

Majority Element



$$\frac{6}{\cancel{3}} \rightarrow 4$$

$\Rightarrow 3, 3, 4, 2, 4, 4, 2, 4, 4$

O(1)
Space

Sort

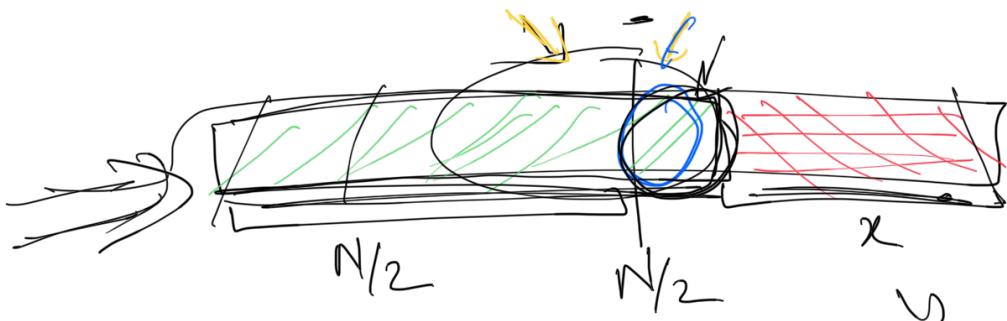
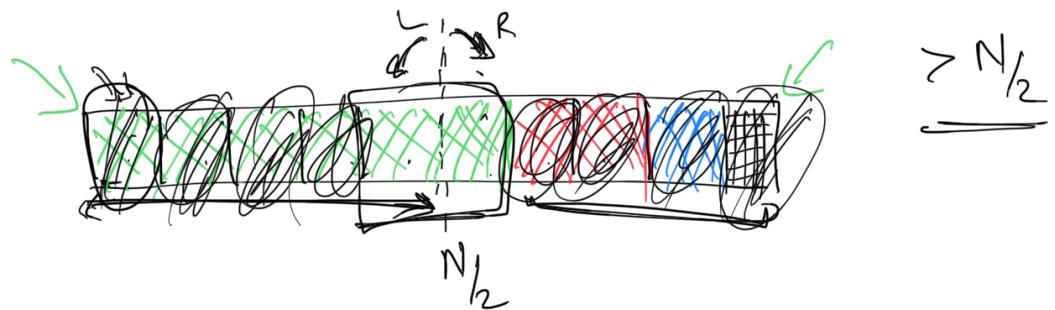
- - - 2 2 1 1 . . .

$\Rightarrow \underline{2, 2, 2, 2}, \underline{4, 4, 4, 4, 4}$

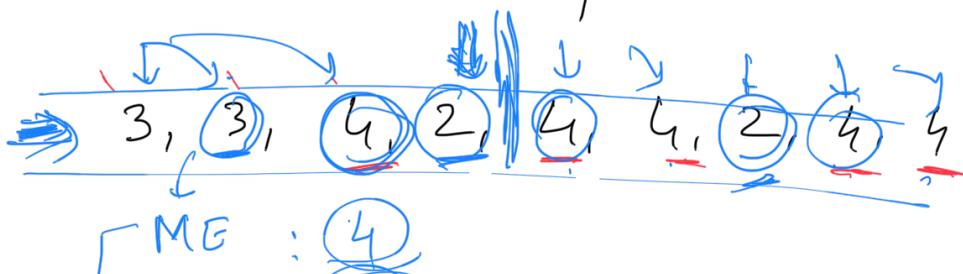
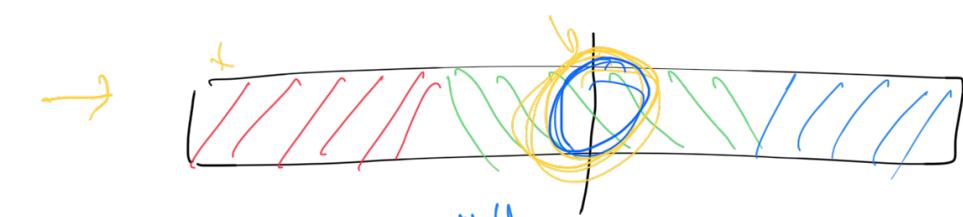
$N \log N$ $O(1)$

