

WELCOME!!

2 POINTERS

1) Different approaches

Intuition → Pseudo code
= Dry run

90-100 mins

DOUBT

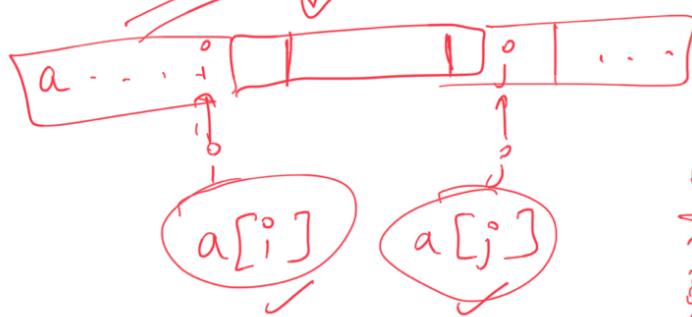
2 POINTERS

Technique

DS
AI
FW

stack
queue
Heap

ST..
Sorting
Binary Search



Arr^{ra}
→ SORTED → +ve numbers

$$Ex: [1, 4, \underline{5}, 6] \rightarrow K=9$$

① Count of pairs that sum up to K

B.F

array → a → size = n

```
for(i → 0 to n-1) {  
    for(j → i+1 to n-1) {
```

$\Theta(n^2)$

 $x = a[i]$

$$y = a[j]$$

if ($x+y == k$) \rightarrow count++

3 } return count

array Ag Ag

$$a_i^{\circ} < a_j^{\circ}$$

300

1

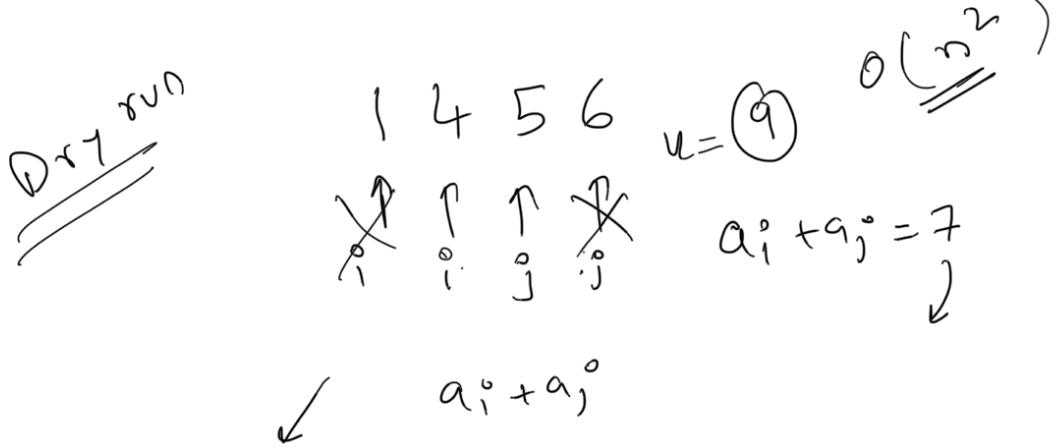
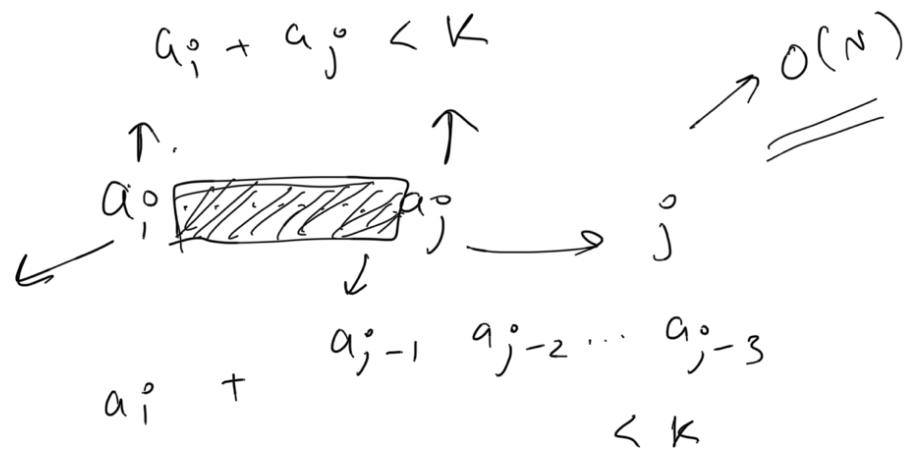
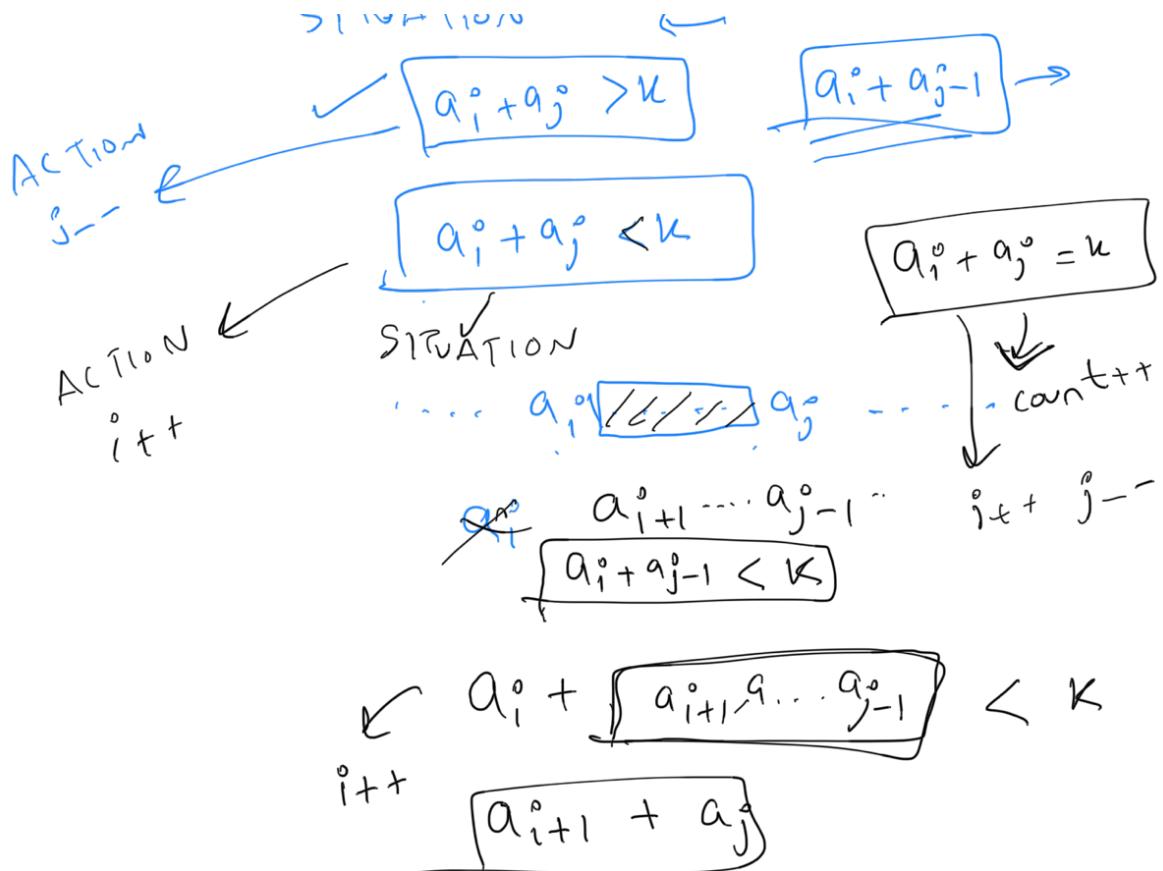
$$a_i + a_j > k$$

