

9. SPUR GEAR DESIGN

GEAR: It's a toothed wheel used for transmission of power from one shaft to another.

| | | |
|------------------------|--|---------------------|
| TOOTH DIRECTION | In the direction of axis of wheel | SPUR GEAR |
| | Tooth is inclined with the axis of wheel | HELICAL GEAR |

Gear Pair is made of **GEAR** and **PINION**.

| | | |
|--|---|--|
| $m = \frac{d_p}{Z_p} = \frac{d_g}{Z_g}$ $d = \frac{d_p + d_g}{2} = \frac{m(Z_p + Z_g)}{2}$ | m = Module of Gear, d = Centre to centre Distance between two gears, | Z_p = No. of tooth on Pinion, Z_g = No. of tooth on Gear, d_p = Pinion Diameter (PCD), d_g = Gear Diameter (PCD), |
|--|---|--|

ASSUMPTIONS IN WILFRED LEWIS EQUATION:

1. At any point of time there will be only one pair of teeth in contact.
2. The tangential load (F_t) is distributed uniformly throughout the width.
3. The effect of radial load is neglected.
4. Consider Tooth as Beam of uniform strength.
5. Stress concentration effects are neglected.

| | | |
|---|---|---|
| <p><i>Circular Pitch</i> (p_c) = πm</p> <p>$M_{max} = F_t h$</p> <p>$\sigma_{max} = \left(\frac{M_{max}}{I}\right) y_{max} = \frac{6 F_t h}{b t^2}$</p> <p>$F_t = \sigma_{max} p_c b y = \sigma_{max} m b Y$</p> <p>$y = \frac{t^2}{6 h p_c}$ and $Y = \frac{t^2}{6 h m}$</p> <p>$Y = \pi y$</p> | <p>Lewis Factor depends on No. of tooth and profile of teeth.</p> <p>Y IS CLOSER OR GREATER THAN 0.3</p> <p>F_t = Uniform Tangential load, σ_{max} = Maximum bending Stress,</p> | <p>M_{max} = Maximum bending moment, h = Depth of teeth base, t = Thickness of teeth base, b = Width of teeth base, Y = Modified Lewis Form factor, y = Lewis Form factor,</p> |
|---|---|---|

EQUIVALENT LOAD ON TEETH:

| | | |
|--|--|--|
| <p>$Power\ P = \frac{2\pi N T}{60}$</p> <p>If $C_v \leq 1$,</p> <p>$T_{max} = \frac{C_s T}{C_v}$ And $F_{eq} = \frac{C_s F}{C_v}$</p> <p>If $C_v > 1$,</p> <p>$T_{max} = C_s C_v T$ And $F_{eq} = C_s C_v F$</p> | <p>C_s is used to incorporate Fluctuation of power transmission.</p> <p>C_v is used to incorporate Impact Load Due to power transmission</p> | <p>T = Mean Torque = $F r$ N = Mean Speed, F = Mean Tangential Load, T_{max} = Maximum Torque, C_s = Service Factor, C_v = Velocity Factor, F_{eq} = The Max. Tangential Load,</p> |
|--|--|--|

DESIGN CONDITION:

| | |
|--|--|
| <p>$\sigma_{max} = \sigma_{yt} / FOS$ And $F_{eq} = F$</p> <p>$\frac{C_s F}{C_v} = \frac{\sigma_{yt}}{FOS} m b Y$</p> | <p>$\sigma_{max}$ = Maximum bending Stress, σ_{yt} = Yield Strength of material,</p> |
|--|--|

WEAR STRENGTH (HERTZ THEORY):

Pitting: Surface Fatigue Failure due to repetitive loads.

| | |
|--|--|
| <p>Failure Condition: $\sigma_c > \sigma_e$</p> <p>$F_w = K d_p b Q$</p> <p>$K = \frac{\sigma_e^2 \sin \phi}{1.4} \left[\frac{1}{E_p} + \frac{1}{E_g} \right]$</p> <p>$Q = \frac{2Z_g}{Z_g - Z_p}$, for External Gear</p> <p>$Q = \frac{2Z_g}{Z_g + Z_p}$, for Internal Gear</p> | <p>K = Load Stress Factor, E_p = Young's Modulus of Pinion, E_g = Young's Modulus of Gear, Q = Ratio Factor, σ_c = Contact Stress, σ_e = Surface Endurance Strength of tooth material, F_w = Wear Strength = Maximum tangential load that can be applied to avoid pitting failure, ϕ = Pressure Angle,</p> |
|--|--|