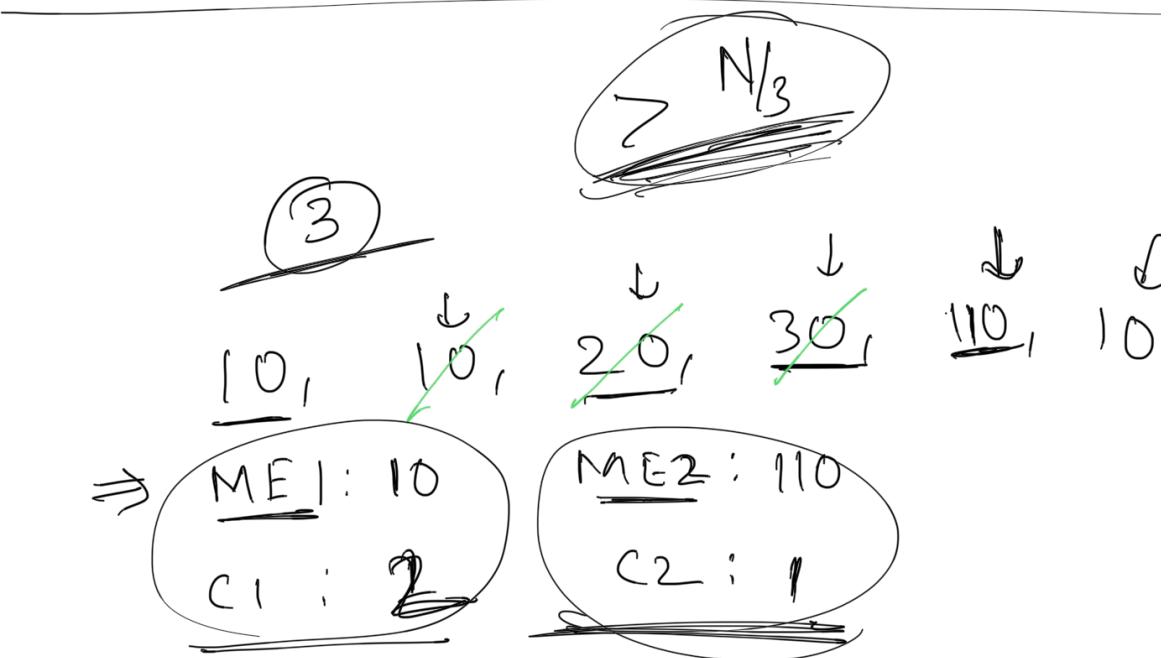
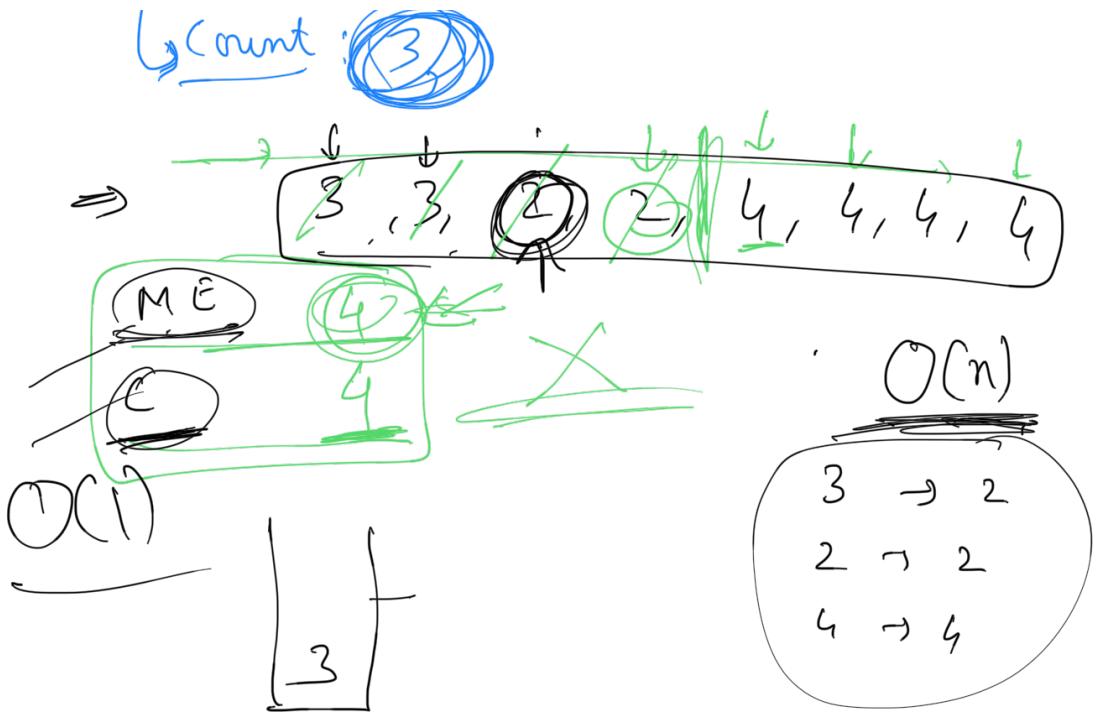
$O(N)$ $O(1)$

