

G. H. RAISONI COLLEGE OF ENGG., NAGPUR
(An Autonomous Institute under UGC Act 1956)
Department of Computer Science & Engg.

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Practical Subject: Design and Analysis of Algorithms
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Student Details:

Roll Number	58
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Semester	3
Section	A
Branch	Artificial Intelligence

Practical Details: Practical Number- 10

Practical Aim	To implement and analyze time complexity of Single Source shortest path Algorithm: Bellman-ford.
Theory & Algorithm	<p>Theory:</p> <p><i>Bellman-Ford Algorithm:</i></p> <p>The Bellman-Ford algorithm is a graph search algorithm that finds the shortest path between a given source vertex and all other vertices in the graph. This algorithm can be used on both weighted and unweighted graphs.</p> <p>It is slower than Dijkstra's algorithm for the same problem, but more versatile, as it is capable of handling graphs in which some of the edge weights are negative numbers.</p>

	<p>Algorithm:</p> <p>Step 1: START</p> <p>Step 2: Initialize distances from the source to all vertices as infinite and distance to the source itself as 0.</p> <p>Step 3: For each edge a->b of the graph If $dis[b] > dis[a] + \text{weight of edge (a->b)}$ then $dis[b] = dis[a] + \text{weight of edge (a->b)}$</p> <p>Step 4: Repeat step 2 for $nv-1$ times (nv is no. of vertices).</p> <p>Step 5: If $dis[b] > dis[a] + \text{weight of edge (a->b)}$ then report a negative cycle in the graph.</p> <p>Step 6: STOP</p>
Complexity	Time Complexity of Bellman-Ford Algorithm is $O(VE)$.
Program	<pre> main.cpp 1 #include "iostream" 2 #include "vector" 3 4 using namespace std; 5 6 struct edge 7 { 8 int a, b, cost; 9 }; 10 11 int n, m, v; 12 vector<edge> e; 13 const int INF = 1000000000; 14 15 void solve() 16 { 17 vector<int> d (n, INF); 18 d[v] = 0; 19 while (true) { 20 bool any = false; 21 22 for (int j=0; j<m; ++j) 23 if (d[e[j].a] < INF) 24 if (d[e[j].b] > d[e[j].a] + e[j].cost) 25 { 26 d[e[j].b] = d[e[j].a] + e[j].cost; 27 any = true; 28 } 29 } </pre>

	<pre> 30 if (!any) break; 31 } 32 cout << "\n Final Cost of Vertices from Starting Vertice " << v << ": "; 33 for (auto x: d) { 34 cout << x << " "; 35 } 36 } 37 38 int main(int argc, char const *argv[]) { 39 int a, b, cost; 40 41 cout << "\n Name: Shivam Tawari"; 42 cout << "\n Roll no: A-58 Section: A"; 43 44 cout << "\n Enter Total Vertices: "; 45 cin >> n; 46 cout << " Enter Total Edges: "; 47 cin >> m; 48 49 for (int i=0; i<m; i++) { 50 cout << " Enter start, end and cost of edge " << i+1 << ": "; 51 cin >> a >> b >> cost; 52 e.push_back({a, b, cost}); 53 } 54 55 cout << " Enter starting vertex: "; 56 cin >> v; 57 58 solve(); 59 60 return 0; 61 } </pre>
<p>Output</p>	<pre> Name: Shivam Tawari Roll no: A-58 Section: A Enter Total Vertices: 2 Enter Total Edges: 4 Enter start, end and cost of edge 1: 2 3 6 Enter start, end and cost of edge 2: 4 9 2 Enter start, end and cost of edge 3: 6 2 6 Enter start, end and cost of edge 4: 3 7 8 Enter starting vertex: 2 Final Cost of Vertices from Starting Vertice 2: 1000000000 1000000000 </pre>