## HW4

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```
#install.packages('tidyverse') # data manipulation
#install.packages('cluster') # clustering algorithms
#install.packages('factoextra') # clustering algorithms & visualization
#install.packages('gridExtra')
library(tidyverse, warn.conflicts = FALSE) # data manipulation
## Warning: replacing previous import 'lifecycle::last_warnings' by
## 'rlang::last_warnings' when loading 'pillar'
## Warning: replacing previous import 'lifecycle::last_warnings' by
## 'rlang::last_warnings' when loading 'tibble'
## Warning: replacing previous import 'lifecycle::last_warnings' by
## 'rlang::last warnings' when loading 'hms'
## -- Attaching packages ------ tidyverse 1.3.1 --
## v ggplot2 3.3.5 v purrr 0.3.4

## v tibble 3.1.4 v dplyr 1.0.7

## v tidyr 1.1.4 v stringr 1.4.0

## v readr 2.0.1 v forcats 0.5.1
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag() masks stats::lag()
library(cluster) # clustering algorithms
## Warning: package 'cluster' was built under R version 4.1.2
library(factoextra) # clustering algorithms & visualization
## Welcome! Want to learn more? See two factoextra-related books at https://goo.gl/ve3WBa
library(gridExtra) # subfigure layout package
```

```
##
## Attaching package: 'gridExtra'
## The following object is masked from 'package:dplyr':
##
##
       combine
read the data file
Essay = read.csv('/Users/shivangi/Desktop/Applied Machine learning/Week 4/HW4-data-fedPapers.csv')
str(Essay)
                    85 obs. of 72 variables:
## 'data.frame':
   $ author : chr
                     "dispt" "dispt" "dispt" ...
                     "dispt_fed_49.txt" "dispt_fed_50.txt" "dispt_fed_51.txt" "dispt_fed_52.txt" ...
   $ filename: chr
              : num 0.28 0.177 0.339 0.27 0.303 0.245 0.349 0.414 0.248 0.442 ...
## $ all
              : num 0.052 0.063 0.09 0.024 0.054 0.059 0.036 0.083 0.04 0.062 ...
              : num 0.009 0.013 0.008 0.016 0.027 0.007 0.007 0.009 0.007 0.006 ...
## $ an
                    0.096 0.038 0.03 0.024 0.034 0.067 0.029 0.018 0.04 0.075 ...
              : num
              : num 0.358 0.393 0.301 0.262 0.404 0.282 0.335 0.478 0.356 0.423 ...
##
   $ and
##
                    0.026 0.063 0.008 0.056 0.04 0.052 0.058 0.046 0.034 0.037 ...
   $ any
              : num
## $ are
              : num 0.131 0.051 0.068 0.064 0.128 0.111 0.087 0.11 0.154 0.093 ...
                     0.122 0.139 0.203 0.111 0.148 0.252 0.073 0.074 0.161 0.1 ...
##
   $ as
##
   $ at
              : num
                    0.017 0.114 0.023 0.056 0.013 0.015 0.116 0.037 0.047 0.031 ...
## $ be
                    0.411 0.393 0.474 0.365 0.344 0.297 0.378 0.331 0.289 0.379 ...
## $ been
                     0.026\ 0.165\ 0.015\ 0.127\ 0.047\ 0.03\ 0.044\ 0.046\ 0.027\ 0.025\ \dots
              : num
##
   $ but
                     0.009 0 0.038 0.032 0.061 0.037 0.007 0.055 0.027 0.037 ...
              : num
##
                     0.14\ 0.139\ 0.173\ 0.167\ 0.209\ 0.186\ 0.102\ 0.092\ 0.168\ 0.174\ \dots
   $ by
              : num
##
   $ can
              : num
                     0.035 0 0.023 0.056 0.088 0 0.058 0.037 0.047 0.056 ...
## $ do
                     0.026 0.013 0 0 0 0 0.015 0.028 0 0 ...
              : num
##
                     0 0 0.008 0 0 0.007 0 0 0 0 ...
   $ down
              : num
##
                    0.009 0.025 0.015 0.024 0.02 0.007 0.007 0.018 0 0.006 ...
   $ even
              : num
                    0.044 0 0.023 0.04 0.027 0.007 0.087 0.064 0.081 0.05 ...
  $ every
              : num
##
                    0.096 0.076 0.098 0.103 0.141 0.067 0.116 0.055 0.127 0.1 ...
   $ for.
              : num
##
   $ from
              : num
                     0.044\ 0.101\ 0.053\ 0.079\ 0.074\ 0.096\ 0.08\ 0.083\ 0.074\ 0.124\ \dots
## $ had
              : num 0.035 0.101 0.008 0.016 0 0.022 0.015 0.009 0.007 0 ...
              : num 0.017 0.013 0.015 0.024 0.054 0.015 0.036 0.037 0.02 0.019 ...
## $ has
                     0.044\ 0.152\ 0.023\ 0.143\ 0.047\ 0.119\ 0.044\ 0.074\ 0.074\ 0.044\ \dots
##
   $ have
              : num
##
   $ her
              : num 0 0 0 0 0 0 0.007 0 0.034 0.025 ...
## $ his
                    0.017 0 0 0.024 0.02 0.067 0 0.018 0.02 0.05 ...
## $ if.
                    0 0.025 0.023 0.04 0.034 0.03 0.029 0 0 0.025 ...
              : num
                     0.262 0.291 0.308 0.238 0.263 0.401 0.189 0.267 0.248 0.274 ...
##
   $ in.
              : num
##
                     0.009 0.025 0.038 0.008 0.013 0.037 0 0.037 0.013 0.037 ...
   $ into
              : num
## $ is
                     0.157 0.038 0.15 0.151 0.189 0.26 0.167 0.083 0.208 0.23 ...
              : num
## $ it
                     0.175\ 0.127\ 0.173\ 0.222\ 0.108\ 0.156\ 0.102\ 0.165\ 0.134\ 0.131\ \dots
              : num
##
                     0.07 0.038 0.03 0.048 0.013 0.015 0 0.046 0.02 0.019 ...
   $ its
              : num
                    0.035 0.038 0.12 0.056 0.047 0.074 0.08 0.092 0.027 0.106 ...
##
   $ may
              : num
                     0.026 0 0.038 0.056 0.067 0.045 0.08 0.064 0.06 0.081 ...
   $ more
              : num
   $ must
                     0.026 0.013 0.083 0.071 0.013 0.015 0.044 0.018 0.027 0.068 ...
##
              : num
##
                     0 0 0 0 0 0 0.007 0 0 0 ...
   $ my
              : num
## $ no
                    0.035 0 0.03 0.032 0.047 0.059 0.022 0.018 0.02 0.044 ...
              : num
              : num 0.114 0.127 0.068 0.087 0.128 0.134 0.102 0.101 0.094 0.106 ...
## $ not
              : num 0 0 0 0 0 0 0.007 0 0.007 0.012 ...
## $ now
```