$$a_{i+1} + a_j > k$$

$$a_{i+1}^\circ, a_{i+2}^\circ, \dots, a_{j-1}^\circ$$

$\circ \rightarrow \circ$
 $\circ \rightarrow n - 1$

$a_0 \dots a_j$



$O(N)$

$$10 > 9$$

$$a_i + a_j = 9$$

Count = 1

Array $\rightarrow a$

$i \rightarrow 0$

$j \rightarrow n-1$

while ($i < j$) {

$x = a[i]$

$y = a[j]$

 if ($x+y > k$) $j--$

 else if ($x+y < k$) $i++$

 else { count++; }

}

Elements are not distinct

Example array $\{4, 4, 5, 5, 5, 6, 6, 1\}$ $k = 10$

$a \rightarrow \{4, 4, 5, 5, 5, 6, 6, 1\} \quad k = 10$

$(4, 6) \quad (4, 6')$

$(4', 6) \quad (4', 6')$

$(5, 5') \quad (5', 5'') \quad (5, 5'')$

$a_i + a_j > k \quad a_i + a_j < k$

$O(n^2)$

LAND PROBLEM

$O(1)$

$$a_i + a_j = k$$

$\frac{2}{2}$

[1 4 4 5 5 5 6 6 1 1]

$i \quad j$

$a_i + a_j = 10$

$\frac{\text{Count}(4's) = x}{\text{Count}(6's) = y}$

count i, j, our
 $O(1)$

$k = 10$ (3)

$$\boxed{x * y} \rightarrow \text{Count } t = \boxed{x * y}$$

$$i \rightarrow 5 5 5 \quad j \rightarrow \quad \rightarrow x = \text{Count}(5's)$$

$$y = 3$$

$$\boxed{x * y = 9}$$

$$a_i + a_j = k$$

$$a_i \neq a_j$$

$$\left. \begin{array}{l} \text{Count } t = x * y \\ i \rightarrow \text{inc } x \\ j \rightarrow \text{dec } y \end{array} \right\}$$

$$a_i a_i a_i \dots a_j a_j a_j a_j$$

$x = 3$

$y = 4$

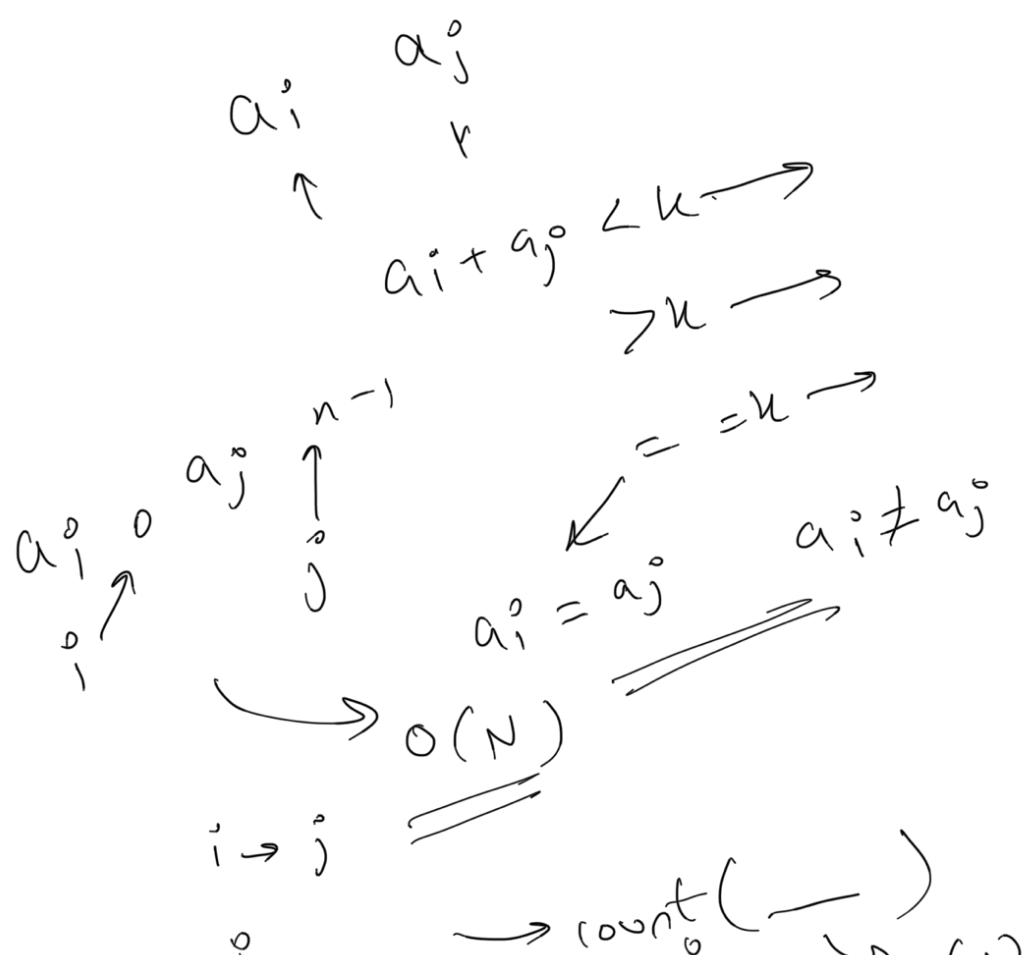
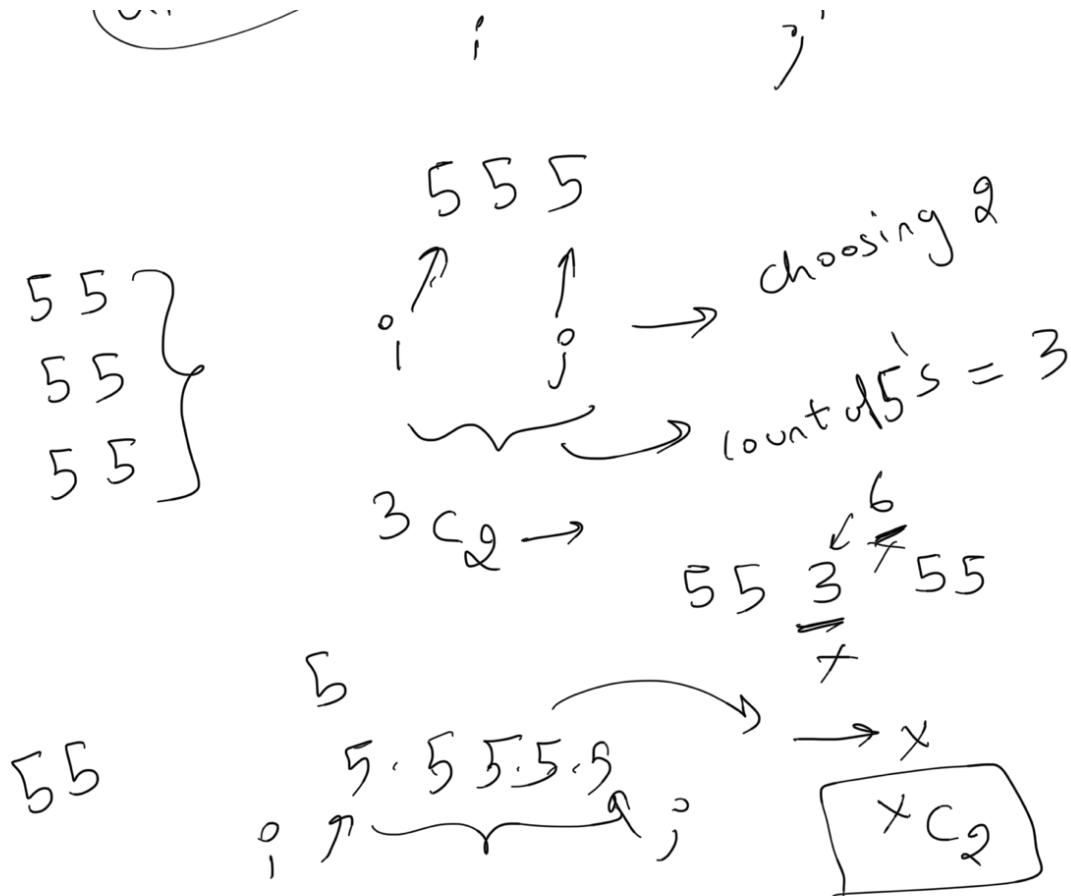
$$\text{array}$$

