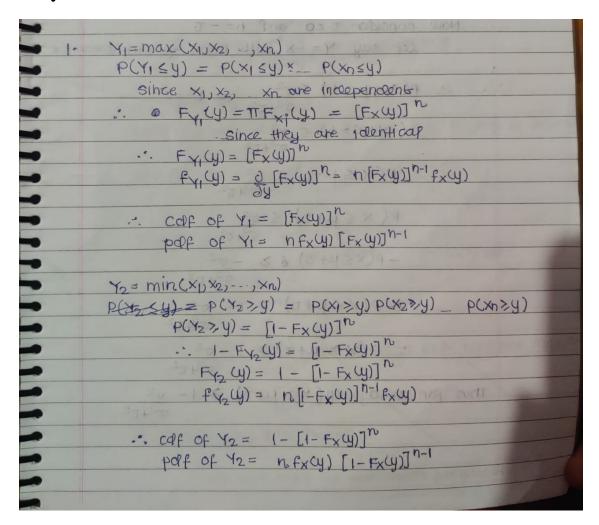
# Assignment 1: CS 215

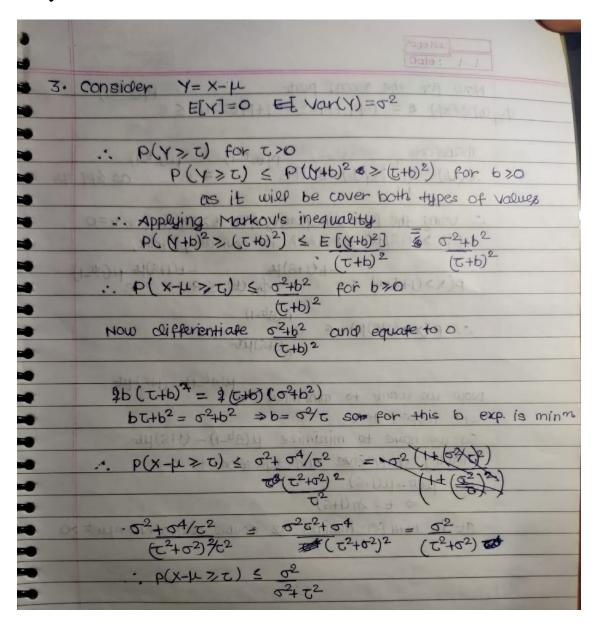
# $\begin{array}{ccc} {\bf 190050113} \ {\rm Shivam} \ {\rm Raj} & {\bf 190050080} \ {\rm Pawan} \ {\rm Kumar} \\ {\bf 190020010} \ {\rm Aman} \ {\rm Singh} \end{array}$

#### September 14, 2020

#### Contents

1	Question 1	2
2	Question 2	3
3	Question 3	3
4	Question 4	5
5	Question 5	8
6	Question 6	15
7	Question 7	15





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. for any random variable and 5701	
P(X-4 > t) \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	
54 bb 52	
Now consider to and b=-t	
let say Y = -x with mean - \mu and raniance \si	
(h30x)d = 6(x3x)d = (h31x)d	
$P(Y+\mu > b) \leq \sigma^{2}$ $\sigma^{2}+\tau^{2}$ $P(-X+\mu > b) \leq \sigma^{2}+\tau^{2}$	
1 ( ( ) 52+ 52 = ( ) 52 + 52 = ( ) 3 = ( )	
P (+x+42b) 5 52	
$\frac{1}{2} \left( b \left( x \leq h - p \right) \leq \frac{a_3 + c_5}{2}$	-
10-+C2	6
P(x < 4+0) < 52	
$P(x \leq \mu + \tau) \leq \sigma^2$	-
$-P(X \leq \mu + \tau) \neq \gamma - \sigma^2$	
52+52	
1-p(x<\u+c) > 1+ 02 (1)	(
1 [ (h) × 4 - 1   = (h \(\sigma_2 + \sigma_2 + \sigma_2 \)	
: P(X > µ+z) > 1-52	
1 (D) A - 11 - 1 - (D) 07+c2	
Thus for to <0, P(X > 1+t) > 1- 52	0
72+72	0
HID -1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1	-
+0 1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -	-
1 10 104	