```
0.9 0.747 0.858 0.802 0.869 ...
              : num
##
                      0.14 0.139 0.15 0.143 0.054 0.141 0.051 0.083 0.127 0.118 ...
    $ on
              : num
                      0.026 0.025 0.03 0.032 0.047 0.052 0.073 0.046 0.06 0.031 ...
##
    $ one
              : num
                     0.035 0 0.023 0.048 0.027 0.022 0.007 0.046 0.02 0.012 ...
##
    $ only
               : num
##
    $ or
              : num
                      0.096\ 0.114\ 0.06\ 0.064\ 0.081\ 0.074\ 0.153\ 0.037\ 0.154\ 0.081\ \dots
##
                     0.017 0 0 0.016 0.027 0.03 0.051 0 0.007 0.025 ...
   $ our
              : num
                     0.017 0 0.008 0.016 0 0.015 0.007 0 0.02 0 ...
    $ shall
              : num
                      0.017 0.013 0.068 0.032 0 0.03 0.007 0 0 0.012 ...
##
    $ should
              : num
##
    $ so
                      0.035 0.013 0.038 0.04 0.027 0.007 0.051 0.018 0.04 0.05 ...
              : niim
##
    $ some
              : num
                      0.009\ 0.063\ 0.03\ 0.024\ 0.067\ 0.045\ 0.007\ 0.028\ 0.027\ 0.025\ \dots
    $ such
                      0.026 0 0.045 0.008 0.027 0.015 0.015 0 0.013 0.031 ...
              : num
##
                      0.009 0 0.023 0 0.047 0.03 0.109 0.055 0.067 0.044 ...
    $ than
              : num
##
                      0.184 0.152 0.188 0.238 0.162 0.208 0.233 0.165 0.208 0.218 ...
    $ that
              : num
##
   $ the
              : num
                      1.43 1.25 1.49 1.33 1.19 ...
##
                      0.114 0.165 0.053 0.071 0.027 0.089 0.109 0.083 0.154 0.081 ...
    $ their
              : num
##
    $ then
                      0 0 0.015 0.008 0.007 0.007 0.015 0.009 0.007 0.012 ...
              : num
                     0.009 0 0.015 0 0.007 0.007 0.036 0.028 0.02 0 ...
##
    $ there
              : num
                      0.009 0 0 0 0 0 0 0 0 0.012 ...
    $ things
              : num
                     0.044\ 0.051\ 0.075\ 0.103\ 0.094\ 0.126\ 0.08\ 0.11\ 0.067\ 0.093\ \dots
##
   $ this
              : num
##
    $ to
              : num
                      0.507 0.355 0.361 0.532 0.485 0.445 0.56 0.34 0.49 0.498 ...
##
   $ up
                     0 0 0 0 0 0 0.007 0 0 0 ...
              : num
                     0 0.013 0 0 0 0 0 0 0 0 ...
##
   $ upon
              : num
                      0.009 0.051 0.008 0.087 0.027 0.007 0.015 0.018 0.027 0 ...
##
    $ was
              : num
                      0.017 0 0.015 0.079 0.02 0.03 0.029 0.009 0.007 0 ...
##
    $ were
              : num
## $ what
                     0 0 0.008 0.008 0.02 0.015 0.015 0.009 0.02 0.025 ...
              : num
   $ when
              : num
                     0.009 0 0 0.024 0.007 0.037 0.007 0 0.02 0.012 ...
##
                      0.175\ 0.114\ 0.105\ 0.167\ 0.155\ 0.186\ 0.211\ 0.175\ 0.201\ 0.199\ \dots
    $ which
              : num
                      0.044 0.038 0.008 0 0.027 0.045 0.022 0.018 0.04 0.031 ...
##
    $ who
              : num
##
                      0.009 \ 0.089 \ 0.173 \ 0.079 \ 0.168 \ 0.111 \ 0.145 \ 0.267 \ 0.154 \ 0.106 \ \dots
  $ will
    $ with
                      0.087 0.063 0.045 0.079 0.074 0.089 0.073 0.129 0.027 0.081 ...
              : num
##
    $ would
              : num
                      0.192 0.139 0.068 0.064 0.04 0.037 0.073 0.037 0.04 0.031 ...
    $ your
                      0 0 0 0 0 0 0 0 0 0 ...
              : num
```

#### typeof (Essay)

#### ## [1] "list"

To remove any missing value that might be present in the data

```
Essay = na.omit(Essay)
```

Remove the label information

```
Essay.unlabeled = Essay[, which(!names(Essay) %in% c('author', 'filename'))]
head(Essay.unlabeled)
```

```
## 1 0.280 0.052 0.009 0.096 0.358 0.026 0.131 0.122 0.017 0.411 0.026 0.009 0.140  
## 2 0.177 0.063 0.013 0.038 0.393 0.063 0.051 0.139 0.114 0.393 0.165 0.000 0.139  
## 3 0.339 0.090 0.008 0.030 0.301 0.008 0.068 0.203 0.023 0.474 0.015 0.038 0.173  
## 4 0.270 0.024 0.016 0.024 0.262 0.056 0.064 0.111 0.056 0.365 0.127 0.032 0.167  
## 5 0.303 0.054 0.027 0.034 0.404 0.040 0.128 0.148 0.013 0.344 0.047 0.061 0.209
```

```
## 6 0.245 0.059 0.007 0.067 0.282 0.052 0.111 0.252 0.015 0.297 0.030 0.037 0.186
                                                 had
                  down even every for. from
                                                       has have her
                                                                       his
##
                                                                              if.
       can
## 1 0.035 0.026 0.000 0.009 0.044 0.096 0.044 0.035 0.017 0.044
                                                                   0 0.017 0.000
## 2 0.000 0.013 0.000 0.025 0.000 0.076 0.101 0.101 0.013 0.152
                                                                   0 0.000 0.025
## 3 0.023 0.000 0.008 0.015 0.023 0.098 0.053 0.008 0.015 0.023
                                                                   0 0.000 0.023
## 4 0.056 0.000 0.000 0.024 0.040 0.103 0.079 0.016 0.024 0.143
                                                                   0 0.024 0.040
## 5 0.088 0.000 0.000 0.020 0.027 0.141 0.074 0.000 0.054 0.047
                                                                   0 0.020 0.034
                                                                   0 0.067 0.030
## 6 0.000 0.000 0.007 0.007 0.007 0.067 0.096 0.022 0.015 0.119
##
            into
                    is
                          it
                               its
                                     may
                                         more must my
                                                                not now
                                                                            of
       in.
                                                           nο
## 1 0.262 0.009 0.157 0.175 0.070 0.035 0.026 0.026
                                                      0 0.035 0.114
                                                                      0 0.900
## 2 0.291 0.025 0.038 0.127 0.038 0.038 0.000 0.013
                                                      0 0.000 0.127
                                                                       0 0.747
## 3 0.308 0.038 0.150 0.173 0.030 0.120 0.038 0.083
                                                                      0 0.858
                                                      0 0.030 0.068
## 4 0.238 0.008 0.151 0.222 0.048 0.056 0.056 0.071
                                                      0 0.032 0.087
                                                                       0 0.802
## 5 0.263 0.013 0.189 0.108 0.013 0.047 0.067 0.013
                                                      0 0.047 0.128
                                                                       0 0.869
## 6 0.401 0.037 0.260 0.156 0.015 0.074 0.045 0.015
                                                      0 0.059 0.134
                                                                       0 0.876
##
                  only
                               our shall should
                                                      some
                                                            such
                                                                         that
             one
                          or
                                                   so
## 1 0.140 0.026 0.035 0.096 0.017 0.017
                                         0.017 0.035 0.009 0.026 0.009 0.184
## 2 0.139 0.025 0.000 0.114 0.000 0.000
                                          0.013 0.013 0.063 0.000 0.000 0.152
## 3 0.150 0.030 0.023 0.060 0.000 0.008
                                         0.068 0.038 0.030 0.045 0.023 0.188
## 4 0.143 0.032 0.048 0.064 0.016 0.016
                                         0.032 0.040 0.024 0.008 0.000 0.238
## 5 0.054 0.047 0.027 0.081 0.027 0.000
                                         0.000 0.027 0.067 0.027 0.047 0.162
## 6 0.141 0.052 0.022 0.074 0.030 0.015
                                          0.030 0.007 0.045 0.015 0.030 0.208
##
       the their then there things this
                                             to up upon
                                                           was were what when
## 1 1.425 0.114 0.000 0.009
                             0.009 0.044 0.507
                                                 0 0.000 0.009 0.017 0.000 0.009
## 2 1.254 0.165 0.000 0.000 0.000 0.051 0.355
                                                 0 0.013 0.051 0.000 0.000 0.000
## 3 1.490 0.053 0.015 0.015
                              0.000 0.075 0.361
                                                 0 0.000 0.008 0.015 0.008 0.000
## 4 1.326 0.071 0.008 0.000
                              0.000 0.103 0.532
                                                 0 0.000 0.087 0.079 0.008 0.024
                              0.000 0.094 0.485
## 5 1.193 0.027 0.007 0.007
                                                 0 0.000 0.027 0.020 0.020 0.007
## 6 1.469 0.089 0.007 0.007
                              0.000 0.126 0.445
                                                 0 0.000 0.007 0.030 0.015 0.037
                  will with would your
     which
             who
## 1 0.175 0.044 0.009 0.087 0.192
## 2 0.114 0.038 0.089 0.063 0.139
                                      0
## 3 0.105 0.008 0.173 0.045 0.068
                                      0
## 4 0.167 0.000 0.079 0.079 0.064
                                      0
## 5 0.155 0.027 0.168 0.074 0.040
                                      0
## 6 0.186 0.045 0.111 0.089 0.037
                                      0
```

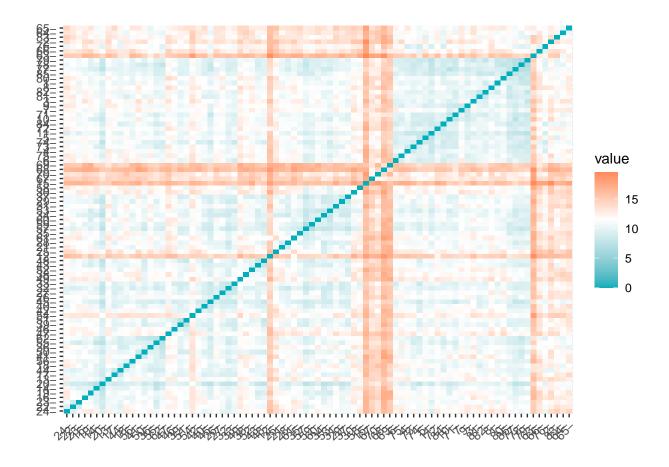
Since we don't want the clustering algorithm to depend on an arbitrary variable unit, we start by scaling/standardizing the data using the R function scale:

```
Essay.unlabeled = scale(Essay.unlabeled)
head(Essay.unlabeled)
```

```
##
                     all
                               also
                                           an
                                                     and
                                                               any
## 1 -0.1723368 -0.03534435
                         0.15950160 0.93187600 -0.23253417 -0.68518464
              0.43010589
                         0.63520811 -1.02557977
                                              0.07316143
                                                         0.93870812
## 2 -1.5135000
    0.5959023
              1.57257465
                         0.04057497 -1.29557367 -0.73038129 -1.47518652
## 4 -0.3025468 -1.22012677
                         0.99198800 -1.49806910 -1.07101353
                                                         0.63148517
    0.1271463
              0.04928297
                         2.30018092 -1.16057672 0.16923719 -0.07073873
## 5
## 6 -0.6280719
               0.26085126 -0.07835166 -0.04685188 -0.89633033
                                                         0.45592919
##
          are
                      as
                               at
                                          be
                                                  been
     1.5654231 -0.05418106 -1.0404489
                                   1.26866739 -1.0162916 -1.3159303 0.2605755
```

```
## 3 -0.2632943 1.94066694 -0.8115322 1.99627946 -1.3483086 0.3206833 0.9299109
## 4 -0.3794034 -0.32508634 0.4475097 0.73739509 2.0322282 -0.0179264 0.8082135
## 5 1.4783413 0.58614052 -1.1930600 0.49485773 -0.3824410 1.6186872 1.6600949
## 6 0.9848779 3.14742684 -1.1167544 -0.04796397 -0.8955582 0.2642484 1.1935884
            can
                        do
                                 down
                                            even
                                                       every
## 1 -0.02062228 3.0053860 -0.4239542 -0.2431406 1.09472692 0.06360606
## 2 -1.27268916 1.0262730 -0.4239542 1.3777967 -1.30239174 -0.50550078
## 3 -0.44990235 -0.9528399 1.7936523 0.3647109 -0.04935244 0.12051674
## 4 0.73061785 -0.9528399 -0.4239542 1.2764881 0.87680704 0.26279345
## 5 1.87536471 -0.9528399 -0.4239542 0.8712538 0.16856744 1.34409646
## 6 -1.27268916 -0.9528399 1.5164515 -0.4457577 -0.92103196 -0.76159886
           from
                        had
                                   has
                                             have
                                                        her
## 1 -1.31170510 0.61463684 -1.1001862 -1.3396177 -0.3769551 -0.2733913
## 2 0.77813746 3.54670543 -1.2606596 1.5116901 -0.3769551 -0.6732398
## 3 -0.98172996 -0.58484577 -1.1804229 -1.8940386 -0.3769551 -0.6732398
## 4 -0.02846844 -0.22944351 -0.8193579 1.2740811 -0.3769551 -0.1087477
## 5 -0.21178797 -0.94024802 0.3841920 -1.2604147 -0.3769551 -0.2028298
## 6 0.59481793 0.03710818 -1.1804229 0.6404571 -0.3769551 0.9026339
           if.
                                into
                      in.
                                              is
                                                        it.
## 1 -1.5128966 -0.7758578 -0.7853726 0.01246845 0.4072769 0.72662889
## 2 -0.1289512 -0.3693776 0.0471346 -2.02169914 -0.6633995 -0.34810226
## 3 -0.2396668 -0.1310961 0.7235467 -0.10718847 0.3626654 -0.61678505
## 4 0.7014161 -1.1122552 -0.8374043 -0.09009462 1.4556476 -0.01224877
## 5 0.3692692 -0.7618412 -0.5772458 0.55947150 -1.0872090 -1.18773597
## 6 0.1478379 1.1724439 0.6715150 1.77313452 -0.0165325 -1.12056527
           mav
                      more
                                 must
                                              my
## 1 -0.8830840 -0.70385836 -0.2855115 -0.4056847 0.13701191 0.7490012
## 2 -0.7842747 -1.63698791 -0.8122064 -0.4056847 -1.68267750 1.2015142
## 3 1.9165132 -0.27318318 2.0238430 -0.4056847 -0.12294372 -0.8521988
## 4 -0.1914188 0.37282959 1.5376631 -0.4056847 -0.01896147 -0.1908336
## 5 -0.4878468 0.76761517 -0.8122064 -0.4056847 0.76090542 1.2363229
## 6 0.4014371 -0.02195599 -0.7311764 -0.4056847 1.38479893 1.4451751
                        of
                                   on
                                             one
                                                         only
## 1 -0.8475975 -0.07882731 1.8402042 -0.6574777 0.826718310 -0.0164496
## 2 -0.8475975 -1.36832319
                           1.8141910 -0.7019372 -1.561133119 0.3830407
## 3 -0.8475975 -0.43280657
                           2.1003361 -0.4796396 0.008026391 -0.8154303
## 4 -0.8475975 -0.90477892 1.9182438 -0.3907206 1.713634554 -0.7266546
## 5 -0.8475975 -0.34009772 -0.3969308 0.2761720 0.280923697 -0.3493582
## 6 -0.8475975 -0.28110118 1.8662174 0.4984695 -0.060197935 -0.5047156
                               should
                     shall
                                                       some
           our
                                              SO
## 1 -0.1827435 -0.09108447 -0.4841143 0.3222109 -0.7284739 -0.1937633 -1.3055544
## 2 -0.7005166 -0.97442043 -0.6865729 -1.0471854 2.8824281 -1.7565984 -1.6416073
## 3 -0.7005166 -0.55873292 2.0972330 0.5089468 0.6757658 0.9483085 -0.7828055
## 4 -0.2132007 -0.14304541 0.2751055 0.6334373 0.2745544 -1.2757260 -1.6416073
## 5 0.1218290 -0.97442043 -1.3445634 -0.1757514 3.1499023 -0.1336542 0.1133355
## 6 0.2132007 -0.19500635 0.1738762 -1.4206571 1.6787941 -0.8549627 -0.5214311
           that
                       the
                                 their
                                             then
                                                       there
                                                                things
## 1 -0.47881966 0.7661753 0.68392790 -1.0008309 -0.7880202 1.4470317
## 2 -1.02535321 -0.1422477 1.90906321 -1.0008309 -1.1961687 -0.6067331
## 3 -0.41050296 1.1114823 -0.78143002 1.4673691 -0.5159211 -0.6067331
## 4 0.44345572 0.2402462 -0.34902932 0.3155424 -1.1961687 -0.6067331
## 5 -0.85456148 -0.4663051 -1.40600880 0.1509958 -0.8787198 -0.6067331
## 6 -0.06891949 0.9999216 0.08337138 0.1509958 -0.8787198 -0.6067331
##
          this
                                            upon
                                   up
```