\uparrow

$a_i = a_j$

$$n - 1$$

$n - 1$



\downarrow \downarrow \downarrow \downarrow \downarrow
 5 5 5 5 5 $\rightarrow 10$

$\text{count}()$ $\text{count}()$
 $\Rightarrow b \underset{\neq}{\equiv} O(N)$ $a_i + a_j = 10$ $\underset{\neq}{\equiv} 5+5$
 $\Rightarrow i \rightarrow j \Rightarrow$

SORTED ARRAY

tve numbers $\rightarrow k$ $O(n-1)$

array $\rightarrow a$

Subarray $[i \dots j] \rightarrow$

true or false \rightarrow sums up to k

$\left(\begin{array}{c} \\ \text{B.F} \\ \end{array} \right)$ $[1 2 3 3 4 5 6] \quad k=10$ $\underset{\neq}{\equiv}$

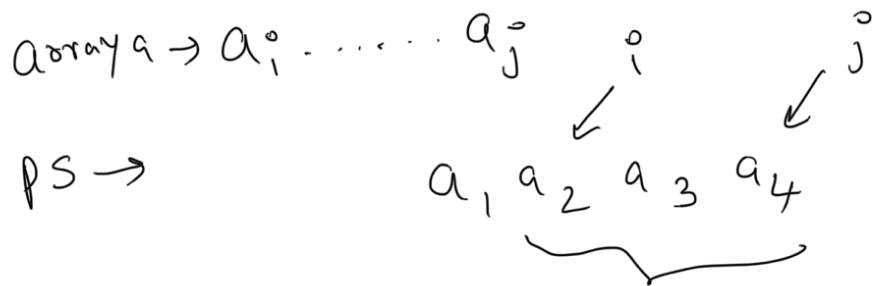
\hookrightarrow Find out all sub arrays

i j

$0, 0 1 \quad 0 2 \dots \dots \quad n-2, n-1$

$B.F$
 $T.C \rightarrow O(N^3)$ $O(N^2) \rightarrow [a_0 \dots a_j]$
 $O(N) \leftarrow$ is summing to k

$$i, j \rightarrow O(n^2) \quad (i, j) \rightarrow O(n)$$



$$PS[0] = a_1$$

$$PS[1] = a_1 + a_2$$

$$PS[3] - PS[0]$$

$$PS[2] = a_1 + a_2 + a_3$$

$$PS[3] = a_1 + a_2 + a_3 + a_4$$

$$\text{array } a \rightarrow a_1 \ a_2 \ \dots \ a_n$$

prefixsum $PS \rightarrow p_1 \ p_2 \ \dots \ p_n$

for ($a \rightarrow a_1 \text{ to } a_n$)
 $\text{sum} += a$
 $PS[\text{index}] = \text{sum}$
 $\text{index}++;$

$\text{sum} = 0$
 $\rightarrow O(N)$
 $\rightarrow O(N)$
 Extra Space.

