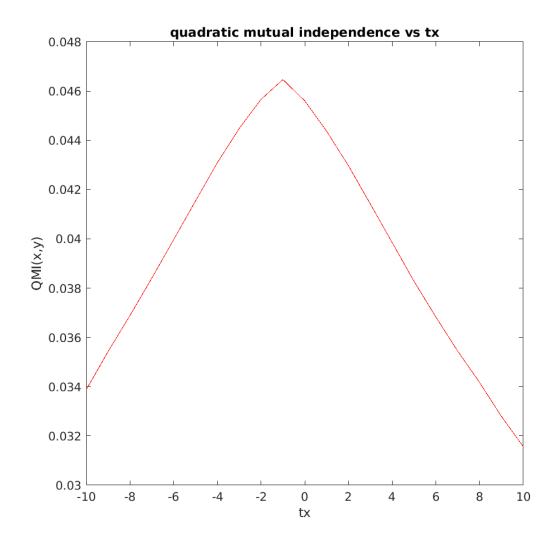


Figure 2: This plot correspond to T1.jpg and T2.jpg

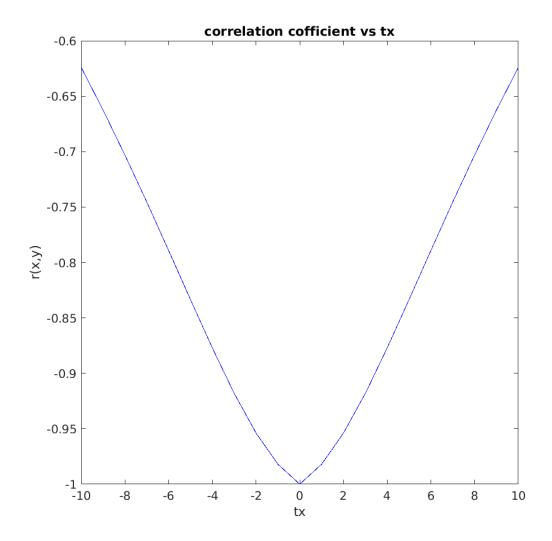


Figure 3: This plot correspond to T1.jpg and negative of T1.jpg

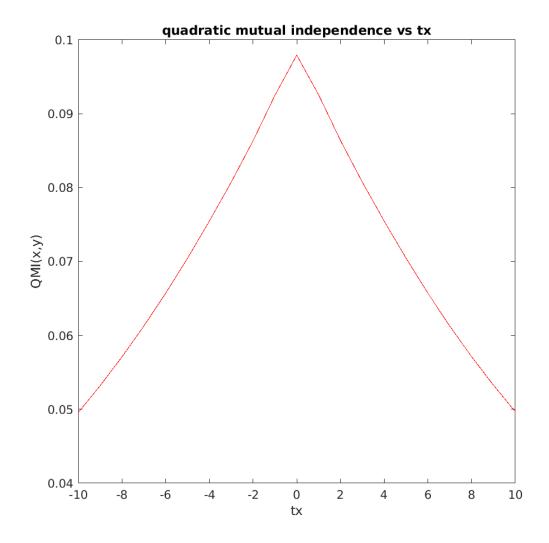


Figure 4: This plot correspond to T1.jpg and negative of T1.jpg

By observation we can see that correlation coefficient between the two images will be always postive, and it will minimum when the shift is equal to -1(that is one unit along negative x axis). By similar type of arguments we can say that QMI will attains it's maximum when the shift is equal to 1. We can say that correlation coefficient increases and QMI decreases when images are moved out of alignment as the point of minimum correlation coefficient and maximum QMI is somewhat close to no shift.

By observation we can see that correlation coefficient between the two images will be always negative, and it will minimum when the shift is equal to 0 and it will be equal to -1 as we can clearly see that the images are negative of each other. By similar type of arguments we can say that QMI will attains it's maximum when the shift is equal to 0. We can say that correlation coefficient increases and QMI decreases when images are moved out of alignment as the point of minimum correlation coefficient and maximum QMI is equal to no shift.

```
= n(n-1) PiPj (\leq P_i = 1)
= hpi because &pi=1
```

```
E[X_i^2] = \frac{\partial^2}{\partial t_i^2} \Phi_X(t_i) \Big|_{t=(0,0...)}
= \frac{\partial^2}{\partial t_i^2} (\underbrace{x \text{ pieti}}_{t=(0,0...)}^{t_i} \text{ where } t=(b_i,b_2,...,t_k)^2
= \frac{\partial^2}{\partial t_i^2} (\underbrace{x \text{ pieti}}_{t=(0,0...)}^{t_i} \text{ xeti}
= \frac{\partial^2}{\partial t_i^2} (\underbrace{x \text{ pieti}}_{t=(0,0...)}^{t_i} \text{ pieti}
= \frac{\partial^2}{\partial t_i^2} (\underbrace{x \text{ pieti}}_{t=(0
```