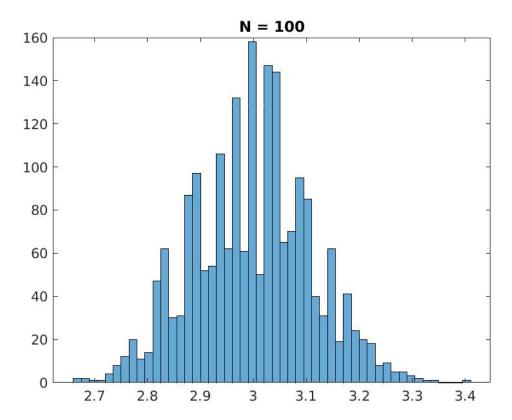
efect
A ROBERTON .
For t <0
For continuous, $\phi_{x}(t) = \int_{-\infty}^{\infty} e^{+tx} f_{x}(x) dx > \int_{-\infty}^{\infty} e^{+tx} f_{x}(x) dx$
φ <sub>x</sub> ( <del>tt</del> ) - <del>1</del> - <del>0</del> 0
if t<0, e+tx1 > e+tx2 ip x1 < x2
12 400)
(1) = 0 xo fx (x) dx = 6 xo fx (x) dx
$\therefore \phi_{x}(t) \geqslant \int_{\infty}^{x_{0}} e^{tx} f_{x}(x) dx \geqslant \int_{\infty}^{x_{0}} e^{x_{0}t} f_{x}(x) dx$
$\frac{1}{100} \frac{1}{100} \frac{1}$
· φ <sub>x</sub> (t) / ε - ελοφ <sub>y</sub> (t)
THE PORT OF THE PROPERTY OF TH
For discrete, no xit p(x=xi)
For discrete, $n$ part $p(x=xi)$ $ \frac{dy}{dx}(t) = \frac{1}{2} e^{xit} p(x=xi) $
XOTALL VIDEO VICXO
φ <sub>x</sub> (t) = 7 ≤ e <sup>xot</sup> p(x=x <sub>j</sub> ) where x <sub>j</sub> ≤ x <sub>o</sub> because if t < 0, e <sup>xot</sup> ≤ e <sup>xjt</sup>
the city and an all
φx(th) > e xot p(x ≤ xo)
ψx (8) 2 E P (3 (3 (0))
p(x ≤ x0) ≤ e-tx0 (x (4))
als is and fix=xid tax s (1) x

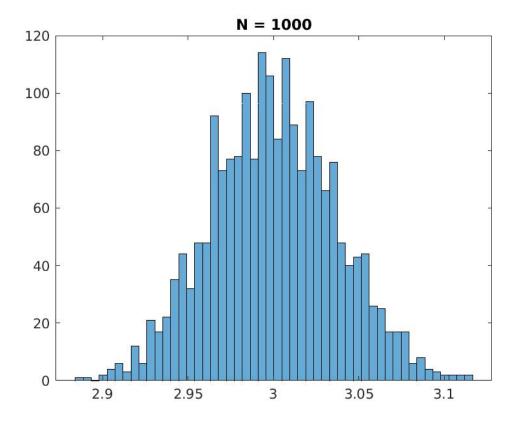
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Now for the second part

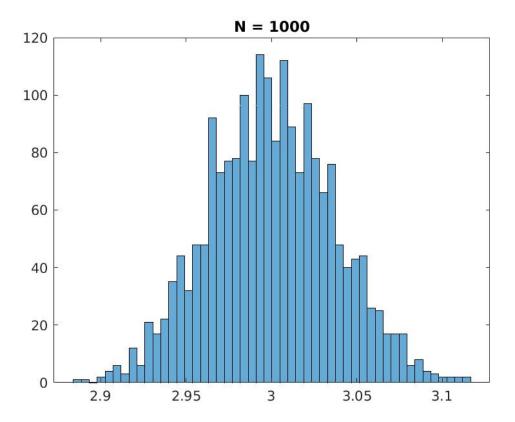
\phi_{x_i}(t)