3, 3, 4, 2, 4, 4, 2, 4, 9, 4



$x < N$





Size of array = N

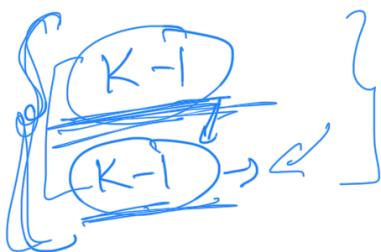
Min count of ME = $\frac{\text{Size}}{2} + 1$

$\Rightarrow \frac{N}{2} + 1$

$\Rightarrow C_{\min} - C_{\max}$

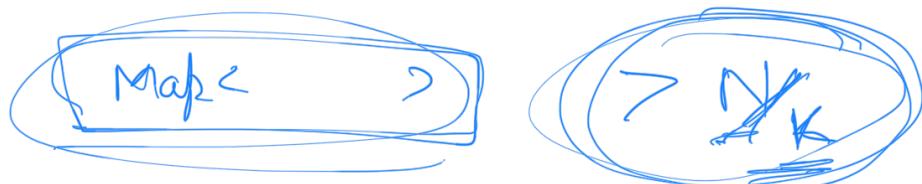
$$\rightarrow \alpha_{\text{avg}} = \frac{(N-1)}{2} \leftarrow$$

$$\frac{(N-2)}{2} + 1 \Rightarrow \frac{N}{2} = N/2$$



$$> N/2$$

$$> N/3$$



43	10	20	30	40
15	15	25	35	45
27		29	37	48
32		33	39	50

Diagram illustrating a step in the proof, showing a grid of numbers. Red arrows point from the top-left to the top-right and from the bottom-left to the bottom-right. Blue arrows point from the left to the right and from the top to the bottom. Labels include 43 , 10 , 20 , 30 , 40 , 15 , 25 , 35 , 45 , 27 , 32 , 33 , 39 , 48 , 50 , $A(0,0)$, 33 , 28 , and $\text{col} < 0 \text{ iff } n \geq m$.