```
## 1 -1.4818540 -0.27620743 -0.5120406 -1.0657505 -0.57950415 -0.15447029
## 2 -1.2406879 -1.73456457 -0.5120406 -0.5916546 0.86621899 -0.96910375
## 3 -0.4138329 -1.67699784 -0.5120406 -1.0657505 -0.61392613 -0.25030952
## 4 0.5508314 -0.03634605 -0.5120406 -1.0657505 2.10541024 2.81654586
## 5 0.2407607 -0.48728543 -0.5120406 -1.0657505 0.04009148 -0.01071144
## 6 1.3432342 -0.87106363 -0.5120406 -1.0657505 -0.64834810 0.46848471
          what
                    when
                             which
                                          who
                                                   will
                                                             with
                                                                       would
## 2 -1.1025238 -0.8858546 -1.0164186 0.2198537 -0.1463229 -0.6496151 0.4995915
## 3 -0.4165986 -0.8858546 -1.2254963 -0.9857954 1.1277571 -1.3505396 -0.4518237
## 4 -0.4165986 0.9249103 0.2148172 -1.3073018 -0.2979991 -0.0265710 -0.5054246
## 5 0.6122890 -0.3577148 -0.0639532 -0.2222177 1.0519190 -0.2212723 -0.8270297
## 6 0.1835858 1.9057413 0.6562036 0.5011718 0.1873647 0.3628315 -0.8672304
##
          your
## 1 -0.2087646
## 2 -0.2087646
## 3 -0.2087646
## 4 -0.2087646
## 5 -0.2087646
## 6 -0.2087646
typeof (Essay.unlabeled)
## [1] "double"
distance = factoextra::get_dist(Essay.unlabeled) # default method is euclidean
# visualization of the distance matrix
factoextra::fviz_dist(distance, gradient = list(low = "#00AFBB", mid = "white", high = "#FC4E07"))
```



## k-Means Clustering

```
# the kmeans() function is available in pre-loaded {stats} package
model.r = kmeans(Essay.unlabeled, centers = 7, nstart = 25)
model.r
```

```
## K-means clustering with 7 clusters of sizes 15, 7, 4, 15, 1, 24, 19
## Cluster means:
##
                                 also
              а
                      all
                                             an
                                                        and
                                                                  any
## 1 0.57333261 -0.5543919 0.01678964 0.6708819 -0.65235612 0.4325217
## 2 -0.79362463 -0.4524361
                           0.14251208 -0.7845138 1.24728209 -0.9735980
## 3 -1.98551138 -0.6065787
                           1.52715783 -1.3208856 2.84844078 0.1377340
## 4 0.40319151 0.4554941 -0.36377557 0.1713932 -0.10326860 -0.5535177
    1.27299447 -0.3315400
                           0.87306137 -1.2955737 -1.00114025 0.1487062
                0.1180427
                           0.39239958 -0.4391868 0.04586718 -0.2938411
## 6 -0.04049915
## 7 -0.07639257
                 0.2408079 -0.64168833
                                     0.5251089 -0.46789679
                                                            0.7885616
##
                                  at
                                            be
                                                      been
            are
## 1 -0.70837900 0.0295533
                           ## 2 -0.09327752 -0.2899038
                           0.5456169 -1.6483805 0.26434540 -0.5177788
## 3 0.47690082 0.9617138 -0.8019940 0.1195023 -1.31812527 1.0261202
## 4 -0.10074167 -0.3841929 0.4882060 -0.4983905 0.23329965 -0.2248546
## 5 -0.49551242 -0.8422692 -1.1167544 0.8644385 -0.89555817 -0.1307963
## 6  0.26040583  0.2721367 -0.3982103  0.1993856  0.02880736  0.1960561
```

```
## 7 0.26989062 -0.1151023 -0.2231761 0.3690301 0.06077789 0.2583078
            by
##
                                 do
                                           down
                     can
                                                     even
                                                              everv
## 1 -0.5439792 -0.3378126 0.01134333 0.53700864 0.3376953 -0.3144883
## 2 0.5851017 -1.0478282 -0.51787001 -0.42395419 -0.3444492 -0.6408493
## 3 0.4329801 0.2029611 0.60761453 -0.42395419 -0.1924863 -1.1253318
## 4 -0.2343270 -0.2161832 0.03164193 -0.10979326 0.4795273 -0.4561362
## 5 -1.0578124 0.8737112 1.33075194 -0.42395419 -1.1549178 1.1492069
## 6  0.6873613  0.0375094  -0.10283626  -0.08900320  -0.1080625  0.6952071
## 7 -0.5048367 0.6873133 0.08879849 0.04291034 -0.2804648 0.1427611
           for.
                      from
                                 had
                                             has
                                                         have
## 1 0.46577490 0.08396753 0.1763074 -0.110600733 -0.014287599 -0.35522174
## 3 -0.05732915 0.84229929 -0.4182510 -0.859476253 -0.613590249 0.48461743
## 4 -0.53395613 -0.09201921 -0.0902443 0.651647564 0.323645173 0.08565501
## 5 -1.81444652 -0.17512406 -0.9402480 -0.578647933 -0.917201724 6.60876813
    0.09561832 -0.25761785 -0.1702098 -0.145704273 -0.195574450 -0.00244272
## 7 0.06360606 0.02363289 -0.4796280 -0.008545329 -0.001503958 -0.27890987
                      if.
           his
                                in.
                                           into
                                                       is
                                                                 it
## 1 1.0280766 0.48736590 0.5192723 -0.37952535 0.1560568 0.5143446
## 2 0.3213415 -0.49273111 -0.4514745 0.59718401 -1.0668858 -0.4594612
## 3 -0.4086342 1.76705416 -0.7022708 0.97069729 -1.2695699 0.6582167
## 4 -0.0507305 -0.11418907 -0.1301616 -0.20955512 -0.2427996 -0.7496485
## 5 -0.6732398 0.97820523 -1.0842221 4.20967065 -0.3635961 -1.4887126
## 6 -0.1979296 -0.36422189 -0.5101272 0.02545472 0.3173087 -0.1373554
## 7 -0.5184997 -0.07650691 0.7084221 -0.21302390 0.3471480 0.4683243
           its
                      may
                                more
                                          must
                                                        my
## 1 -0.2563023 -0.02454088 0.04264529 -0.3395315 -0.09861408 -0.2650528
## 2 -0.3624960 -1.23597444 -0.38085197 -0.7022372 0.03891560 -0.7988284
## 3 -0.5915960 0.01443391 1.86224792 -0.6197602 -0.40568466 -0.8248239
## 4 -0.0727024 -0.58446033 -0.42152685 -0.1315546 -0.05711806 -0.3863654
## 5 -0.6167850 1.91651322 1.59307593 0.4842733 -0.40568466 0.6569232
## 6 -0.1619835 0.27518071 0.24721600 0.2074209 -0.22413956 0.3536416
## 7 0.7549113 0.48464490 -0.34874023 0.4736115 0.49849187 0.5009498
                                  of
           not
                      now
                                            on
                                                      one
                                                                only
## 1 0.09691833 -0.4075517 0.50271004 -0.7801919 -0.1654591 -0.15116370
## 2 -0.66820994 0.7774954 -0.64350851 0.3017094 0.1110367 -0.44030490
## 3 0.79251208 -0.6018273 -2.45765222 0.1688563 1.7433358 1.38956900
## 4 -0.46698253 0.3508250 0.87972605 -0.4489572 -0.3877567 -0.28306407
## 5 -0.60853789 -0.8475975 -0.18839232 -0.6310496 4.1886087 -1.56113312
## 6 0.25297731 -0.2741336 -0.20103444 1.0305434 0.1224162 0.22407009
## 7 0.08397193 0.2759235 -0.07306073 -0.4448498 -0.3462611 0.01161715
            or
                     our
                              shall
                                         should
                                                        so
## 1 0.3238570 -0.3979747 -0.06337197 0.51468154 0.46330021 -0.14003062
## 2 -0.4666689 -0.3263276 -0.53646395 -0.46242227 -0.14907485 0.80950286
## 3 1.8755810 1.5457052 0.03881788 0.83186670 0.92910244 -0.12665691
## 5 -1.1483389 -0.7005166 1.36382183 -1.34456335 0.94466376 -1.33029091
## 6 -0.2032483 -0.1345195 -0.20150147 -0.33437925 -0.02013818 0.35814012
## 7 -0.1297553 -0.1939646 0.33554219 0.12592549 -0.59181199 -0.47859668
                                that
          such
                     than
                                            the
                                                     their
## 1 0.0867456 0.26767087 -0.03817698 0.3620776 -0.17126459 -0.2877954
## 2 -0.2366983 -0.45208682 -0.57153517 -0.4549213 1.39086872 0.3390491
## 3 1.8349169 0.87878924 0.12322121 -2.3814309 1.09831190 0.2744058
## 4 -0.3740904 -0.29988509 -0.41505741 -0.3200366 -0.41789314 -0.3316745
```