$$B.F \rightarrow O(n^3)$$

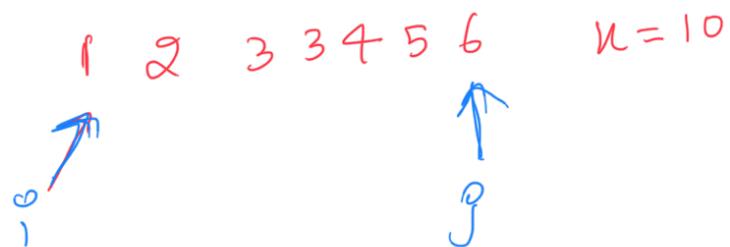
$$i, j \rightarrow O(n^2)$$

$$P.S. \ B.F \rightarrow$$

$$\sum[i..j] O(n)$$

$$\rightarrow O(1)$$

T.C $\underline{O(n)}$ S.C $O(n)$



$\text{Sum} = a_1 + a_2 + \dots + a_n$

$O(n)$ ← Sum
 $= \text{if } (\text{sum} < k)$

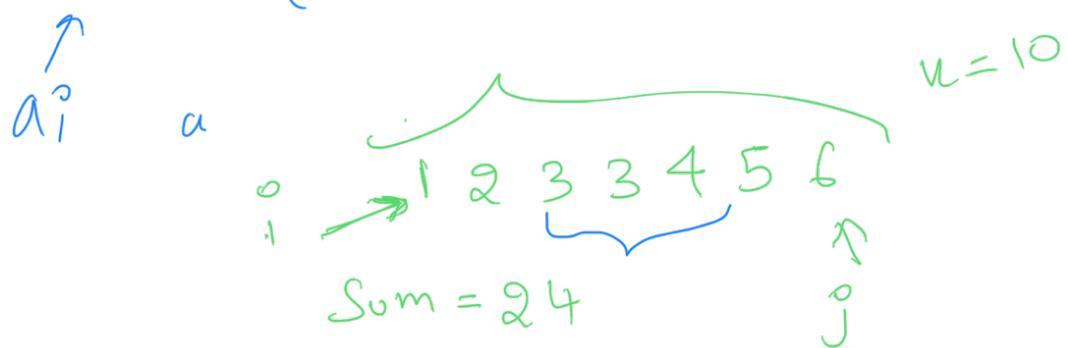
$i \rightarrow 0 \ j \rightarrow 0 \dots n-1$ → compute sum
Sum.

$i \rightarrow 0 \ j \rightarrow n-1$

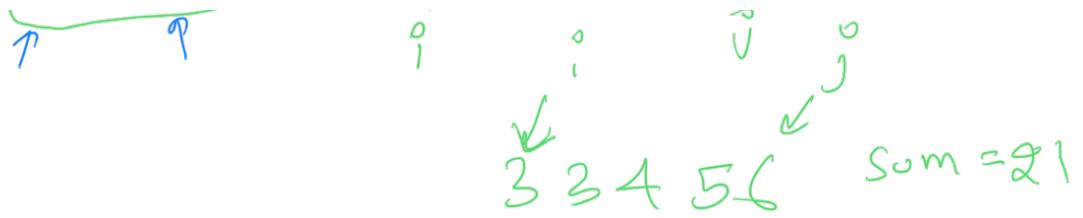
if ($\text{sum} < k$) return false;

if ($\text{sum} = k$) return true;

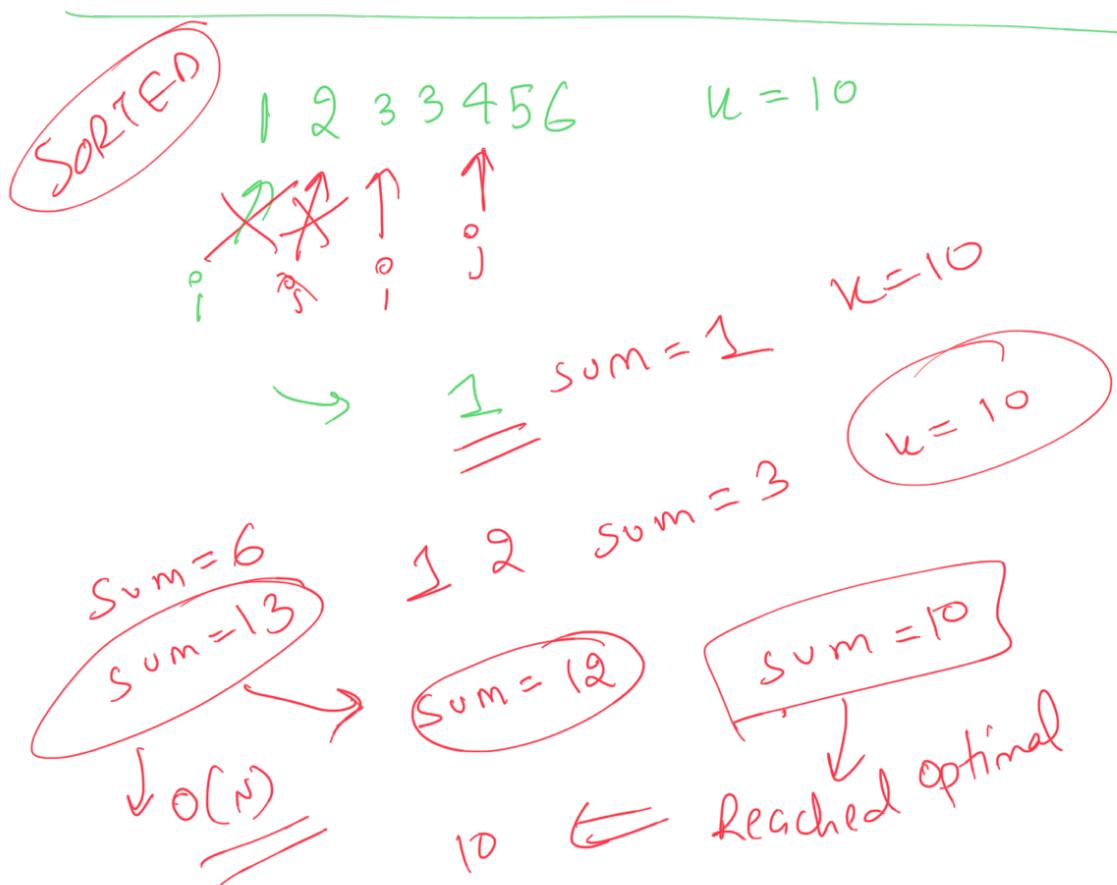
if ($\text{sum} > k$)