n_1 n_2
 \downarrow
 $n+m$

$A(0) \{n-1\}$

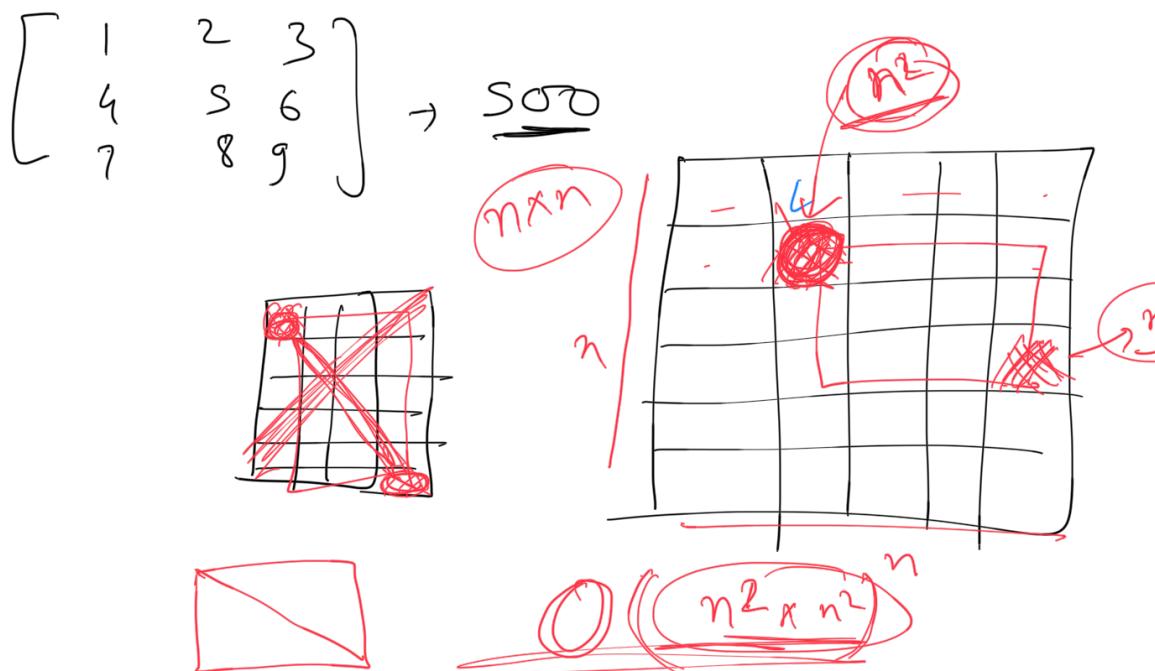
11

$$\left(\begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} \right) \quad \begin{bmatrix} (1) & (1) \\ (1) & (1) \end{bmatrix}$$

n

Sum of all possible sub-matrices

$$4 \times 1 + 4 \times 2 + 1 \times 4 = 16$$

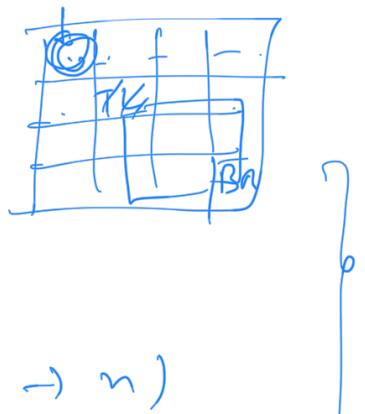


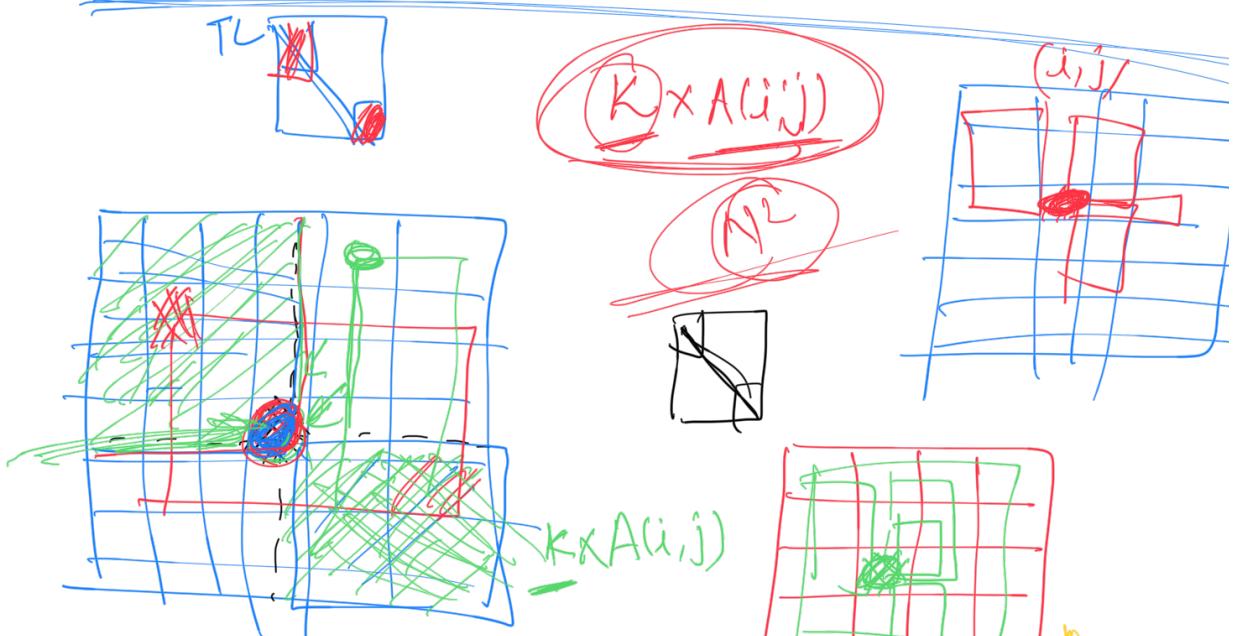
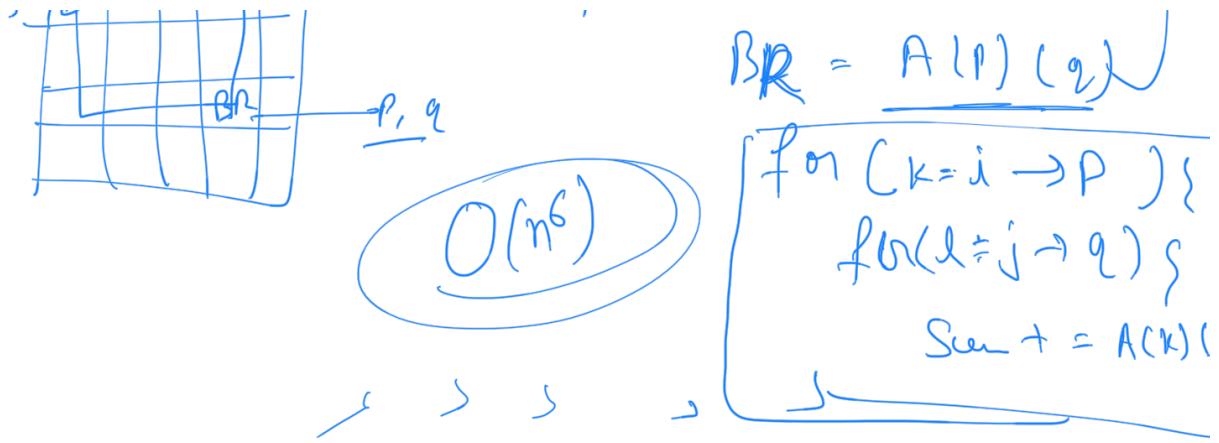
~~$O(n^4)$~~ ~~$O(n^2)$~~ $\rightarrow O(n^6)$

