

G. H. Raison College of Engineering, Nagpur

(An Autonomous Institution)

2020-2021 ODD TERM**CAE-2 EXAMINATION FOR SPLIT-II COURSES WINTER-2020 (ONLINE MODE)****Third Semester B.Tech. Artificial Intelligence****Discrete Mathematics****Time: 1 hr.]****[Max. Marks : 15**

- 1) [CO1/CO2/CO...] indicates the question related to specific course outcome.
- 2) All questions carry marks as indicated
- 3) Assume suitable data wherever necessary.
- 4) Due credit will be given to neatness and adequate dimensions.
- 5) Illustrate your answer wherever necessary with the help of neat sketches.
- 6) Use of non-programmable calculator is permitted.

CO.2 (1) Let $(G, *)$ be a group and $a, b \in G$. Suppose that $a * b = b * a^{-1}$ and $b * a = a * b^{-1}$, then show that $O(a) = O(b) = 4$ [5M]

CO.2 (2) Prove that the set of all matrices of the form $\begin{bmatrix} a & b \\ 0 & c \end{bmatrix}$, $ac \neq 0$, $a, b, c \in \mathbb{Q}$ with respect to multiplication is a non commutative group. [5M]

CO2 (3) In a group $(G, *)$ prove that

- (i) The inverse of the inverse of an element is equal to the element.
- (ii) The inverse of the product of two elements is the product of the inverse in reverse order. [5M]