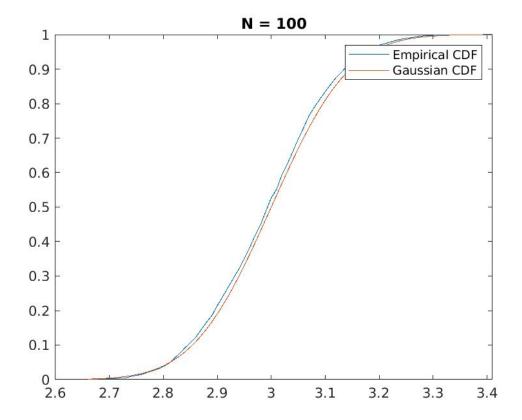
\phi_{x_i}(t)
                            .. using the first inequality for t>0, as for t=0
                                  p(x>(1+8) \mu) \le 1 which is obviously true,
                                    -\frac{1}{2}(1+8)\mu -\frac{1
                                  Now we want to minimize e (1+6) put
                                      with respect to t
                                           so we have to minimize \mu(e^{t}-1)-(1+8)\mu t
                                            Taking derivative and equation to 0
                                                     met=mu+s)
                                                                                   => t=ln(1+s)
                                                      It is minifor minima as double derivative = met >0
```

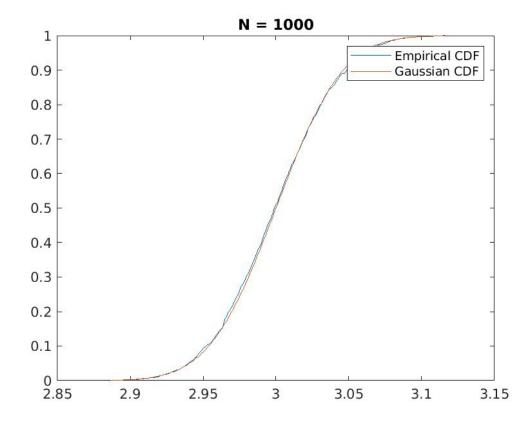
Code for this qsn is in file named 'q5.m'

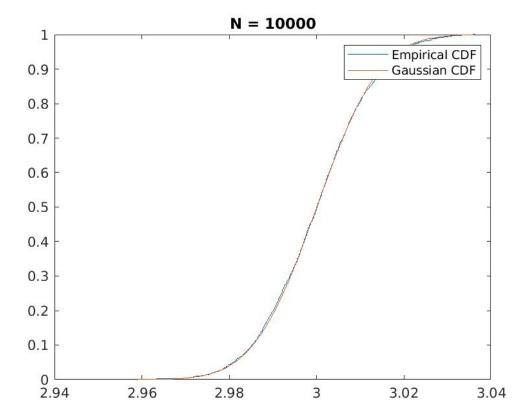


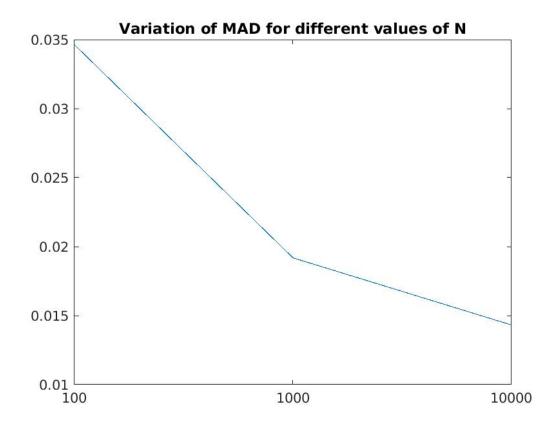


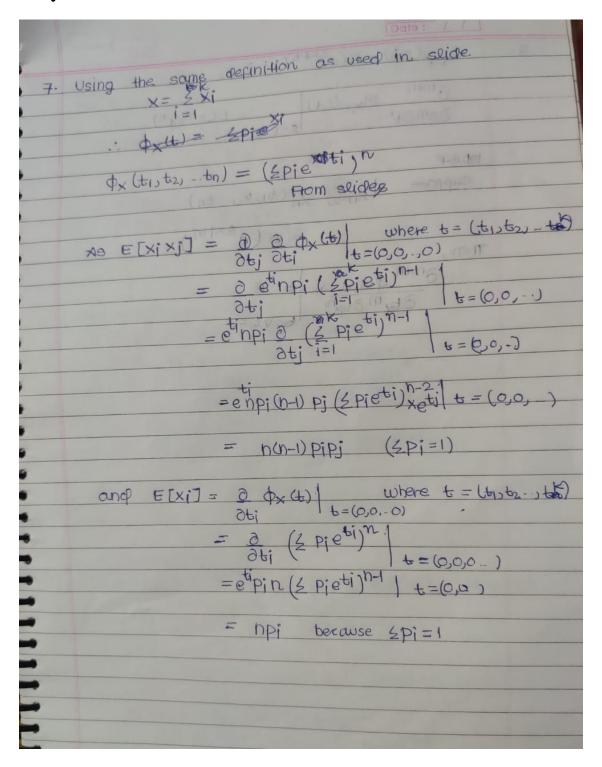