```
## 5 -0.8549627 3.95927391 0.98998928 -1.2153557 -1.69427594 -1.0008309
## 6 -0.2388450 -0.06402576 -0.22619021 0.3883298 -0.02973344 0.1235713
## 7 0.2744545 -0.12052588 0.77605015 0.2092105 -0.15179392
##
         there
                    things
                                 this
                                              to
                                                          up
## 1 0.2399095 -0.40896320
                           0.17874661 0.7228951
                                                  0.09571931
                                                              0.75040160
## 2 -0.8204129 -0.60673314 -0.56640730 -1.2219466
                                                 0.05510862 -0.72190069
## 3 -0.4025465 -0.20738998 -1.53353242 -0.3673547 -0.51204063 -1.06575048
    0.1310699 1.00585259 0.36708582 0.2777124 0.56624313 0.46594405
     3.5655645 -0.60673314 -1.96418610 1.0574218 1.69353979
                                                              0.02831704
## 6 -0.7105475 -0.15984913 -0.07792298 -0.7751191 -0.29148259 -1.01560572
    0.8039979 0.02981385 0.30241221 0.6610193 -0.15605221
                                                              0.81143905
##
                       were
                                  what
                                             when
                                                       which
                                                                    who
## 1 0.06762907
                0.23208127
                            0.4007955
                                      0.74383380 -0.5223756
                                                              0.7905275
                                                              0.6561838
## 2 2.01689658
                1.28311817 -0.4043500 0.05186294 -0.6480435
## 3 -0.42460524 0.02522827 0.5051132 0.60425401 -1.3590738 0.5815484
## 4 -0.12283922 -0.07140962 -0.3365740 -0.33256531
                                                  0.2411455 -0.6107046
## 5 -0.88930196 -0.96910375 -1.1025238 2.50932955 0.1683554 0.5011718
## 6 -0.07177995 -0.06661766 -0.1022163 -0.23511095 0.2709584 -0.2942217
## 7 -0.47261484 -0.46973092 0.1790732 -0.30609214 0.3957734 -0.1608776
           will
                       with
                                 bluow
                                             your
## 1 -0.07756304 0.01496527
                            0.5594458 -0.20876463
## 2 -1.01521083 0.22932210 -0.7293996 -0.20876463
## 3 0.82819663 0.58673800 0.5866929 0.61658391
## 4 -0.55281512 0.40696383
                            0.5147784 -0.13998559
## 5 0.55138758 2.73818703 1.4510068 -0.20876463
## 6 0.32387329 -0.10931904 -0.5165914 -0.06260916
## 7 0.25921133 -0.54714071 -0.1266922 0.31250813
## Clustering vector:
         3 4 5
                    7
                        8
                          9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26
                 6
              6
                 6
                     6
                       6
                          6
                             6
                                6
                                   7
                                      4
                                         4
                                            5
                                               4
                                                  1
                                                    4
                                                       4
                                                             7
## 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52
        7 7 7 7
                    1
                       7
                          7
                             2 7
                                   1
                                      1
                                         1
                                            4
                                                  4
                                                    4
                                                       1
                                                          1
                                                             1
                                               1
                                                                1
## 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78
     7 4 4 7 7
                     7
                        7
                          7
                             4 2 2 2 2
                                            3
                                              3 3 3 6 6 6 6
                                                                   6
## 79 80 81 82 83 84 85
##
   6 6 6 6 6
##
## Within cluster sum of squares by cluster:
## [1] 756.1569 427.1200 278.8521 718.4455
                                              0.0000 1108.9977 1105.4565
   (between SS / total SS = 25.3 %)
##
## Available components:
##
## [1] "cluster"
                     "centers"
                                    "totss"
                                                  "withinss"
                                                                 "tot.withinss"
## [6] "betweenss"
                                    "iter"
                                                  "ifault"
                     "size"
```

Print just the centroids

```
model.r$centers
```

```
## a all also an and any ## 1 0.57333261 -0.5543919 0.01678964 0.6708819 -0.65235612 0.4325217
```

```
## 2 -0.79362463 -0.4524361 0.14251208 -0.7845138 1.24728209 -0.9735980
## 3 -1.98551138 -0.6065787 1.52715783 -1.3208856 2.84844078 0.1377340
## 4 0.40319151 0.4554941 -0.36377557 0.1713932 -0.10326860 -0.5535177
    1.27299447 -0.3315400
                         0.87306137 -1.2955737 -1.00114025
                                                         0.1487062
## 6 -0.04049915 0.1180427
                          0.39239958 -0.4391868 0.04586718 -0.2938411
               0.2408079 -0.64168833 0.5251089 -0.46789679 0.7885616
## 7 -0.07639257
                                 at
                                           be
           are
                       as
                                                    been
## 1 -0.70837900
               0.0295533
                          ## 2 -0.09327752 -0.2899038 0.5456169 -1.6483805 0.26434540 -0.5177788
## 3 0.47690082 0.9617138 -0.8019940 0.1195023 -1.31812527 1.0261202
## 4 -0.10074167 -0.3841929 0.4882060 -0.4983905
                                             0.23329965 -0.2248546
## 5 -0.49551242 -0.8422692 -1.1167544 0.8644385 -0.89555817 -0.1307963
    0.26040583 0.2721367 -0.3982103 0.1993856
                                              0.02880736 0.1960561
## 7 0.26989062 -0.1151023 -0.2231761
                                    0.3690301 0.06077789
                                                         0.2583078
##
           by
                                 do
                                          down
                     can
                                                    even
                                                             every
## 1 -0.5439792 -0.3378126  0.01134333  0.53700864  0.3376953 -0.3144883
    0.5851017 -1.0478282 -0.51787001 -0.42395419 -0.3444492 -0.6408493
## 3 0.4329801 0.2029611 0.60761453 -0.42395419 -0.1924863 -1.1253318
## 4 -0.2343270 -0.2161832 0.03164193 -0.10979326 0.4795273 -0.4561362
## 5 -1.0578124 0.8737112 1.33075194 -0.42395419 -1.1549178 1.1492069
## 6  0.6873613  0.0375094  -0.10283626  -0.08900320  -0.1080625  0.6952071
## 7 -0.5048367 0.6873133 0.08879849 0.04291034 -0.2804648 0.1427611
##
           for.
                      from
                                 had
                                            has
                                                        have
                                                                    her
     0.46577490 0.08396753 0.1763074 -0.110600733 -0.014287599 -0.35522174
## 1
## 2 -0.06241046 0.38007221 2.0743247 -0.062840815 0.493365873 0.12202513
## 3 -0.05732915 0.84229929 -0.4182510 -0.859476253 -0.613590249
                                                             0.48461743
## 4 -0.53395613 -0.09201921 -0.0902443 0.651647564 0.323645173
                                                            0.08565501
## 5 -1.81444652 -0.17512406 -0.9402480 -0.578647933 -0.917201724 6.60876813
    0.09561832 -0.25761785 -0.1702098 -0.145704273 -0.195574450 -0.00244272
    ##
           his
                      if.
                                in.
                                          into
                                                      is
                                                                it
## 1
     1.0280766 0.48736590 0.5192723 -0.37952535 0.1560568 0.5143446
    0.3213415 -0.49273111 -0.4514745 0.59718401 -1.0668858 -0.4594612
## 3 -0.4086342 1.76705416 -0.7022708 0.97069729 -1.2695699 0.6582167
## 4 -0.0507305 -0.11418907 -0.1301616 -0.20955512 -0.2427996 -0.7496485
## 6 -0.1979296 -0.36422189 -0.5101272 0.02545472 0.3173087 -0.1373554
## 7 -0.5184997 -0.07650691 0.7084221 -0.21302390 0.3471480 0.4683243
##
           its
                      may
                                more
                                          must
                                                       my
                                                                 nο
## 1 -0.2563023 -0.02454088
                         0.04264529 -0.3395315 -0.09861408 -0.2650528
## 2 -0.3624960 -1.23597444 -0.38085197 -0.7022372 0.03891560 -0.7988284
## 3 -0.5915960 0.01443391 1.86224792 -0.6197602 -0.40568466 -0.8248239
## 4 -0.0727024 -0.58446033 -0.42152685 -0.1315546 -0.05711806 -0.3863654
## 5 -0.6167850 1.91651322 1.59307593 0.4842733 -0.40568466 0.6569232
## 6 -0.1619835 0.27518071 0.24721600 0.2074209 -0.22413956 0.3536416
    0.5009498
           not
                                  of
                                                               only
                      now
                                            on
                                                     one
    0.09691833 -0.4075517 0.50271004 -0.7801919 -0.1654591 -0.15116370
## 2 -0.66820994 0.7774954 -0.64350851 0.3017094 0.1110367 -0.44030490
     0.79251208 -0.6018273 -2.45765222 0.1688563 1.7433358 1.38956900
## 4 -0.46698253 0.3508250 0.87972605 -0.4489572 -0.3877567 -0.28306407
## 5 -0.60853789 -0.8475975 -0.18839232 -0.6310496 4.1886087 -1.56113312
## 6 0.25297731 -0.2741336 -0.20103444 1.0305434 0.1224162 0.22407009
## 7 0.08397193 0.2759235 -0.07306073 -0.4448498 -0.3462611 0.01161715
```

