

# 7. AVAILABILITY

**AVAILABLE ENERGY:** The maximum work which can be obtained in a cycle.

**UNAVAILABLE ENERGY:** The minimum heat which is rejected to the atmosphere.

**AVAILABILITY:** the maximum work which can be obtained in a process.

**IRREVERSIBILITY:** It's defined as difference between the maximum work and the actual work.

## METHODS TO IMPROVE CARNOT CYCLE EFFICIENCY:

INCREASING SOURCE TEMPERATURE	DECREASING SINK TEMPERATURE
Efficiency increase per unit increase in temperature is less in comparison.	Efficiency increase per unit increase in temperature is more. So, it's best method to increase efficiency of Carnot cycle.
It depends on working fluid and it's calorific value. So, maximum value increase with quality of working fluid.	It depends on minimum possible heat rejection temperature. E.g. $T_2 = T_{min} = T_{amb} = T_{sur} = T_{atm} = T_0$

## AVAILABLE ENERGY:

$\eta_{carnot} = 1 - T_2/T_1 = W_{max}/Q_1$	$\therefore \text{Available energy, } W_{max} = Q_1[1 - T_2/T_1] = Q_1 - Q_2$
It can be increase by decreasing $T_2$ temperature.	It can be increase by increasing $T_1$ temperature.
<b>1<sup>st</sup> Law of T.D. is Quantitative law.</b>	<b>2<sup>nd</sup> Law of T.D. is Qualitative law.</b>

## UNAVAILABLE ENERGY:

$\text{Unavailable energy} = \text{Heat Rejection Area on } T-S \text{ diagram} = [Q_2]_{min} = [T_2]_{min} \Delta S$	
$\therefore \text{Available energy, } W_{max} = Q_1 - Q_2 = Q_1 - \text{Unavailable Energy}$	$\therefore Q_1 = A.E. + U.A.E.$

## AVAILABLE ENERGY BETWEEN FINITE BODY & THERMAL RESERVOIR:

$Q_1 = A.E. + U.A.E.$ $A.E. = Q_1 - T_0 \Delta S$ $U.A.E. = [T_2]_{min} \Delta S = T_0 \Delta S$	$Q_1$ Always consider magnitude. $\Delta S$ will be negative but consider magnitude in this equation. $\Delta S = mC \ln[T_2/T_1]$	<table border="1"> <tr> <td><math>Q_1</math></td><td><math>T_1 \rightarrow T_2</math></td><td>Finite Body</td></tr> <tr> <td></td><td><math>HE</math></td><td><math>\rightarrow W_{net}</math></td></tr> <tr> <td><math>Q_2</math></td><td><math>T_0</math></td><td>Reservoir</td></tr> </table>	$Q_1$	$T_1 \rightarrow T_2$	Finite Body		$HE$	$\rightarrow W_{net}$	$Q_2$	$T_0$	Reservoir
$Q_1$	$T_1 \rightarrow T_2$	Finite Body									
	$HE$	$\rightarrow W_{net}$									
$Q_2$	$T_0$	Reservoir									

## LOSS OF A.E. OR DECREASING A.E. OR INCREASING U.A.E.:

$A.E._1 = Q_1[1 - T_0/T_1]$	$A.E._2 = Q_1[1 - T_0/T_2]$	Here, $T_1 > T_2$	Hence, $A.E._1 > A.E._2$
$\text{Loss of A.E.} = A.E._1 - A.E._2 = U.A.E._2 - U.A.E._1 = Q_1 T_0 [(1/T_2) - (1/T_1)]$			

**EXERGY:** The maximum useful work which can be obtained from a system as it reversibly comes into equilibrium with its environment. It is combined word used for A.E. & Availability.

**DEAD STATE:** It's state at which system and surroundings are in equilibrium.

## AVAILABILITY IN NON-FLOW PROCESS:

**CHANGE IN AVAILABILITY ( $W_{max}$ ):**  $W_{max} = (U_1 - U_2) - T_0(S_1 - S_2) - d(K.E.) - d(P.E.) = a_1 - a_2$

$\therefore$ N.F.E.E.: $Q = dE + W$	$E = KE + PE + U$	$Q_{Loss} = T_0 \Delta S$
-------------------------------------	-------------------	---------------------------

**AVAILABILITY/ WORK POTENTIAL AT A STATE "i":**  $a_i = (U_i - U_0) - T_0(S_i - S_0)$

Availability/ work ability at a state "i" is composite property (extensive) of system and surroundings.

<b>SURROUNDINGS WORK:</b>	$W_{sys} = P_{sys} dV$	$W_{surr} = -P_{surr} dV$	$dV_{sys} = dV_{surr} = dV$	$P_{sys} > P_{surr}$
---------------------------	------------------------	---------------------------	-----------------------------	----------------------

<b>MAXIMUM USEFUL WORK:</b>	$W_{useful} = W_{utilised} = W_{sys} - W_{surr}$	$[W_{useful}]_{max} = [W_{sys}]_{max=Rev.} - W_{surr}$
-----------------------------	--	--

**AVAILABILITY FUNCTION:**  $\phi_i = U_i - T_0 S_i + P_0 V_i$

$[W_{useful}]_{max} = W_{max} - W_{surr} = \phi_1 - \phi_2$	$W_{max} = (U_1 - U_2) - T_0(S_1 - S_2)$
---	--