```
E[X_i^2] = \frac{\partial^2}{\partial t_i^2} \Phi_X(t_i) \Big|_{t=(0,0...)}
where t=(t_1,t_2,...,t_k)
= \frac{\partial^2}{\partial t_i^2} (\angle P_i e^{t_i})^{t_i}
                                                                     = \frac{\partial^{2}}{\partial t_{i}^{2}} \left( \neq p_{i} e^{t_{i}} \right)^{n-1} \times e^{t_{i}}
= \frac{\partial^{2}}{\partial t_{i}^{2}} \left( \neq p_{i} e^{t_{i}} \right)^{n-1} \times e^{t_{i}^{2}}
= \frac{\partial^{2}}{\partial t_{i}^{2}} \left( \neq p_{i} e^{t_{i}^{2}} \right)^{n-1} + p_{i} n e^{t_{i}^{2}} (n-1) \left( \neq p_{i} e^{t_{i}^{2}} \right)^{n-2}
= \frac{\partial^{2}}{\partial t_{i}^{2}} \left( \neq p_{i} e^{t_{i}^{2}} \right)^{n-1} + p_{i} n e^{t_{i}^{2}} (n-1) \left( \neq p_{i} e^{t_{i}^{2}} \right)^{n-1} \right)
= \frac{\partial^{2}}{\partial t_{i}^{2}} \left( \neq p_{i} e^{t_{i}^{2}} \right)^{n-1} \times e^{t_{i}^{2}} \left( \neq p_{i} e^{t_{i}^{2}} \right)^{n-1} 
= \frac{\partial^{2}}{\partial t_{i}^{2}} \left( \neq p_{i} e^{t_{i}^{2}} \right)^{n-1} \times e^{t_{i}^{2}} \left( \neq p_{i} e^{t_{i}^{2}} \right)^{n-1} + p_{i} n e^{t_{i}^{2}} \left( p_{i} e^{t_{i}^{2}} \right)^{n-1} \times e^{t_{i}^{2}} \left( p_{i} e^{t_{i}^{2}} \right)^{n-1} + p_{i} n e^{t_{i}^{2}} \left( p_{i} e^{t_{i}^
                                                                 = 2 (z pieti)"

= 2 pin(z pieti)"-1 xeti

2 dti
         .. COVOLITORICE .
              COV(X_i, X_i) = E[X_i^2] - (E[X_i])^2
                     COV(X_i)X_j) = E[X_iX_j] - E[X_i]E[X_j]
                            Therefore motifix is
                                              np1(1-p1) -np1p2
                                                   -np2P1 np2(1-p2)
                                                      - nP3P1 - nP3P2
```

Page 16