

# Matrix theory Assignment 19

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**Abstract**—This document contains the concept of matrix diagonalization.

Download all python codes from

[https://github.com/shivangi-975/EE5609-Matrix\\_Theory/tree/master/Assignment19/Codes](https://github.com/shivangi-975/EE5609-Matrix_Theory/tree/master/Assignment19/Codes)

Download latex-tikz codes from

[https://github.com/shivangi-975/EE5609-Matrix\\_Theory/blob/master/Assignment19/Assignment\\_19.tex](https://github.com/shivangi-975/EE5609-Matrix_Theory/blob/master/Assignment19/Assignment_19.tex)

## 1 PROBLEM

Let  $A$  be a  $3 \times 3$  matrix with real entries. Identify the correct statements.

1.  $A$  is necessarily diagonalizable over  $\mathbf{R}$
2. If  $A$  has distinct real eigen values than it is diagonalizable over  $\mathbf{R}$
3. If  $A$  has distinct eigen values than it is diagonalizable over  $\mathbf{C}$
4. If all eigen values are non zero than it is diagonalizable over  $\mathbf{C}$

## 2 SOLUTION

Given	A $3 \times 3$ matrix with real entries.
Statement 1.	A is necessarily diagonalizable over $\mathbf{R}$
False statement	matrix A is diagonalizable if and only if there is a basis of $\mathbf{R}^3$ consisting of eigenvectors of A.
Statement 2.	If A has distinct real eigen values than it is diagonalizable over $\mathbf{R}$
True statement	A has n linearly independent eigenvectors which implies it is diagonalizable.
Statement 3.	If all eigen values are non zero than it is diagonalizable over $\mathbf{C}$
True statement	A has n linearly independent eigenvectors which implies it is diagonalizable.
Statement 4.	If all eigen values are non zero than it is diagonalizable over $\mathbf{C}$
False statement	matrix A is diagonalizable if and only if there is a basis of $\mathbf{R}^3$ consisting of eigenvectors of A.

TABLE 1: Summary