```
shall
                                           should
                      our
                                                          so
            or
## 1 0.3238570 -0.3979747 -0.06337197 0.51468154 0.46330021 -0.14003062
## 2 -0.4666689 -0.3263276 -0.53646395 -0.46242227 -0.14907485 0.80950286
## 3 1.8755810 1.5457052 0.03881788 0.83186670 0.92910244 -0.12665691
## 4 -0.0401231 0.6456936 0.10983116 -0.05557687 0.07737943 -0.08207787
## 5 -1.1483389 -0.7005166 1.36382183 -1.34456335 0.94466376 -1.33029091
## 6 -0.2032483 -0.1345195 -0.20150147 -0.33437925 -0.02013818 0.35814012
## 7 -0.1297553 -0.1939646 0.33554219 0.12592549 -0.59181199 -0.47859668
##
          such
                      than
                                  that
                                              the
                                                        their
                                                                   then
## 1 0.0867456 0.26767087 -0.03817698 0.3620776 -0.17126459 -0.2877954
## 2 -0.2366983 -0.45208682 -0.57153517 -0.4549213 1.39086872 0.3390491
## 3 1.8349169 0.87878924 0.12322121 -2.3814309 1.09831190 0.2744058
## 4 -0.3740904 -0.29988509 -0.41505741 -0.3200366 -0.41789314 -0.3316745
## 5 -0.8549627 3.95927391 0.98998928 -1.2153557 -1.69427594 -1.0008309
## 6 -0.2388450 -0.06402576 -0.22619021 0.3883298 -0.02973344 0.1235713
## 7 0.2744545 -0.12052588 0.77605015 0.2092105 -0.15179392
                                                              0.2029579
          there
                                  this
                    things
                                               to
                                                          up
## 1 0.2399095 -0.40896320 0.17874661 0.7228951
                                                  0.09571931
                                                              0.75040160
## 2 -0.8204129 -0.60673314 -0.56640730 -1.2219466 0.05510862 -0.72190069
## 3 -0.4025465 -0.20738998 -1.53353242 -0.3673547 -0.51204063 -1.06575048
## 4 0.1310699 1.00585259 0.36708582 0.2777124 0.56624313 0.46594405
## 5 3.5655645 -0.60673314 -1.96418610 1.0574218 1.69353979 0.02831704
## 6 -0.7105475 -0.15984913 -0.07792298 -0.7751191 -0.29148259 -1.01560572
    0.8039979 0.02981385 0.30241221 0.6610193 -0.15605221
                                                              0.81143905
##
                                  what
            was
                       were
                                              when
                                                        which
                                                                     who
## 1 0.06762907 0.23208127 0.4007955 0.74383380 -0.5223756
                                                              0.7905275
    2.01689658 1.28311817 -0.4043500 0.05186294 -0.6480435
                                                              0.6561838
## 3 -0.42460524 0.02522827 0.5051132 0.60425401 -1.3590738
                                                              0.5815484
## 4 -0.12283922 -0.07140962 -0.3365740 -0.33256531 0.2411455 -0.6107046
## 5 -0.88930196 -0.96910375 -1.1025238 2.50932955 0.1683554 0.5011718
## 6 -0.07177995 -0.06661766 -0.1022163 -0.23511095
                                                   0.2709584 -0.2942217
## 7 -0.47261484 -0.46973092 0.1790732 -0.30609214
                                                   0.3957734 -0.1608776
           will
                       with
                                 would
                             0.5594458 -0.20876463
## 1 -0.07756304
                0.01496527
## 2 -1.01521083 0.22932210 -0.7293996 -0.20876463
## 3 0.82819663 0.58673800 0.5866929 0.61658391
## 4 -0.55281512  0.40696383  0.5147784 -0.13998559
## 5 0.55138758 2.73818703 1.4510068 -0.20876463
## 6 0.32387329 -0.10931904 -0.5165914 -0.06260916
## 7 0.25921133 -0.54714071 -0.1266922 0.31250813
```

Get cluster assignment

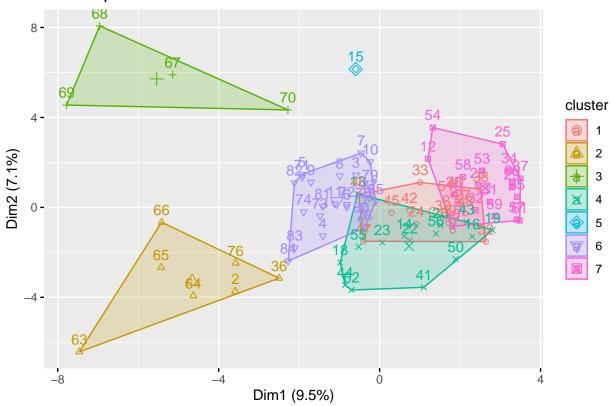
```
cluster.assignment = data.frame(Essay, model.r$cluster) |> relocate(model.r.cluster, .after = author)
glimpse(cluster.assignment)
```