Sum = 24
 $k=23$ $2 \ 3 \ 3 \ 4 \ 5 \ 6$ Sum = 21
1 (2 3 3 4 5 6) ? ?



$\cdot 3 \ 4 \ 5 \ 6$
 $i = 1 \quad \quad \quad j = 4$



	T.C	S.C	
$\checkmark B.F$	$O(N^3)$	$O(1)$	$\rightarrow \text{True}$
$\checkmark P.F$	$O(N^2) \rightarrow O(N)$		
$2^{pts} O.A$	$O(N)$	$O(1)$	$\dots \text{Linear}$

~~Hashing~~

$a_i \rightarrow a_j$ sum $\leq k$
sum $\leq k$

1 0 4 [3 1 2] 0 5
~~1 0 4~~

$$\text{sum} = 6$$

6

$$\text{sum} = 9$$

if ($\text{sum} > k$)

if ($\text{sum} < k$) \rightarrow return false

problem

String \rightarrow characters

a a b a a b a

beauty(string)

number of contiguous
same characters

$K=0$

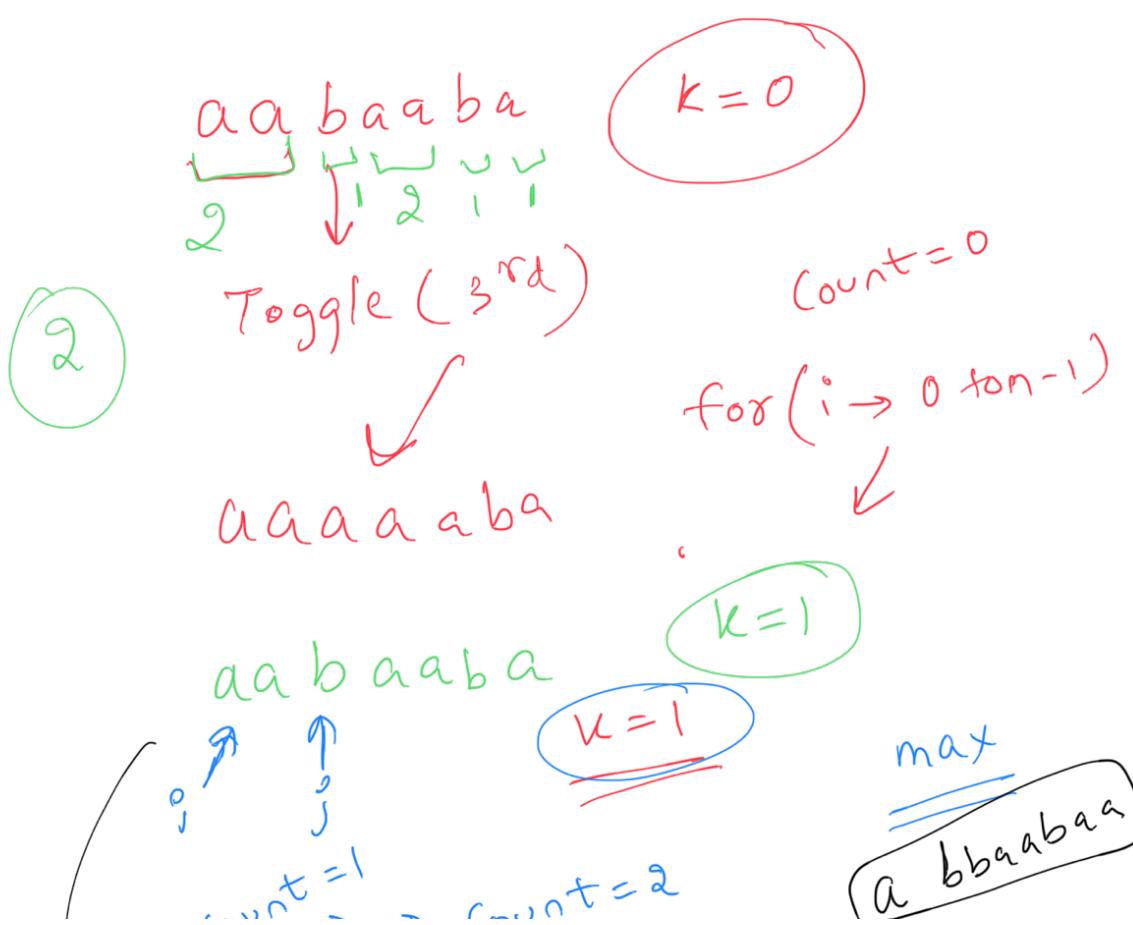
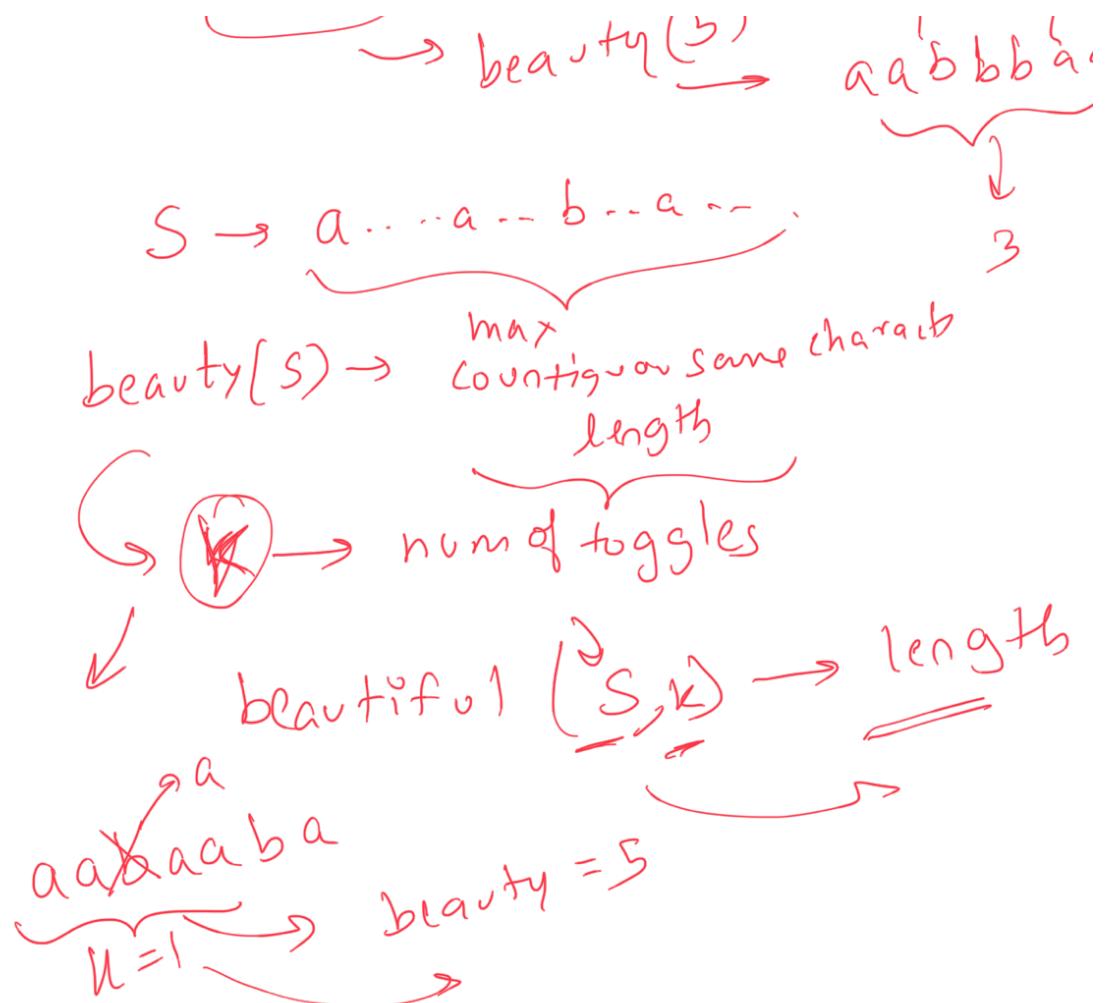
beauty(- 2)

Max bea

beauty

$\rightarrow K$ number of toggles

$K=1$



$\text{lo}^- \rightarrow \text{lo}^-$
 a a b a a b a
 | | | | | |
 ; ; ; ; ; ;
 $k = 0$
 $\text{count} = 3$
 $\text{count} = 4$
 $\text{count} = 5$