## AVAILABILITY IN FLOW PROCESS:

### CHANGE IN AVAILABILITY ( $w_{max}$ ):

$$w_{max} = (h_1 - h_2) - T_0(s_1 - s_2) - (1/2)[V_1^2 - V_2^2] - g(z_1 - z_2) = b_1 - b_2$$

$\therefore$	S.F.E.E.	$q_{Loss}(\text{in J/kg}) = T_0 \Delta s$
--------------	----------	---

**SURROUNDINGS WORK:**  $w_{surr} = 0$  ( $\therefore$  No atmospheric resistance)

**MAXIMUM USEFUL WORK:**  $[w_{useful}]_{max} = w_{max} = (h_1 - h_2) - T_0(s_1 - s_2)$

**AVAILABILITY/ WORK POTENTIAL AT A STATE "i":**  $b_i = (h_i - h_0) - T_0(s_i - s_0)$

Availability/ work potential at a state "i" is composite property (intensive) of system and surroundings.

**AVAILABILITY FUNCTION:**  $\psi_i = h_i - T_0 s_i$

$[w_{useful}]_{max} = w_{max} = \psi_1 - \psi_2$	$w_{max} = (h_1 - h_2) - T_0(s_1 - s_2)$
--	--

**IRREVERSIBILITY (I):** It represents loss of work or available energy or availability.

$I = W_{max} - W_{act}$	$I \propto \Delta S_{Univ.}$
$I = T_0 \Delta S_{Univ.}$	$I = T_0 [\Delta S_{sys.} + \Delta S_{surr.}]$

**IRREVERSIBILITY BETWEEN THERMAL RESERVOIRS:**

$$I = T_0 \Delta S_{Univ.} = T_0 [\Delta S_{sys.} + \Delta S_{surr.}] = T_0 \left[ \frac{-Q}{T_1} + \frac{Q}{T_2} \right] + 0$$

**IRREVERSIBILITY IN FREE EXPANSION/ THROTTLING PROCESS:**

$$I = T_0 \Delta S_{Univ.} = T_0 [\Delta S_{sys.} + \Delta S_{surr.}] = T_0 \left[ m C_p \ln \left( \frac{T_2}{T_1} \right) - m R \ln \left( \frac{P_2}{P_1} \right) \right] + T_0 \frac{Q}{T_{surr}}$$

**IRREVERSIBILITY IN ADIABATIC MIXING PROCESS:**

$$I = T_0 \Delta S_{Univ.} = T_0 [\Delta S_{sys.} + \Delta S_{surr.}] = T_0 [\Delta S_1 + \Delta S_2] + T_0 \frac{Q}{T_{surr.}}$$

$$\text{Where, } \Delta S_1 = m_1 C_{p1} \ln \left( \frac{T_f}{T_1} \right) - m_1 R \ln \left( \frac{P_f}{P_1} \right) \text{ \& } \Delta S_2 = m_2 C_{p2} \ln \left( \frac{T_f}{T_2} \right) - m_2 R \ln \left( \frac{P_f}{P_2} \right)$$

**IRREVERSIBILITY IN FLUID FRICTION IN AN ADIABATIC PIPELINE:**

From, S.F.E.E.: $h_1 = h_2 \Rightarrow T_1 = T_2$	$h_1 = m_1 C_p dT$
$\dot{I}(\text{in KW}) = T_0 \Delta \dot{S}_{Univ.} = T_0 [\Delta \dot{S}_{sys.} + \Delta \dot{S}_{surr.}] = -T_0 \dot{m} R \ln \left( \frac{P_2}{P_1} \right) = -T_0 \dot{m} R \ln \left( 1 - \frac{\Delta P}{P_1} \right) = T_0 \dot{m} R \left( \frac{\Delta P}{P_1} \right) (\text{Forier})$	

## SECOND LAW EFFICIENCY:

FOR HEAT ENGINES,	FOR TURBINES,
$\eta_{II-LAW} = \frac{\eta_{act}}{\eta_{ideal}} = \frac{1 - Q_2/Q_1}{1 - T_2/T_1}$	$\eta_{II-LAW} = \frac{W_{act}(\text{From SFEE})}{W_{ideal}(\text{From } \psi_1 - \psi_2)} = \eta_{ISE-T} = \frac{h_1 - h'_2}{h_1 - h_2}$
FOR REFRIGERATOR,	FOR COMPRESSORS,
$\eta_{II-LAW} = \frac{COP_{act}}{COP_{ideal}} = \frac{Q_2/(Q_1 - Q_2)}{T_2/(T_1 - T_2)}$	$\eta_{II-LAW} = \frac{W_{ideal}(\text{From } \psi_1 - \psi_2)}{W_{act}(\text{From SFEE})} = \eta_{ISE-C} = \frac{h_2 - h_1}{h'_2 - h_1}$
FOR HEAT PUMP,	FOR HEATING COIL,
$\eta_{II-LAW} = \frac{COP_{act}}{COP_{ideal}} = \frac{Q_1/(Q_1 - Q_2)}{T_1/(T_1 - T_2)}$	$\eta_{II-LAW} = \frac{COP_{act}}{COP_{ideal HP}} = \frac{1}{T_1/(T_1 - T_2)}$