

- Aim: Write a program in R for implementing Linear Regression.

- Theory:

A linear regression is one of the easiest statistical models in machine learning. It is used to show the linear relationship between a dependent variable and one or more independent variables.

### Regression:

Regression Analysis is a form of predictive modelling technique which investigates the relationship between a dependent and an independent variable.

There are 3 types of regression:-

- 1) Linear Regression
- 2) Logistic Regression
- 3) Polynomial Regression

### Least Squares Method:

In this case, linear regression assumes that there exists a linear relationship between the response variable and the explanatory variables.

Least squares is a statistical method used to determine the best fit line or the regression line by minimizing the sum of squares created by a mathematical fn.

The "square" here refers to squaring the distance between a data point and the regression line.

The line with the minimum value of the sum of square is the best-fit regression line.

The line with the minimum value of the sum of square is the best fit regression line. Equation of regression line in simplest form:

$$y = mx + c \quad \text{where,}$$

$y$  = Dependent variable

$x$  = Independent variable

$c$  =  $y$ -intercept

In general,

$$h_0(x) = \sum_{i=0}^n \theta_i x_i$$

where  $h_0(x)$  is the hypothesis fn.

$\theta_i$  are the parameters

$x_i$  are the feature variables with

$$x_0 = 1$$



- `lm()` function:

This function creates the relationship model between the predictor and the response variable.

Syntax:

The basic syntax for `lm()` function in linear regression:

- formula is a symbol presenting the relation between  $x$  and  $y$ .
- data is the vector on which the formula applied.

- `predict()` function:

`predict(object, newdata)`

- object is the formula which is already created using `lm()` function.
- newdata is the vector containing the new value for predictor variable.

Code:

```
## Example 1: Predicting weight of a person  
## when height is known  
x <- c(151, 174, 138, 186, 128, 136, 179, 163, 152, 135)  
y <- c(63, 81, 56, 91, 47, 57, 76, 72, 62, 48)  
relation <- lm(y ~ x)  
print(relation)  
print(summary(relation, a))
```

⇒ Output: 076.22869

```
## Example 2: Calculate height of a child  
## if age is given.
```

```
install.packages("readxl")  
library(readxl)
```

```
ageandht <- read_excel("ageandheight2.xls",  
                        sheet = "Hoja2")
```

```
lmheight <- lm(height ~ age, data = ageandht)
```

```
str(ageandht)
```

```
names(ageandht)
```

```
summary(lmheight)
```



⇒ Output :

	Estimate	Std.	Error
(Intercept)	4.9283		0.5084
Age	0.6350		0.0214

## Example 3: Income and happiness dataset

```
install.packages("ggplot2")
```

```
install.packages("dplyr")
```

```
install.packages("broom")
```

```
install.packages("ggpubr")
```

```
install.packages("readxl")
```

```
library(ggplot2)
```

```
library(dplyr)
```

```
library(broom)
```

```
library(ggpubr)
```

```
library(readxl)
```

```
income <- read_excel("income2.xls", sheet = "income")  
summary(income)
```

```
hist(income$happiness)
```

```
plot(happiness ~ income, data = income)
```

```
income.happiness.lm <- lm(happiness ~ income,  
                           data = income)
```

`summary (income . happiness . lm)`

`predict (income . happiness . lm, data.frame (income = 7.95))`

⇒ Output : 5.88

Conclusion : Hence , implemented Linear regression in R .

## Code:

```
Practical 6.R x  Untitled2* x  Untitled3* x
1 ## Practical 6: Shivam Tawari (A-58)
2 ## Example 1
3 x <- c(151, 174, 138, 186, 128, 136, 179, 163, 152, 131)
4 y <- c(63, 81, 56, 91, 47, 57, 76, 72, 62, 48)
5
6 relation <- lm(y~x)
7
8 print(relation)
9 print(summary(relation))
10
11 a <- data.frame(x=170)
12 print(predict(relation,a))
13
14
15
13:1 (Top Level)  R Script
```

## Output:

```
> ## Practical 6: Shivam Tawari (A-58)
> ## Example 1
> x <- c(151, 174, 138, 186, 128, 136, 179, 163, 152, 131)
> y <- c(63, 81, 56, 91, 47, 57, 76, 72, 62, 48)
>
> relation <- lm(y~x)
>
> print(relation)

Call:
lm(formula = y ~ x)

Coefficients:
(Intercept)          x
   -38.4551         0.6746

> print(summary(relation))

Call:
lm(formula = y ~ x)

Residuals:
    Min       1Q   Median       3Q      Max
-6.3002 -1.6629  0.0412  1.8944  3.9775

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept) -38.45509    8.04901  -4.778  0.00139 **
x             0.67461    0.05191  12.997 1.16e-06 ***

Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 3.253 on 8 degrees of freedom
Multiple R-squared:  0.9548,    Adjusted R-squared:  0.9491
F-statistic: 168.9 on 1 and 8 DF,  p-value: 1.164e-06

>
> a <- data.frame(x=170)
> print(predict(relation,a))
      1
76.22869
```

## Code:

```
15 ##Example 2
16 install.packages("readxl")
17 library(readxl)
18
19 ageandht <- read_excel('ageandheight2.xls', sheet='Hoja2')
20 lmheight <- lm(height~age, data=ageandht)
21
22 str(ageandht)
23 names(ageandht)
24 summary(lmheight)
25
```

## Output:

```
> summary(lmheight)

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)  64.9283      0.5084   127.7 < 2e-16 ***
age           0.6350      0.0214    29.7  4.4e-11 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

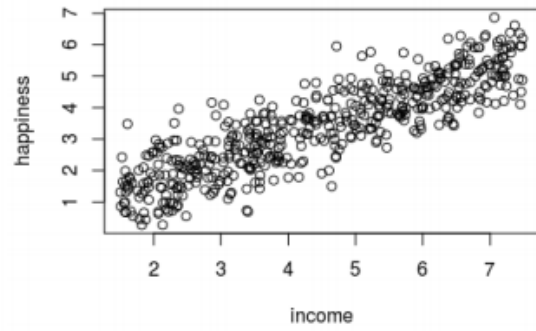
Residual standard error: 0.256 on 10 degrees of freedom
Multiple R-squared:  0.989,    Adjusted R-squared:  0.988
F-statistic: 880 on 1 and 10 DF,  p-value: 4.43e-11
```

## Code:

```
26 ##Example 3
27 install.packages("ggplot2")
28 install.packages("dplyr")
29 install.packages("broom")
30 install.packages("ggpubr")
31 install.packages("readxl")
32
33 library(ggplot2)
34 library(dplyr)
35 library(broom)
36 library(ggpubr)
37 library(readxl)
38
39 income <- read_excel("income2.xls", sheet='income')
40 summary(income)
41
42 hist(income$happiness)
43
44 plot(happiness~income, data=income)
45
46 income.happiness.lm <- lm(happiness~income, data=income)
47 summary(income.happiness.lm)
48
49 a <- data.frame(income=7.95)
50 predict(income.happiness.lm, a)
```



## Output:



```
> a <- data.frame(income=7.95)
> predict(income.happiness.lm, a)
      1
5.88
> |
```