```
## $ also
                     <dbl> 0.009, 0.013, 0.008, 0.016, 0.027, 0.007, 0.007, 0.009~
## $ an
                     <dbl> 0.096, 0.038, 0.030, 0.024, 0.034, 0.067, 0.029, 0.018~
## $ and
                     <dbl> 0.358, 0.393, 0.301, 0.262, 0.404, 0.282, 0.335, 0.478~
                     <dbl> 0.026, 0.063, 0.008, 0.056, 0.040, 0.052, 0.058, 0.046~
## $ any
## $ are
                     <dbl> 0.131, 0.051, 0.068, 0.064, 0.128, 0.111, 0.087, 0.110~
## $ as
                     <dbl> 0.122, 0.139, 0.203, 0.111, 0.148, 0.252, 0.073, 0.074~
## $ at
                     <dbl> 0.017, 0.114, 0.023, 0.056, 0.013, 0.015, 0.116, 0.037~
                     <dbl> 0.411, 0.393, 0.474, 0.365, 0.344, 0.297, 0.378, 0.331~
## $ be
## $ been
                     <dbl> 0.026, 0.165, 0.015, 0.127, 0.047, 0.030, 0.044, 0.046~
## $ but
                     <dbl> 0.009, 0.000, 0.038, 0.032, 0.061, 0.037, 0.007, 0.055~
## $ by
                     <dbl> 0.140, 0.139, 0.173, 0.167, 0.209, 0.186, 0.102, 0.092~
                     <dbl> 0.035, 0.000, 0.023, 0.056, 0.088, 0.000, 0.058, 0.037~
## $ can
## $ do
                     <dbl> 0.026, 0.013, 0.000, 0.000, 0.000, 0.000, 0.015, 0.028~
## $ down
                     <dbl> 0.000, 0.000, 0.008, 0.000, 0.000, 0.007, 0.000, 0.000~
## $ even
                     <dbl> 0.009, 0.025, 0.015, 0.024, 0.020, 0.007, 0.007, 0.018~
## $ every
                     <dbl> 0.044, 0.000, 0.023, 0.040, 0.027, 0.007, 0.087, 0.064~
                     <dbl> 0.096, 0.076, 0.098, 0.103, 0.141, 0.067, 0.116, 0.055~
## $ for.
## $ from
                     <dbl> 0.044, 0.101, 0.053, 0.079, 0.074, 0.096, 0.080, 0.083~
                     <dbl> 0.035, 0.101, 0.008, 0.016, 0.000, 0.022, 0.015, 0.009~
## $ had
## $ has
                     <dbl> 0.017, 0.013, 0.015, 0.024, 0.054, 0.015, 0.036, 0.037~
## $ have
                     <dbl> 0.044, 0.152, 0.023, 0.143, 0.047, 0.119, 0.044, 0.074~
## $ her
                     <dbl> 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.007, 0.000~
                     <dbl> 0.017, 0.000, 0.000, 0.024, 0.020, 0.067, 0.000, 0.018~
## $ his
## $ if.
                     <dbl> 0.000, 0.025, 0.023, 0.040, 0.034, 0.030, 0.029, 0.000~
## $ in.
                     <dbl> 0.262, 0.291, 0.308, 0.238, 0.263, 0.401, 0.189, 0.267~
## $ into
                     <dbl> 0.009, 0.025, 0.038, 0.008, 0.013, 0.037, 0.000, 0.037~
                     <dbl> 0.157, 0.038, 0.150, 0.151, 0.189, 0.260, 0.167, 0.083~
## $ is
## $ it
                     <dbl> 0.175, 0.127, 0.173, 0.222, 0.108, 0.156, 0.102, 0.165~
## $ its
                     <dbl> 0.070, 0.038, 0.030, 0.048, 0.013, 0.015, 0.000, 0.046~
## $ may
                     <dbl> 0.035, 0.038, 0.120, 0.056, 0.047, 0.074, 0.080, 0.092~
                     <dbl> 0.026, 0.000, 0.038, 0.056, 0.067, 0.045, 0.080, 0.064~
## $ more
## $ must
                     <dbl> 0.026, 0.013, 0.083, 0.071, 0.013, 0.015, 0.044, 0.018~
## $ my
                     <dbl> 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.007, 0.000~
                     <dbl> 0.035, 0.000, 0.030, 0.032, 0.047, 0.059, 0.022, 0.018~
## $ no
## $ not
                     <dbl> 0.114, 0.127, 0.068, 0.087, 0.128, 0.134, 0.102, 0.101~
## $ now
                     <dbl> 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.007, 0.000~
## $ of
                     <dbl> 0.900, 0.747, 0.858, 0.802, 0.869, 0.876, 0.902, 1.029~
## $ on
                     <dbl> 0.140, 0.139, 0.150, 0.143, 0.054, 0.141, 0.051, 0.083~
## $ one
                     <dbl> 0.026, 0.025, 0.030, 0.032, 0.047, 0.052, 0.073, 0.046~
## $ only
                     <dbl> 0.035, 0.000, 0.023, 0.048, 0.027, 0.022, 0.007, 0.046~
                     <dbl> 0.096, 0.114, 0.060, 0.064, 0.081, 0.074, 0.153, 0.037~
## $ or
## $ our
                     <dbl> 0.017, 0.000, 0.000, 0.016, 0.027, 0.030, 0.051, 0.000~
## $ shall
                     <dbl> 0.017, 0.000, 0.008, 0.016, 0.000, 0.015, 0.007, 0.000~
## $ should
                     <dbl> 0.017, 0.013, 0.068, 0.032, 0.000, 0.030, 0.007, 0.000~
## $ so
                     <dbl> 0.035, 0.013, 0.038, 0.040, 0.027, 0.007, 0.051, 0.018~
                     <dbl> 0.009, 0.063, 0.030, 0.024, 0.067, 0.045, 0.007, 0.028~
## $ some
## $ such
                     <dbl> 0.026, 0.000, 0.045, 0.008, 0.027, 0.015, 0.015, 0.000~
## $ than
                     <dbl> 0.009, 0.000, 0.023, 0.000, 0.047, 0.030, 0.109, 0.055~
## $ that
                     <dbl> 0.184, 0.152, 0.188, 0.238, 0.162, 0.208, 0.233, 0.165~
                     <dbl> 1.425, 1.254, 1.490, 1.326, 1.193, 1.469, 1.259, 1.176~
## $ the
## $ their
                     <dbl> 0.114, 0.165, 0.053, 0.071, 0.027, 0.089, 0.109, 0.083~
## $ then
                     <dbl> 0.000, 0.000, 0.015, 0.008, 0.007, 0.007, 0.015, 0.009~
## $ there
                     <dbl> 0.009, 0.000, 0.015, 0.000, 0.007, 0.007, 0.036, 0.028~
                     <dbl> 0.009, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000~
## $ things
```

```
<dbl> 0.044, 0.051, 0.075, 0.103, 0.094, 0.126, 0.080, 0.110~
## $ this
## $ to
                     <dbl> 0.507, 0.355, 0.361, 0.532, 0.485, 0.445, 0.560, 0.340~
## $ up
                     <dbl> 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.007, 0.000~
                     <dbl> 0.000, 0.013, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000~
## $ upon
## $ was
                     <dbl> 0.009, 0.051, 0.008, 0.087, 0.027, 0.007, 0.015, 0.018~
## $ were
                     <dbl> 0.017, 0.000, 0.015, 0.079, 0.020, 0.030, 0.029, 0.009~
## $ what
                     <dbl> 0.000, 0.000, 0.008, 0.008, 0.020, 0.015, 0.015, 0.009~
                     <dbl> 0.009, 0.000, 0.000, 0.024, 0.007, 0.037, 0.007, 0.000~
## $ when
## $ which
                     <dbl> 0.175, 0.114, 0.105, 0.167, 0.155, 0.186, 0.211, 0.175~
                     <dbl> 0.044, 0.038, 0.008, 0.000, 0.027, 0.045, 0.022, 0.018~
## $ who
## $ will
                     <dbl> 0.009, 0.089, 0.173, 0.079, 0.168, 0.111, 0.145, 0.267~
                     <dbl> 0.087, 0.063, 0.045, 0.079, 0.074, 0.089, 0.073, 0.129~
## $ with
                     <dbl> 0.192, 0.139, 0.068, 0.064, 0.040, 0.037, 0.073, 0.037~
## $ would
                     <dbl> 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000~
## $ your
```

fviz\_cluster(model.r, data = Essay.unlabeled)

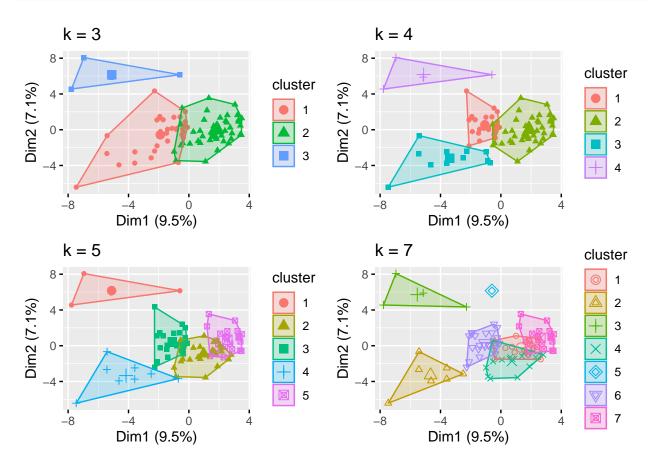
### Cluster plot



