

1. Let $A[0 : n-1]$ be an array of n distinct numbers. If $i < j$ (i and j are ordered indices) and $A[i] > A[j]$, then the pair $(a[i], a[j])$ is called an out of ordered pair of an array A . Write a program to count the out of ordered pair(s) of a given array. Implement an $O(n \log n)$ algorithm.

Input : $A = \{5, 9, 14, 25, 31, 45\}$

Output : 0

Input : $A = \{54044, 14108, 79294, 29649, 25260, 60660, 2995, 53777, 49689, 9083\}$

Output : 28

Input : $A = \{8, 7, 6, 5, 4, 3, 2, 1\}$

Output : 28

Input : $A = \{2, 4, 1, 3, 5\}$

Output : 3

Input: $A = \{1, 20, 6, 4, 5\}$

Output: 5

Input: $A = \{2, 3, 6, 9, 1\}$

Output: 4

Input : $A = \{1, 3, 5, 2, 4, 6\}$

Output : 3

Input : $A = 4, 3, 5, 2, 1)$

Output : 8

2. Suppose you are given an array $A[0 \dots n-1]$ of integers, some of the integers may be negative, zero, containing at least one positive integer. A sub-array $A[i, j]$ of A , where $0 \leq i \leq j < n$, is defined by the sequence $A[i], A[i + 1], \dots, A[j]$. Your task is to find the contiguous subarray (containing at least one integer) which has the largest sum. Write a program to implement an $O(n \log n)$ time algorithm.

Input :

The given array is : $\{8, 3, 8, -5, 4, 3, -4, 3, 5\}$

Output :

The largest sum of contiguous subarray is : 25 $(8+3+8+-5+4+3-4+3+5)$

Input :

The given array is : $\{-2, 1, -3, 4, -1, 2, 1, -5, 4\}$

Output :

The largest sum of contiguous subarray is : 6 $(4, -1, 2, 1)$

Input :

The given array is : $\{3, -5, 3, 8, 2, -4, 9, -6, 3, -2, -8, 3, -5, 1, 7, -9\}$

Output :

The largest sum of contiguous subarray is : 18 $(3, 8, 2, -4, 9)$

Input :

The given array is : $\{-2, 1, -3, 4, -1, 2, 1, -5, 4\}$

Output:

The largest sum of contiguous subarray is : 6 $(4, -1, 2, 1)$

Input :

The given array is : $\{1, 2, 3, 4, -10\}$

Output:

The largest sum of contiguous subarray is : 10 (1,2,3,4)

Input :

The given array is : { -1, 2, 3, -4, 5, 10 }

Output:

The largest sum of contiguous subarray is : 16 (2,3,-4,5,10)

3. You are given an unsorted array of n integers and an arbitrary integer k . Determine whether there is pair(s) of elements in the array that sums to exactly k . Array elements can be positive, negative, or zero and the pair should consist of two different array elements. Also count how many such pairs exist. For example, given the array [1, 3, 7] and $k = 8$, the answer is “yes,” but given $k = 6$ the answer is “no.” For example, if the given array is [3, 5, 2, -4, 8, 11] and $k = 7$, your program should return [[11, -4], [2, 5]] because $11 + -4 = 7$ and $2 + 5 = 7$. Write a program to implement an $O(n \log n)$ time algorithm to find all pair(s) with given sum in the array.

Input

The given array : {6, 8, 4, -5, 7, 9}

The given sum : 15

Output

(6, 9)

(8, 7)

Input

The given array : {-5, 1, -40, 20, 6, 8, 7}

The given sum : 15

Output

(7, 8)

(-5, 20)

Input

The given array : {-5, 4, -2, 16, 8, 9}

The given sum : 15

Output

There is no pair of elements whose sum is equal to 15

Input

The given array : {1, 5, 7, -1}

The given sum : 6

Output

(1, 5)

(7, -1)

Input

The given array : {1, 5, 7, -1, 5}

The given sum : 6

Output

(1, 5)

(7, -1)

(1, 5)

4. Given an unsorted array of integers containing duplicate elements. Your task is to find if there exist any integer x that appears more than $n/2$ times (if it exists) in an array $A[0...n-1]$ of size n , otherwise prints "No such integer"(there is at most one such element). **You are not allowed to sort the array.** No array can have more than one such integer. Write a program that implement an $O(n \log n)$ time algorithm.

Input :

The given array is : {1, 3, 3, 7, 4, 3, 2, 3, 3}

Output : 3

Input :

The given array is : {4, 8, 4, 6, 7, 4, 4, 8}

Output :

No such integer in the given array.

Input :

The given array is : {2, 3, 2, 3, 2, 3, 2, 3}

Output :

No such integer in the given array.

[count is = $n/2$ not $> n/2$, so neither 2 nor 3 is present more than $n/2$ times]