

## 1. Maximum Positivity:

Topic: Maths, Two pointer

We can use this problem using a single while loop:-

For all elements in array :-

1. If ith element is negative, we need to ignore it and go on next element
2. If ith element is non-negative, we will start a second while loop from this position until a negative element arrives.
  - a. If size of subarray received using this is greater than size of previous such arrays, then update the answer
  - b. else ignore it.

## 2. Area under the hills

Topic: Maths

This problem can be solved using 2 ways.

- I. for every next subsequent point there always are 2 regions: 1 rectangle and 1 triangle. You can see that every time min would be added as a rectangle and maximum-minimum would be added as triangle. Now base always remains 1. So you always add minimum + (maximum-minimum)/2 or (max+min)/2 for each consecutive point.
- II. You can use your observation to note that answer is always sum of numbers. Which can be proved from above argument.

Complete Solution:

```
string solve(vector<int> A)
{
    long long ans=0;
    for(int x:A)
        ans+=(long long) x;
    return to_string(ans);
}
```

### 3. Maximum Product

Topic:- Dp, array

Observation 1:- Maximum sum of all array would be always  $\leq 100000$ .

Observation 2:- Now, if we have all possible sums, our answer would be maximum of  $((\text{sums}) * (\text{total sum of array} - \text{sums}))$  where sum iterates over all possible sums.

To calculate all possible sums :-

To check whether a sum can be obtained by taking a subset of an array is nothing but subset sum problem and can be solved by dynamic programming, idea is :-

So it can be solved by taking a  $10^5$  boolean array dp. Here  $10^5$  is used for the sum of the elements of the array.

where  $dp[i]$  denotes whether sum  $i$  is possible or not. Initialize  $dp[i]$  for all  $i$  to be false/0. Base Case:  $dp[0] = 1$ . Recurrence is :  $dp[i] = dp[i - A[j]]$ , where  $j$  goes from 1 to  $N$  and  $i$  goes from  $10^5$  to  $A[j]$

#### 4. Mysterious Function

Topic: Number Theory(Euler Theorem)

Solution Approach:

If you were not able to solve this problem and did not know euler theorem, I would request you to first learn it and try again.

We know,

$$A^{\varphi(m)} \equiv 1 \pmod{m}$$

Implies we can write:

$$A^X \equiv A^{X \pmod{\varphi(m)}} \pmod{m}$$

Now, Question ask us to calculate  $A[1]^{A[2] \dots} \pmod{m}$

$$A[1]^{A[2] \dots} \pmod{m} \equiv A[1]^{A[2] \dots \pmod{\varphi(m)}} \pmod{m}$$

So problem reduces to calculate  $A[2]^{A[3] \dots} \pmod{\varphi(m)}$

**You can solve this recursively until there exist only 1 element.**

Complete Solution:

```
int phi[40004];
void precompute()
{
    if(phi[5]==4 and phi[3]==2 and phi[2]==1)
        return;
    phi[0]=phi[1]=0;
    for(int i=2;i<=40000;i++)
        phi[i]=i;
    for(int i=2;i<=40000;i++)
        if(phi[i]==i)
            for(int j=i;j<=40000;j+=i)
            {
```

```

        phi[j]/=i;
        phi[j]*=(i-1);
    }
}
int fast_power(int x, int y, int p)
{
    int res = 1; x %= p;
    while (y > 0)
    {
        if (y & 1)
            res = (res*x) % p;
        y>>=1;
        x = (x*x) % p;
    }
    return res;
}
int recursion(vector<int> &A,int m,int idx)
{
    if(m<=1)
        return 0;
    if(idx==0)
        return A[idx]%m;
    int x=recursion(A,phi[m],idx-1);
    return fast_power(A[idx],x,m);
}
int Solution::mysterious_function(vector<int> &A, int B)
{
    precompute();
    return recursion(A,B,A.size()-1);
}

```