$\cancel{k=0}$
 a a b a a b a
 | | | | | |
 ; ; ; ; ; ;
 $\text{Count} = 5$
 $\cancel{\max = 5}$

$\cancel{k=1}$
 a a b a a b a
 | | | | | |
 ; ; ; ; ; ;
 \downarrow
 Toggled
 $k = 1$
 $\cancel{k = 0}$
 $\text{Count} = 3$

a a b a a b a
 | | | | | |
 ; ; ; ; ; ;
 $\text{Count} = 4$

$\cancel{\max = 5}$
 $\cancel{\text{Count} = 5}$
 a a b a a b a
 | | | | | |
 ; ; ; ; ; ;
 $\text{Count} = 5$

\downarrow
 APPROACH
 $\sim \text{DPBROACH}(\text{Toggled } b)$
 $\sim \text{DPBROACH}(\text{replaced } a)$

$$x_1 = APPROACH[10]$$

$$x_2 = APPROACH(\max(x_1, x_2))$$

$\frac{x_1}{\parallel} \quad \downarrow \quad \frac{\max(x_1, x_2)}{\parallel} \rightarrow O(n)$

String $S \downarrow$
 $a..aba$

$\frac{x=0}{\parallel}$ abbaabbaa ~~random~~
 $\frac{x=1}{\parallel}$ \downarrow random \downarrow
 $K = \text{Toggling} \rightarrow \text{NCE}$

aaababbaa
 $\frac{\cancel{a}}{1} \quad \frac{\cancel{a}}{2} \quad \frac{\cancel{b}}{3} \quad \frac{\cancel{b}}{4} \quad \frac{a}{5} \quad \frac{b}{6} \quad \frac{b}{7} \quad \frac{a}{8} \quad \frac{a}{9} \quad \frac{a}{10}$ $K=2$
 $\frac{a}{1} \quad \frac{a}{2} \quad \frac{b}{3} \quad \frac{b}{4} \quad \frac{a}{5} \quad \frac{b}{6} \quad \frac{a}{7} \quad \frac{b}{8} \quad \frac{a}{9} \quad \frac{a}{10}$
 $x_1 = APPROACH(\text{toggle } b)$
 $x_2 = APPROACH(t..a)$

$\frac{x_1}{\parallel} \quad \frac{\max(x_1, x_2)}{\parallel} \rightarrow O(N)$ Pseudo code
 $\frac{x_2}{\parallel}$

~~Doubts~~
 ↗ p1
 ↗ p2

String - S $k \rightarrow k$
~~beauty~~ \dots

~~beauty~~ (S, k)

beauty (String S, int k) {

$x_1 = \text{beautyUtil}(S, k, a)$

$x_2 = \text{beautyUtil}(S, k, b)$

return $\max(x_1, x_2)$.

}

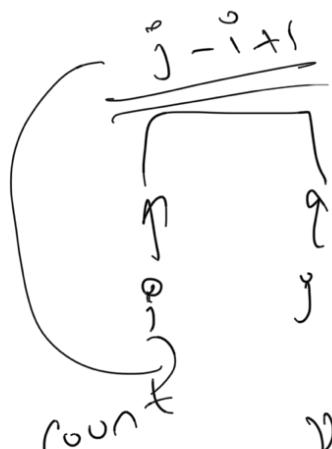
beauty Util (S, k, c)

$S \rightarrow \text{array} \rightarrow$
 $i \rightarrow 0$ count
 $j \rightarrow 0$ max
 $\text{toggles_used} \rightarrow 0$
~~for~~ ~~for~~ $\text{for}(j \dots) \{$


```

if (array[i] == c)
    ↓      equal to c
count++
if (array[j] != c)
    ↓
if (toggle-used < k)
    count++; toggle-used++
if (toggle-used == k)
    increment (i to the first)

```



Updating the max value

~~ij~~ ~~ll~~ ~~ll~~ ~~ll~~ ~~ll~~

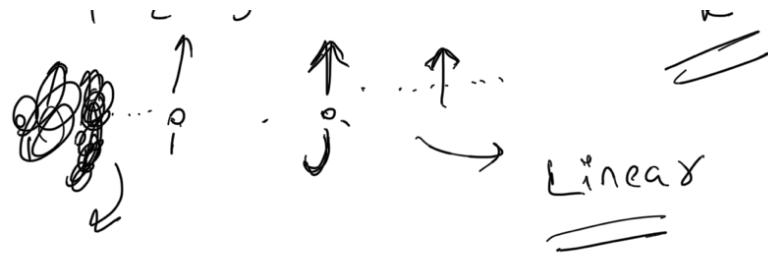
a a b a a a b b b b b b
 ↑ ↑ ↑ ↑ ↑ ↑
 i j l l l l
 $U=1$

a a b a a a b
P → i j P ↓
flipped ($b \rightarrow a$) → $\max = 5$

flipped ($a \rightarrow b$) → $\max = 2$

~~max = 6~~

a_1, a_2, \dots, a_n v



First probly

