

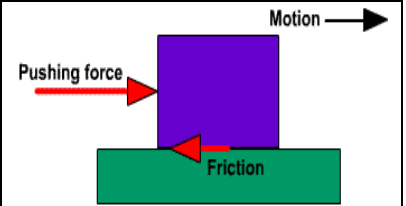
# 2. FRICTION

## TERMINOLOGIES IN FRICTION:

1. NORMAL REACTION ( $N$ ):
2. FORCE IN DIRECTION OF POSSIBLE MOTION ( $P$ ):
3. COEFFICIENT OF FRICTION ( $\mu$ ):

Static Friction Coefficient ( $\mu_s$ )	Kinetic or Dynamic Friction Coefficient ( $\mu_k$ )
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4. FRICTIONAL FORCE ( $f$ ):  $f = \mu N$



## DYNAMICS ANALYSIS

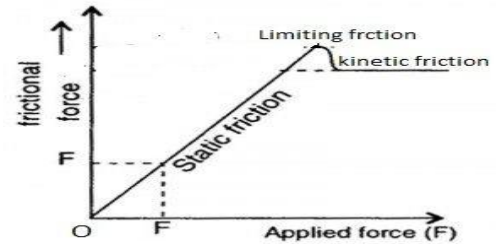
**KINEMATICS:** Without considering Force

**KINETICS:** With considering force

## LAW OF DRY FRICTION:

1. The frictional force opposes the relative motion. (Coulomb's Law Statement-I)
2. The frictional force acts tangential to the contact surfaces. (Coulomb's Law Statement-II)
3. The total friction developed doesn't depend upon the contact area.
4. The maximum friction in static case,  $f_{max} = \mu_s N = \text{Limiting Friction}$
5. Force required to sliding is greater than that is required to maintain sliding.  $\mu_s > \mu_k$

## GRAPHICAL REPRESENTATION OF FRICTIONAL FORCE:



## UNDERSTANDING THE FRICTIONAL FORCE:

If  $P \leq f_{max}$ ,  $f = P$ .

If  $P > f_{max}$ ,  $f = \mu_k N = \text{Constant and opposite to } P$

**Impending Condition:** Body is about to move but block hasn't started motion.  $P = f_{max}$

**Condition for Static Equilibrium:**  $\mu_s N \leq P$  or  $f \leq \mu_s N$

**When to use the limiting frictional force ( $f_{max}$ ):**

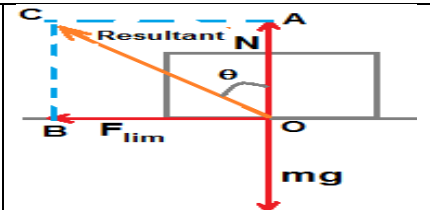
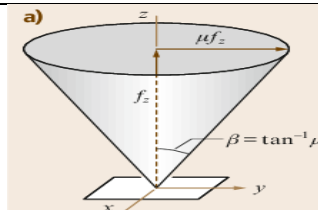
1. Limiting Friction
2. Impending Condition
3. Maximum Force for equilibrium
4. Minimum force to start motion (Force just to start motion)

## ANGLE OF FRICTION ( $\phi$ ):

$$R = \sqrt{N^2 + f^2} \quad \phi = \tan^{-1} \frac{f}{N}$$

**At Limiting Friction,**  $\phi = \tan^{-1} \mu_s$

**CONE OF FRICTION:** Cone generated with cone angle  $2\phi$  is known as cone of friction.



- Minimum force required to cause the motion in the block,  $F_{min} = W \sin \theta$ , Where  $\theta = \phi$

## BELT FRICTION:

$$\frac{T_1}{T_2} = e^{\mu\theta}$$

$\theta$  = Angle of contact,  
 $\mu$  = Friction between belt and friction,  
 $T_1$  &  $T_2$  = Tight side and slack side tension.

The side of belt which will try to create the motion or higher force is applied is the tight side.

- After deciding tight side and slack side we can decide the Force/ Tension is either minimum or maximum.

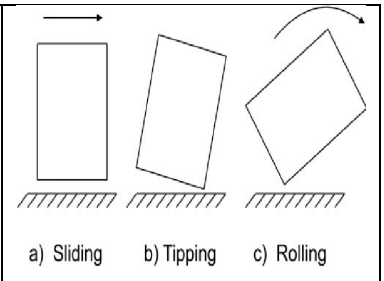
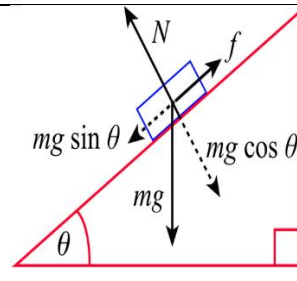
Sliding: Consider Equilibrium of forces.

Tipping: Consider Moment Equilibrium about tipping point.

For Inclined Block at  $\theta$  angle with self-weight,

$\theta < \phi$	$\theta = \phi$	$\theta > \phi$
Static Cond.	Impending Cond.	Motion
$f = P$	$f_{max} = \mu_s N$	$f_{max} = \mu_k N$

$\phi$  = Angle of friction.



**ANGLE OF REPOSE:** It's the angle at which block slides on any surface. E.g. For inclined surface  $\text{AOR} = \phi$

Min. and Max. force required to **stop sliding** the block on inclined surface found by changing the direction of friction.

Both are smooth (Unstable)	Wall is rough & floor is smooth (Unstable)	Floor is rough & Wall is smooth (stable)	Floor is rough & Wall is rough (stable)
Pythagoras Theorem	$\sum F = 0$	$\sum M_{@Rough Normal Reaction} = 0$	

Stability of inclined ladder increases including angle of inclination Because *Restoring Couple* = *Turning Couple*.