```
k3 = kmeans(Essay.unlabeled, centers = 3, nstart = 25)
k4 = kmeans(Essay.unlabeled, centers = 4, nstart = 25)
k5 = kmeans(Essay.unlabeled, centers = 5, nstart = 25)

# plots to compare
p1 = fviz_cluster(k3, geom = "point", data = Essay.unlabeled) + ggtitle("k = 3")
p2 = fviz_cluster(k4, geom = "point", data = Essay.unlabeled) + ggtitle("k = 4")
p3 = fviz_cluster(k5, geom = "point", data = Essay.unlabeled) + ggtitle("k = 5")
```

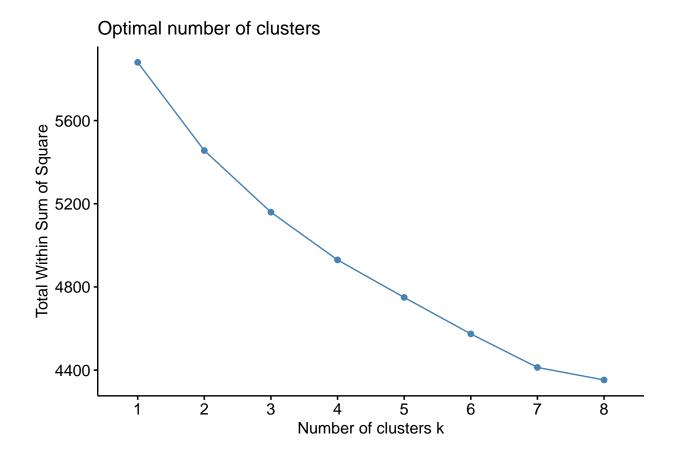
```
p4 = fviz_cluster(model.r, geom = "point", data = Essay.unlabeled) + ggtitle("k = 7")
library(gridExtra)
grid.arrange(p1, p2, p3, p4, nrow = 2)
```



#### Elbow method

Fortunately, this process to compute the "Elbow method" has been wrapped up in a single function (fviz\_nbclust):

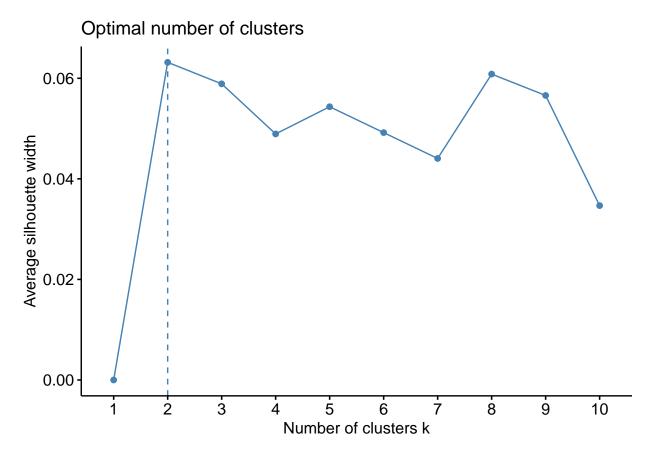
```
set.seed(123)
fviz_nbclust(Essay.unlabeled, kmeans, method = "wss", k.max = 8)
```



# Average Silhouette Method

Similar to the elbow method, this process to compute the "average silhoutte method" has been wrapped up in a single function

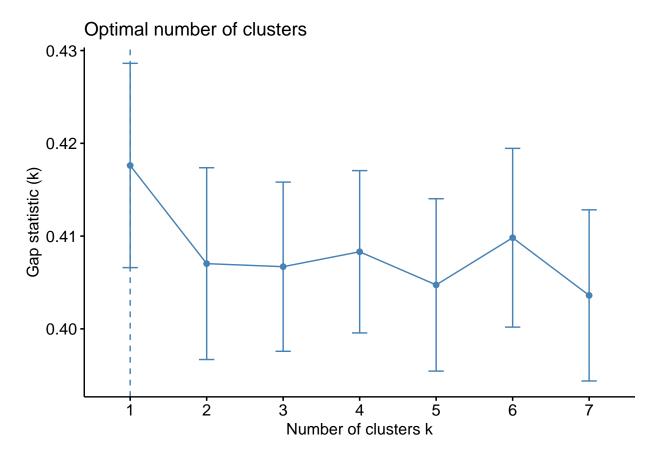
```
set.seed(123)
fviz_nbclust(Essay.unlabeled, kmeans, method = "silhouette")
```



according to silhouette method, the number of clusters k should be 2 or 8. We can take 2 as we want to decide between two authors.

## Gap Statistic Method

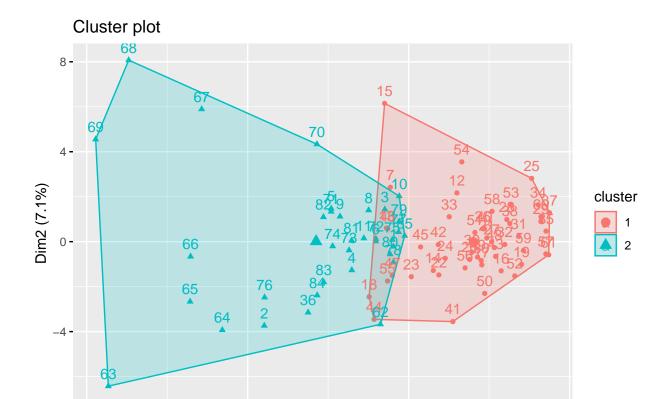
```
set.seed(123)
gap.stat = clusGap(Essay.unlabeled, FUN = kmeans, K.max = 7, B = 50)
set.seed(123)
fviz_gap_stat(gap.stat)
```



 $2,\,5$  and 7 clusters offer least gap statistic. We can use 2.

# **Extracting Results**

```
set.seed(123)
final.res = kmeans(Essay.unlabeled, 2, nstart = 25)
fviz_cluster(final.res, data = Essay.unlabeled)
```



```
Essay.unlabeled = as.data.frame(Essay.unlabeled)
Essay.unlabeled$cluster = final.res$cluster
# Essay.unlabeled |> group_by(cluster) |> summarise_all(mean)
```

Dim1 (9.5%)

ò

<u>-4</u>

Let's inspect the clusters

cluster n

1 50

## 1

```
Essay$cluster = final.res$cluster
Essay |>
   count(cluster) |>
   left_join(
   Essay |>
      select(cluster, author) |>
      group_by(cluster) |>
      slice(1:10) |> # just preview 10
      mutate(authors = str_c(author, collapse = ', ')) |> # collapse all animal names into one vector
      select(-author) |>
      ungroup() |>
      distinct()
   )

## Joining, by = "cluster"
```

```
## 2 2 35
##

authors

## 1 dispt, Hamilton, Hamilt
```

### Conclusion

We observe that the documents in the left cluster have features that are similar to those of Hamilton, while the documents in the right cluster have traits that are more similar to those of other. We can suspect that the other author is Madison. Since the cluster with Madison includes most disputed documents, this suggests that Madison was the author for most of the disputed documents but Hamilton was the author for one of the disputed documents.