$\text{Sum} = 0$
 $\text{for}(i=0 \rightarrow n)$
 $\quad \text{for}(j=0 \rightarrow n) \{$
 $\quad \quad T_L = A(i)(j),$



$\quad \quad \text{for}(p=i \rightarrow n)$
 $\quad \quad \quad \text{for}(q=j \rightarrow n)$





$$\cancel{(P \times q)} \cap A(i)(j)$$

$$P = (x+1) \times (y+1)$$

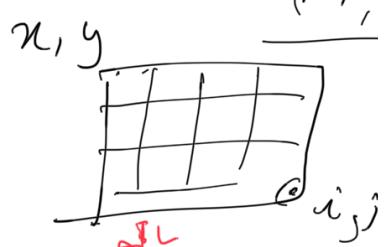
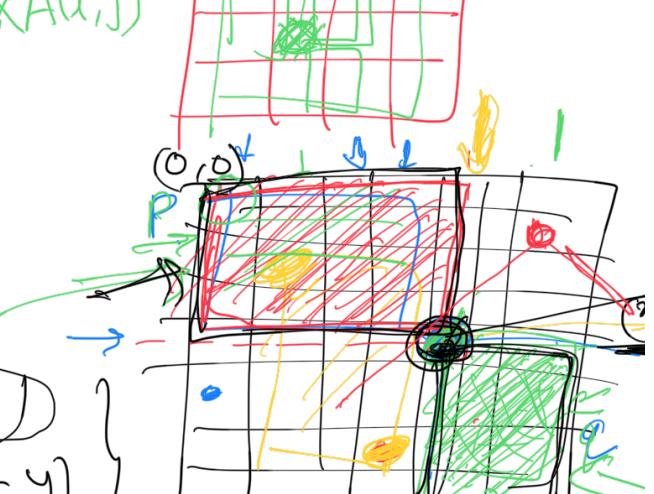
$$q = (n-x) \times (n-y)$$

0,0	0,1	0,2
1,0	1,1	1,2
2,0	2,1	2,2

$$x(2+1) \times (2+1)$$

= 9

for (i=0 → n) {



for ($j=0 \rightarrow n$) {
 $\text{No_TL} = (i+1) \times (j+1)$
 $\text{No_BR} = (n-i) \times (N-j)$
 $\text{Scen}^+ = \text{No_TL} \times \text{No_BR} \times A$